

#### Outline

- Constructing arguments in propositional logic
- Normal forms

Enumeration

#### Outline

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1.	Dun	umg	Argume	m

2

Our final topic on logic deals with constructing and validating arguments. We start
by giving examples of valid and non-valid arguments and define various concepts
that we will need to breakdown an argument.

#### 2. Inference Rules for Propositional Logic

6

Breaking down arguments take effort. To simplify things we will collect some standard arguments which we will use, like lego bricks, when working with complicated arguments.

#### 3. Using the Rules of Inference to Build Valid Arguments

15

- In our final topic in logic, we will use the properties of logical operators to construct a valid argument.
- This is a relatively advanced topic and could be ignored until you are comfortable with the earlier topics in logic.

#### Notation

## Single-line vs Double-line Arrows

For the purpose of this module the single line arrows (representing the IFTHEN and IFF connectives)

$$\rightarrow$$
 and  $\leftrightarrow$ 

mean the same thing as the corresponding double-line arrow

$$\Rightarrow$$
 and  $\Leftrightarrow$ 

I will use the double-lined arrows in places where I want to treat a complicated proposition as two smaller propositions. For example, I want to think of the proposition

$$(p \rightarrow q) \land \neg q \implies \neg p$$

in terms of the two proposition  $(p \rightarrow q) \land \neg q$  and  $\neg p$ .

#### Motivation

Remember the Socrates example when we started Logic.

"All men are mortal.

Socrates is a man.

Therefore, Socrates is mortal."

#### Here we have two premises:

- All men are mortal
- Socrates is a man.

#### and the conclusion:

Socrates is mortal.

**Q:** How do we get the conclusion from the premises?

**A:** We construct an argument, a sequence of propositions that follow from the rules of inference until we reach the conclusion.

#### Motivation

Remember the Socrates example when we started Logic.

"All men are mortal.

Socrates is a man.

Therefore, Socrates is mortal."

#### Here we have two premises:

- All men are mortal
- Socrates is a man.

#### and the conclusion:

Socrates is mortal.

**Q:** How do we get the conclusion from the premises?

**A:** We construct an argument, a sequence of propositions that follow from the rules of inference until we reach the conclusion.



## Arguments

#### Definition 1 (Argument)

A argument in propositional logic is a sequence of propositions. All but the final proposition are called premises. The last statement is the conclusion. The argument is valid if the premises imply the conclusion.

• If the premises are  $p_1, p_2, \dots p_n$  and the conclusion is q then the argument is valid iff

$$(p_1 \wedge p_2 \wedge \cdots \wedge p_n) \rightarrow q$$

is a tautology.

- We could use truth tables to test if an argument is valid construct the above expression, then build the truth table and check the output column.
- Alternatively, we could sequently apply inference rules to arrive at the conclusion.
- Inference rules are simple arguments that will be used to construct more complex argument forms.

#### Outline

#### 1. Building Arguments

2

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# Detachment (Modus Ponens)

# Argument $\begin{array}{c} p \rightarrow q \\ \hline p \\ \hline \vdots q \end{array}$

Corresponding Tautology

$$(p \rightarrow q) \land p \implies q$$

#### Example

#### Let

p ="It is snowing."

q ="I will study discrete maths."

#### Then the argument is

"If it is snowing, then I will study discrete maths."

"It is snowing."

Therefore "I will study discrete maths."

# Indirect Reasoning (Modus Tollens)

# Argument $p \rightarrow q$ $\neg q$ $\therefore \neg p$

```
Corresponding Tautology (p \to q) \land \neg q \implies \neg p
```

#### Example

#### Let

p ="It is snowing."

q ="I will study discrete maths."

#### Then the argument is

"If it is snowing, then I will study discrete maths."

"I will not study discrete maths."

Therefore "It is not snowing."

# Chain Rule (Hypothetical Syllogism)

# $\begin{array}{c} p \rightarrow q \\ q \rightarrow r \\ \hline \therefore p \rightarrow r \end{array}$

```
Corresponding Tautology  (p \to q) \land (q \to r) \implies (p \to r)
```

#### Example

#### Let

p ="It is snowing."

q ="I will study discrete maths."

r = "I will get an A."

#### Then the argument is

"If it is snowing, then I will study discrete maths."

"If I will study discrete maths, then I will get an A."

Therefore "If it is snowing, then I will get an A."

# Chain Rule (Hypothetical Syllogism)

# Argument $\begin{array}{c} p \to q \\ q \to r \\ \hline \therefore p \to r \end{array}$

#### Example

#### Let

p ="It is snowing."

q ="I will study discrete maths."

r = "I will get an A."

#### Then the argument is

"If it is snowing, then I will study discrete maths."

"If I will study discrete maths, then I will get an A."

Therefore "If it is snowing, then I will get an A."

# Disjunctive Simplification (Disjunctive Syllogism)

# $\begin{array}{ccc} & p \lor q & p \lor q \\ \hline & p \lor q & \neg q \end{array}$

$$\begin{array}{c} \underline{\text{Corresponding Tautology}} \\ (p \lor q) \land (\neg p) \implies q \\ (p \lor q) \land (\neg q) \implies p \end{array}$$

#### Example

 $\therefore q$ 

#### Let

p ="I will study discrete maths."

 $\therefore p$ 

q ="I will study programming."

#### Then the argument is

"I will study discrete maths or I will study programming."

"I will not study discrete maths."

Therefore "I will study programming."

# Disjunctive Addition

# $\frac{p}{\therefore p \lor q}$

Corresponding Tautology 
$$p \implies (p \lor q)$$

#### Example

#### Let

p ="I will study discrete maths."

q ="I will get high."

#### Then the argument is

"I will study discrete maths."

Therefore "I will study discrete maths or I will get high."

# Conjunctive Simplification

#### Argument

$$\begin{array}{c} p \wedge q \\ \therefore p \end{array} \qquad \begin{array}{c} p \wedge q \\ \therefore q \end{array}$$

#### Corresponding Tautology

$$(p \land q) \implies p$$

$$(p \land q) \implies q$$

#### Example

#### Let

p ="I will study discrete maths."

q ="I will get high."

#### Then the argument is

"I will study discrete maths and I will get high."

Therefore "I will study discrete maths."

#### Resolution

# 

#### Example

#### Let

p ="I will study discrete maths."

p ="I will study programming."

p ="I will study databases."

#### Then the argument is

"I will not study discrete maths or I will study programming."

"I will study discrete maths or I will study databases."

Therefore "I will study programming or I will study databases."

#### Outline

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#### 2. Inference Rules for Propositional Logic

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Breaking down arguments take effort. To simplify things we will collect some standard arguments which we will use, like lego bricks, when working with complicated arguments.

#### 3. Using the Rules of Inference to Build Valid Arguments

15

- In our final topic in logic, we will use the properties of logical operators to construct a valid argument.
- This is a relatively advanced topic and could be ignored until you are comfortable with the earlier topics in logic.

A valid argument is a sequence of statements. Each statement is either a premise or follows from previous statements by rules of inference. The last statement is called conclusion.

#### Example 2

Assuming the following two propositions

$$p$$
 and  $(p \rightarrow q)$ 

show that q is a conclusion.

#### Method 1

Construct argument using inference rules ...

	Step	Reason
1)	$p \land (p \rightarrow q)$	Premise
2)	p	Conjunctive Simplification from (1)
3)	$p \rightarrow q$	Conjunctive Simplification from (1)
<i>:</i> .	q	Detachment (Modus Ponens) from (2) and (3)

#### Method 2

#### Construct an expression of the form

(premise 1)  $\land$  (premise 2)  $\land \cdots \land$  (premise n)  $\implies$  (conclusion) and verify that the expression is a tautology (using a truth table).

So for this example ...

$$\underbrace{(\text{premise 1})}_{p} \land \underbrace{(\text{premise 2})}_{(p \to q)} \underbrace{\Longrightarrow}_{q} \underbrace{(\text{conclusion})}_{q}$$

		argument premise	argument conclusion	argument

#### Method 2

#### Construct an expression of the form

(premise 1)  $\land$  (premise 2)  $\land \cdots \land$  (premise n)  $\implies$  (conclusion) and verify that the expression is a tautology (using a truth table). So for this example . . .

$$\underbrace{(\text{premise 1})}_{p} \land \underbrace{(\text{premise 2})}_{(p \to q)} \underbrace{\Longrightarrow}_{q} \underbrace{(\text{conclusion})}_{q}$$

	indiv	argument premise	argument conclusion	argument

#### Method 2

#### Construct an expression of the form

$$(premise 1) \land (premise 2) \land \cdots \land (premise n) \implies (conclusion)$$

$$\underbrace{(\text{premise 1})}_{p} \land \underbrace{(\text{premise 2})}_{(p \rightarrow q)} \underbrace{\Longrightarrow}_{q} \underbrace{(\text{conclusion})}_{q}$$

inp	inputs individual premises		argument premise	argument conclusion	argument	
p	q	p	$(p \rightarrow q)$	$p \land (p \rightarrow q)$	q	$p \land (p \rightarrow q) \Rightarrow q$
F	F	F	T	F	F	T
$\mathbb{F}$	T	F	T	$\mathbf{F}$	T	T
T	F	T	${f F}$	$\mathbf{F}$	F	T
T	T	T	T	T	T	T

#### Method 2

#### Construct an expression of the form

$$(premise 1) \land (premise 2) \land \cdots \land (premise n) \implies (conclusion)$$

$$\underbrace{(\text{premise 1})}_{p} \land \underbrace{(\text{premise 2})}_{(p \rightarrow q)} \underbrace{\Longrightarrow}_{q} \underbrace{(\text{conclusion})}_{q}$$

inputs individual premises		argument premise	argument conclusion	argument		
p	q	p	$(p \rightarrow q)$	$p \land (p \rightarrow q)$	q	$p \land (p \rightarrow q) \Rightarrow q$
F	F	F	T	F	F	T
$\mathbf{F}$	T	F	T	F	T	T
T	$\mathbf{F}$	T	$\mathbf{F}$	$\mathbf{F}$	$\mathbf{F}$	T
T	$\mathbf{T}$	T	T	T	T	T

#### Method 2

#### Construct an expression of the form

(premise 1) 
$$\land$$
 (premise 2)  $\land \cdots \land$  (premise  $n$ )  $\implies$  (conclusion)

$$\underbrace{(\text{premise 1})}_{p} \land \underbrace{(\text{premise 2})}_{(p \rightarrow q)} \underbrace{\Longrightarrow (\text{conclusion})}_{q}$$

inputs individual pre		vidual premises	argument premise	argument conclusion	argument	
p	q	p	$(p \rightarrow q)$	$p \land (p \rightarrow q)$	q	$p \land (p \rightarrow q) \Rightarrow q$
F	F	F	T	F	F	T
$\mathbf{F}$	T	F	T	F	T	T
T	$\mathbf{F}$	T	$\mathbf{F}$	$\mathbf{F}$	F	T
T	T	T	T	T	T	T

#### Method 2

#### Construct an expression of the form

$$(premise 1) \land (premise 2) \land \cdots \land (premise n) \implies (conclusion)$$

$$\underbrace{(\text{premise 1})}_{p} \land \underbrace{(\text{premise 2})}_{(p \rightarrow q)} \underbrace{\Longrightarrow}_{q} \underbrace{(\text{conclusion})}_{q}$$

inputs		indiv	vidual premises	argument premise	argument conclusion	argument	
	p	q	p	$(p \rightarrow q)$	$p \land (p \rightarrow q)$	q	$p \land (p \rightarrow q) \Rightarrow q$
	F	F	F	T	F	F	T
	$\mathbf{F}$	T	F	T	$\mathbf{F}$	T	T
	T	$\mathbf{F}$	T	${f F}$	$\mathbf{F}$	F	T
	T	T	T	T	T	$\mathbf{T}$	T

#### Method 2

#### Construct an expression of the form

(premise 1) 
$$\land$$
 (premise 2)  $\land \cdots \land$  (premise  $n$ )  $\implies$  (conclusion)

$$\underbrace{(\text{premise 1})}_{p} \land \underbrace{(\text{premise 2})}_{(p \rightarrow q)} \underbrace{\Longrightarrow}_{q} \underbrace{(\text{conclusion})}_{q}$$

inputs		indiv	vidual premises	argument premise	argument conclusion	argument	
	p	q	p	$(p \rightarrow q)$	$p \land (p \rightarrow q)$	q	$p \land (p \rightarrow q) \Rightarrow q$
	F	F	F	T	F	F	T
	$\mathbf{F}$	T	F	T	$\mathbf{F}$	T	T
	$\mathbf{T}$	$\mathbf{F}$	T	${f F}$	$\mathbf{F}$	F	T
	T	T	T	Т	Т	Т	T

With these hypotheses:

- "It is not sunny this afternoon and it is colder than yesterday."
- "We will go swimming only if it is sunny."
- "If we do not go swimming, then we will take a canoe trip."
- "If we take a canoe trip, then we will be home by sunset."

Using the inference rules, construct a valid argument for the conclusion:

• "We will be home by sunset."

General procedure ...

STEP 1) Choose propositional variables

STEP 2 Translation into propositional logic.

STEP 3 Construct the valid argument (OR verify related tautology using truth table.)

# e 3

# Example 3

With these hypotheses:

- "It is not sunny this afternoon and it is colder than yesterday."
- "We will go swimming only if it is sunny."
- "If we do not go swimming, then we will take a canoe trip."
- "If we take a canoe trip, then we will be home by sunset."

Using the inference rules, construct a valid argument for the conclusion:

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General procedure ...

STEP 1) Choose propositional variables.

**STEP 2**) Translation into propositional logic.

STEP 3 Construct the valid argument (OR verify related tautology using truth table.)

#### II

#### STEP 1 Choose propositional variables.

- s = "It is Sunny this afternoon."
- c = "It is Colder than yesterday."
- w = "We will go sWimming"
- t = "We will take a canoe Trip."
- h = "We will be Home by sunset."

# STEP 2 Translation into propositional logi

#### Premises ...

- "It is not sunny this afternoon and it is colder than yesterday."  $\neg s \land c$
- **b** "We will go swimming only if it is sunny."  $w \rightarrow s$ 
  - **9** "If we do not go swimming, then we will take a canoe trip."  $\neg w \rightarrow t$
- ① "If we take a canoe trip, then we will be home by sunset."  $t \rightarrow h$

#### and conclusion

• "We will be home by sunset."

h

#### (STEP 1) Choose propositional variables.

- s = "It is Sunny this afternoon."
- c = "It is Colder than yesterday."
- w = "We will go sWimming"
- t = "We will take a canoe Trip."
- h = "We will be Home by sunset."

#### (STEP 2) Translation into propositional logic.

#### Premises . . .

- "It is not sunny this afternoon and it is colder than yesterday."  $\neg s \wedge c$
- "We will go swimming only if it is sunny."  $w \rightarrow s$
- "If we do not go swimming, then we will take a canoe trip."  $\neg w \rightarrow t$
- "If we take a canoe trip, then we will be home by sunset."  $t \rightarrow h$

#### and conclusion

• "We will be home by sunset."

h

III

STEP 3 Construct the valid argument
We have

(Note the truth table here would have 32 rows)

	Conclusion			
(a)	(b)	(c)	(d)	
$\neg s \land c$	$w \rightarrow s$	$\neg w \rightarrow t$	$t \rightarrow h$	h

	Step	Reason
1)	$\neg s \wedge c$	Premise (a)
2)		Conjunctive Simplification from (1)
3)		Premise (b)
4)		Indirect Reasoning (Modus Tollens) from (2) and (3)
5)		Premise (c)
6)		Detachment (Modus Ponens) from (4) and (5)
7)		Premise (d)
		Detachment (Modus Ponens) from (6) and (7)

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STEP 3 Construct the valid argument
We have

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# Premises Conclusion (a) (b) (c) (d) $\neg s \land c \quad w \rightarrow s \quad \neg w \rightarrow t \quad t \rightarrow h$

	Step	Reason
1)	$\neg s \wedge c$	Premise (a)
2)		Conjunctive Simplification from (1)
3)		Premise (b)
4)		Indirect Reasoning (Modus Tollens) from (2) and (3)
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(Note the truth table here would have 32 rows)

### We have

Premises			Conclusion	
(a)	(b)	(c)	(d)	
$\neg s \land c$	$w \rightarrow s$	$\neg w \rightarrow t$	$t \rightarrow h$	h

	Step	Reason
1)	$\neg s \wedge c$	Premise (a)
2)	$\neg s$	Conjunctive Simplification from (1)
3)		Premise (b)
4)		Indirect Reasoning (Modus Tollens) from (2) and (3)
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 $\Pi$ 

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Premises			Conclusion	
(a)	(b)	(c)	(d)	
$\neg s \land c$	$w \rightarrow s$	$\neg w \rightarrow t$	$t \rightarrow h$	h

	Step	Reason
1)	$\neg s \wedge c$	Premise (a)
2)	$\neg s$	Conjunctive Simplification from (1)
3)	$w \rightarrow s$	Premise (b)
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STEP 3 Construct the valid argument
We have

(Note the truth table here would have 32 rows)

# Premises (a) (b) (c) (d)

Premises Conclusion
(a) (b) (c) (d) 
$$\neg s \land c \quad w \rightarrow s \quad \neg w \rightarrow t \quad t \rightarrow h$$
  $h$ 

_		
	Step	Reason
1)	$\neg s \wedge c$	Premise (a)
2)	$\neg s$	Conjunctive Simplification from (1)
3)	$w \rightarrow s$	Premise (b)
4)	$\neg w$	Indirect Reasoning (Modus Tollens) from (2) and (3)
5)		Premise (c)
6)		Detachment (Modus Ponens) from (4) and (5)
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STEP 3 Construct the valid argument

(Note the truth table here would have 32 rows)

# We have

Premises			Conclusion	
(a)	(b)	(c)	(d)	
$\neg s \land c$	$w \rightarrow s$	$\neg w \rightarrow t$	$t \rightarrow h$	h

	Step	Reason
1)	$\neg s \wedge c$	Premise (a)
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3)	$w \rightarrow s$	Premise (b)
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5)	$\neg w \rightarrow t$	Premise (c)
6)		Detachment (Modus Ponens) from (4) and (5)
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STEP 3 Construct the valid argument

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# We have

Premises			Conclusion	
(a)	(b)	(c)	(d)	
$\neg s \land c$	$w \rightarrow s$	$\neg w \rightarrow t$	$t \rightarrow h$	h

	Step	Reason
1)	$\neg s \wedge c$	Premise (a)
2)	$\neg s$	Conjunctive Simplification from (1)
3)	$w \rightarrow s$	Premise (b)
4)	$\neg w$	Indirect Reasoning (Modus Tollens) from (2) and (3)
5)	$\neg w \rightarrow t$	Premise (c)
6)	t	Detachment (Modus Ponens) from (4) and (5)
7)		Premise (d)
		Detachment (Modus Ponens) from (6) and (7)

III

STEP 3 Construct the valid argument

(Note the truth table here would have 32 rows)

### We have

Premises			Conclusion	
(a)	(b)	(c)	(d)	
$\neg s \land c$	$w \rightarrow s$	$\neg w \rightarrow t$	$t \rightarrow h$	h

$\mathcal{C}$		
	Step	Reason
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5)	$\neg w \rightarrow t$	Premise (c)
6)	t	Detachment (Modus Ponens) from (4) and (5)
7)	$t \rightarrow h$	Premise (d)
	10	Data ahmant (Madua Danana) from (6) and (7)

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STEP 3 Construct the valid argument

(Note the truth table here would have 32 rows)

## We have

	Prer	nises	Conclusion	
(a)	(b)	(c)	(d)	
$\neg s \land c$	$w \rightarrow s$	$\neg w \rightarrow t$	$t \rightarrow h$	h

	Step	Reason
1)	$\neg s \wedge c$	Premise (a)
2)	$\neg s$	Conjunctive Simplification from (1)
3)	$w \rightarrow s$	Premise (b)
4)	$\neg w$	Indirect Reasoning (Modus Tollens) from (2) and (3)
5)	$\neg w \rightarrow t$	Premise (c)
6)	t	Detachment (Modus Ponens) from (4) and (5)
7)	$t \rightarrow h$	Premise (d)
··.	h	Detachment (Modus Ponens) from (6) and (7)

# That was a bit painful ... let Python do the work ...

```
Premises
                                                                                        Conclusion
0
      1 # individual premises
                                             (a) (b) (c) (d) \neg s \land c \quad w \rightarrow s \quad \neg w \rightarrow t \quad t \rightarrow h
      2 p1 = "not s and c"
      3 p2 = "not w or s"
      4 p3 = "w or t"
      5 p4 = "not t or h"
      7 # construct argument premise - each premise is inside ( )
      8 p = f''(\{p1\}) \text{ and } (\{p2\}) \text{ and } (\{p3\}) \text{ and } (\{p4\})''
      9
     10 # argument conclusion
     11 c = "h"
     12
     13 # output argument premise and conclusion
     14 print(f"argument premise: {p}")
     15 print(f"argument conclusion: {c}")
     16
     17 # build expression for testing (is it a tautology?)
     18 argument = f''(not(\{p\})) or (\{c\})''
     19
     20 # generate truth table - show premises, conclusion and argument
     21 TruthTable([p1,p2,p3,p4, c, argument])
```

# That was a bit painful ...let Python do the work ... II

argument premise: (not s and c) and (not w or s) and (w or t) and (not t or h) argument conclusion: h

c	h	s	t	w	not s and c	not w or s	w or t	not t or h	h	(not ((not s and c) and (not w or s) and (w or t) and (not t or h))) or (h)
False	False	False	False	False	False	True	False	True	False	e True
False	False	False	False	True	False	False	True	True	False	e True
False	False	False	True	False	False	True	True	False	False	e True
False	False	False	True	True	False	False	True	False	False	e True
False	False	True	False	False	False	True	False	True	False	e True
False	False	True	False	True	False	True	True	True	False	e True
False	False	True	True	False	False	True	True	False	False	e True
False	False	True	True	True	False	True	True	False	False	e True
False	True	False	False	False	False	True	False	True	True	True
False	True	False	False	True	False	False	True	True	True	True
False	True	False	True	False	False	True	True	True	True	True
False	True	False	True	True	False	False	True	True	True	True
	True					True	False	True	True	True
	True					True	True			True
	True					True				True
	True					True				True
	False					True	False			e True
	False					False	True			e True
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	False					True	False			e True
	False					True	True			e True
	False					True	True			e True
	False					True	True			e True
	True					True	False			True
	True					False	True			True
	True					True	True			True
	True					False	True			True
	True					True	False			True
	True					True				True
	True					True				True
irue	True	irue	irue	rrue	raise	True	True	irue	irue	True

# That was a bit painful ...let Python do the work ...

argument premise: (not s and c) and (not w or s) and (w or t) and (not t or h) argument conclusion: h

inot s and c not w or s w or t not t or high linot ((not s and c) and (not w or s) and (w or t) and (not t or h))) or (h) False False False False False True False True False True False False False True False False True True False True False False False True False False True True False False True False False True True False False True False False True False False True False False True False True False True False False True False True False True True True False True False False True True False False True True False False True False False True True False True True False False True False True False False False True False True True True False True False False True False False True True True True False True False True False False True True True True True False True False True True False False True True True True False True True False False True False True True True False True True False True False True True True True True False True True False False True True True True True All rows are True so False True True True False True True True True True True False False False True True False True False True we have a tautology True False False False True True False True True False True True False False True False True True True False False True True False False True True True False True False False True True False True False False True False True False True True False True False True False True True True False True True False True True False False True True False False True True False True True False True True False False True True True False False False True True False True True True True True False False True True False True True True True True True False True False True True True True True True True False True True False True True True True True True False False False True False True True True True True False True False True True True True True True True False False True True True True True True True True True False True True True True True