

Notch-mediated lateral inhibition regulates proneural wave propagation when combined with EGF-mediated reaction diffusion

Makoto Sato^{a,b,c,1,2}, Tetsuo Yasugi^{a,1}, Yoshiaki Minami^d, Takashi Miura^{c,e}, and Masaharu Nagayama^{c,f}

^aMathematical Neuroscience Unit, Institute for Frontier Science Initiative, Kanazawa University, Ishikawa 920-8640, Japan; ^bLaboratory of Developmental Neurobiology, Graduate School of Medical Sciences, Brain/Liver Interface Medicine Research Center, Kanazawa University, Ishikawa 920-8640, Japan; ^cCore Research for Evolutional Science and Technology, Japan Science and Technology Agency, Saitama 332-0012, Japan; ^dGraduate School of Science, Hokkaido University, Hokkaido 060-0810, Japan; ^eGraduate School of Medical Sciences, Kyushu University, Fukuoka 812-8582, Japan; and ^fResearch Institute for Electronic Science, Hokkaido University, Hokkaido 060-0811, Japan

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Notch-mediated lateral inhibition regulates binary cell fate choice, resulting in salt and pepper patterns during various developmental processes. However, how Notch signaling behaves in combination with other signaling systems remains elusive. The wave of differentiation in the Drosophila visual center or "proneural wave" accompanies Notch activity that is propagated without the formation of a salt and pepper pattern, implying that Notch does not form a feedback loop of lateral inhibition during this process. However, mathematical modeling and genetic analysis clearly showed that Notch-mediated lateral inhibition is implemented within the proneural wave. Because partial reduction in EGF signaling causes the formation of the salt and pepper pattern, it is most likely that EGF diffusion cancels salt and pepper pattern formation in silico and in vivo. Moreover, the combination of Notch-mediated lateral inhibition and EGF-mediated reaction diffusion enables a function of Notch signaling that regulates propagation of the wave of differentiation.

Notch | lateral inhibition | EGF | reaction diffusion | proneural wave

Notch signaling is evolutionarily conserved throughout the animal kingdom and regulates various biological processes. In particular, when the expression of its ligand and targets are not predetermined but are regulated by Notch signaling interplay between neighboring cells (Fig. 1A), lateral inhibition takes place. Notch-mediated lateral inhibition plays an essential role in specifying differentiated cells from a sheet of undifferentiated cells in a spatially regulated manner (1, 2). During the development of the nervous system, neural precursor cells and neuroepithelial cells (NEs) form a salt and pepper pattern as a result of Notch-mediated lateral inhibition (Fig. 1 A and B). The differentiating cells up-regulate the basic helix-loop-helix proneural transcription factors of the Drosophila Achaete-Scute Complex (AS-C) family in the process of becoming neural precursors. These factors induce the expression of Delta (Dl), a Notch ligand, in differentiating cells (3). Because DI is a transmembrane ligand, it activates the Notch receptor only in neighboring cells, which remain undifferentiated and eventually become epithelial cells. In undifferentiating cells, Notch activity downregulates AS-C expression to prevent neural differentiation and Dl expression. Furthermore, Dl autonomously represses Notch in differentiating cells through the process of cis-inhibition (4, 5). Consequently, differentiating cells send stronger Notch signals and undifferentiating cells send weaker Notch signals to neighboring cells, establishing a binary cell fate and resulting in a salt and pepper pattern. Notch-mediated lateral inhibition takes place when DI expression is not predetermined but is under the control of Notch signaling and/or AS-C expression and was first discovered by fly geneticists (2). Its system behavior has been extensively studied via mathematical modeling (6, 7).

Notch signaling plays more diverse roles when combined with other signaling systems. For example, Notch and EGF cooperate to regulate vulval development in *Caenorhabditis elegans* and photoreceptor cell differentiation in the fly retina (8–10). When the interplay between Notch and other signaling includes complex feedback with oscillatory behavior, the role of Notch becomes difficult to study without mathematical models. For example, vertebrate segmentation is controlled by the interplay between Notch and FGF, including multiple negative feedbacks. Interdisciplinary approaches have revealed that oscillatory gene networks constitute the segmentation clock machinery (11, 12).

The waves of differentiation in visual system development are key examples of such complex interplays between Notch and other signaling systems. The development of the retina in fly, fish, and chicken includes waves of differentiation that accompany Notchmediated lateral inhibition and secreted factors, such as Hedgehog, that trigger neural differentiation (13-16). During the propagation of the differentiation wave, the expression of Dl and proneural genes is not predetermined, but always accompanies the propagating wave. Therefore, many of the theoretical studies regard the mode of Notch action during wave propagation as lateral inhibition. Previous mathematical modeling has revealed essential roles for Notch signaling in the formation of a salt and pepper pattern of photoreceptor neurons (17-20). Although it was suggested that DI restricts wave propagation during eye development (17), Notch signaling is also required for undifferentiated cells to acquire a proneural state before the wave progression in

Significance

Notch-mediated lateral inhibition regulates binary cell fate choice, resulting in salt and pepper patterns during various developmental processes. The wave of differentiation in the *Drosophila* visual center accompanies Notch activity that is propagated without the formation of a salt and pepper pattern, implying that Notch does not regulate lateral inhibition during this process. In this study, by combining mathematical modeling and genetic analysis, we showed that Notch-mediated lateral inhibition is implemented within the proneural wave. The combination of Notch-mediated lateral inhibition and EGF-mediated reaction diffusion enables a function of Notch signaling that regulates propagation of the wave of differentiation.

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¹M.S. and T.Y. contributed equally to this work.

²To whom correspondence should be addressed. Email: makotos@staff.kanazawa-u.ac.jp.

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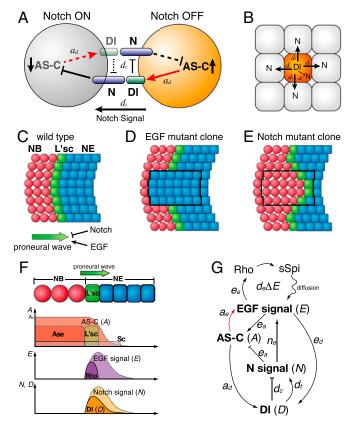


Fig. 1. The molecular mechanisms of Notch-mediated lateral inhibition and proneural wave progression. (A) Notch signaling between two cells mediates the binary cell fate decision. (B) The differentiating cells prevent the neighboring cells from differentiating via DI/Notch signaling. (C-F) The proneural wave sweeps across the NE sheet (blue). The NE cells express L'sc (green), triggering the differentiation from NE to NB (red). (C) The WT. (D and E) In clones mutant for EGF and Notch signaling (black lines), the proneural wave is eliminated and accelerated, respectively. (F) A schema showing the relative distributions of AS-C family (L'sc, Sc, and Ase), Rho and DI expression, and the activities of EGF and Notch signaling. (G) A schema showing the relationship between the EGF signal (E), Notch signal (N), DI expression (D), and AS-C expression (A). Black and red arrows are based on known observations and findings in this work, respectively.

the fly retina (21, 22). Therefore, the loss of Notch signaling causes the loss of photoreceptor differentiation, which conflicts with the prediction of the above theoretical study, in which the early proneural function of Notch was not implemented (17). The previous in vivo studies using the fly retina did not specifically inhibit the later function of Notch to examine its role to suppress the wave propagation (21, 22).

A wave of differentiation has also been observed in the developing fly brain. In this study, we focused on a wave of differentiation called the "proneural wave" (23, 24), which occurs in the largest component of the fly visual center, the "medulla." During proneural wave progression, the sheet-like NEs sequentially differentiate to neural stem cells called neuroblasts (NBs) (Fig. 1 C and F). The differentiation boundary is defined by the transient expression of the proneural transcription factor Lethal of scute (L'sc) in NEs, which acts as a trigger of differentiation. The proneural wave sweeps across the NE sheet as L'sc expression progresses, and all NEs eventually differentiate into NBs without exhibiting the salt and pepper pattern. EGF and Notch play central roles in this process by positively and negatively regulating wave progression, respectively (Fig. 1 D and E) (25–27). The ligands of the EGF and Notch signaling pathways are produced in L'sc-positive NEs immediately before NB differentiation. These pathways induce their own ligand production, forming positive feedback loops (26, 27). Additionally, EGF and Notch positively regulate each other to form a mutual feedback loop (Fig. 1G) (27). The wave progression and NB differentiation are eliminated in EGF mutant clones and accelerated in Notch mutant clones (Fig. 1 D and E). A significant decrease in the number of NBs and neurons is observed in Notch mutant brains, because NEs are precociously differentiated to NBs before they extensively proliferate via symmetric division (25, 27). Additionally, JAK/STAT and Hippo signaling has also been shown to regulate the proneural wave progression (24, 26, 28). Among these signaling systems, ligand expressions and signal activations of EGF and Notch are restricted to the cells nearby the wave front. In this study, we focused on the roles of EGF and Notch that constitute the central components of the proneural wave.

There are critical differences between the proneural wave and the waves of differentiation in the retina. (i) During development of the retina, the distribution of differentiated cells exhibits a salt and pepper pattern (29). By contrast, all NE cells eventually differentiate to NBs during proneural waves without exhibiting a salt and pepper pattern (24). Nevertheless, all of the components required for lateral inhibition are expressed in the proneural wave and the expression of Dl and AS-C is not predetermined, but accompanies wave progression. (ii) The loss of Notch signaling clearly indicates acceleration of proneural wave propagation and precocious differentiation of NBs in vivo (26, 27) in contrast to the loss of differentiation phenotype observed in the fly retina, in which the early proneural function of Notch was impaired (22). The proneural function of Notch has not been observed in the proneural wave (27). Thus, Notch signaling seems to regulate the speed of proneural wave propagation instead of generating the salt and pepper pattern by unidentified mechanisms. Does Notch form a lateral inhibitory feedback? If so, how does Notch control wave propagation without forming a salt and pepper pattern? By combining mathematical modeling and genetic analysis, we show that EGF diffusion cancels salt and pepper pattern formation and that Notchmediated lateral inhibition plays a role in the control of proneural wave propagation when combined with EGF-mediated reaction diffusion.

Our results also suggest that the difference between the retinal wave and the proneural wave is much smaller than it looks and that the core mechanisms of the wave progression are conserved because both systems include Notch-mediated lateral inhibition. The comparative analyses of the two systems in silico and in vivo will expand our understanding of the wave of differentiation.

Results

Establishing the Four-Component Model. During proneural wave progression, no salt and pepper pattern is observed in the distribution of NB and Notch activity (Fig. 1*C*) (24, 26, 27). Thus, the model of Notch-mediated lateral inhibition is superficially inconsistent with the proneural wave. However, the proneural wave is associated with Dl, Notch, and proneural genes, which form a feedback loop of lateral inhibition during neural precursor differentiation processes. Therefore, it is very unlikely that the behavior of Notch signaling is completely different from that of lateral inhibition. We assume that these components form a feedback loop of lateral inhibition.

Contradicting this notion, DI is expressed in Notch-ON cells, and DI expression is up-regulated by the activation of Notch signaling during proneural wave progression as shown previously (Fig. 1F) (26, 27). During Notch-mediated lateral inhibition, the down-regulation of DI expression in Notch-ON cells is essential for establishing binary cell fate (Fig. 1A). However, DI expression may be indirectly activated by Notch signaling via EGF signaling, because EGF and Notch signaling pathways are mutually dependent, and DI expression remains in Notch mutant clones as shown previously (Fig. 1G) (27, 30). Additionally, DI expression is up-regulated in clones in which EGF signaling is activated (31). To

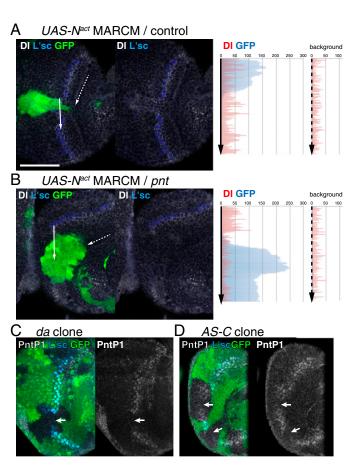


Fig. 2. Notch activity along the proneural wave. The proneural wave in vivo in late third instar larval brain (anterior to the left and dorsal to the top). (A) In cells expressing the active form of Notch (GFP-positive; green), L'sc (blue) is suppressed, and DI (white) is induced (white arrow). (B) In pnt mutant cells expressing the active form of Notch, L'sc and DI are suppressed (white arrow). Left shows the expression levels of DI (red) and GFP (blue) along the arrows (mutant clones), and Right shows the expression levels of DI (red) and GFP (blue) along the dashed arrows (background) in A and B. (C) L'sc (blue) and PntP1 (white) are reduced in da mutant clone visualized by the absence of GFP (green). (D) L'sc (blue) is eliminated and PntP1 (white) is reduced in clones homozygous for Df(1)260–1 visualized by the absence of GFP (green). (Scale bar: 50 μm.)

confirm this idea in vivo, we performed the following genetic experiments. In clones expressing the constitutively active form of Notch, Dl expression was activated, despite the absence of L'sc expression (Fig. 24) (n=11 of 17) (26). However, Dl expression was suppressed by the *pnt* mutation, which eliminates EGF signaling (Fig. 2B) (n=22 of 22), in the presence of the active form of Notch. These results suggest that Dl expression is not directly activated by Notch but is primarily activated by EGF signaling in vivo (Fig. 1G). These observations imply that EGF, Dl, Notch, and AS-C are all essential for understanding proneural wave progression. Therefore, we formulated a four-component model of the proneural wave using a reaction diffusion system for EGF and a lateral inhibition system for Notch based on previous observations and our own findings (Figs. 1G, black and red arrows, respectively, and 3A) (23, 24, 26, 27, 30, 31).

In this model, E is a composite variable for the EGF ligand concentration and EGF signaling. The rate of change in E is influenced by its diffusion $(d_e\Delta E)$, degradation (k_eE) , EGF signaling (e_eE) , and Notch signaling (n_eN) . The diffusion of E was calculated as described in *Methods*. N and D are variables for Notch signal activity and DI expression, respectively. N is influenced by its

degradation (k_nN) , trans-activation by DI expression in adjacent cells (trans-DI; d_iD), and cis-inhibition by the autonomous action of DI (cis-DI; d_cD) (4, 5). Notch receptor expression levels are largely uniform in NEs in vivo (25, 30) and constant in our model. D is regulated by its degradation (k_dD) and EGF signaling (e_dE) , because EGF signaling induces DI transcription (31, 32). A is an abstract value specifying the state of differentiation (A = 0 in undifferentiated NE, $A = A_0$ in differentiated NB, and $A_0 = 1$ in the followings). We assume that A is intimately related to the expression levels of AS-C proteins. Among AS-C family proteins, at least

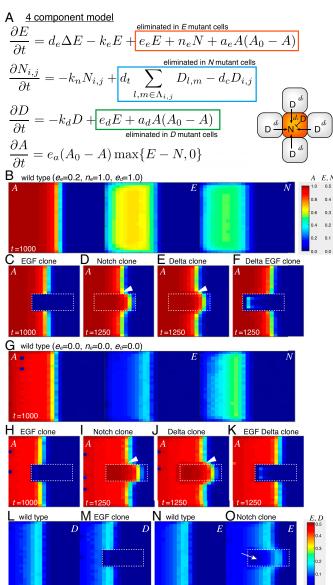


Fig. 3. The four-component model. (*A*) The four-component model. (*B–F*) Results of in silico experiments visualizing *A*, *N*, and *E* ($e_e = 0.2$ and $n_e = e_d = 1.0$). Mutant clones are surrounded by white dotted lines. (*B*) The WT. (*C*) EGF mutant clone. (*D*) Notch mutant clone. (*E*) DI mutant clone. (*F*) DI EGF double-mutant clone. (*D* and *E*) Proneural wave is nonautonomously accelerated (arrowheads). (*G*–*O*) Results of in silico experiments in the absence of the feedbacks ($e_e = n_e = e_d = 0$). Mutant clones are surrounded by white dotted lines. (*G–K*) The results of the WT and mutant clones are very similar to those in *B–F*. (*L* and *M*) *D* is down-regulated in EGF mutant clone. (*N* and *O*) *E* is down-regulated in Notch mutant clone (arrow). (*F* and *K*) The residual *A* value inside the DI EGF double-mutant clone is most likely caused by EGF diffused from the WT cells.

L'sc, Sc, and Ase are expressed near the wave front of the proneural wave and act redundantly to trigger NB differentiation (24, 30, 33). Because AS-C expression is positively and negatively regulated by E and N, respectively, A should be similarly regulated by E and N. After NEs become NBs, they stop producing EGF ligand and DI and start producing multiple types of neurons (34, 35). In differentiated NBs $(A = A_0)$, the state of differentiation must be maintained, because NB differentiation is an irreversible process. This property is incorporated in the model by setting the rate of change of A as $e_a(A_0 - A)\max\{E - N, 0\}$. When N is greater than E, the value of E - N is zero to avoid dedifferentiation of differentiating cells. AS-C triggers the expression of Dl (3). The loss of AS-C function in the da mutant clone, in which AS-C cannot heterodimerize with Da, reduces or delays the onset of EGF signaling as visualized by PntP1 expression (n = 8 of 46) (Figs. 1G, red arrow and 2C). Similar results were obtained in clones deficient for AS-C (n = 13 of 29) (Fig. 2D). Thus, A up-regulates E and D. However, EGF ligand and Dl are only produced at the interface between undifferentiated and differentiated cells but not produced in differentiated NBs. Thus, we include the EGF and Dl production terms $a_e A(A_0 - A)$ and $a_d A(A_0 - A)$, respectively (Fig. 3A).

Four-Component Model Reproduces Proneural Wave Progression. Before the initiation of the proneural wave at the second larval instar stage, L'sc expression and the activation of EGF and DI expression were observed in optic lobe cells adjacent to the central brain (Fig. S1). Thus, moderate levels of A, E, and D in the anteriormost cells in the NE field are the initial conditions of the proneural wave in our in silico experiments (Methods). As a first step, we assumed that the magnitudes of the reaction rates for these molecules are equivalent in vivo. Thus, all parameters, except e_a , e_e , d_t , and d_c , were set to one in the computer simulation of the four-component model; e_e was set smaller than the degradation rate of EGF $(k_e E)$, because EGF does not increase infinitely in vivo. As a typical value, e_e was set to 0.2 unless otherwise noted; d_t was set to 0.25 to make Notch signaling comparable with EGF signaling, because one cell receives Dl from as many as four neighboring cells (Fig. 3A). The effects of trans-activation and cisinhibition by DI were set as equivalent ($d_c = 0.25$); e_a seems to determine the speed of differentiation and is not crucial for reproducing the following in silico experiments. For example, similar results were obtained for $e_a = 1$, $e_a = 4$, and $e_a = 10$ (Fig. S2). We set $e_a = 10$, because this condition is more robust to changes in other parameter values.

Stochastic noise is required for Notch-mediated lateral inhibition to establish a salt and pepper pattern. Otherwise, two neighboring cells equally activate Notch signaling in each other without exhibiting any bias between them. Therefore, we added mild fluctuations to the initial conditions and differences of variables in each iteration. Because the equation for A is unstable at A = 0, the simple addition of noise induces spontaneous differentiation apart from the wave front. We, therefore, included noise by multiplying $1 + 0.1 \times \theta$ to the initial conditions and differences of E, N, D, and A in each iteration (θ is Gaussian noise). When E, N, D, and A became negative values, they were regarded as zero.

The four-component model reproduced the progression of the proneural wave in a WT condition without exhibiting any salt and pepper pattern, despite the presence of noise (Fig. 3B and Movie S1). Additionally, the four-component model reproduces many characteristics of the proneural wave. We can generate mutant clones of EGF, Notch, and DI in silico in the central area of the NE field (Fig. 3 C-E). In the EGF mutant clone, the wave progression and NB differentiation disappeared autonomously (Fig. 3C) (27). In contrast, the wave was nonautonomously accelerated in the Notch mutant clone as observed in vivo (Fig. 3D and Movie S2) (27). Because DI activates Notch only in adjacent cells and autonomously inactivates Notch, it is not trivial whether the mutants for Notch and Dl show the same phenotype. Therefore, it is important that wave progression was similarly accelerated in the Dl mutant clone (Fig. 3E). Note that the nonautonomous accelerations of the wave propagation observed in vivo were also reproduced in silico (Fig. 3 D and E) (27). The above results were reproduced using various parameter sets as discussed later, indicating that these in silico results do not depend on the details of the actual parameter values.

It has been suggested that multiple feedbacks, including the induction of EGF production by EGF signaling (e_eE) , the induction of EGF production by Notch signaling (n_eN) , and the induction of Dl expression by EGF signaling $(e_d E)$, play essential roles in vivo (23, 27). Interestingly, the behavior of the proneural wave did not change significantly when these feedbacks were abolished in silico $(e_e = n_e = e_d = 0 \text{ and } e_e = 0, n_e = 0, \text{ and } e_d = 0)$ (Fig. 3 G-K and Figs. S3 and S4). Even in the absence of these feedbacks, loss of EGF reduces DI and loss of Notch reduces EGF expression in silico (Fig. 3 L-O). The presence of these feedbacks has been suggested by genetic experiments (23, 27), and it is not clear whether such feedbacks indeed exist in vivo. We do not have any in vivo evidence that Pnt directly activates Rhomboid (Rho) expression, that Su(H) directly activates Rho expression, and that Pnt directly activates DI expression in the developing fly brain. Our in silico study suggests that these direct regulations are dispensable to account for the behavior of the proneural wave. In the following in silico experiments, these feedbacks were ignored by setting $e_e = n_e = e_d = 0$ unless otherwise noted.

In the above in silico studies, a square grid was always used for representing the cell arrangement. Although the actual cell arrangement is not uniform in vivo (27), we obtained essentially the same results when a hexagonal grid was used (SI Results and Fig. S5). Moreover, the results of these discrete models were confirmed by using the continuous models. Thus, the difference in cell arrangement does not change our conclusions.

Salt and Pepper Patterns in Notch Activity Are Cancelled by EGF Activity.

Under WT conditions, Notch activity does not exhibit obvious salt and pepper patterns in vivo as visualized by $E(spl)m\gamma$ -GFP (Fig. 4A) (36). Similarly, the four-component model, which explicitly includes the lateral inhibition system, reproduced the progression of the proneural wave without exhibiting any salt and pepper pattern, despite the presence of noise (Fig. 4B and Movie S3). There are conditions that have to be fulfilled for coupled equations to yield a salt and pepper pattern (6, 37).

In the case of proneural wave progression, diffusible EGF upregulates Dl expression. Therefore, the salt and pepper pattern may be obscured by EGF activity, because Notch-ON cells produce EGF, which in turn, activates Notch signaling in surrounding Notch-OFF cells. Indeed, a decrease in the diffusion constant of EGF ($d_e = 0.85$) or EGF production rate (EP; $a_e = 0.85$) resulted in a salt and pepper-like fluctuation in Notch activity (Fig. 4 C and D and Movies S3 and S4), suggesting that EGF cancels the fluctuation in Notch activity. We tested this idea in vivo by using a mutant of Rho, a metalloprotease that triggers EGF ligand secretion (38), and the pnt mutation to reduce EGF activity. Interestingly, ectopic Notch-ON cells isolated from the wave front were observed in the *rho* and *pnt* heterozygous background (Fig. 4 E-G), probably because EGF is diffusible and/or EGF signaling is weakly up-regulated before the wave front. The salt and pepper pattern was not detectable within the wave front, in which GFP was uniformly up-regulated. In the WT, the average number of isolated GFP-positive cells was 0.43 (Fig. 4E) (n = 35). By contrast, 2.36 and 2.39 cells were observed in rho and pnt heterozygotes, respectively (n = 28 and 41, respectively; P < 0.0001 by Welch's t test) (Fig. 4 F and G), supporting the notion that EGF cancels the fluctuation in Notch activity. When diffusion or production of EGF was reduced in silico, the value of A also exhibited a salt and pepper pattern (Fig. 4 C and D). However, we did not detect such fluctuations in L'sc expression pattern at the wave

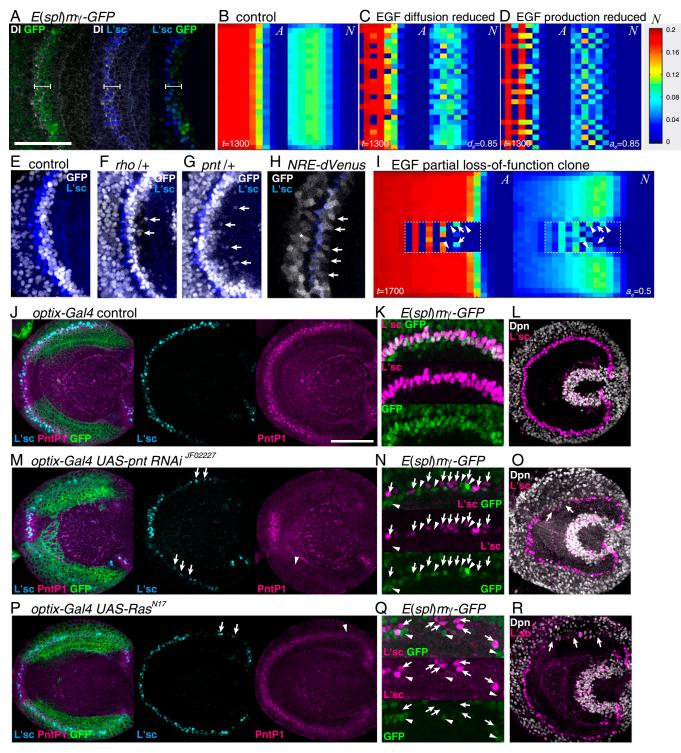


Fig. 4. Salt and pepper pattern is canceled by EGF in silico and in vivo. (A) Notch activity as visualized by $E(spl)m\gamma$ -GFP (green) and DI expression (white) is found at the wave front expressing L'sc (blue). White brackets indicate the coexpression of GFP and DI. Anterior is to the left, and dorsal is to the top. (B–D) Reducing (C) EGF diffusion ($d_e = 0.85$) or (D) EP ($a_e = 0.85$), A and N show fluctuations compared with the control (B). (B–D and I) Results of in silico experiments in the absence of the feedbacks ($e_e = n_e = e_d = 0$). (E–G) Maximum intensity projection images of $E(spl)m\gamma$ -GFP (white) and L'sc (blue) in (E) control, (F) rho heterozygous, and (G) pnt heterozygous backgrounds. Ectopic GFP-positive cells are indicated by arrows. (H) Notch activity as visualized by NRE-dVenus exhibits a salt and pepper pattern (white; arrows). *Signals behind the proneural wave reflect the Notch activity in NBs. (I) A and N show fluctuations in clones in which EGF production is reduced ($a_e = 0.5$). Arrows indicate the cells in which A is up-regulated while N is down-regulated. Arrowheads indicate the cells in which A is up-regulated while N is up-regulated. Scale bars: 50 μm in A and E-H.) (J–R) EGF signaling was partially reduced under the control of optix-Gal4 in the dorsal and ventral regions of the optic lobe as visualized by GFP (green in J, M, and P). (J–L) Control. (M–O) UAS-pnt RNAi^{PC2227}. (P–R) UAS-Ras^{N17}. (I, M, and P) L'sc expression became stochastic when EGF signaling was reduced as visualized by PntP1 (arrows and arrowheads in M and P). (K, N, and Q) Notch activity as visualized by E(spl)mγ-GFP (green) and L'sc expression (magenta) was compared at the dorsal regions of the optic lobe. (N and Q) L'sc and GFP showed stochastic expression when EGF signal was reduced (arrows and arrowheads, respectively). Note that the L'sc and GFP signals were largely complementary to each other. (L, O, and R) NB differentiation as visualized by Dpn expression (white) was not impaired in the absence of

front in the heterozygous backgrounds for either rho or pnt (Fig. 4 F and G).

Furthermore, we speculated that the salt and pepper pattern in Notch activity may be detectable depending on the temporal resolution of the Notch activity markers, because the fluctuation in Notch activity is likely to be rapidly cancelled by EGF signaling. To detect mild fluctuations in Notch signaling, we used a more sensitive marker, NRE-dVenus, which directly monitors the transcriptional activity of the Su(H)/Notch complex with dVenus, a rapidly degraded form of the fluorescent protein Venus (39). In this case, salt and pepper-like fluctuations of Notch signaling were observed at the wave front of the proneural wave in the WT background (Fig. 4H). However, fluctuations in L'sc expression pattern were not observed, despite the salt and pepper patterns in the Notch activity. The biological significance of the salt and pepper pattern in the Notch activity remains elusive.

Further reduction in EGF signaling activity may be required to observe a salt and pepper pattern in L'sc expression. As shown previously, the complete loss of EGF signaling eliminates L'sc expression (27). However, our in silico experiments suggest that salt and pepper patterns in the values of A and N should be observed in clones in which EP is reduced to 50% of WT cells (Fig. 4I) $(a_e = 0.5)$. Therefore, we searched for in vivo conditions in which EGF signaling is partially reduced and L'sc expression becomes fluctuated. Among many different combinations of Gal4 and UAS strains, we found that UAS-pntRNAiJF02227 and UAS-Ras^{N17} under the control of optix-Gal4 caused salt and pepper-like fluctuations in L'sc expression (Fig. 4 J, M, and P) (n = 14 of 14 and)18 of 48, respectively). The mean distance between L'sc-positive cells was 6.92 and 12.22 µm in control and UAS-pntRNAi^{JF02227}. respectively (P < 0.006 by Welch's t test). pnt RNAi degrades pnt mRNA, and Ras^{N17} inhibits the activity of Ras to down-regulate the EGF signaling. In both cases, EGF signaling was reduced in a nonstochastic manner in the dorsal and ventral regions of the optic lobe as visualized by PntP1 expression. Nevertheless, expression of L'sc and $E(spl)m\gamma$ -GFP became stochastic (Fig. 4 M, N, P, and Q). Importantly, the distributions of L'sc and GFP signals were largely complementary to each other (arrows and arrowheads in Fig. 4 N and Q, respectively) as observed in silico (Fig. 4I), suggesting that Notch-mediated lateral inhibition implemented in the proneural wave caused the salt and pepper patterns in L'sc and $E(spl)m\gamma$ -GFP in vivo. Although we observed this phenomenon only in the dorsal and ventral regions of the brain, the molecular mechanisms of the proneural wave are thought to be the same along the dorsoventral axis (24, 27).

To confirm that EGF signaling was partially reduced by pnt RNAi in the above experiments, optix-Gal4 UAS-pntRNAi flies were raised at a higher temperature (30 °C) to increase the effect of pnt RNAi. L'sc expression was almost completely lost as in the case of pnt null mutant clones (n = 24 of 24) (Fig. S6.4) (27). Additionally, its effect was compared with the more potent pnt RNAi strain. Under the control of GMR-Gal4, UAS-pntRNAi^{HMS01452} caused smaller eyes compared with UASpntRNAi^{F02227}, suggesting that the former is more potent than the latter (Fig. S6 B–D). Indeed, UAS-pntRNAi^{HMS01452} under the control of *optix-Gal4* eliminated the proneural wave (n = 26 of 26)(Fig. S6E). The residual PntP1 signal suggests that UAS-Ras^{N17} only partially reduced EGF signaling (Fig. 4P). These results support the conclusions that the partial reduction in EGF signaling causes the salt and pepper patterns in Notch and AS-C (Fig. 4 N and Q) as predicted in silico (Fig. 4I) and that the proneural wave indeed involves Notch-mediated lateral inhibition.

However, even in the presence of fluctuated L'sc expression, NBs were uniformly formed behind the proneural wave as visualized by Dpn expression (Fig. 4 L, O, and R). The final pattern of NB formation may be rescued by unidentified mechanisms.

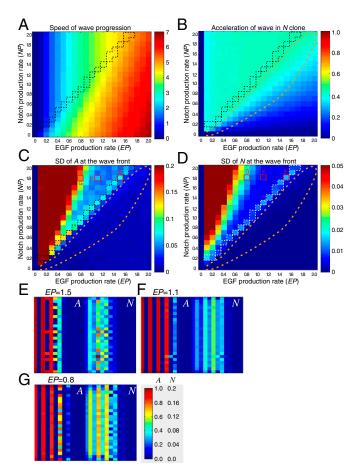


Fig. 5. Phase diagrams of the four-component model. Results of in silico experiments in the absence of the feedbacks ($e_e = n_e = e_d = 0$). (A) Speed of wave progression, (B) acceleration of wave in Notch clone, and (C and D) SDs of A and N at the wave front, respectively, were examined by changing NP ($d_t = d_c = 0.25 \times NP$) and EP ($a_e = EP$). Orange dotted lines indicate the area in which NP and EP are equivalent, showing wave acceleration in N clone without showing salt and pepper patterns in A and N. White and black dotted lines indicate the area in which NP is relatively larger or EP is relatively smaller showing salt and pepper patterns in A and N. The red rectangles indicate the conditions shown in E-G. (E-G) Salt and pepper and striped patterns of A and N at the wave front by changing the value of EP (NP = 1.8). (E) EP = 1.5, (F) EP = 1.1, and (G) EP = 0.8.

Salt and Pepper Pattern Formation Requires a Higher Notch Activity Compared with Wave Speed Control. The above results indicate that Notch signaling has two distinct functions: regulation of the wave progression speed and formation of a salt and pepper pattern. In the fly brain, the former is prominent, but the latter is obscure as discussed above. Therefore, it is likely that different levels of Notch signaling activity are required for these two functions. We surveyed the presence of two phenotypes (i.e., wave acceleration in a Notch clone and the salt and pepper pattern in N) under various parameter conditions. Here, we defined the Notch production rate (NP) and EP, both of which vary from 0.0 to 2.0 in intervals of 0.1. For simplicity, all parameters related to NP and EP were proportionally changed according to NP and EP $(d_t = d_c = 0.25 \times NP, n_e = a_e = EP, \text{ and } e_e = 0.2 \times EP), \text{ re-}$ spectively. Under these conditions, we examined (i) the speed of wave progression, (ii) the acceleration of the wave in Notch clones, (iii) the salt and pepper index of A (SD of A at the wave front), and (iv) the salt and pepper index of N (SD of N at the wave front) (Fig 5 A–D and Figs. S2 and S4).

In general, proneural wave progression was observed when EP was greater than 0.2. EP and NP positively and negatively influenced the speed of wave progression, respectively (Fig. 5A). Acceleration of the wave in Notch clones was observed for a wide range of EP and NP values (Fig. 5B), whereas salt and pepper patterns in A and N were observed only when NP was significantly larger than EP (Fig. 5 C and D). When EP and NP were roughly equivalent, wave acceleration in the Notch clones was observed in the absence of salt and pepper patterns (orange dotted areas in Fig. 5 B–D). However, when NP was larger relative to EP, salt and pepper patterns appeared in A and N (Fig. 5 C and D), suggesting that the threshold NP required for salt and pepper pattern formation was significantly higher than that for wave speed control. These results are consistent with in vivo observations that the salt and pepper pattern was hardly detectable in WT brains (Fig. 4 A, E, and K).

The salt and pepper patterns appeared when the EP was lower than the NP (Fig. 5 C and D). Interestingly, when EP was decreased, the salt and pepper index of N did not monotonically rise but exhibited a biphasic response (Fig. 5D). For example, when NP = 1.8, N displayed salt and pepper patterns when EP = 1.5 and EP = 0.8 but not when EP = 1.0-1.4 (compare E-G in Fig. 5D). Note that the degree of wave acceleration in N clones monotonically increased with increasing EP (Fig. 5B). Similar phenomena were observed in the other parameter sets (Figs. S2 and S4). These results suggest that wave speed control and salt and pepper pattern formation are both regulated by Notch signaling but by distinct mechanisms. These different mechanisms may underlie the different threshold levels of NP required for salt and pepper pattern formation and wave speed control.

Solving the Paradox of the Notch Mutant Phenotype. The above results are all consistent with in vivo observations. To further confirm the validity of our model, we determined if the model can solve the paradox of the Notch mutant phenotype. EGF signaling is diminished in clones in which Notch signaling is eliminated in vivo (27). However, if EGF signaling is lost in Notch mutant clones, the wave should be eliminated, because EGF is essential for wave

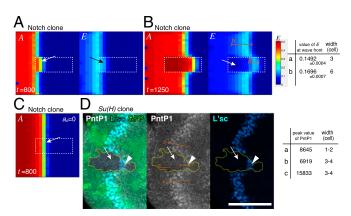


Fig. 6. Wave acceleration mechanism in Notch mutant clone. (A–C) Results of in silico experiments in the absence of the feedbacks (e_e = n_e = e_d = 0). Notch mutant clones are indicated by white dotted lines. (A and B) E is activated when the proneural wave encounters Notch mutant cells (arrows in A) but quickly inactivated (arrow in B). (B) The peak values of E at the wave front and the widths of E activated areas (E > 0.09) are compared along the lines E and E. (E) The wave acceleration in Notch mutant clone is suppressed when E0. (E0) PntP1 (white) is transiently up-regulated when proneural wave encounters E1. Mutant cells (arrowheads; GFP-negative) but eventually down-regulated (arrows). The peak levels of PntP1 and the widths of PntP1-activated areas are compared along the lines E1. The line E3 indicates the background level. (Scale bar: 50 E10.

progression. However, the wave is not eliminated; rather, its progression is accelerated in Notch and Dl mutant clones (26, 27).

A similar phenomenon was observed in vivo. In Su(H) mutant clones, in which Notch signaling is eliminated, EGF signaling, as revealed by PntP1, remained strong at the wave front and was eventually degraded (Fig. 6D) (n=18 of 32). Again, the peak value of PntP1 at the wave front in Su(H) clones remained comparable with that of control cells (8,645 in Notch mutant clones but 6,919 or 15,833 in WT cells), whereas the width of the EGF active area was significantly reduced (one to two cells wide in Notch mutant clones but three to four cells wide in WT areas) (Fig. 6D). Similar results were observed in clone mutant for Dl in vivo (Fig. S7). Although N was instantaneously diminished in Notch (and Dl) mutant clones, E remained relatively high for a short period. As a result, the temporal increase in the value of E-N at the wave front caused wave acceleration.

Wave Acceleration and a Neurogenic Phenotype Share the Same Mechanism.

To understand the mechanism of wave acceleration, we searched for conditions under which the wave acceleration was not observed in the presence of a Notch mutant clone. Intriguingly, the wave acceleration phenotype of the Notch clone was significantly suppressed only when a_d was set to zero (Fig. 6C). In the absence of this term, the wave was constitutively accelerated (compare Fig. 6 A and C). Consequently, additional acceleration of the wave did not occur, even in the Notch mutant clone. This result suggests that the AS-C input to Dl expression (the term of a_d) is significant and responsible for the Notch mutant phenotype. Similarly, the positive regulation of DI expression by AS-C is particularly important to establish binary cell fates during lateral inhibition, because it is essential for the Notch signaling feedback loop between adjacent cells (Fig. 1A). Thus, the mechanisms responsible for the formation of binary cell fates and the control of wave progression are identical.

In the fly retina, Notch signaling also plays an early proneural function that is required for photoreceptor differentiation prior to the wave progression (21, 22). Although we have never observed similar proneural defects in Notch mutant clones in the course of proneural wave progression, an unidentified function of Notch that is distinct from lateral inhibition could act to restrict the proneural wave progression. Although we cannot exclude this possibility, the above results suggest that the fourcomponent model with Notch-mediated lateral inhibition is essentially consistent with proneural wave progression in silico and in vivo and that the wave acceleration phenotype is equivalent to the classical neurogenic phenotype of Notch mutant clones (2). Although nonlinear regulations of Notch signaling were implemented in the previous models (5, 6, 17-19), the equation for N in the four-component model was sufficient to reproduce all of the experimental conditions described above.

Notch Exhibits a Pulse Wave That Restricts the Speed of Wave Propagation. The equations of N and D in the four-component model only describe that they form a part of lateral inhibitory

feedback (Fig. 3A). However, it is difficult to envisage how Notch-mediated lateral inhibition, which generally forms a salt and pepper pattern, controls wave propagation. To clarify the system behavior of proneural wave progression, we derived a three-component model from the four-component model by assuming that the DI expression level is proportional to Notch signaling activity (SI Discussion). The DI expression level was largely proportional to Notch activity in vivo as indicated by E $(spl)m\gamma$ -GFP (Fig. 4A). In the resulting three-component model, N is a composite variable for DI expression and Notch activity. The rate of change in N is influenced by its diffusion $(d_n \Delta N)$, degradation $(\bar{k}_n N)$, and AS-C $[\bar{a}_n A(A_0 - A)]$ (Fig. S8A). Note that the equation exhibits the same structure as that of E, revealing symmetry between Notch and EGF and suggesting that Notch activity propagates as a pulse wave, similar to EGF signaling. Indeed, the three-component model reproduced the progression of the proneural wave with the pulse waves of E and N, producing their peaks near the wave front (Fig. S8B). Because the three-component model is only mathematically derived from the four-component model, the diffusion term of N does not necessarily indicate that Dl acts as a diffusible factor. Although the diffusion term could correspond to the long-range action of Dl via filopodia (40–42), this cellular extension is not observed in cells at the wave front of the proneural wave.

The three-component model reproduced the phenotypes of EGF and Notch mutant clones as well as the four-component model (Fig. S8 C-E). In EGF mutant clones, wave progression and NB differentiation disappeared autonomously (Fig. S8C). Notch mutant clones caused nonautonomous acceleration of the wave progression (Fig. S8E). EGF activity remained high when the wave front came across Notch mutant cells but was eventually diminished, identical to the results obtained using the fourcomponent model (Fig. S8 D and E). Finally, the wave acceleration phenotype of the Notch mutant clones was suppressed when \bar{a}_n was set to zero (Fig. S8F). Because N is the composite variable for Notch activity and DI expression, this result is consistent with the above finding that the AS-C input to Dl expression (the term of a_d) is responsible for the Notch mutant phenotype in the four-component model (Fig. 6C).

Thus, the essential characteristics of the proneural wave, except the salt and pepper patterns, are conserved in the threecomponent model, suggesting that the lateral inhibitory feedback of Notch signaling can be approximated by a reaction diffusion equation during proneural wave progression. The incorporation of EGF-mediated reaction diffusion in Notch-mediated lateral inhibition enables a unique behavior of Notch signaling that is approximated by a pulse wave negatively regulating the speed of proneural wave propagation (Fig. S8 G and H).

Discussion

Notch-mediated lateral inhibition plays essential roles in specifying differentiated cells from undifferentiated cells in a wide variety of developmental processes and induces the formation of a salt and pepper pattern via binary cell fate decisions. During proneural wave progression, EGF is produced at the wave front to suppress the formation of a salt and pepper pattern. Indeed, salt and pepper patterns are hardly detectable in the WT fly brain when regular GFP is used to detect Notch activity (Fig. 4E). Similar mathematical models describing the combinatorial action of Notch and a diffusible factor reproduce the patterns observed in retinal development (17–20). In these studies, differentiated neurons exhibit obvious salt and pepper patterns.

In our system, a part of the lateral inhibition system also controlled the sequential progression of differentiation. In contrast to the obscured salt and pepper pattern in the proneural wave, Notch mutant clones obviously exhibited a wave acceleration phenotype (26, 27). Thus, Notch-mediated lateral inhibition controls the proneural wave progression speed without exhibiting a salt and pepper pattern. In this study, we showed that the wave speed control and salt and pepper pattern formation required distinct threshold levels of Notch signaling activity (Fig. 5). When the NP and EP were approximately equal, the salt and pepper pattern was obscured. However, when the EP was reduced relative to the NP, the salt and pepper pattern became obvious. Consistent with this result, decreasing EGF production enhanced the salt and pepper pattern in vivo (Fig. 4 E–G and J–Q), showing that the fly brain indeed uses Notch-mediated lateral inhibition to control proneural wave progression. Although the final patterns are distinct, the proneural wave and retinal wave share the same mechanism to regulate the salt and pepper pattern formation.

As discussed above, however, wave speed control and salt and pepper pattern formations have distinct response to relative Notch activity. Surprisingly, salt and pepper pattern formation exhibited a biphasic response to the changes in the EP relative to the NP (Fig. 5). These results suggest that Notch regulates wave speed and salt and pepper pattern formation by distinct mechanisms. We do not yet understand exactly how Notch controls salt and pepper patterns during proneural wave progression. However, it is intriguing that N exhibits striped as well as salt and pepper patterns (Fig. 5 E–G). When EP was higher (EP = 1.5), N exhibited a rather uniform salt and pepper pattern (Fig. 5E). When EP was reduced to 1.1, the salt and pepper pattern was rather obscured, but a striped pattern became obvious (Fig. 5F). When EP = 0.8, N exhibited both striped and salt and pepper patterns simultaneously (Fig. 5G). The value of A also exhibited both striped and salt and pepper patterns (Fig. 5 *E*–*G*). Similar striped pattern was observed in the hexagonal grid model (Fig. S5 *I–K*).

Intriguingly, a striped pattern was observed in a model of the retinal differentiation wave and in vivo genetic experiments (18). Notch-mediated lateral inhibition seems to form both salt and pepper and striped patterns depending on parameter values in both previous nonlinear models (18) and our semilinear model. Our model further suggests that the formation of a striped pattern requires a higher threshold level of relative Notch activity. In the presence of a striped pattern, the salt and pepper index is reduced, because the value of N along the wave front becomes similar within the striped patterns (Fig. 5 D and F). Consequently, the salt and pepper index exhibits a biphasic response to the changes in relative Notch activity. Unfortunately, we have never observed the striped pattern in the proneural wave in vivo. The formation of striped pattern may be suppressed by unidentified mechanisms in the medulla, or special experimental conditions might be required to reproduce the striped pattern in vivo.

Notch signaling plays diverse roles when combined with other signaling systems (8–10). When these signaling systems have complex feedbacks and show oscillatory or propagating behavior, the exact mechanisms by which the system behavior is regulated cannot be established without formulating mathematical models. In the developing cerebral cortex, the oscillatory behavior of Notch signaling in neural progenitor cells is important for cell fate determination (43). During this process, Notch signaling seems to form lateral inhibitory feedback, a role similar to that observed in the proneural wave. Additionally, the combinatorial action of Notch and EGF signaling controls the maintenance of neural stem cells and neural progenitor cells (44). Similarly, vertebrate segmentation is controlled by the interplay between Notch and FGF (11). Notch signaling controls the synchronization between neighboring cells and positively regulates boundary formation by activating Mesp2. By contrast, Notch-mediated lateral inhibition causes desynchronization of cell differentiation between neighboring cells and negatively regulates NB formation during the proneural wave. Thus, the roles of Notch signaling in vertebrate segmentation seem to be opposite those observed in the proneural wave.

Finally, the behavior of the differentiation wave observed in the retina is similar to that of the proneural wave. Although the wave in the retina clearly accompanies the salt and pepper pattern, all NE cells are differentiated to NBs behind the proneural wave without exhibiting a salt and pepper pattern. By formulating mathematical models of the proneural wave based on biological evidence, we have shown that the combination of Notch-mediated lateral inhibition and EGF-mediated reaction diffusion reproduces the behavior of the proneural wave. Comparative analysis of the mathematical structures of these two systems may provide fruitful insights on the roles of Notch signaling during differentiation wave control. Future studies should include comparative analyses of the interplay between Notch and other signaling systems in a wide variety of biological processes in vivo and in silico.

Methods

Mathematical Modeling. The differential equations were calculated using the explicit finite difference method with the zero flux boundary condition. In the square grid model, the mesh size was equal to the cell size (dx = 2), and the time step size was 0.01 (dt = 0.01). Note that the minimal length of a side of an NE is ~2 μm in vivo. Details of the hexagonal grid model are described in SI Results. For 25 \times 25 cells, the initial conditions for A, E, and D in the anterior-most cells (x = 1, 2, and 3, respectively) were A = 0.90, 0.31, and 0.02, respectively; E = 0.90, 0.31, and 0.02, respectively0.054, 0.021, and 0.0016, respectively; and D = 0.062, 0.021, and 0.0013, respectively, to stabilize the proneural wave progression. The initial condition of N was zero in all cells. Gaussian noise was added to 10% of the difference of all variables in each iteration by multiplying $1 + 0.1 \times \theta$ (θ is Gaussian noise with mean = 0 and SD = 1).

The four-component model contains four equations and four variables (Fig. 3A). E and N represent EGF and Notch signaling, respectively. D and A represent the expression levels of DI and AS-C, respectively. Notch receptor expression level is constant; d_e is the diffusion coefficient of EGF, and d_t and d_c represent the trans-activation and cis-inhibition of Notch signaling by DI, respectively. Additionally, i,l and j,m are integers indicating the location of a cell along the x and y axes, respectively, and I and m indicate the location of four cells that are adjacent to a cell indicated by i and j. The diffusion of E was calculated as follows: $d_e \Delta E(i,j) = d_e \{E(i+1,j) + E(i-1,j) + E(i,j+1) + E(i,j-1) - 4E(i,j)\}/dx^2$; k_e , k_{n} , and k_{d} are the degradation rate constants of EGF, Notch, and DI, respectively, and ee, ne, and ed reflect EGF regulation by EGF, EGF regulation by Notch, and DI regulation by EGF, respectively ($e_e = 0.2$ and $n_e = e_d = 1$). EGF does not directly regulate Notch signaling in this model; ae and ad indicate EGF and DI regulation by AS-C, respectively. A_0 sets the maximum value for A. When $A = A_0$, the cells are fully differentiated as NBs. A_0 is always set to one; e_a reflects the regulation of differentiation by EGF and Notch and is set to 10 unless otherwise noted. The other parameters are set to one unless otherwise noted. We set $e_e = n_e = a_e = 0$, $d_t = d_c = 0$, and $e_d = a_d = 0$ in EGF, Notch, and DI mutant clones, respectively, in 11×6 cells in the central area (Fig. 3A). The values of E in Notch mutant and control areas were compared in Fig. 6B (a: y = 13; b: y = 21). The widths of areas with E above the threshold value (0.09) were counted.

A wide range of parameter sets was examined in Fig. 5 and Figs. S2 and S4 in the presence of Notch mutant clone. Here, NP and EP vary from 0.0 to 2.0 by 0.1. All parameters related to Notch and EGF productions were proportionally changed according to NP and EP, respectively ($n_e = a_e = EP$, $e_e = 0.2 \times EP$, and $d_t = d_c = 0.25 \times NP$). For each parameter set, the same in silico experiments were repeated 10 times, and the averages are shown; 4,999 iterations were calculated for each experiment. When T is the time at which the wave front of WT cells (A > 0.5) reaches the central area (x = 13), "speed of wave progression" is defined as 4,999/T - 1. T = 4,999 in cases where the wave front does not reach the central area after 4,999 iterations (speed of wave progression becomes zero). At the time of T, "acceleration of wave in N clone" is defined as the difference between the maximum values of A in Notch clone ($y = \sim 11-14$)

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and WT cells ($y = \sim 3-7$ and $\sim 18-22$) at the central area (x = 13). At the same time, "salt and pepper index of A" and "salt and pepper index of N" were defined as SDs of A and N at the wave front of WT cells (x = 13; $y = \sim 3-7$ and $\sim 18-22$).

The three-component model was derived from the four-component model and contains three equations and three variables (Fig. S8A and SI Discussion). N is the composite variable for Notch signaling and DI expression; d_n represents the diffusion coefficients of Notch signaling. The diffusion of E and N was calculated as described for E in the four-component model. According to *SI Discussion*, d_n , \bar{k}_n , and \bar{a}_n are set to 0.571, 0.571, and 0.429, respectively. We set $a_e = 0$ and $d_n = \bar{a}_n = 0$ in EGF and Notch mutant clones, respectively, in 11×6 cells in the central area (Fig. S8A).

Fly Strains. Flies were raised at 25 °C unless otherwise noted. The following mutant and transgenic flies were used: UAS-Nact, Df(1)260-1 FRT19A, Su(H)44 FRT40A, da¹⁰ FRT40A, rho^{P Δ 5}, DI^{RevF10} FRT82B, pnt^{Δ 88} FRT82B, E(spl)m γ -GFP (36), NRE-dVenus (39), hs-flp, act-Gal4 UAS-GFP, tub-Gal80 FRT82B, FRT2A-FRT82B, ubi-GFP FRT19A, ubi-GFP FRT40A, and ubi-GFP FRT82B. Mutant clones were generated by crossing hs-flp; act-Gal4 UAS-GFP; tub-Gal80 FRT82B with UAS-N^{act}; FRT2A-FRT82B or UAS-N^{act}; pnt $^{\Delta 88}$ FRT82B, Df(1)260-1 FRT19A with ubi-GFP FRT19A; hs-flp, hs-flp; ubi-GFP FRT40A with da¹⁰ FRT40A or Su(H)^{△47} FRT40A, and hs-flp; ubi-GFP FRT82B with Di^{RevF10} FRT82B. EGF signaling was reduced by crossing UAS-pntRNAi^{JF02227}, UAS-pntRNAi^{HMS01452}, or UAS-Ras^{N17} with optix-Gal4 (35).

Histochemistry. The following antibodies were used: mouse anti-DI (1:100; DSHB), rat anti-Dpn (1:50; Abcam), guinea pig anti-L'sc (1:1,200) (35), and rabbit anti-PntP1 (1:200; James Skeath) antibodies. The following secondary antibodies were used: Cy3-conjugated donkey anti-mouse, Alexa546-conjugated goat anti-rabbit, and Alexa647-conjugated donkey anti-guinea pig antibodies.

Image Analysis. Confocal images were obtained by Zeiss LSM510 or LSM880 and processed with ZEN software, Adobe Photoshop, and ImageJ. The DI and GFP expression levels along the arrows in Fig. 2 A and B were quantified by using ZEN software. To compare the salt and pepper patterns of L'sc in Fig. 4 J and K, the mean distances between L'sc-positive cells were quantified. Single optical sections showing the greatest number of L'sc-expressing cells were manually selected at the lateral regions of the optic lobe using ZEN. Cells strongly expressing L'sc above a threshold value (100 of 256) were regarded as L'scpositive cells. The cell shape and the center of mass of L'sc-positive cells were determined according to the distribution patterns of membrane-bound CD8GFP and L'sc. For each of the L'sc-positive cells, the distance to the closest L'sc-positive cell were quantified by using ImageJ. In Fig. 6D, PntP1 expression levels were quantified by using ImageJ along multiple lines nearby and parallel to the orange lines indicated and subtracting a threshold value (13,500 of 65,536) according to the background data along the line d.

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