Statistics 305: Introduction to Biostatistical Methods for Health Sciences

R Demos for Chapters 8-10: Review of Statistical Inference

Jinko Graham, Brad McNeney

Confidence Intervals (Chapter 9)

Example

- Example from the text, page 223, summarizes data on plasma aluminum levels, in $\mu g/l$, for $n = 10$ infants receiving antacids that contain aluminum.
  - The sample mean of the plasma aluminum levels is $\bar{x} = 37.20 \mu g/l$, and the sample SD is $s = 7.13$
- I can't access the data from the text, but I have simulated a data set of $n = 10$ subject with similar properties for this demo.
  - Read these data into R:

```
uu <- url("http://people.stat.sfu.ca/~jgraham/Teaching/S305_18/Data/pa.csv")
plasmaAlu <- read.csv(uu)
head(plasmaAlu)
```

```
##        alu
## 1 33.20381
## 2 35.55883
## 3 48.31359
## 4 37.70272
## 5 38.12182
## 6 49.42841
```

Simulated Data Summary Statistics

- Our simulated data are similar to the data from the text, but the sample mean and SD are different:

```
library(dplyr)
summarize(plasmaAlu,mean(alu))
```

```
##   mean(alu)
## 1  37.73208
```

```
summarize(plasmaAlu,sd(alu))
```

```
##   sd(alu)
## 1 6.80048
```

Software Notes

- Recall from the chapter 2-3 demo that `dplyr` is an add-on package for R that includes useful tools for manipulating datasets in R.
  - To use `dplyr` functions we must first load the package with `library(dplyr)`.
- The package consists of 5 main "verbs" for manipulating a dataframe:

1. `select()`: select columns
2. `filter()`: filter rows
3. `arrange()`: re-order or arrange rows
4. `mutate()`: create new columns
5. `summarize()`: summarise columns

- The `summarize()` function takes the dataframe as its first argument, and the summaries to compute as additional arguments.

Do-It-Yourself CIs in R

- In R, the quantile function `qt()` for the t distribution can be used to find the quantile or critical value (t^*) for the CI when σ is unknown.
  - When the argument `lower.tail=FALSE`, the first argument, `p`, is the upper-tail area to the right of the desired quantile, under the t distribution.

```
tstar<-qt(p=(1-0.95)/2,df=9,lower.tail=FALSE)
tstar
```

```
## [1] 2.262157
```

- Once we have the quantile or critical value, we can calculate the 95% CI.

- Use assignment operator <- to put the critical value into an R object called `tstar`.
- Then use `summarize()` function in `dplyr` package to get sample mean, sample sd and the number of observations, n. Assign these to an R object `mysummary`.
- Use the saved objects to calculate lower and upper bounds of CI and put them into the R object `CI`.

```
tstar <- qt(p=(1-0.95)/2,df=9,lower.tail=FALSE)
mysummary <- plasmaAlu %>%
  summarize(xbar=mean(alu),s=sd(alu),n=n()) %>%
  mutate(CI.lower=xbar-tstar*s/sqrt(n),
         CI.upper=xbar+tstar*s/sqrt(n))
mysummary
```

```
##       xbar       s  n CI.lower CI.upper
## 1 37.73208 6.80048 10 32.86731 42.59685
```

Chaining Data Manipulations

- In the above code chunk we used the "forward pipe", %>% to push the dataset from one data manipulation to another.
- Push the `plasmaAlu` dataframe through the pipe to use as input to `summarize()`, then take the dataframe output by summarize and push it through the pipe to use as input to `mutate()`.
- Each data-processing step is a verb (summarize, mutate)
- We are intended to read the result like a sentence:
  - Start with `plasmaAlu`,
  - summarize it (mean, SD and sample size),
  - then mutate it to add the lower and upper CI limits.
- Notice that we do not need to explicitly specify the input data to `summarize()` and `mutate()` when they receive these data through the forward pipe.

CIs with the `t.test()` Function

- R's `t.test()` uses data to test hypotheses about a mean, or about differences between two means, but the function also returns summary statistics and a CI.
- Set the level or coverage probability of the CI with the argument `conf.level` (default $C = 0.95$):

```
with(plasmaAlu,t.test(alu,conf.level=0.95))
```

```
##
##  One Sample t-test
##
## data:  alu
## t = 17.546, df = 9, p-value = 2.872e-08
## alternative hypothesis: true mean is not equal to 0
## 95 percent confidence interval:
##  32.86731 42.59685
## sample estimates:
## mean of x
##  37.73208
```

Hypothesis Tests (Chapter 10)

Example

- In the **population** of infants **not taking antacids**, the mean plasma-aluminum levels are known to be $\mu_0 = 4.13$ μg/l.
- Want to assess whether the mean level μ in infants taking antacids is the same as μ_0; i.e. whether

$$H_0 : \mu = 4.13.$$

- Our alternative hypothesis is $H_a : \mu \neq 4.13$; i.e.,the mean plasma-aluminum levels of infants taking antacids is different from infants not taking antacids.

Do-It-Yourself Hypothesis Test

- The t-statistic is

$$t = \frac{\bar{x} - \mu_0}{s/\sqrt{n}}$$

- We can implement this as follows using the summaries in the object `mysummary` from the CI demo:

```
mysummary
```

```
##       xbar       s  n CI.lower CI.upper
## 1 37.73208 6.80048 10 32.86731 42.59685
```

```
with(mysummary,(xbar - 4.13)/(s/sqrt(n)))
```

```
## [1] 15.62524
```

- The p-value is $2P(T \geq |15.63|)$ for T with $10 - 1 = 9$ df:

```
2*pt(15.63,df=9,lower.tail=FALSE)
```

```
## [1] 7.887651e-08
```

Using the `t.test()` Function

- The `t.test()` function will also perform the test.
  - Specify the null hypothesis $H_0 : \mu = 4.13$ with the `mu` argument.
  - The function's default is to use the two-sided alternative hypothesis, which in this case is $\mu \neq 4.13$:

```
with(plasmaAlu,t.test(alu,mu=4.13))
```

```
##
##  One Sample t-test
##
## data:  alu
## t = 15.625, df = 9, p-value = 7.909e-08
## alternative hypothesis: true mean is not equal to 4.13
## 95 percent confidence interval:
##  32.86731 42.59685
## sample estimates:
## mean of x
##  37.73208
```