# Statistics 305/605: Introduction to Biostatistical Methods for Health Sciences

R Demo for Chapter 18, part 2: Inference in Simple Linear Regression

Jinko Graham

## Load the Data and Fit the Regression Model

Load the data on low-birthweight babies:

```
uu <- url("http://people.stat.sfu.ca/~jgraham/Teaching/S305_17/Data/lbwt.csv")
lbwt <- read.csv(uu)</pre>
```

► Fit the regression model and print out the fitted regression coefficients:

```
lfit <- lm(headcirc ~ gestage,data=lbwt)
coefficients(lfit)

## (Intercept) gestage
## 3.9142641 0.7800532</pre>
```

▶ The regression parameters are estimated by  $\hat{\alpha} = 3.91$  (intercept) and  $\hat{\beta} = 0.78$  (gestage).

## Testing Example

summary(lfit)

► For the low-birthweight data, the model summary includes the p-value from the tests of  $H_0$ :  $\beta = 0$  vs.  $H_a$ :  $\beta \neq 0$ 

```
##
## Call:
## lm(formula = headcirc ~ gestage, data = lbwt)
##
## Residuals:
      Min
##
               10 Median
                              30
                                     Max
## -3.5358 -0.8760 -0.1458 0.9041 6.9041
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 3.91426 1.82915 2.14 0.0348 *
## gestage 0.78005 0.06307 12.37 <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.59 on 98 degrees of freedom
## Multiple R-squared: 0.6095, Adjusted R-squared: 0.6055
## F-statistic: 152.9 on 1 and 98 DF, p-value: < 2.2e-16
```

- We're interested specifically in the coefficients component of the summary.
- Can extract the coefficients component with the \$ operator.

#### summary(lfit)\$coefficients

```
## Estimate Std. Error t value Pr(>|t|)
## (Intercept) 3.9142641 1.82914689 2.13994 3.48424e-02
## gestage 0.7800532 0.06307441 12.36719 1.00121e-21
```

- ▶ The test statistic value is about 12.37 and the p-value is tiny.
- Strong statistical evidence for an association between gestational age and head circumference.

### Software Notes

- The output of the summary() function includes a lot of components that we are not yet ready for.
  - ► However summary(lfit)\$coefficients extracts just the coefficients table.
- Statistics related to a particular coefficient are in the row of the table labelled by the name of the explanatory variable.
  - ▶ E.G., Below the summaries related to the slope of the regression line are in the row labelled gestage.

#### summary(lfit)\$coefficients

```
## Estimate Std. Error t value Pr(>|t|)
## (Intercept) 3.9142641 1.82914689 2.13994 3.48424e-02
## gestage 0.7800532 0.06307441 12.36719 1.00121e-21
```

## CI Example

We can use the confint() function in R to extract a confidence interval.

```
## 2.5 % 97.5 %
## (Intercept) 0.2843817 7.5441466
## gestage     0.6548841 0.9052223
```

- ▶ The 95% CI for  $\beta$  is about (0.65, 0.91).
- ▶ Interpret: "With 95% confidence, we estimate that a one-week increase in gestational age is associated with an increase in head circumference of between 0.65 to 0.91 cm."

## Cls at Observed Values of Explanatory Variable

- Use the predict() function to get predictions and confidence intervals for each observed value of the explanatory variable.
- ▶ Default coverage probability or level for the CI is C = 0.95

```
lpred <- predict(lfit,interval="confidence")
head(lpred)</pre>
```

```
## fit lwr upr
## 1 26.53581 26.21989 26.85172
## 2 28.09591 27.68437 28.50745
## 3 29.65602 29.05247 30.25956
## 4 28.09591 27.68437 28.50745
## 5 27.31586 26.97102 27.66070
## 6 23.41559 22.83534 23.99584
```

- ▶ In a given row, 1st entry is fitted value  $\hat{y}$ , 2nd entry is lower bound of CI and last entry is upper bound of CI.
- Attach lpred to the corresponding values for y (headcirc) and x (gestage), to create a new R object called lbwtFits

. . .

lbwtFits <- data.frame(headcirc=lbwt\$headcirc,gestage=lbwt\$gestage,lpred)
head(lbwtFits)</pre>

```
##
    headcirc gestage
                          fit
                                   lwr
                                            upr
## 1
          27
                  29 26.53581 26.21989 26.85172
## 2
          29
                  31 28.09591 27.68437 28.50745
## 3
          30
                  33 29.65602 29.05247 30.25956
## 4
          28
                  31 28.09591 27.68437 28.50745
                  30 27.31586 26.97102 27.66070
## 5
          29
          23
                  25 23.41559 22.83534 23.99584
## 6
```

- ▶ The values of the response, y, are in the column headcirc.
- ► The values of the explanatory variable, x, are in the column gestage.
- ▶ The fitted values  $\hat{y}$  are in the column fit.
- ► The lower limits of the Cls are in the column lwr and the upper limits are in the column upr.

## 90% Cls at New Values of Explanatory Variable

- ► Suppose that we want 90% Cl's at new values of the explanatory variable, such as gestage of 25.5 and 30.5 weeks.
- Create a dataset with the new values of the explanatory variables and pass this to predict().
- Specify the level of the confidence interval with the level argument.

```
newdat <- data.frame(gestage = c(25.5,30.5))
predict(lfit,newdata = newdat, interval="confidence", level=.90)

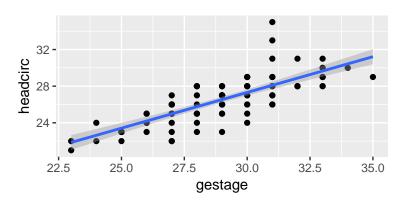
## fit lwr upr
## 1 23.80562 23.36311 24.24813
## 2 27.70589 27.39254 28.01923</pre>
```

- ► The fitted values ŷ of headcirc for gestages of 25.5 and 30.5 are in the column fit and are about 23.8 and 27.7, respectively.
- ► The lower limits of the 90% CIs are in the column lwr and the upper limits are in the column upr.

## Adding CIs to a Scatterplot

► By default, pointwise 95% CIs around the fitted regression line are added by ggplot() + geom\_smooth(method="lm")

```
library(ggplot2)
ggplot(lbwt, aes(x=gestage,y=headcirc)) +
   geom_point() +
   geom_smooth(method="lm")
```



- ► To change the default and add, e.g., pointwise 99% Cls around the fitted regression line, use the argument level in geom\_smooth():
  - ▶ geom\_smooth(method="lm", level=.99) for 99% Cls.

```
library(ggplot2)
ggplot(lbwt, aes(x=gestage,y=headcirc)) +
    geom_point() +
    geom_smooth(method="lm", level=.99)
```

