



Energy-Efficient UAV Flight Planning for a General Pol-Visiting Problem with a Practical Energy Model

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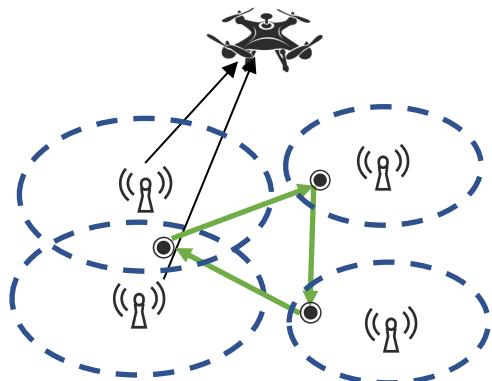
Outline

- ◆ **Background**
- ◆ **Problem Modeling**
- ◆ **Solution**
- ◆ **Simulation**
- ◆ **Conclusion**

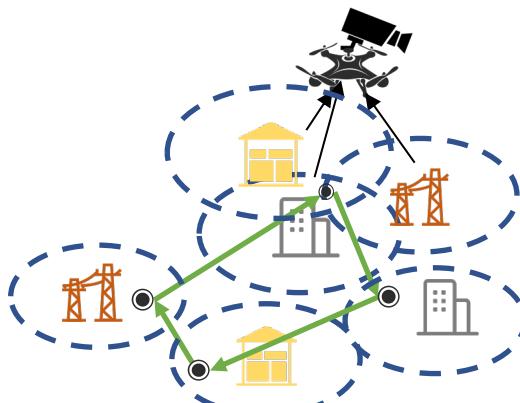
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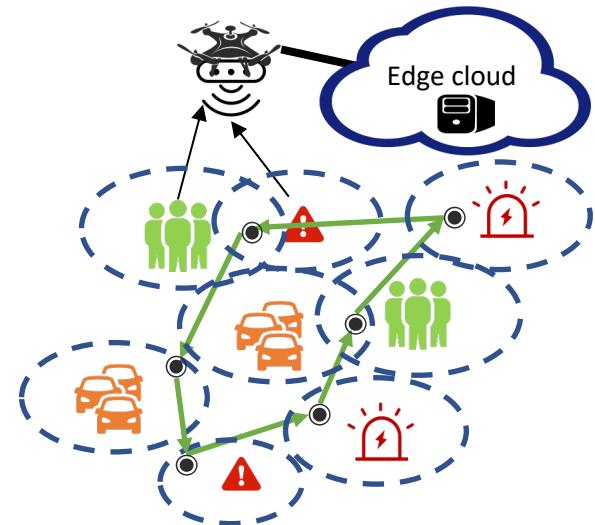
UAV application scenarios



Data collection



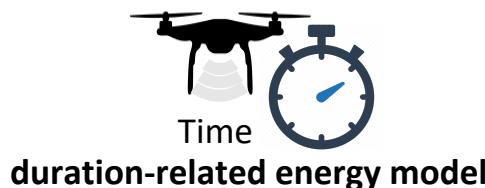
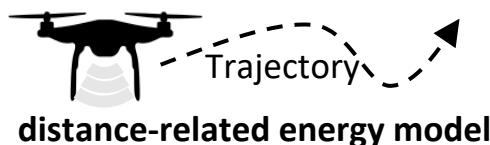
Surveillance & Monitor



Edge computing

Energy consumption problem of UAVs

- Limited energy supply on board
- Flight power **1000 times** communication power
- Related flight energy consumption models

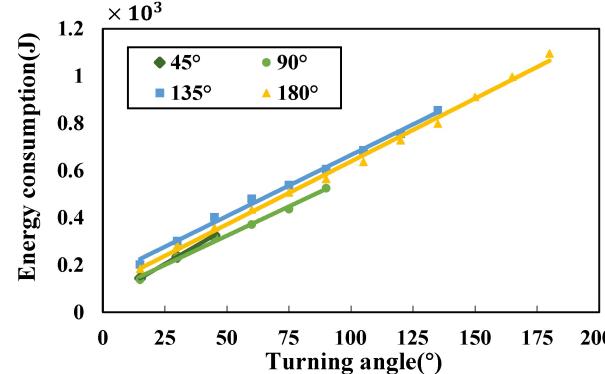
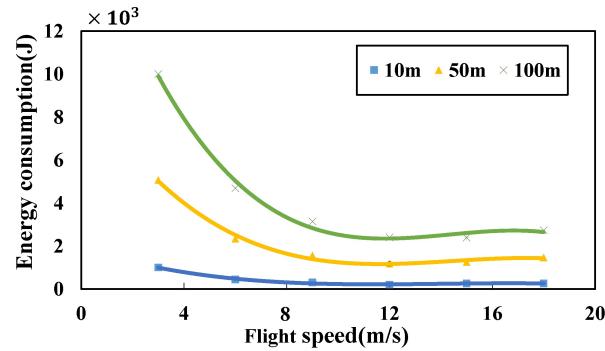
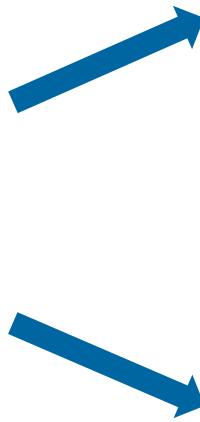


Too simple to be accurate

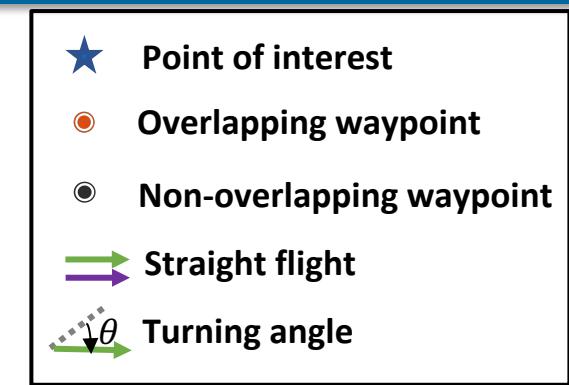
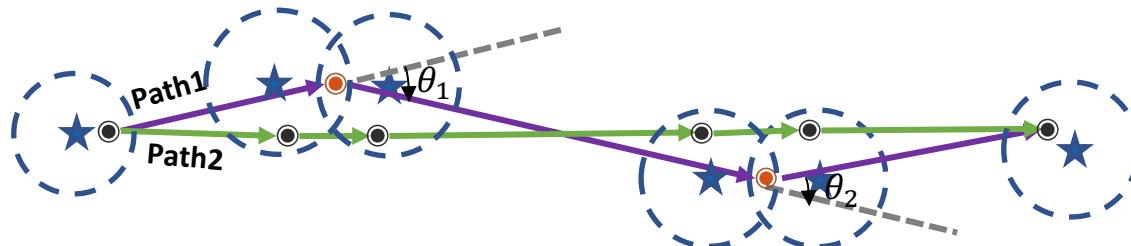
Our practical flight energy model



Our flight tests



Challenges to our problem



A two-fold tradeoff:

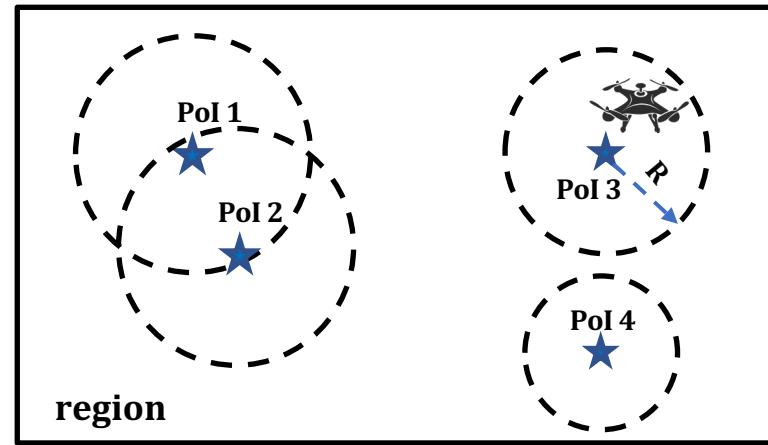
- waypoints and straight flight distance
- waypoints and turning angle and the number of switching

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System model

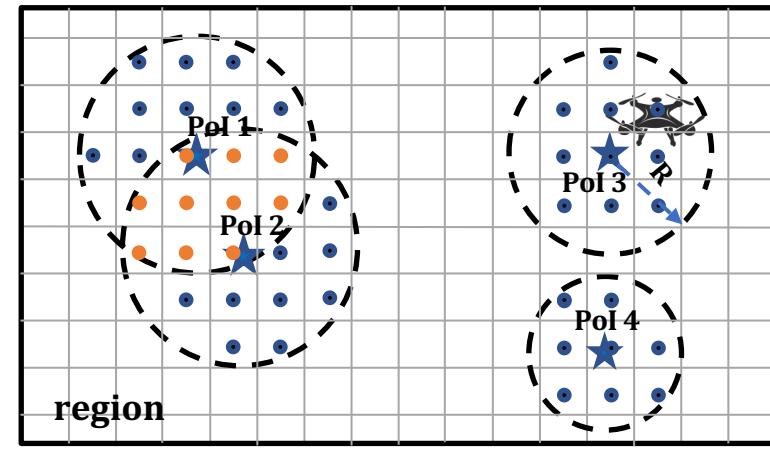
- N Pols are randomly located in a rectangle region.
- Each Pol has a circle range.
- The UAV files at a fixed height.



Original system model

System model

- Rasterize the region at a certain granularity.
- Take grid centers that fall within each Pol range as its candidate waypoints.
- Waypoints may overlap.



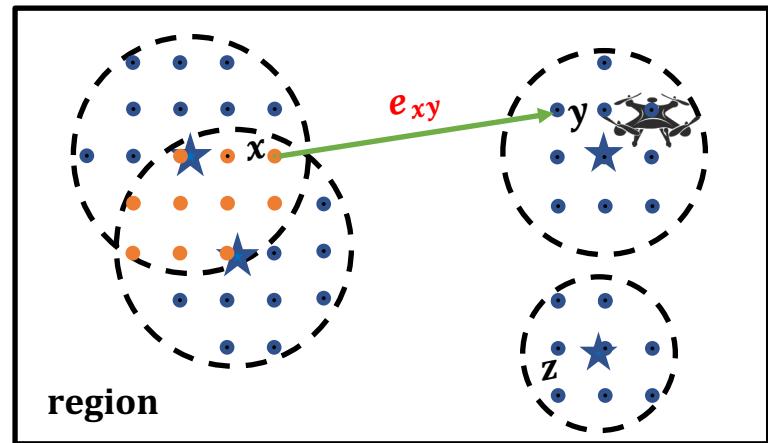
Rasterize region

Energy consumption model

- Straight flight energy consumption:

$$E(e_{xy}) = c_1 |e_{xy}| + c_1$$

$$E_C = \sum_{\forall x, \forall y} E(e_{xy}) w_{xy}$$

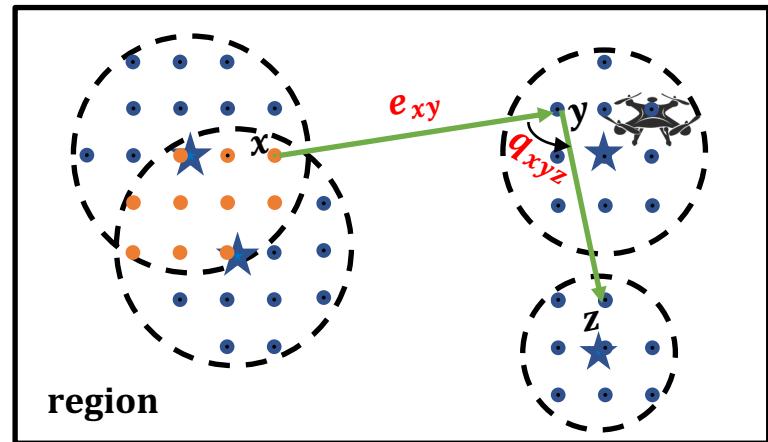


Energy consumption model

- Turning energy consumption:

$$E(q_{xyz}) = c_2 q_{xyz} + C_2$$

$$E_T = \sum_{\forall x, \forall y, \forall z} E(q_{xyz}) w_{xy} w_{yz}$$

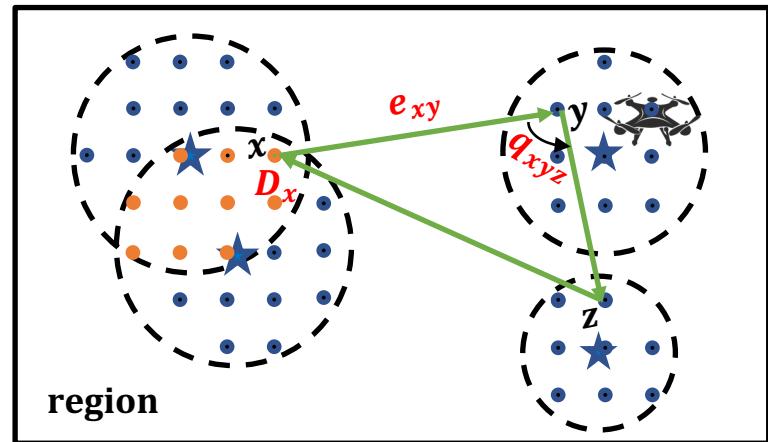


Energy consumption model

- Switching energy consumption:

$$E(D_x) = c_3(|D_x| - 1)$$

$$E_S = \sum_{\forall x} E(D_x)$$

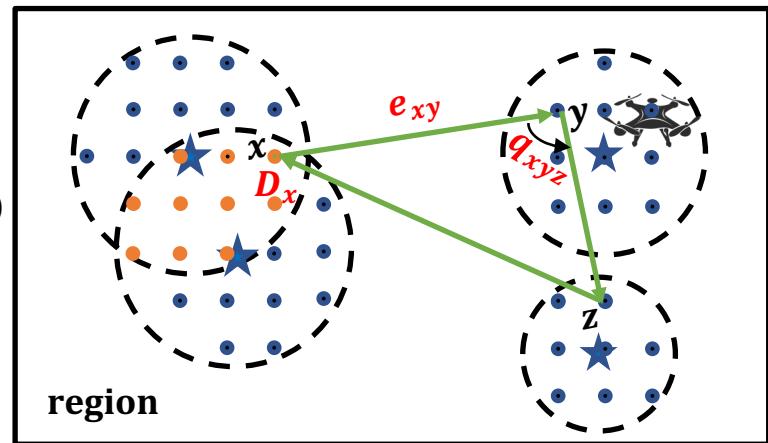


Energy consumption model

- Total UAV energy consumption:

$$E_{ALL} = E_C + E_T + E_S$$

$$= \sum_{\forall x, \forall y} E(e_{xy}) w_{xy} + \sum_{\forall x, \forall y, \forall z} E(q_{xyz}) w_{xy} w_{yz} + \sum_{\forall x} E(D_x)$$



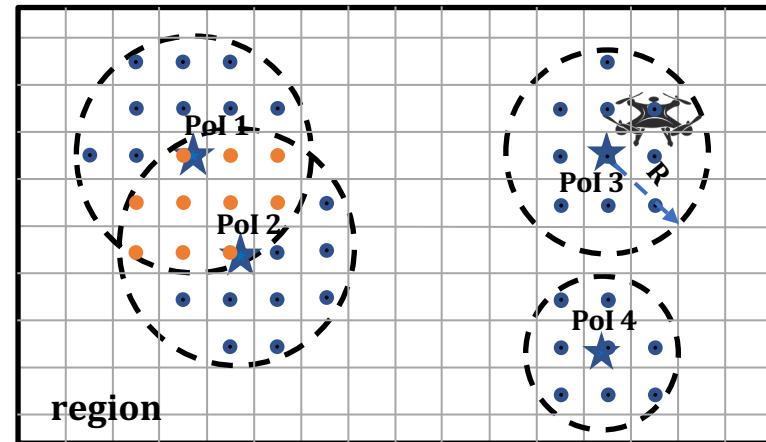
System model

1. Visiting constraint

- Visit each Pol at least once.

2. Range constraint

- Visit each Pol within its range.



Waypoint-based Pol-visiting problem

Waypoint-based Pol-visiting problem : find a route to

△ minimize UAV energy consumption E_{ALL}

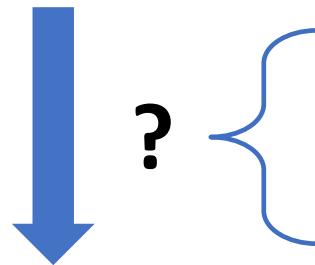
- satisfy visiting constraint
- satisfy range constraint

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Problem Transformation

Waypoint-based Pol-visiting problem

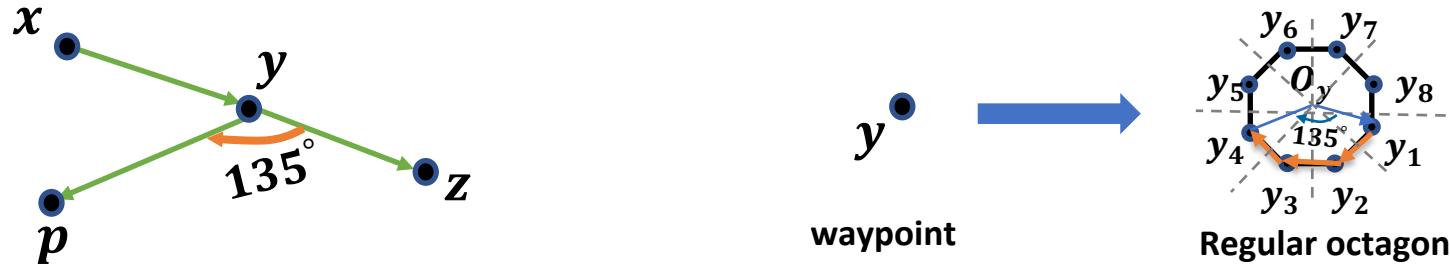


Turning energy consumption
Switching energy consumption

Generalized traveling salesman problem

Modeling energy cost of making turns

- How to embed the energy cost of **making turns** into a graph?

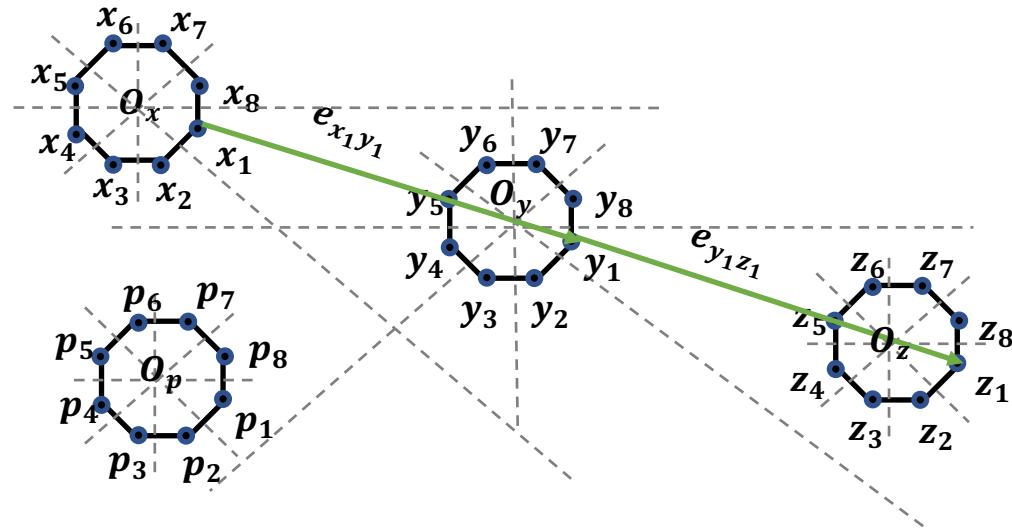
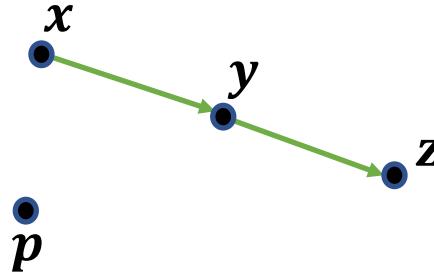


Turning energy cost : $E(q_{xyp}) = E(135^\circ)$

$$E(q_{xyp}) = E(e_{y_1y_2}) + E(e_{y_2y_3}) + E(e_{y_3y_4})$$

Modeling energy cost of making turns

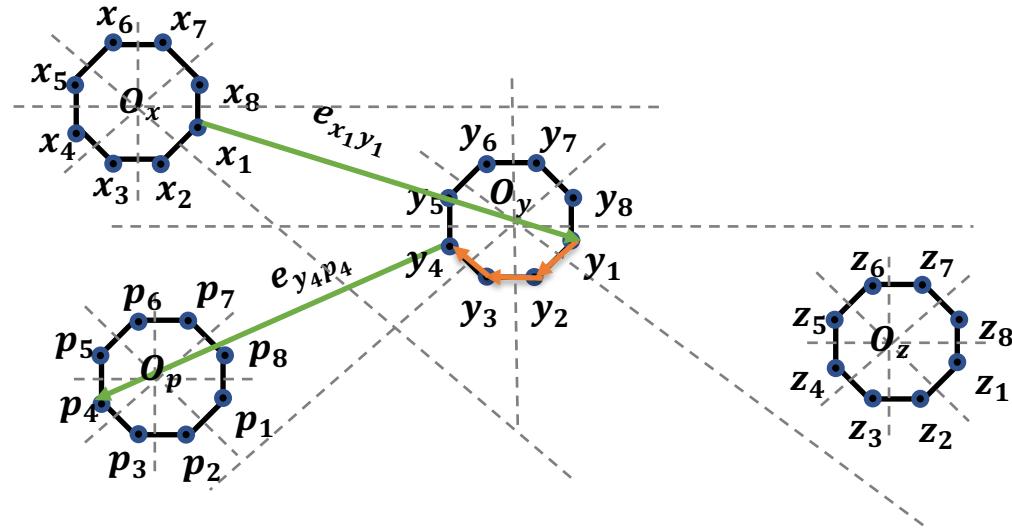
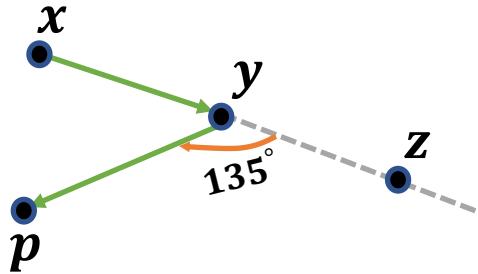
- How to embed the energy cost of **making turns** into a graph?



No turning energy cost

Modeling energy cost of making turns

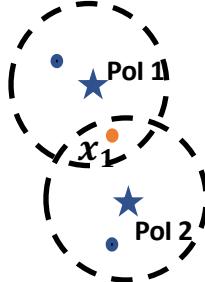
- How to embed the energy cost of **making turns** into a graph?



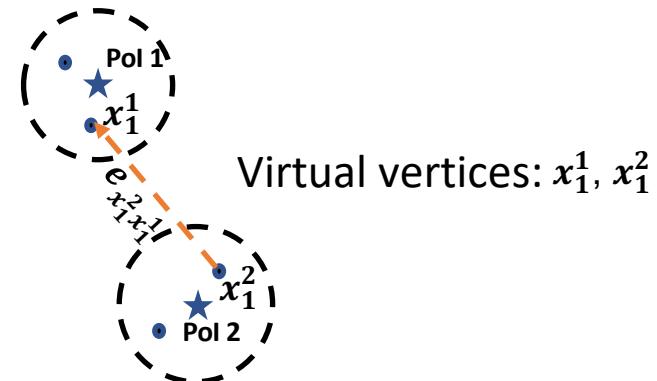
135° turning energy cost

Modeling energy cost of Pol-switching

- How to embed the energy cost of **Pol-switching** into a graph?



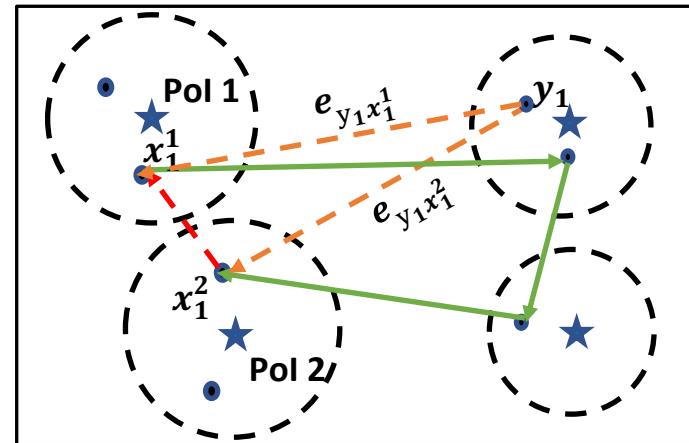
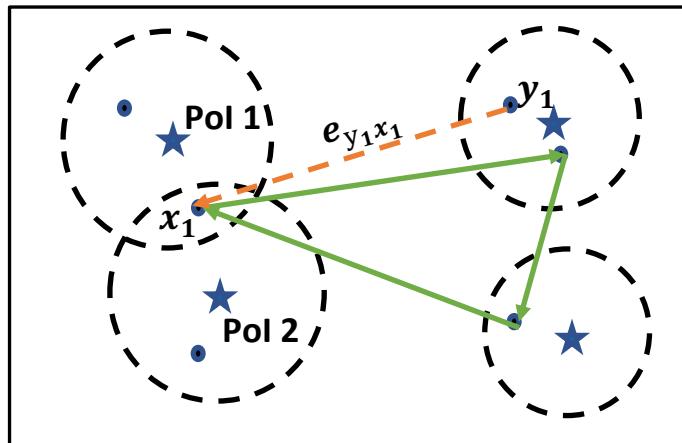
Switching energy cost : $E(D_{x_1}) = E(1)$



$E(D_{x_1}) = E(e_{x_1^2 x_1^1})$

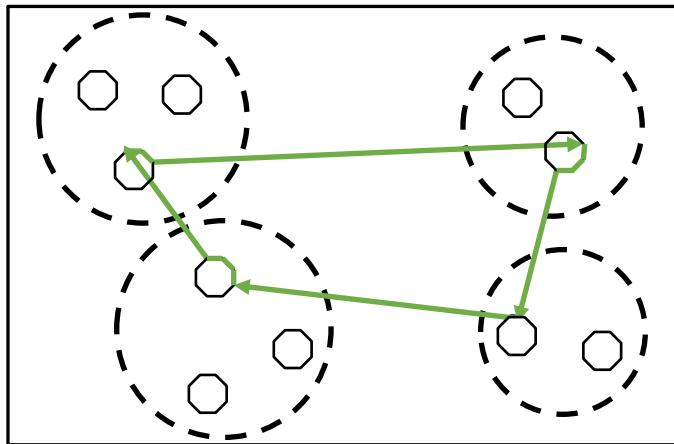
Modeling energy cost of Pol-switching

- How to embed the energy cost of Pol-switching into a graph?



Redefinition of the problem

- Given a directed weighted graph $D = (S, E, W)$, to find a cycle to visit each subset at least once with the minimum sum of weights of all visiting-edges.



Redefinition of the problem

- Objective function:

$$\text{Min} \sum_{v_i, v_j \in S, < v_i, v_j > \in E} c_{ij} w_{ij}$$

Waypoint-based Pol-visiting problem

- Constraints:

1. Subset coverage
2. Tour continuity
3. Subloop avoidance



redefine

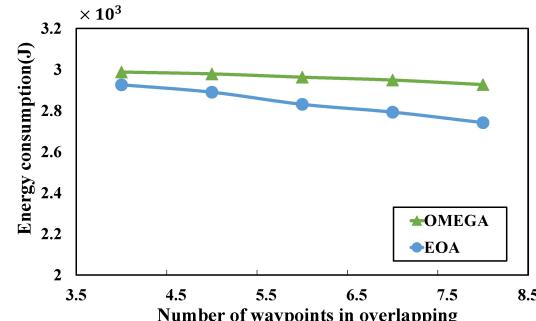
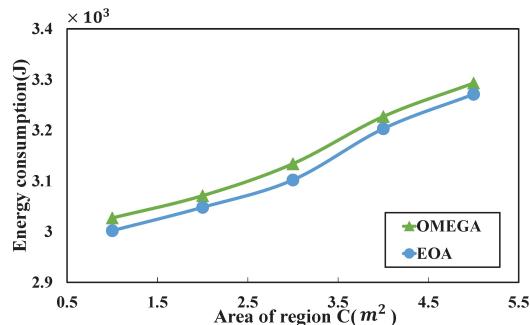
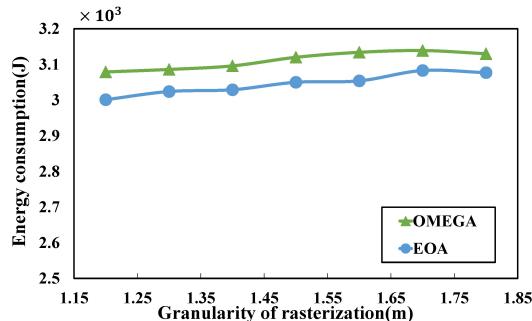
Generalized traveling salesman problem

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Simulation

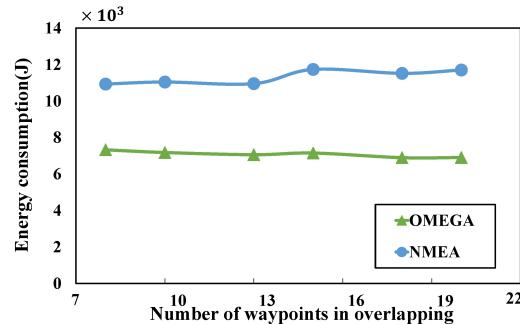
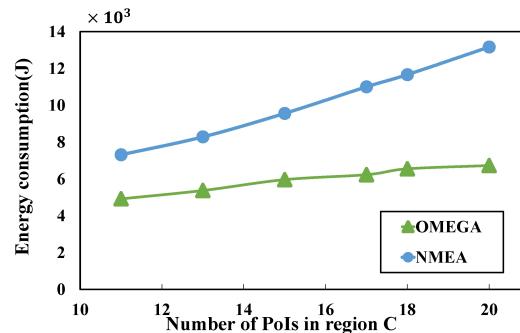
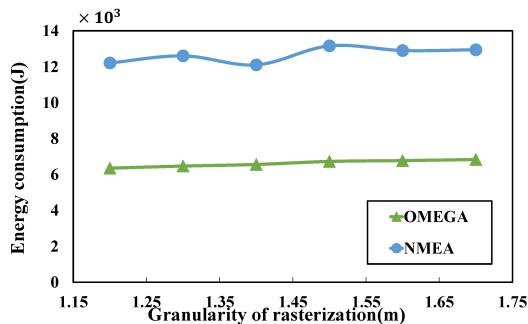
- Small scale problem



→ OMEGA spends < 107% of the energy of EOA.

Simulation

- Large scale problem



→ OMEGA saves ~50% more energy than NMEA.

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Conclusion

1. Real-world flight tests: a more practical energy model.
2. Investigate the general waypoint-based Pol-visiting problem to find a tour with the minimum UAV energy cost.
3. Propose a graph-based algorithm to transfer the problem into a classic graph problem.
4. Conduct simulations to evaluate the performance of our proposed algorithm.

Thank You!

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