



TSS Transformation-Specific Smoothing for Robustness Certification

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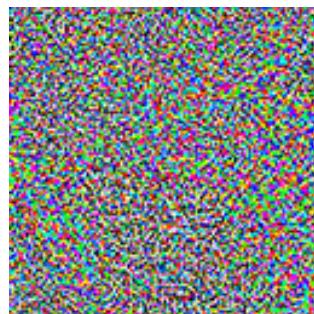
Neural Networks are Vulnerable to Adversarial Attacks

- *W.l.o.g, consider image classification problem*
- Given an image as input, ML model predicts a class label
- However, attacker can usually craft adversarial input:
 - Indistinguishable from original input
 - But fool NN to make wrong prediction



Predicted as
“cat”

+ 0.001 *



Small
Perturbation

=



Predicted as
“dog”



Adversarial Attack via Semantic Transformations

- Certifying and improving robustness for ML models against ℓ_p bounded perturbations is well-studied
 - *Clean input* = x_0
 - *Attacker needs to input* x s.t. $\|x - x_0\|_p \leq \epsilon$
- However, in the real-world, attacker can also apply semantic transformations (e.g., brightness, rotation, scaling) to fool ML models



Adversarial examples found on Nvidia DAVE-2 self-driving car platform by DeepXplore

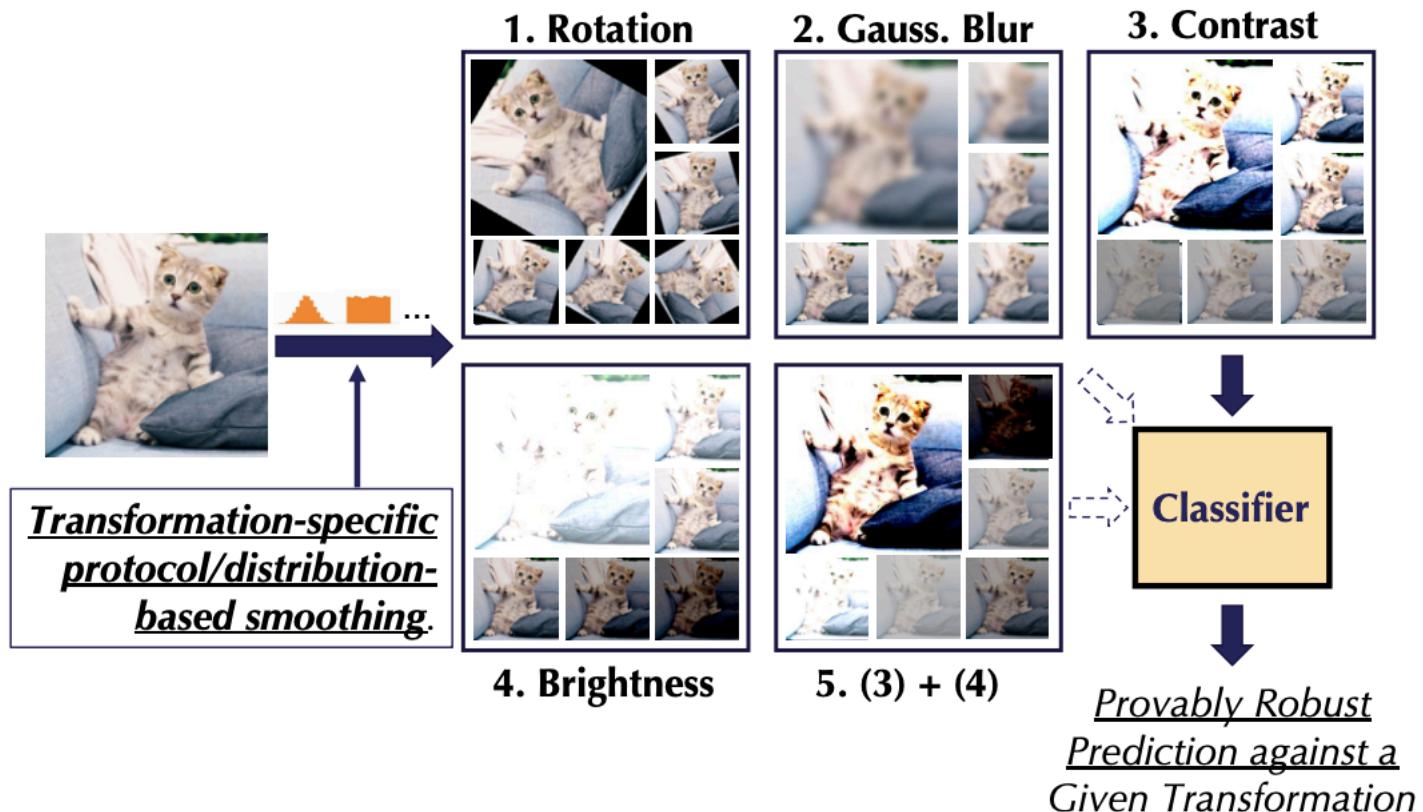


Can we get ML models that are certifiably robust to various semantic transformations?



Certify Robustness against Semantic Transformations

- We propose a **framework for certifying ML robustness against semantic transformations: TSS**





Compared with Existing Work

- Existing certified robustness methods:
 - Too **loose** on small models
 - Too **slow** for large models
 - Too **specific** for certain transformations
- Our work:
 - **Tight**: achieves state-of-the-art certified accuracy
 - **Scalable**: for the first time, achieve certified robustness on ImageNet
 - 30.4% certified accuracy against arbitrary rotation within 30°
 - **General**: general methodology for analyzing and certifying against transformations
 - Support > 10 common transformations:
 - rotation, scaling, brightness, contrast, blur, ...



➤ Threat Model & Certification Goal

Challenges

Our Framework: TSS

Experimental Evaluation



Threat Model

- Image classification task:
 - Input space: $\mathcal{X} \subseteq \mathbb{R}^d$
 - Output space: $\mathcal{Y} = \{1, \dots, C\}$
- Semantic transformation as a function
$$\phi: \mathcal{X} \times \mathcal{Z} \rightarrow \mathcal{X}$$
 - Parameter space: $\mathcal{Z} \subseteq \mathbb{R}^m$
- Attacker can:
 1. arbitrarily choose parameter $\alpha \in \mathcal{Z}$
 2. transform x to $\phi(x, \alpha)$
 3. input $\phi(x, \alpha)$ to the classifier

Example:

- $\phi_R(x, \alpha)$ rotates input image x by α degree clockwise
- Define $\mathcal{Z} = [-30^\circ, 30^\circ]$

➤ Attacker can arbitrarily rotate the image within 30°



Certification Goal

- For our classifier $h: \mathcal{X} \rightarrow \mathcal{Y} = \{1, \dots, C\}$
- Given clean input $x \in \mathcal{X}$
- Wish to find a set $\mathcal{S} \subseteq \mathcal{Z}$ such that we can guarantee

$$h(x) = h(\phi(x, \alpha)), \forall \alpha \in \mathcal{S}$$



Threat Model & Certification Goal

➤ Challenges

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Experimental Evaluation



Real-Valued Parameter Space

- The parameter space is real-valued
 - The input image space is real-valued
-
- Infinite possible inputs after transformation
 - Cannot certify via enumeration



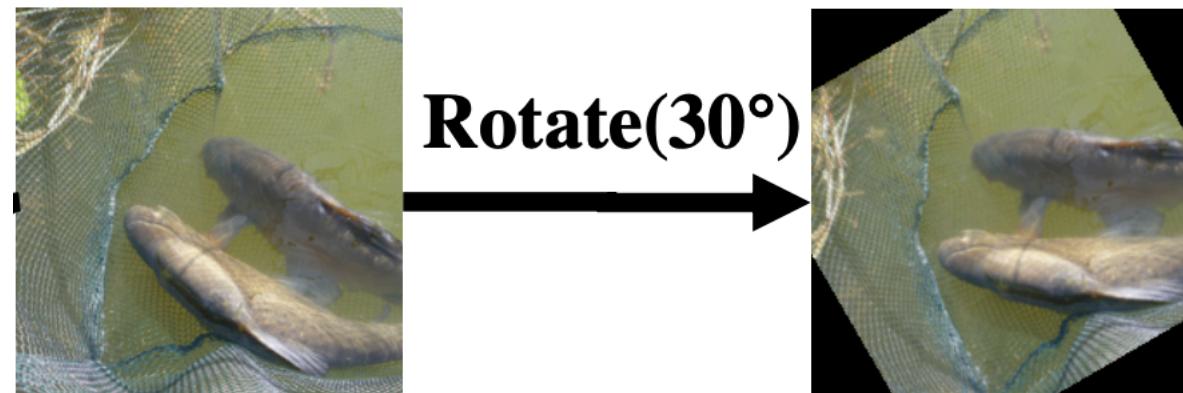
Large ℓ_p Difference

- Semantic transformation incurs large ℓ_p difference
 - Brightness +10% incurs ℓ_2 difference $0.1 \times \sqrt{\# \text{ pixels}} \approx 38.7$ on ImageNet
- Cannot certify with existing ℓ_p based methods



Interpolation

- Some transformations like rotation and scaling uses bilinear interpolation
- Certification needs to take complex interpolation effects into account





Threat Model & Certification Goal

Challenges

➤ Our Framework: TSS

- Generalized Randomized Smoothing
- TSS-R: Certifying Resolvable Transformations
- TSS-DR: Certifying Differentially Resolvable Transformations

Experimental Evaluation



Generalized Randomized Smoothing

- Given an arbitrary base classifier $h: \mathcal{X} \rightarrow \mathcal{Y} = \{1, 2, \dots, C\}$
- Let $\phi(x, b) = x + b \cdot (1, \dots, 1)^T$ be the brightness transformation
- Let $\varepsilon \sim \mathcal{N}(0, \sigma^2)$ be the **smoothing distribution**
- Define $q(y|x; \varepsilon) = \Pr_{\varepsilon} (h(\phi(x, \varepsilon)) = y)$
 - q is probability of predicting class y under noise in parameter space
- We construct **smoothed classifier** $g: \mathcal{X} \rightarrow \mathcal{Y} = \{1, 2, \dots, C\}$:

$$g(x; \varepsilon) = \operatorname{argmax}_{y \in \mathcal{Y}} q(y|x; \varepsilon)$$

➤ Returns the class with highest q



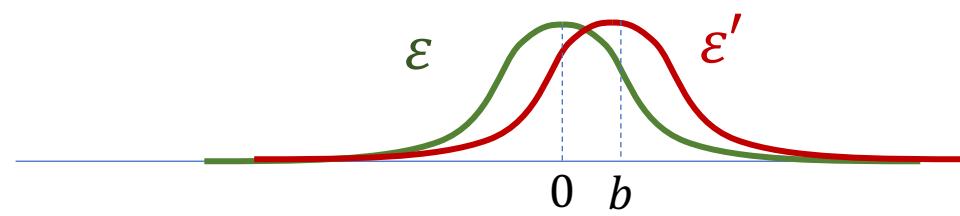
Smoothness Brings Robustness

Recall $g(x; \varepsilon) = \operatorname{argmax}_{y \in \mathcal{Y}} q(y|x; \varepsilon) = \operatorname{argmax}_{y \in \mathcal{Y}} \Pr_{\varepsilon} (h(\phi(x, \varepsilon)) = y)$

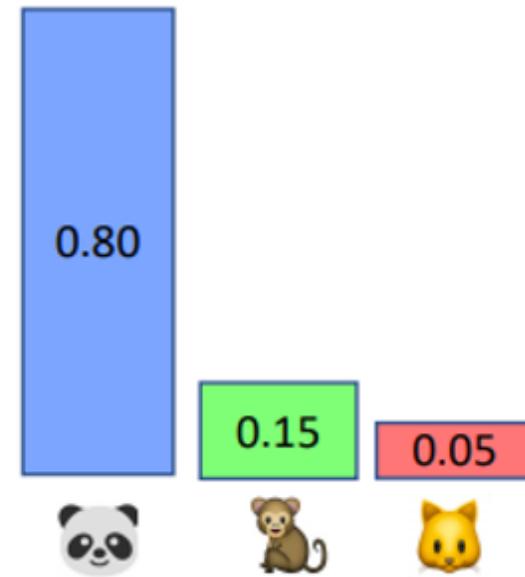
- If for the clean input x_0 , $q(\{\text{panda, monkey, cat}\}|x_0, \varepsilon) = \{0.80, 0.15, 0.05\}$
- Slightly change the brightness by b :

$$\varepsilon \sim \mathcal{N}(0, \sigma^2) \text{ becomes } \varepsilon' \sim \mathcal{N}(b, \sigma^2)$$

- Slightly shifting ε mean,
 $q(\text{panda}|x_0, \varepsilon')$ is still **guaranteed** to be the largest



Prob. Density
over Brightness
Change





Robustness Guarantee

- p_A : probability of top class (panda)
- p_B : probability of runner-up class (monkey)
- $\varepsilon \sim \mathcal{N}(0, \sigma^2)$: smoothing distribution:

g probably returns the top-class panda as long as brightness change

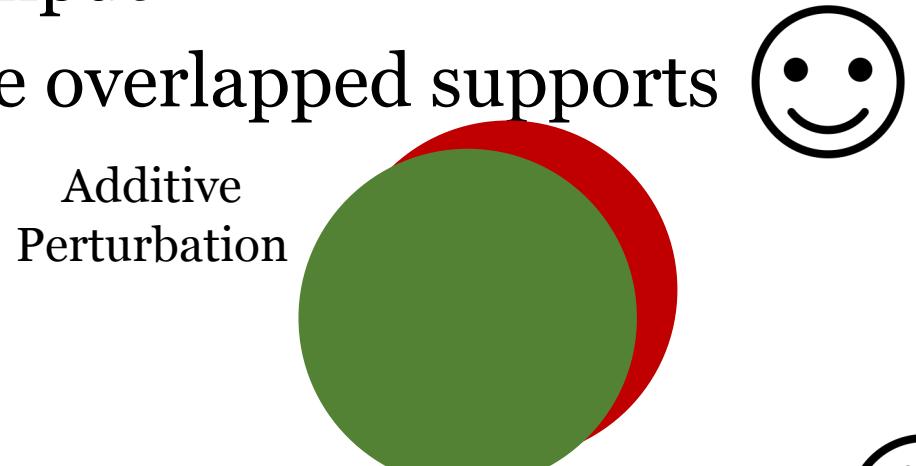
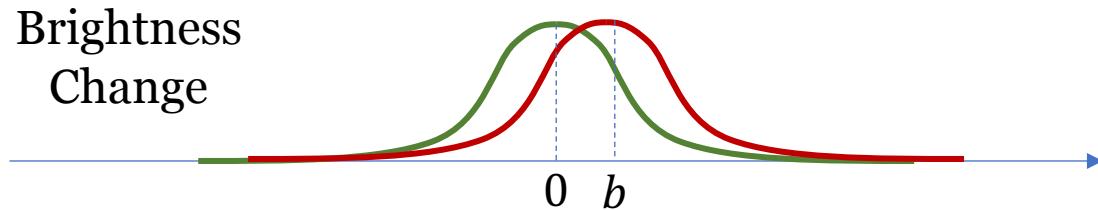
$$b \leq \frac{\sigma}{2} (\Phi^{-1}(p_A) - \Phi^{-1}(p_B)),$$

where Φ^{-1} is the inverse standard Gaussian CDF

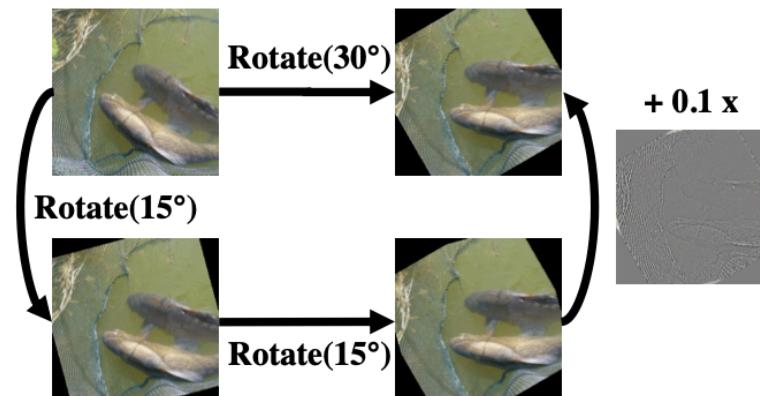


However...

- Guaranteed robustness relies on **overlapped supports** between original and transformed input
- For some transformations, there are overlapped supports



- For some transformations, hard to find overlapped supports
 - Smoothing over rotated input = Rotating two times
 - Rotate 15° + rotate $15^\circ \neq$ rotate 30°
 - Due to interpolation





Resolvable Transformations vs. Differentially Resolvable Transformations

- Transformation with overlapped supports = resolvable
 - Formally, for any $\alpha \in \mathcal{Z}$, there exists function $\gamma_\alpha: \mathcal{Z} \rightarrow \mathcal{Z}$,
$$\phi(\phi(x, \alpha), \beta) = \phi(x, \gamma_\alpha(\beta))$$
- (**informal*) Transformation without overlapped supports but continuous = differentially resolvable





TSS-R: Certifying Resolvable Transformations

- For resolvable transformations, use our generalized randomized smoothing to smooth and provide robustness certification
 - Brightness, contrast, translation, Gaussian blur, ...

Interesting findings:

- Although Gaussian and uniform smoothing distribution shown best for ℓ_p bounded additive perturbations
- For these low-dimensional transformations, **Exponential distribution** usually performs the best
- Some transformations have constrained parameter space, customized smoothing distributions lead to higher certified robustness for them
 - *E.g.*, Gaussian blur's radius cannot be negative, use exponential or folded Gaussian as smoothing distributions



TSS-DR: Certifying Differentially Resolvable Transformations

- Differentially resolvable transformations may not have overlapped supports → **cannot** directly apply generalized randomized smoothing
- Luckily, we find
 - Transformations have low-dimensional parameter space
 - *E.g.*, one-dimensional rotation angle
 - Moderate number of samples lead to an ϵ -cover of parameter space
 - (*informal) By definition, they are continuous w.r.t. parameter change
 - *E.g.*, rotated image w.r.t the rotation angle is continuous
 - *Preprocessing masks out pixels outside of inscribed circle to improve continuity*
 - Given Lipschitz L , maximum ℓ_2 difference from the nearest sample in ϵ -cover is ϵL



Reduction to Certifying ℓ_2 Robustness

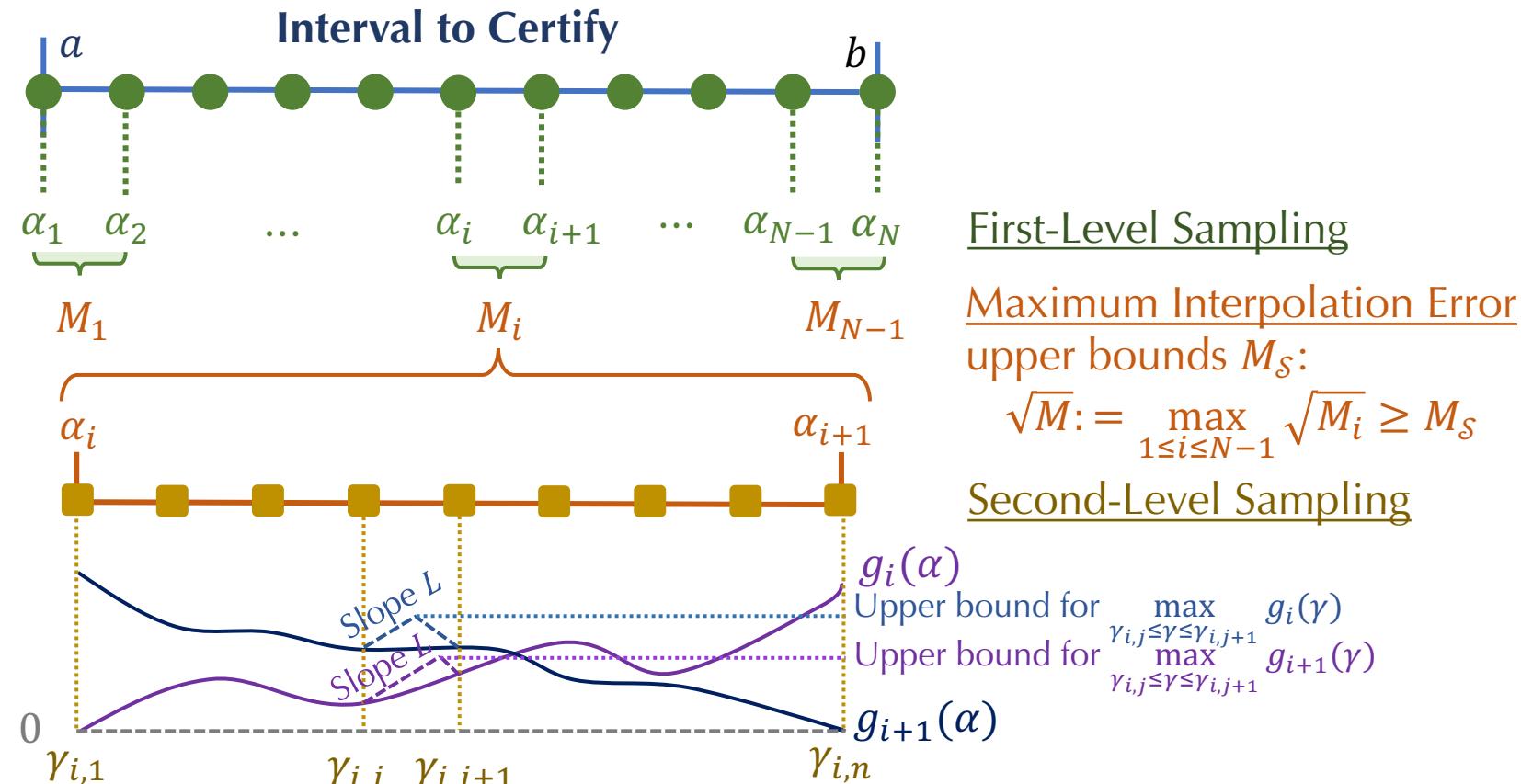
- Moderate number of samples lead to an ϵ -cover of parameter space
- Given Lipschitz L , maximum ℓ_2 difference from the nearest sample in ϵ -cover is ϵL
- If for any sample in ϵ -cover, we can certify an ℓ_2 robust radius $\geq \epsilon L$, then we are done
 - Certify an ℓ_2 robust radius?
 - Apply additive transformation suffices
 - Problem to solve: compute the maximum ℓ_2 difference





Interpolation Error

- Given these samples, we now need to figure out the maximum interpolation error
 - i.e., maximum ℓ_2 difference from any transformed image to their nearest samples
- We combine stratified sampling and efficient Lipschitz computation to upper bound such difference



Bounding M_i from second-level sampling and Lipschitz constant:

$$M_i = \max_{1 \leq j \leq n-1} \min \{ \text{Upper bound for } \max_{\gamma_{i,j} \leq \gamma \leq \gamma_{i,j+1}} g_i(\gamma), \text{Upper bound for } \max_{\gamma_{i,j} \leq \gamma \leq \gamma_{i,j+1}} g_{i+1}(\gamma) \}$$



Threat Model & Certification Goal

Challenges

Our Framework: TSS

- Experimental Evaluation



Experimental Setup

- Base Classifier Training:
 - We combined consistency-enhanced training [1] with transformation-specific data augmentation to obtain base classifier for smoothing
- Metric: **Certified Robust Accuracy**
 - The fraction of samples (within the test subset) that are
 - both **certified robust** and **classified correctly**
 - under any attack whose parameter is within predefined range

Set-of-the-art Certified Robustness

Transformation	Type	Dataset	Attack Radius	TSS	Certified Robust Accuracy				
					DeepG [2]	Interval [47]	VeriVis [39]	Semanify-NN [35]	DistSPT [13]
Gaussian Blur	Resolvable	MNIST	Squared Radius $\alpha \leq 36$	90.6%	-	-	-	-	-
		CIFAR-10	Squared Radius $\alpha \leq 16$	63.6%	-	-	-	-	-
		ImageNet	Squared Radius $\alpha \leq 36$	51.6%	-	-	-	-	-
Translation (Reflection Pad.)	Resolvable, Discrete	MNIST	$\sqrt{\Delta x^2 + \Delta y^2} \leq 8$	99.6%	-	-	98.8%	98.8%	-
		CIFAR-10	$\sqrt{\Delta x^2 + \Delta y^2} \leq 20$	80.8%	-	-	65.0%	65.0%	-
		ImageNet	$\sqrt{\Delta x^2 + \Delta y^2} \leq 100$	50.0%	-	-	43.2%	43.2%	-
Brightness	Resolvable	MNIST	$b \pm 50\%$	98.2%	-	-	-	-	-
		CIFAR-10	$b \pm 40\%$	87.0%	-	-	-	-	-
		ImageNet	$b \pm 40\%$	70.0%	-	-	-	-	-
Contrast and Brightness	Resolvable, Composition	MNIST	$c \pm 50\%, b \pm 50\%$	97.6%	$\leq 0.4\%$ $(c, b \pm 30\%)$	0.0% $(c, b \pm 30\%)$	-	$\leq 74\%$ $(c \pm 5\%, b \pm 50\%)$	-
		CIFAR-10	$c \pm 40\%, b \pm 40\%$	82.4%	0.0% $(c, b \pm 30\%)$	0.0% $(c, b \pm 30\%)$	-	-	-
		ImageNet	$c \pm 40\%, b \pm 40\%$	61.4%	-	-	-	-	-
Gaussian Blur, Translation, Bright- ness, and Contrast	Resolvable, Composition	MNIST	$\alpha \leq 1, \sqrt{\Delta x^2 + \Delta y^2} \leq 5, c, b \pm 10\%$	90.2%	-	-	-	-	-
		CIFAR-10	$\alpha \leq 1, \sqrt{\Delta x^2 + \Delta y^2} \leq 5, c, b \pm 10\%$	58.2%	-	-	-	-	-
		ImageNet	$\alpha \leq 10, \sqrt{\Delta x^2 + \Delta y^2} \leq 10, c, b \pm 20\%$	32.8%	-	-	-	-	-
Rotation	Differentially Resolvable	MNIST	$r \pm 50^\circ$	97.4%	$\leq 85.8\%$ $(r \pm 30^\circ)$	$\leq 6.0\%$ $(r \pm 30^\circ)$	-	$\leq 92.48\%$	82%
		CIFAR-10	$r \pm 10^\circ$	70.6%	62.5%	20.2%	-	-	37%
			$r \pm 30^\circ$	63.6%	10.6%	0.0%	-	$\leq 49.37\%$	22%
		ImageNet	$r \pm 30^\circ$	30.4%	-	-	-	-	16% (rand. attack)
Scaling	Differentially Resolvable	MNIST	$s \pm 30\%$	97.2%	85.0%	16.4%	-	-	-
		CIFAR-10	$s \pm 30\%$	58.8%	0.0%	0.0%	-	-	-
		ImageNet	$s \pm 30\%$	26.4%	-	-	-	-	-
Rotation and Brightness	Differentially Resolvable, Composition	MNIST	$r \pm 50^\circ, b \pm 20\%$	97.0%	-	-	-	-	-
		CIFAR-10	$r \pm 10^\circ, b \pm 10\%$	70.2%	-	-	-	-	-
			$r \pm 30^\circ, b \pm 20\%$	61.4%	-	-	-	-	-
		ImageNet	$r \pm 30^\circ, b \pm 20\%$	26.8%	-	-	-	-	-
Scaling and Brightness	Differentially Resolvable, Composition	MNIST	$s \pm 50\%, b \pm 50\%$	96.6%	-	-	-	-	-
		CIFAR-10	$s \pm 30\%, b \pm 30\%$	54.2%	-	-	-	-	-
		ImageNet	$s \pm 30\%, b \pm 30\%$	23.4%	-	-	-	-	-
Rotation, Brightness, and ℓ_2	Differentially Resolvable, Composition	MNIST	$r \pm 50^\circ, b \pm 20\%, \ \delta\ _2 \leq .05$	96.6%	-	-	-	-	-
		CIFAR-10	$r \pm 10^\circ, b \pm 10\%, \ \delta\ _2 \leq .05$	64.2%	-	-	-	-	-
			$r \pm 30^\circ, b \pm 20\%, \ \delta\ _2 \leq .05$	55.2%	-	-	-	-	-
		ImageNet	$r \pm 30^\circ, b \pm 20\%, \ \delta\ _2 \leq .05$	26.6%	-	-	-	-	-
Scaling, Brightness, and ℓ_2	Differentially Resolvable, Composition	MNIST	$s \pm 50\%, b \pm 50\%, \ \delta\ _2 \leq .05$	96.4%	-	-	-	-	-
		CIFAR-10	$s \pm 30\%, b \pm 30\%, \ \delta\ _2 \leq .05$	51.2%	-	-	-	-	-
		ImageNet	$s \pm 30\%, b \pm 30\%, \ \delta\ _2 \leq .05$	22.6%	-	-	-	-	-



Robustness under Existing Attacks

- We study actual robustness under a random attack and an adaptive attack
 - TSS accuracy under attack > TSS certified robust accuracy
 - TSS certification is correct
 - TSS certified robust accuracy >> Standard models' accuracy under attack
 - TSS certification is meaningful in practice
 - Adaptive attack reduces standard models' accuracy more
 - TSS models provides strong robustness against adaptive attacks
 - The gap between accuracy under attack and certified robust accuracy is larger for larger dataset (e.g., ImageNet)
 - Improvement rooms exist



Other Findings

There are many more transformations in the wild world

- Evaluated on natural corruption datasets CIFAR-10-C and ImageNet-C:
 - TSS models are still better than standard models
 - Sometimes even better than SOTA on CIFAR-10-C and ImageNet-C
 - * Evaluated on the highest level of corruptions
 - Provides strong robustness guarantees against transformation compositions, even on large-scale ImageNet

	CIFAR-10			ImageNet		
	Vanilla	AugMix [21]	TSS	Vanilla	AugMix [21]	TSS
Empirical Accuracy on CIFAR-10-C and ImageNet-C	53.9%	65.6%	67.4%	18.3%	25.7%	21.9%
Certified Accuracy against Composition of Gaussian Blur, Translation, Brightness, and Contrast	0.0%	0.4%	58.2%	0.0%	0.0%	32.8%



Other Findings (Cont.d)

- If the attack's perturbation radius (i.e., rotation angle) beyond the predefined radius used in training...
 - TSS still preserves high certified robust accuracy
 - For model defending 40% brightness change on ImageNet,
 - Certified accuracy against 40% change is 70.4%
 - Certified accuracy against 50% change is 70.0%
- Smoothing variance is a tunable hyperparameter
 - Small smoothing variance → high clean accuracy, small certified radius
 - Large smoothing variance → low clean accuracy, large certified radius
 - For highest certified accuracy under a given radius, an optimal smoothing variance exists



Conclusion

- **TSS**: a framework for certifying ML robustness against semantic transformations
- Categorize semantic transformations into resolvable (R) and differentiable resolvable (DR)
- Apply TSS-R and TSS-DR respectively
- Achieve significantly higher certified robustness than state-of-the-arts
- **First** work that achieves nontrivial certified robustness on ImageNet
- Achieve high empirical robustness against adaptive attacks and unforeseen transformations

Full paper

arxiv.org/abs/2002.12398

Slides

linyin1.com/res/pub/TSS-CCS21-slides.pdf

Code

github.com/AI-secure/semantic-randomized-smoothing

