



Looking before Crossing: An Optimal Algorithm to Minimize UAV Energy by Speed Scheduling with a Practical Flight Energy Model

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Outline

■ Background

■ Problem Modeling

■ Solutions

■ Simulation

■ Conclusion



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■ Background

■ Problem Modeling

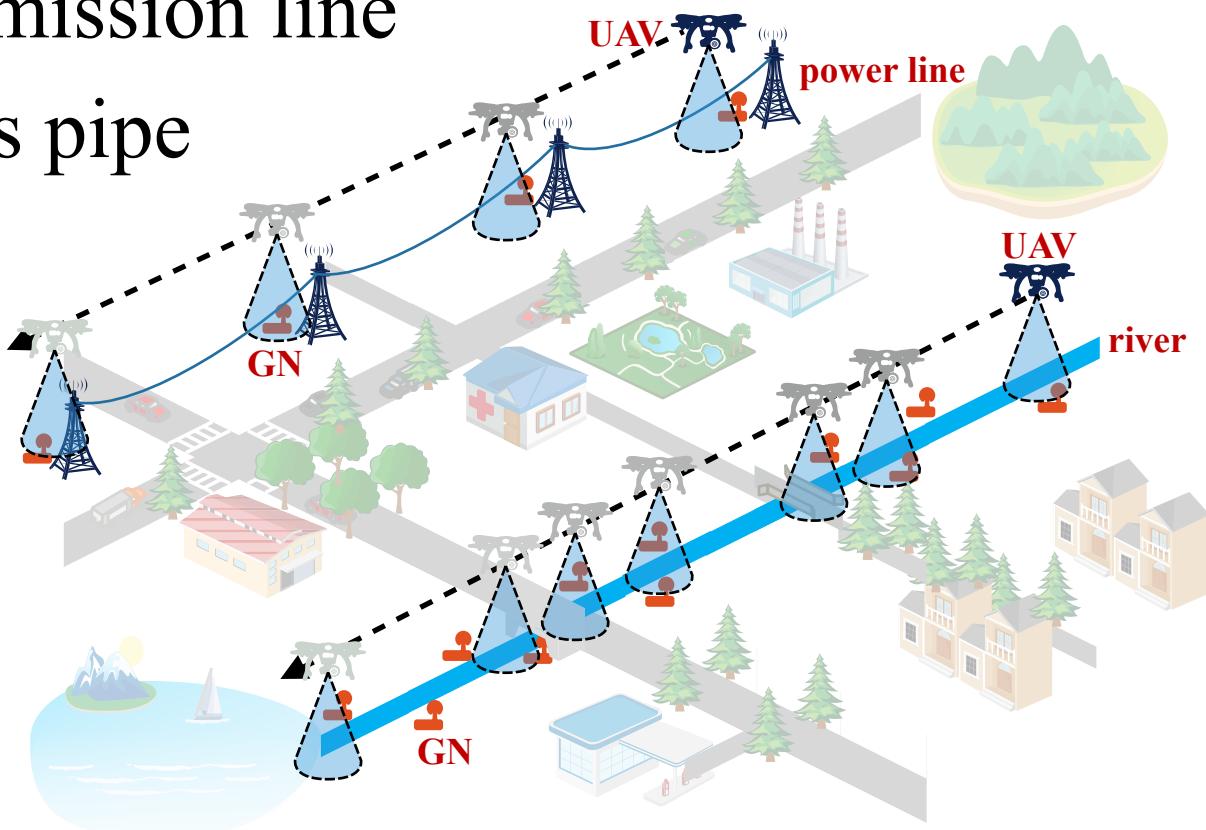
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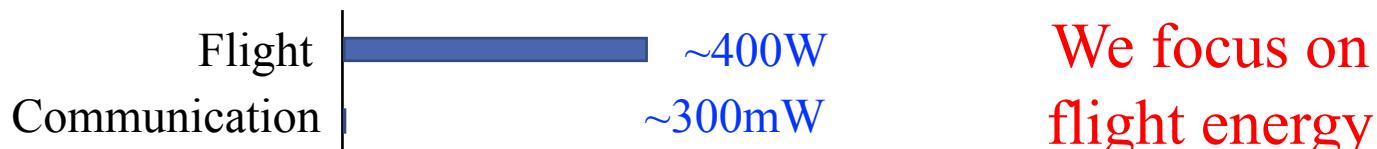
UAV data collection application scenarios

- A UAV collects data from wireless sensors or IoT devices (GNs) deployed along a straight line
 1. power transmission line
 2. water/oil/gas pipe
 3. river/coast
 4. road
 5. ...

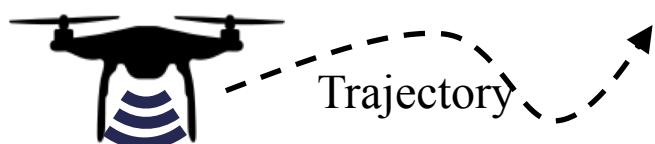


Energy consumption problem of UAVs

- Key issues: limited energy supply on board.
- Flight power **1000 times** communication power



- Related flight energy consumption models



distance-related
energy model

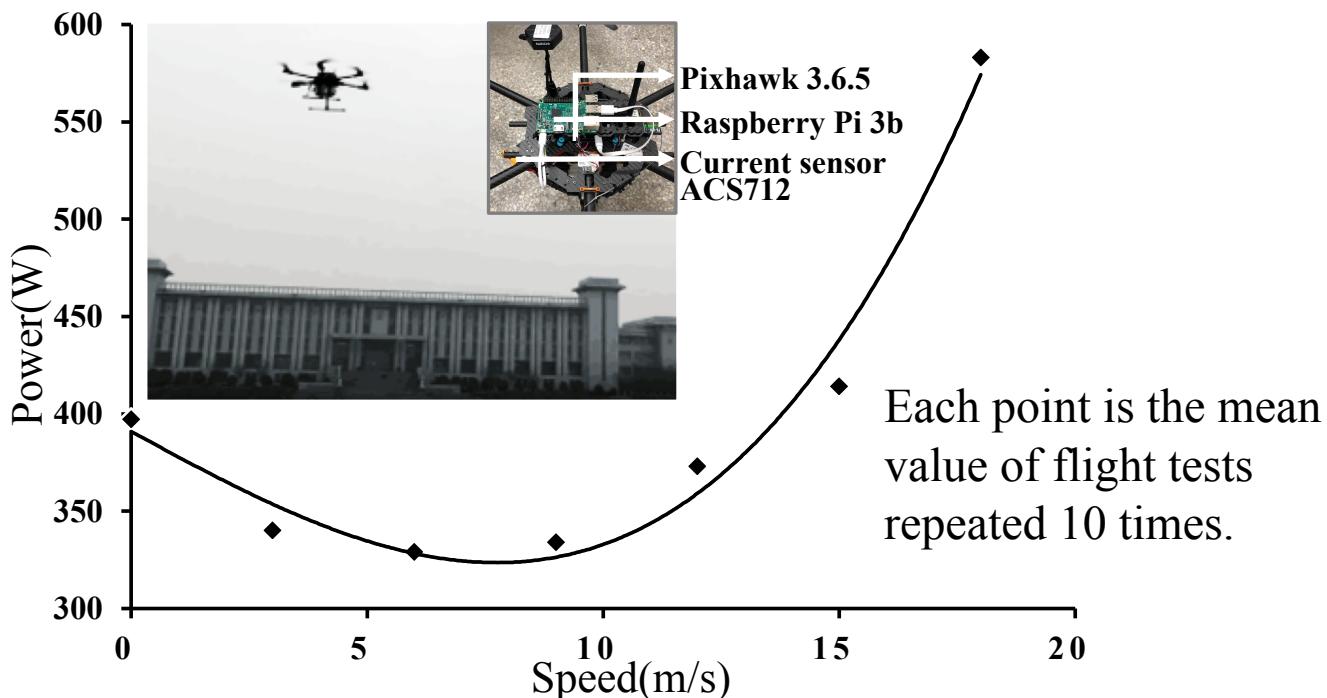


duration-related
energy model

Too simple to be accurate

Our practical flight energy model

- We conduct a set of real-world flight tests

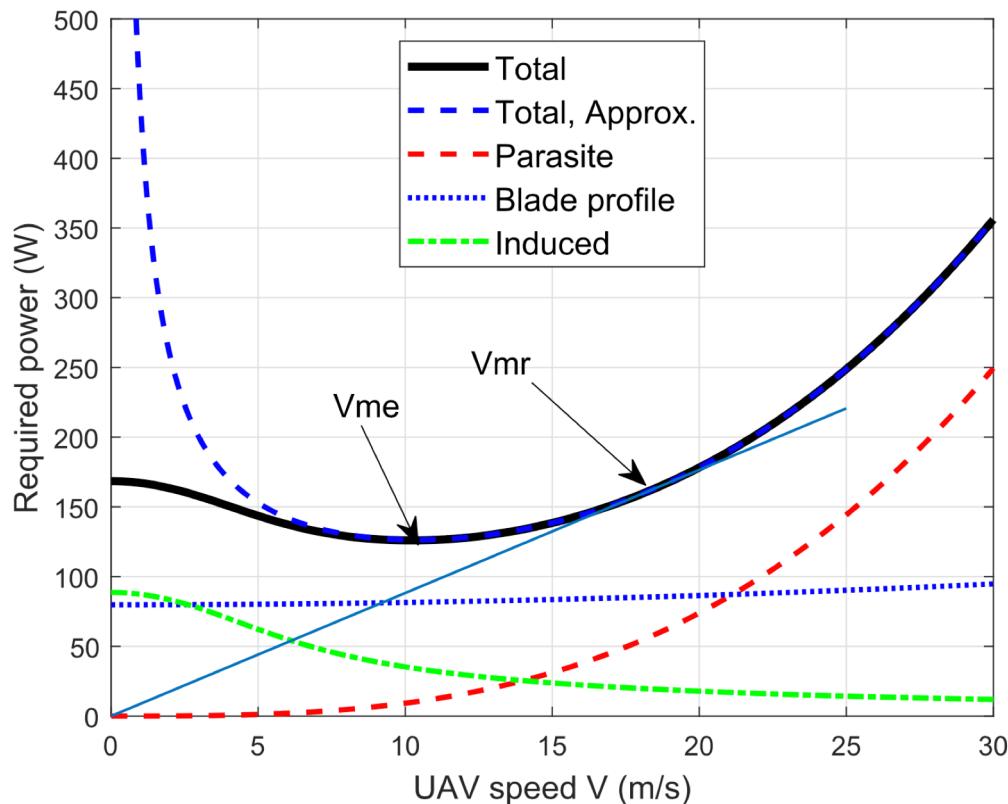


- The flight power is a convex function of the flight speed

Consistent with theoretical analysis

- Consistent with a most recent theoretical analysis.

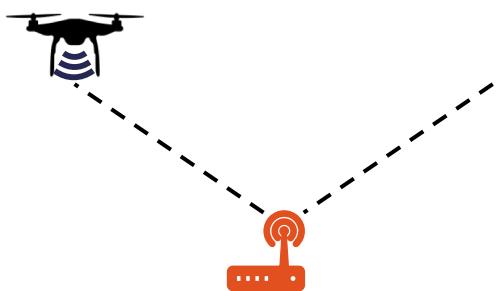
$$P(V) = \underbrace{P_0 \left(1 + \frac{3V^2}{U_{\text{tip}}^2} \right)}_{\text{blade profile}} + \underbrace{P_i \left(\sqrt{1 + \frac{V^4}{4v_0^4}} - \frac{V^2}{2v_0^2} \right)^{1/2}}_{\text{induced}} + \underbrace{\frac{1}{2} d_0 \rho s A V^3}_{\text{parasite}},$$



Y. Zeng, J. Xu, and R. Zhang, "Energy minimization for wireless communication with rotary-wing UAV," *IEEE Transactions on Wireless Communications*, vol. 18, no. 4, pp. 2329–2345, 2019.

Challenges to our problem

1. min UAV flight energy to collection all data



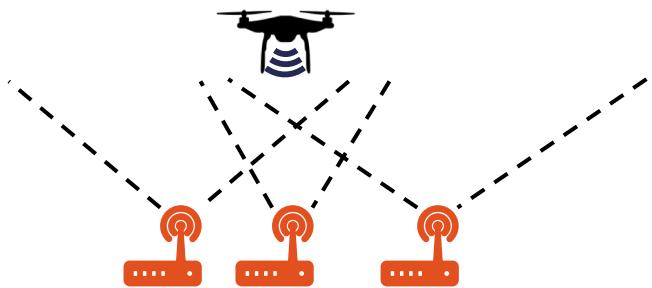
Slow speed {
 Sufficient time to collect data
 Cost more flight energy

Faster speed {
 Less time to collect data
 Save more flight energy

**Best trade-off
must be found**

2. GNs compete for UAV time to upload data

Three GNs compete to upload their own data



Such competition is complicated: each GN has

1. a different amount of data
2. a different transmission range size

**Best GN transmission scheduling
must be found**



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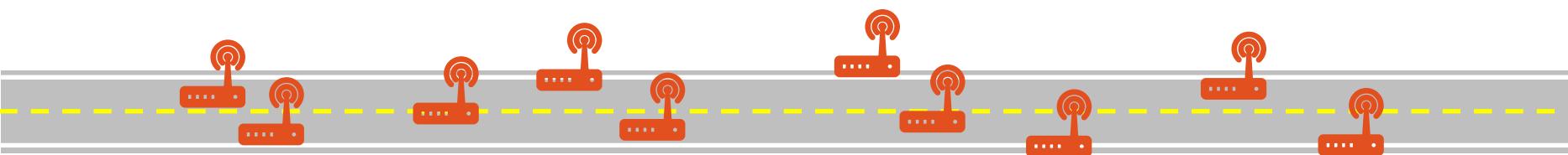
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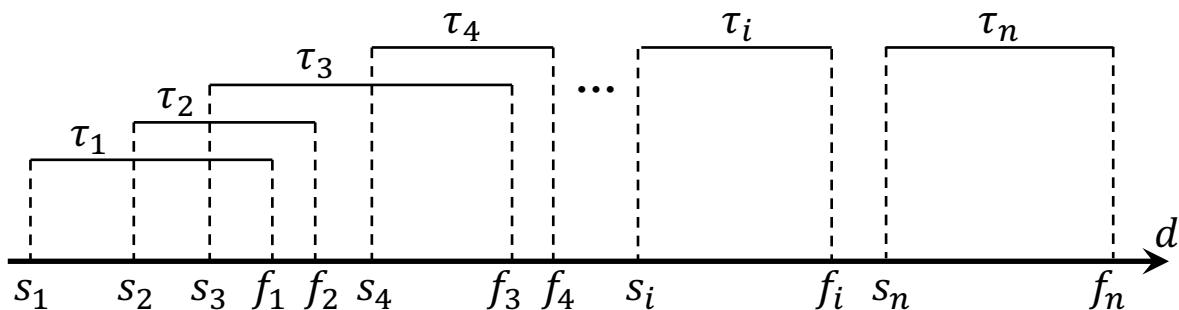
GNs and UAV

- m Ground Nodes (GNs) are deployed along a line
- The UAV flies straightly at a fixed height
- The UAV collects data from GN when flying



Transmission range and required time

- GN i has a transmission range (s_i, f_i)
- Within range, GN i requires τ_i time to upload data
- We allow the ranges be different but aligned
 - $0 = s_1 < s_2 < \dots < s_n$
 - $0 < f_1 < f_2 < \dots < f_n = D$





UAV speed scheduling

- Speed scheduling function $v(t)$

- The speed at time t

- Position of the UAV at time t

$$d(t) = \int_0^t v(\tau) d\tau$$



Range/completion constraint

- Transmission ranges are overlapped but aligned, so the UAV collects data following GN index.
- At switching time t_i : the UAV finishes collecting data from GN i and starts GN $i + 1$
- Range constraint

$$s_i \leq d(t_{i-1}) < d(t_i) \leq f_i$$

- Completion constraint

$$t_i - t_{i-1} \geq \tau_i$$

USS-GTS problem

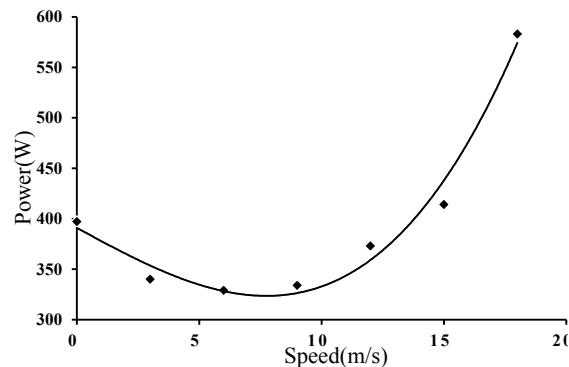
- Flight power $p(v)$ for UAV flight speed v

- The energy consumption of UAV

$$E = \int_{t_0}^{t_n} p(v(t)) dt$$

- USS-GTS problem: find speed scheduling function $v(t)$ to

1. minimize UAV energy consumption E
2. satisfy range constraint
3. satisfy completion constraint





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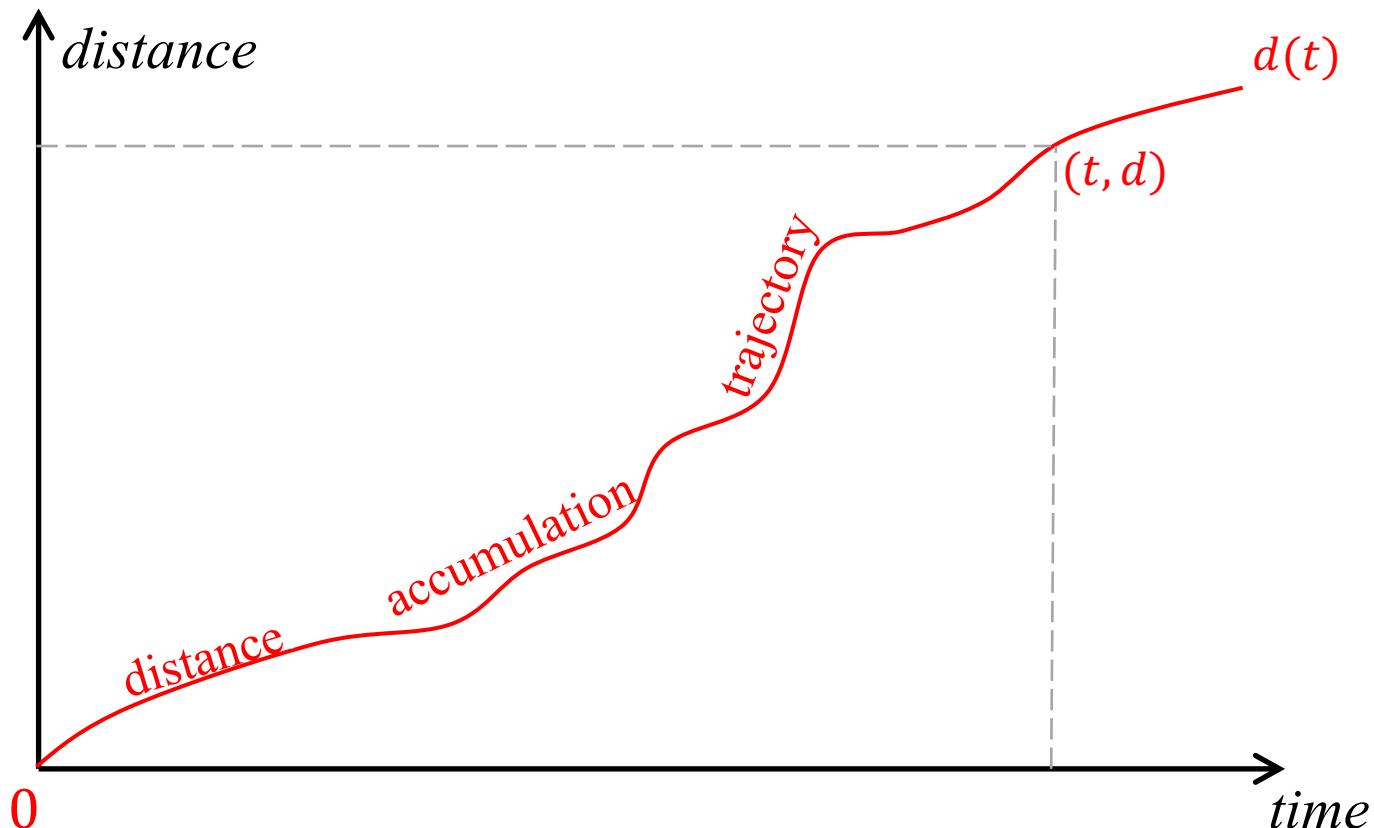
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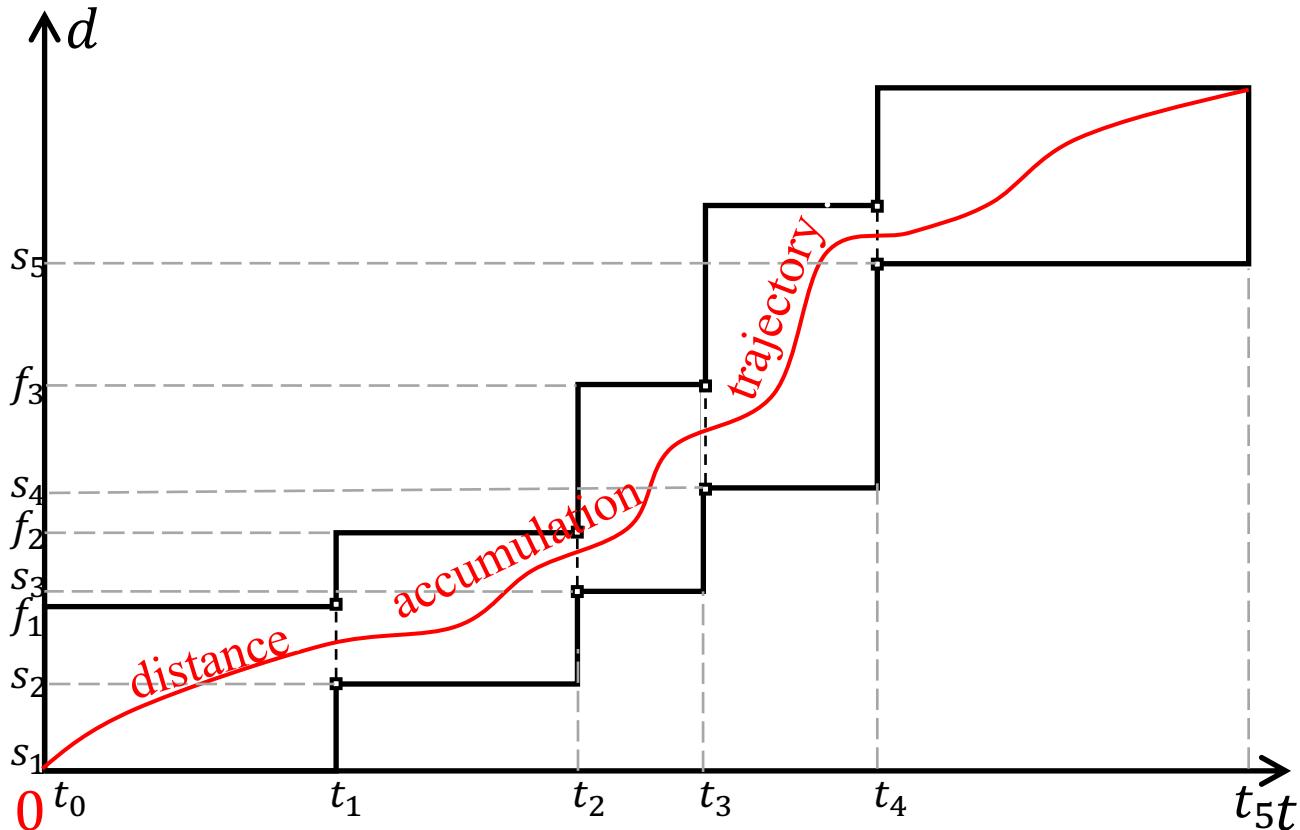
Distance accumulation trajectory

- Time-distance diagram: reaching position d at time t
- *distance accumulation function* $d(t)$ a curve
- *speed scheduling function* $v(t)$ is the curve's slope



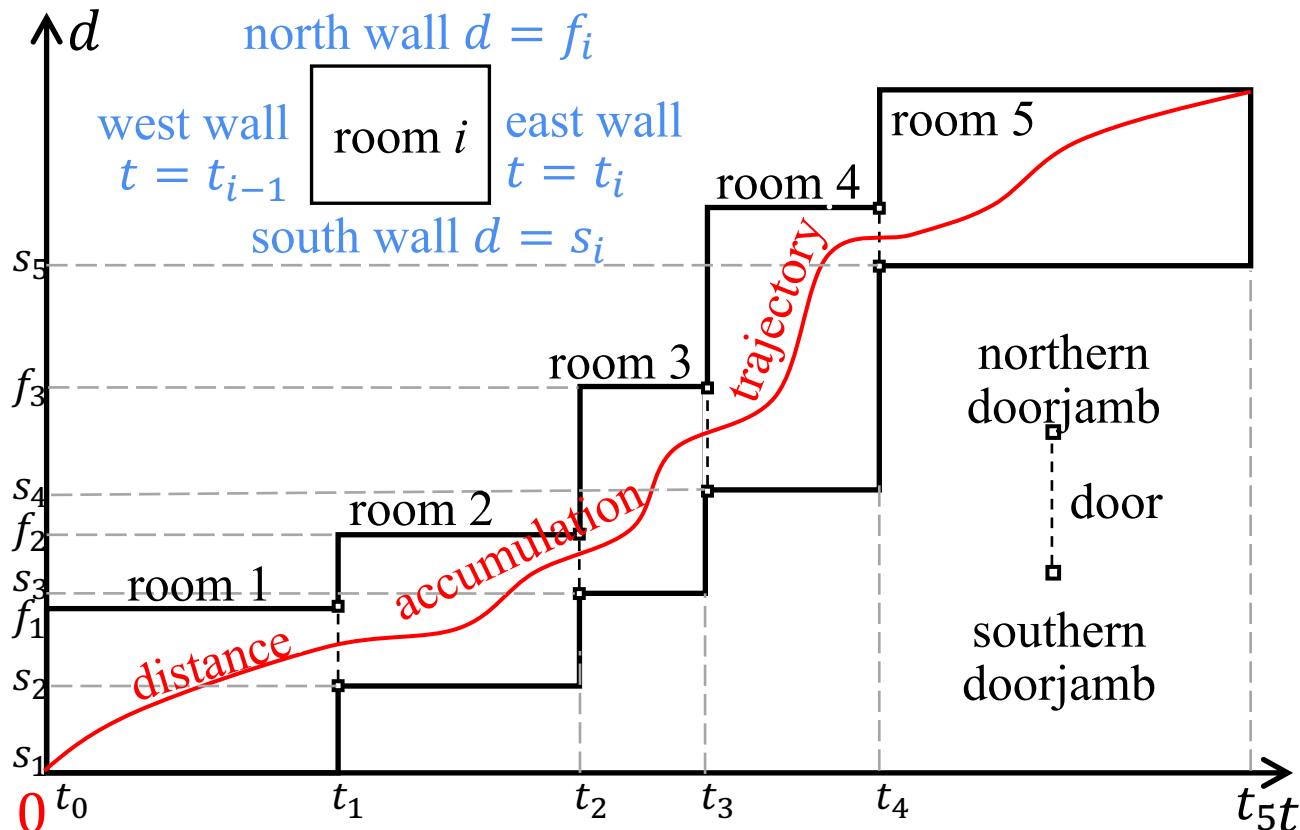
Crossing-the-Rooms problem

- Trajectory does not go freely on the diagram
- *completion constraint*: temporal on transmission times
- *range constraint*: spatial on transmission range



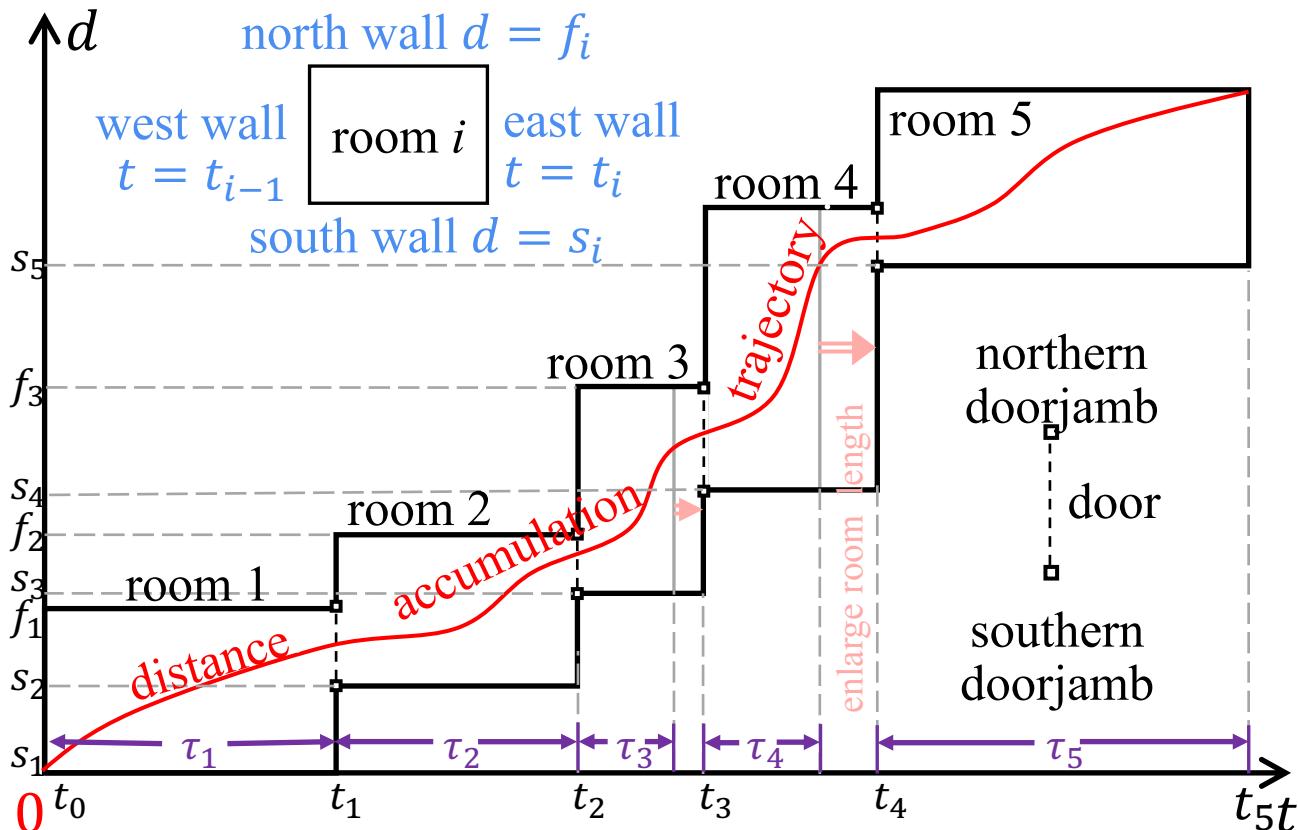
Crossing-the-Rooms problem

- For GN i , we draw a rectangle Room i : the north wall at $d = f_i$, the south wall at $d = s_i$, the west wall at $t = t_{i-1}$, the east wall at $t = t_i$



Crossing-the-Rooms problem

- *Crossing-the-rooms* problem essentially asks:
 1. how to determine the length of each room
 2. how to design the trajectory crossing all the rooms





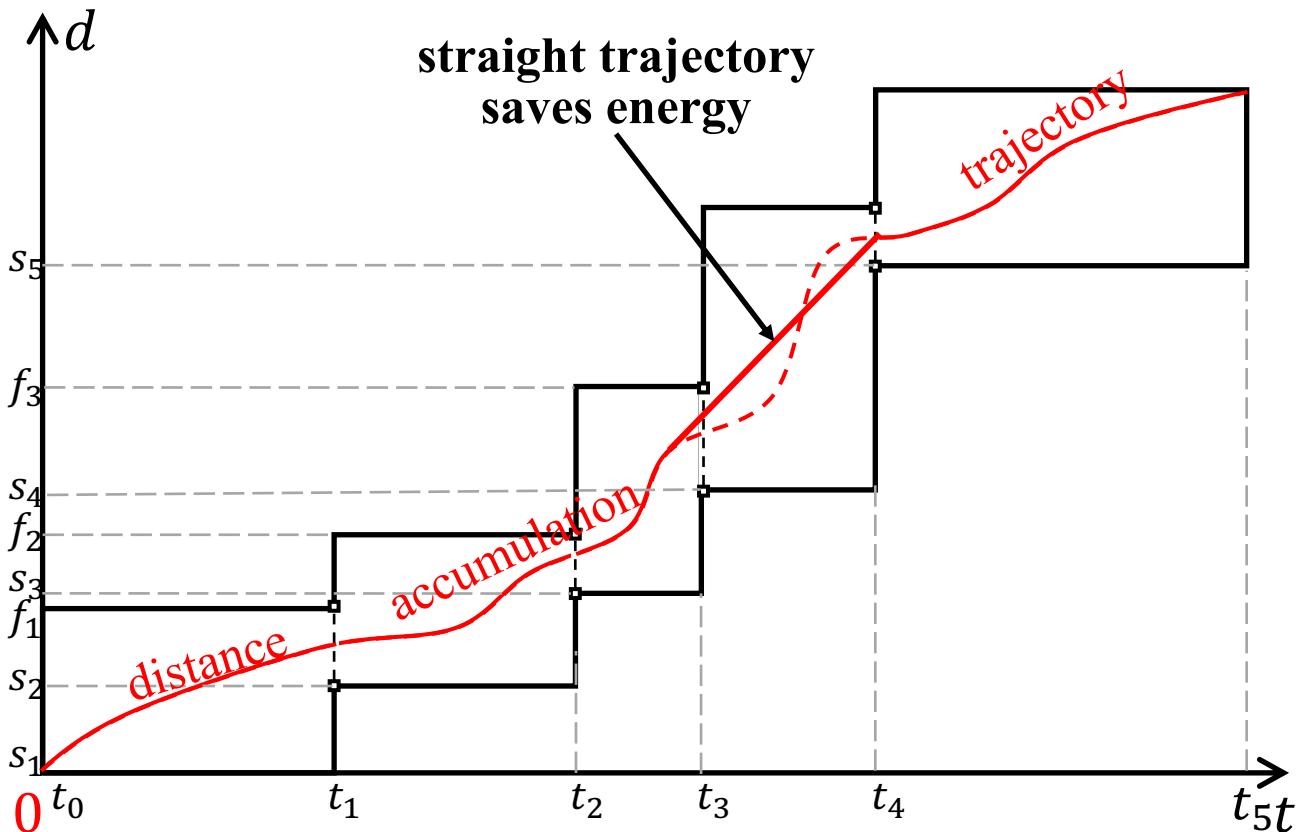
Crossing-the-Rooms problem

- *Crossing-the-rooms* problem essentially asks:
 1. how to determine the length of each room
 2. how to design the trajectory crossing all the rooms
 - equivalent to ask the GN transmission switching times
 - equivalent to ask the UAV speed scheduling function

Therefore, the solution is uniquely mapped to the solution for the original USS-GTS problem.

Theorem: straight trajectory saves energy

- **Theorem.** *The optimal trajectory is straight between any two points, as long as this is feasible.*





The proposed algorithm

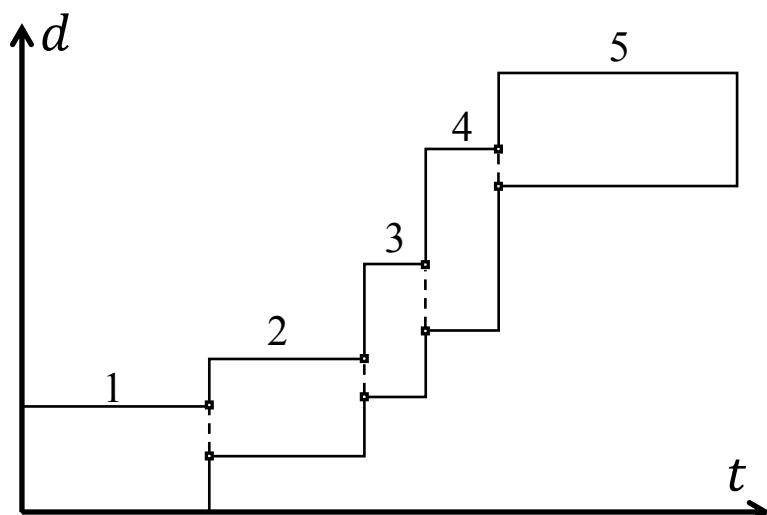
Algorithm 2: USS-GTS-GENERAL

```
1  $k = 0, d = 0, t_0 = 0;$ 
2  $s_{n+1} = f_n$  // dummy for loop purpose
3 while  $k < n$  do
4    $v_n^v = \infty, v_s^v = 0;$ 
5   for  $j = k + 1$  to  $n$  do
6      $t_j = t_{j-1} + \tau_j, v_n^d = (f_j - d)/(t_j - t_k),$ 
       $v_s^d = (s_{j+1} - d)/(t_j - t_k);$ 
7     if  $v_s^d > v_n^v$  then
8        $v_m = v_n^v, k_m = k_n^v, d_m = f_{k_n^v};$ 
9       break;
10    else if  $v_n^d < v_s^v$  then
11       $v_m = v_s^v, k_m = k_s^v, d_m = s_{k_s^v+1};$ 
12      break;
13    end
14    if  $v_n^v > v_n^d$  then  $v_n^v = v_n^d, k_n^v = j$  ;
15    if  $v_s^v < v_s^d$  then  $v_s^v = v_s^d, k_s^v = j$  ;
16  end
17  if  $v_n^v == v_s^v$  then  $v_m = v_n^v, k_m = n, d_m = f_n$  ;
18  if  $v_m > v^*$  then
19     $x = d;$ 
20    for  $i = k + 1$  to  $k_m$  do
21       $t_i = \max\{(s_i - x)/v^*, \tau_i\} + t_{i-1};$ 
22       $x = x + (t_i - t_{i-1})v^*;$ 
23    end
24  end
25  Connect  $(t_k, f_k)$  and  $(t_{k_m}, d_m)$ ;
26   $d = d_m, k = k_m;$ 
27 end
```

Looking before crossing rooms algorithm

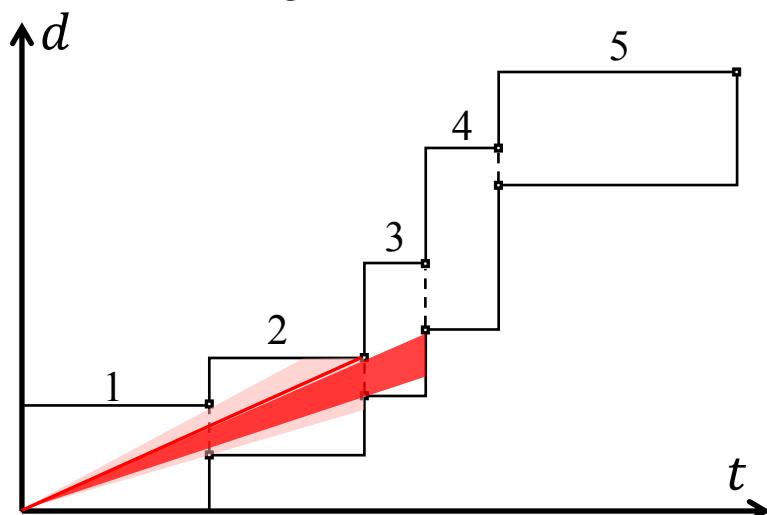
The algorithm works in three phases

1. Construct rooms
 - Room i with length τ_i , the minimal required time
2. Find a walking trajectory across rooms
3. Some room lengths are enlarged



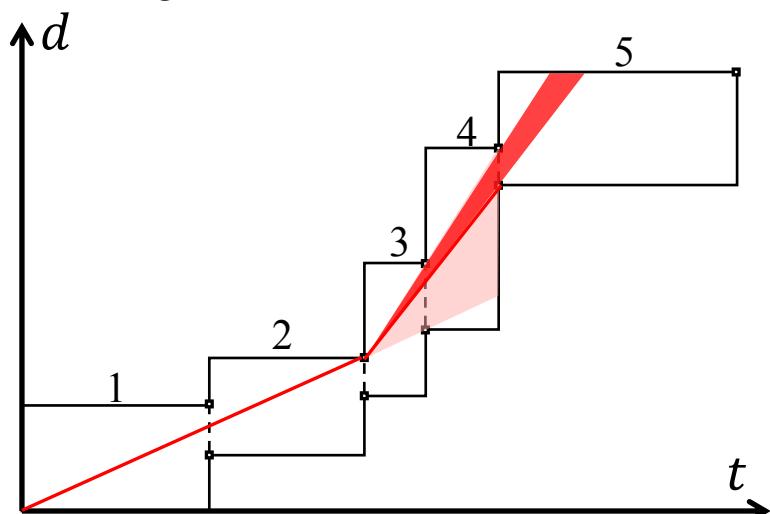
Looking before crossing rooms

- At origin, the view area through door 1 is in pink and view area through door 2 is in red.
- No view through door 3, which is beyond the northern boundary
- We walk along the northern boundary, reaching the farthest doorjamb.



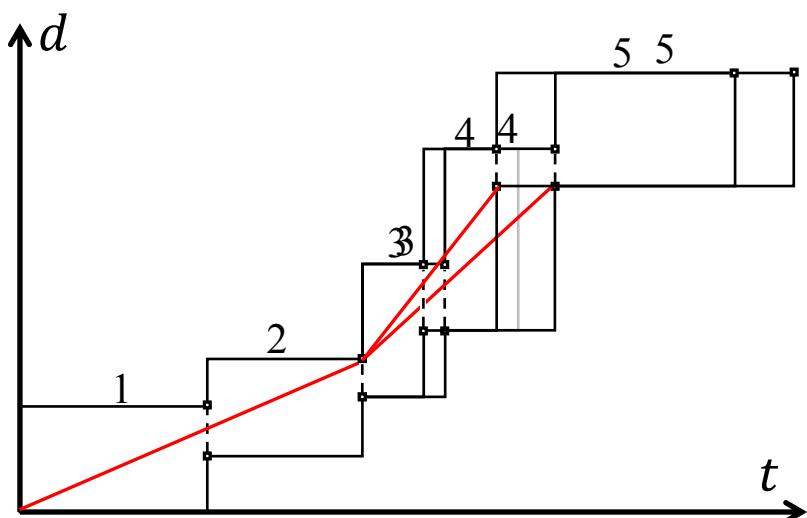
Looking before crossing rooms

- At the new position, two new view areas are in pink and red respectively.
- Since the northeast corner is beyond southern boundary of the current view area
- We walk along the southern boundary to the farthest doorjamb.



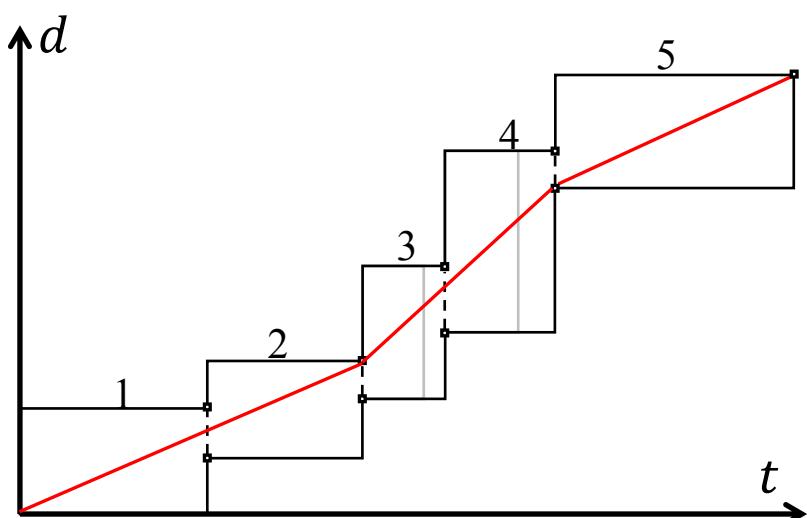
Looking before crossing rooms

- In room 3 and 4, trajectory slope larger than v^*
- **Theorem.** *Any point of the optimal trajectory has a slope no larger than v^* .*
- We enlarge the lengths of room 3 and 4 to reduce the slope to v^*



Looking before crossing rooms

- All room lengths and trajectory are determined
- **Theorem.** *Algorithm USS-GTS-GENERAL produces the optimal distance accumulation trajectory for the offline USS-GTS problem within $O(n^2)$ steps.*





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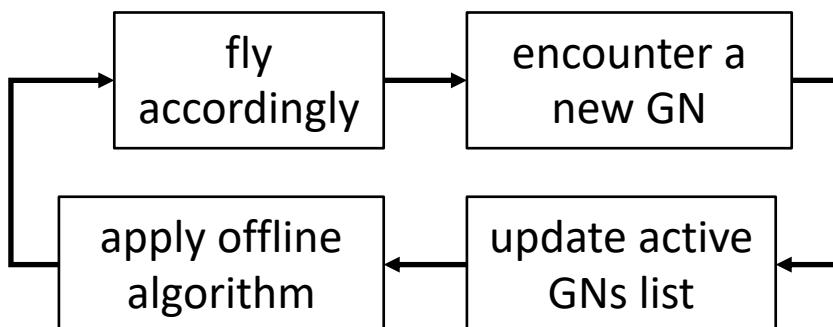
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Online heuristic algorithm

- Previous offline algorithm requires all information
- In the online algorithm, we assume the information of a GN can be obtained only if the UAV flies close

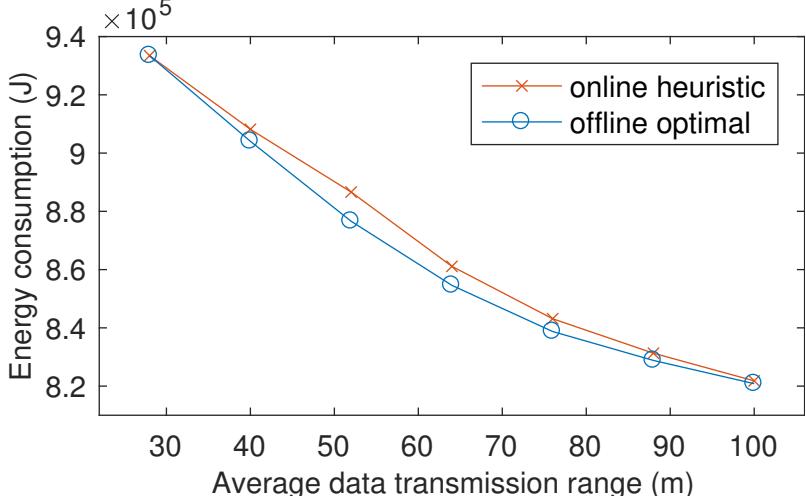
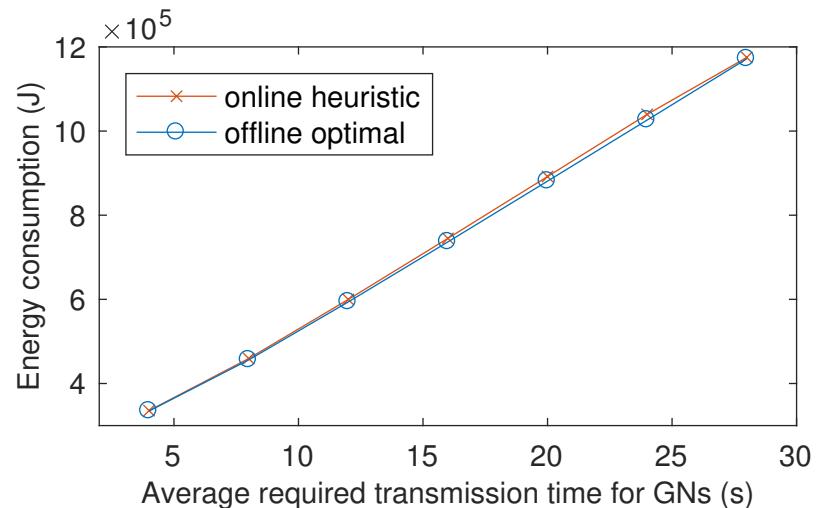
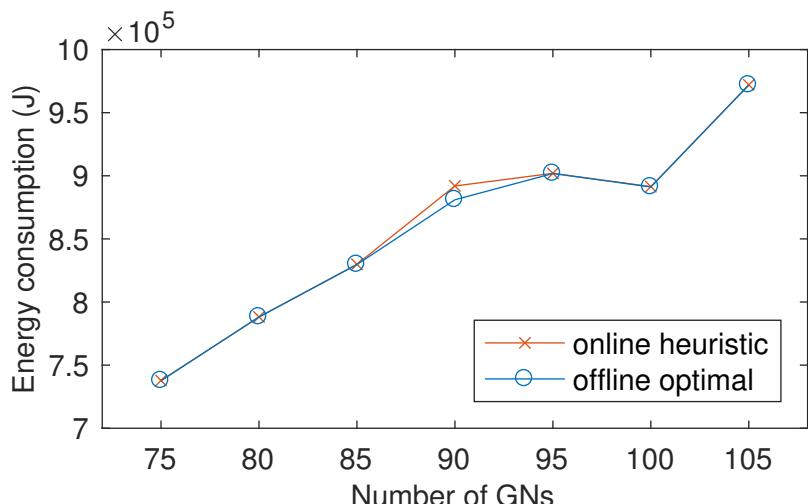
Online heuristic algorithm outline:



Simulation Results

- Performance comparison between online heuristic and offline optimal.

In all three settings, online heuristic performances near optimal.





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Conclusion

1. Investigate a UAV data collection problem from GNs deployed along a straight line
2. Real-world flight tests: a speed-related energy model
3. Propose the *looking before crossing* algorithm on time-distance diagram: the optimal offline solution
4. Present an online heuristic algorithm which performances near optimal.
5. Our study on the practical flight energy model and speed scheduling have shed light on a new direction on UAV-aided wireless communication.



Thank You!

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