

# Statistics 452: Statistical Learning and Prediction

## Case Study

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### Flights dataset

This is the dataset being analyzed by the Stat 652 class for their final project. The data are on flights from three New York City airports in 2013, from the `nycflights13` package. Data were combined from four datasets from this package:

- `flights`
- `weather`
- `airports`, and
- `planes`

You can read about the variables in each dataset by typing `help(datasetname)` from the R console. Our goal is to predict departure delays (variable `dep_delay` in minutes).

```
library(tidyverse)
library(nycflights13)
#help(flights)
#help(weather)
#help(airports)
#help(planes)
fltrain <- read_csv("../Project652/fltrain.csv.gz")
fltrain
```

```
## # A tibble: 200,000 x 43
##   year.x month   day dep_time sched_dep_time dep_delay arr_time
##   <dbl> <dbl> <dbl>   <dbl>         <dbl>         <dbl>   <dbl>
## 1  2013     11     7     600             600           0     826
## 2  2013     10    30    1252            1250           2    1356
## 3  2013     12    18    1723            1715           8    2008
## 4  2013     11    20    2029            2030          -1    2141
## 5  2013     10    21    1620            1625          -5    1818
## 6  2013     11     7     852             900          -8    1139
## 7  2013     9     29    1519            1529         -10    1639
## 8  2013     12    21    1526            1530          -4    1654
## 9  2013     11     7    1650            1650           0    1910
## 10 2013     3     31    1652            1700          -8    1810
## # ... with 199,990 more rows, and 36 more variables: sched_arr_time <dbl>,
## #   arr_delay <dbl>, carrier <chr>, flight <dbl>, tailnum <chr>,
## #   origin <chr>, dest <chr>, air_time <dbl>, distance <dbl>, hour <dbl>,
## #   minute <dbl>, time_hour <dtm>, temp <dbl>, dewp <dbl>, humid <dbl>,
## #   wind_dir <dbl>, wind_speed <dbl>, wind_gust <dbl>, precip <dbl>,
## #   pressure <dbl>, visib <dbl>, name <chr>, lat <dbl>, lon <dbl>,
## #   alt <dbl>, tz <dbl>, dst <chr>, tzone <chr>, year.y <dbl>, type <chr>,
## #   manufacturer <chr>, model <chr>, engines <dbl>, seats <dbl>,
## #   speed <dbl>, engine <chr>
```

```
dim(fltrain)
```

```
## [1] 200000    43
```

There are 43 variables measured on 200,000 flights.

## Missing data

Handling of missing data is an important topic, but one that we did not consider in class. Two common ways to deal with missing data are to (i) remove observations with any missing data (complete-case analysis) and (ii) impute missing data. Both have their strengths and limitations. For simplicity we will remove observations. The danger is that our inference and/or predictions could be biased, which happens when the chance of a missing observation depends on the (unobserved) value of the missing data. However, a complete-case analysis is the most straightforward.

To ensure we are not discarding too many data points, we limit the **variables** to those with only a small proportion of missing values. One rule of thumb is to discard variables with more than 5% missing values, which is 10,000 for these data. To this end we count the number of missing values in each variable. The character variables have NA interpreted as a character string. This will be converted to the missing code NA if we coerce to a factor.

```
fl <- fltrain
for(i in 1:ncol(fl)) {
  if(typeof(fl[[i]]) == "character") {
    fl[[i]] <- factor(fl[[i]])
  }
}
```

Now count the missing values in each variable.

```
num_miss <- function(x) { sum(is.na(x)) }
sapply(fl,num_miss)
```

##	year.x	month	day	dep_time	sched_dep_time
##	0	0	0	4898	0
##	dep_delay	arr_time	sched_arr_time	arr_delay	carrier
##	4898	5169	0	5584	0
##	flight	tailnum	origin	dest	air_time
##	0	1492	0	0	5584
##	distance	hour	minute	time_hour	temp
##	0	0	0	0	948
##	dewp	humid	wind_dir	wind_speed	wind_gust
##	948	948	5862	982	152260
##	precip	pressure	visib	name	lat
##	937	23092	937	4484	4484
##	lon	alt	tz	dst	tzone
##	4484	4484	4484	4484	4484
##	year.y	type	manufacturer	model	engines
##	34298	31163	31163	31163	31163
##	seats	speed	engine		
##	31163	199415	31163		

Some of the variables, particularly those taken from the `planes` dataset (`year.y` to `engine`), have many missing values. In what follows I'll discard all of the variables from `planes`, plus `wind_gust` and `pressure`.

```
fl <- fl%>%
  select(-year.y, -type, -manufacturer, -model, -engines, -seats, -speed, -engine, -wind_gust, -pressure)
summary(fl)
```

##	year.x	month	day	dep_time
##	Min. :2013	Min. : 1.000	Min. : 1.0	Min. : 1

```

## 1st Qu.:2013    1st Qu.: 4.000    1st Qu.: 8.0    1st Qu.: 907
## Median :2013    Median : 7.000    Median :16.0    Median :1401
## Mean   :2013    Mean   : 6.553    Mean   :15.7    Mean   :1349
## 3rd Qu.:2013    3rd Qu.:10.000    3rd Qu.:23.0    3rd Qu.:1745
## Max.   :2013    Max.   :12.000    Max.   :31.0    Max.   :2400
##                                     NA's   :4898
## sched_dep_time  dep_delay      arr_time  sched_arr_time
## Min.   : 106    Min.   : -43.0    Min.   : 1      Min.   : 1
## 1st Qu.: 905    1st Qu.: -5.0    1st Qu.:1104    1st Qu.:1124
## Median :1359    Median : -2.0    Median :1535    Median :1557
## Mean   :1344    Mean   : 12.7    Mean   :1502    Mean   :1537
## 3rd Qu.:1729    3rd Qu.: 11.0    3rd Qu.:1941    3rd Qu.:1945
## Max.   :2359    Max.   :1301.0    Max.   :2400    Max.   :2359
##                                     NA's   :4898    NA's   :5169
## arr_delay      carrier      flight      tailnum
## Min.   : -79.000    UA      :34734    Min.   : 1      N725MQ : 350
## 1st Qu.: -17.000    B6      :32355    1st Qu.: 561    N723MQ : 300
## Median : -5.000    EV      :32217    Median :1499    N722MQ : 294
## Mean   : 6.969     DL      :28731    Mean   :1975    N711MQ : 290
## 3rd Qu.: 14.000    AA      :19415    3rd Qu.:3470    N713MQ : 260
## Max.   :1272.000    MQ      :15608    Max.   :8500    (Other):197014
## NA's   :5584      (Other):36940    NA's   : 1492
## origin      dest      air_time      distance
## EWR:71658    ATL      : 10319    Min.   : 20.0    Min.   : 17
## JFK:65951    ORD      : 10186    1st Qu.: 82.0    1st Qu.: 502
## LGA:62391    LAX      : 9472    Median :129.0    Median : 872
##                                     BOS      : 9217    Mean   :150.5    Mean   :1038
##                                     MCO      : 8425    3rd Qu.:191.0    3rd Qu.:1389
##                                     CLT      : 8319    Max.   :695.0    Max.   :4983
##                                     (Other):144062    NA's   :5584
## hour      minute      time_hour
## Min.   : 1.00    Min.   : 0.00    Min.   :2013-01-01 10:00:00
## 1st Qu.: 9.00    1st Qu.: 8.00    1st Qu.:2013-04-04 20:00:00
## Median :13.00    Median :29.00    Median :2013-07-03 15:00:00
## Mean   :13.18    Mean   :26.22    Mean   :2013-07-03 12:05:05
## 3rd Qu.:17.00    3rd Qu.:44.00    3rd Qu.:2013-10-01 12:00:00
## Max.   :23.00    Max.   :59.00    Max.   :2014-01-01 04:00:00
##
## temp      dewp      humid      wind_dir
## Min.   : 10.94    Min.   : -9.94    Min.   : 12.74    Min.   : 0.0
## 1st Qu.: 42.08    1st Qu.:26.06    1st Qu.: 43.99    1st Qu.:130.0
## Median : 57.20    Median :42.80    Median : 57.69    Median :220.0
## Mean   : 56.98    Mean   :41.62    Mean   : 59.57    Mean   :201.5
## 3rd Qu.: 71.96    3rd Qu.:57.92    3rd Qu.: 75.33    3rd Qu.:290.0
## Max.   :100.04    Max.   :78.08    Max.   :100.00    Max.   :360.0
## NA's   :948      NA's   :948      NA's   :948      NA's   :5862
## wind_speed      precip      visib
## Min.   : 0.000    Min.   :0.0000    Min.   : 0.000
## 1st Qu.: 6.905    1st Qu.:0.0000    1st Qu.:10.000
## Median :10.357    Median :0.0000    Median :10.000
## Mean   :11.107    Mean   :0.0045    Mean   : 9.252
## 3rd Qu.:14.960    3rd Qu.:0.0000    3rd Qu.:10.000
## Max.   :42.579    Max.   :1.2100    Max.   :10.000
## NA's   :982      NA's   :937      NA's   :937

```

```
##                                name                lat
## Hartsfield Jackson Atlanta Intl : 10319  Min.    :21.32
## Chicago Ohare Intl               : 10186  1st Qu.:32.90
## Los Angeles Intl                 :  9472  Median :36.10
## General Edward Lawrence Logan Intl:  9217  Mean   :36.02
## Orlando Intl                     :  8425  3rd Qu.:41.41
## (Other)                           :147897  Max.   :61.17
## NA's                             :  4484  NA's    :4484
##      lon                alt                tz                dst
## Min.    :-157.92  Min.    :   3.0  Min.    :-10.000  A    :192358
## 1st Qu.: -95.28  1st Qu.:  26.0  1st Qu.: -6.000  N    :  3158
## Median : -83.35  Median : 433.0  Median : -5.000  NA's:  4484
## Mean    : -89.44  Mean    : 582.5  Mean    : -5.748
## 3rd Qu.: -80.15  3rd Qu.: 748.0  3rd Qu.: -5.000
## Max.    : -68.83  Max.    :6602.0  Max.    : -5.000
## NA's    :4484    NA's    :4484  NA's    :4484
##                                tzone
## America/New_York    :114518
## America/Chicago     : 44400
## America/Los_Angeles: 27368
## America/Denver      :  6069
## America/Phoenix     :  2759
## (Other)              :   402
## NA's                 :  4484
```

When we omit rows with any missing values we end up with 184,316 rows out of the original 200,000.

```
fl <- na.omit(fl)
summary(fl)
```

```
##      year.x      month      day      dep_time
## Min.    :2013  Min.    : 1.000  Min.    : 1.00  Min.    :   1
## 1st Qu.:2013  1st Qu.: 4.000  1st Qu.: 8.00  1st Qu.: 910
## Median :2013  Median : 7.000  Median :16.00  Median :1408
## Mean    :2013  Mean    : 6.553  Mean    :15.67  Mean    :1353
## 3rd Qu.:2013  3rd Qu.:10.000  3rd Qu.:23.00  3rd Qu.:1747
## Max.    :2013  Max.    :12.000  Max.    :31.00  Max.    :2400
##
## sched_dep_time  dep_delay      arr_time  sched_arr_time
## Min.    : 500  Min.    : -43.00  Min.    :   1  Min.    :   1
## 1st Qu.: 905  1st Qu.:  -5.00  1st Qu.:1106  1st Qu.:1123
## Median :1359  Median :  -2.00  Median :1545  Median :1602
## Mean    :1342  Mean    : 12.67  Mean    :1511  Mean    :1544
## 3rd Qu.:1729  3rd Qu.: 11.00  3rd Qu.:1946  3rd Qu.:1950
## Max.    :2345  Max.    :1301.00  Max.    :2400  Max.    :2359
##
##      arr_delay      carrier      flight      tailnum
## Min.    : -79.000  UA      :32252  Min.    :   1  N725MQ :  322
## 1st Qu.: -17.000  B6      :29282  1st Qu.:  544  N723MQ :  271
## Median :  -5.000  EV      :29137  Median :1499  N711MQ :  268
## Mean    :   7.014  DL      :26998  Mean    :1966  N722MQ :  268
## 3rd Qu.:  14.000  AA      :17742  3rd Qu.:3448  N351JB :  247
## Max.    :1272.000  MQ      :14382  Max.    :8500  N258JB :  244
##
##      (Other):34523      (Other):182696
## origin      dest      air_time      distance
```

```

## EWR:65512   ATL   : 9726   Min.   : 20.0   Min.   : 80
## JFK:60327   ORD   : 9443   1st Qu.: 81.0   1st Qu.: 502
## LGA:58477   LAX   : 9185   Median :127.0   Median : 866
##              BOS   : 8674   Mean    :149.5   Mean    :1035
##              MCO   : 8131   3rd Qu.:184.0   3rd Qu.:1372
##              CLT   : 7822   Max.    :695.0   Max.    :4983
##              (Other):131335
##           hour      minute      time_hour
## Min.      : 5.00   Min.      : 0.00   Min.      :2013-01-01 10:00:00
## 1st Qu.    : 9.00   1st Qu.    : 8.00   1st Qu.    :2013-04-04 13:00:00
## Median     :13.00   Median     :29.00   Median     :2013-07-03 17:00:00
## Mean       :13.15   Mean       :26.06   Mean       :2013-07-03 11:34:16
## 3rd Qu.    :17.00   3rd Qu.    :43.00   3rd Qu.    :2013-10-02 10:00:00
## Max.       :23.00   Max.       :59.00   Max.       :2013-12-30 23:00:00
##
##           temp      dewp      humid      wind_dir
## Min.      : 10.94   Min.      : -9.94   Min.      : 13.00   Min.      : 0.0
## 1st Qu.    : 42.08   1st Qu.    :26.06   1st Qu.    : 43.71   1st Qu.    :130.0
## Median     : 57.02   Median     :42.08   Median     : 57.14   Median     :220.0
## Mean       : 56.86   Mean       :41.33   Mean       : 59.12   Mean       :201.9
## 3rd Qu.    : 71.96   3rd Qu.    :57.20   3rd Qu.    : 74.29   3rd Qu.    :290.0
## Max.       :100.04   Max.       :78.08   Max.       :100.00   Max.       :360.0
##
##           wind_speed      precip      visib
## Min.      : 0.000   Min.      :0.000000   Min.      : 0.000
## 1st Qu.    : 6.905   1st Qu.    :0.000000   1st Qu.    :10.000
## Median     :10.357   Median     :0.000000   Median     :10.000
## Mean       :11.202   Mean       :0.004059   Mean       : 9.294
## 3rd Qu.    :14.960   3rd Qu.    :0.000000   3rd Qu.    :10.000
## Max.       :42.579   Max.       :1.210000   Max.       :10.000
##
##                                     name      lat
## Hartsfield Jackson Atlanta Intl   : 9726   Min.      :21.32
## Chicago Ohare Intl                 : 9443   1st Qu.    :32.90
## Los Angeles Intl                   : 9185   Median     :36.08
## General Edward Lawrence Logan Intl : 8674   Mean       :35.97
## Orlando Intl                       : 8131   3rd Qu.    :41.41
## Charlotte Douglas Intl             : 7822   Max.       :61.17
## (Other)                            :131335
##           lon      alt      tz      dst
## Min.      : -157.92   Min.      : 3.0   Min.      : -10.000   A:181313
## 1st Qu.    : -95.34   1st Qu.    :26.0   1st Qu.    : -6.000   N: 3003
## Median     : -83.35   Median     :433.0   Median     : -5.000
## Mean       : -89.58   Mean       :582.3   Mean       : -5.757
## 3rd Qu.    : -80.15   3rd Qu.    :748.0   3rd Qu.    : -5.000
## Max.       : -68.83   Max.       :6602.0   Max.       : -5.000
##
##           tzone
## America/Anchorage : 3
## America/Chicago   : 41444
## America/Denver     : 5819
## America/Los_Angeles: 26461
## America/New_York   :107586
## America/Phoenix    : 2629

```

```
## Pacific/Honolulu : 374
```

## Summaries of the response variable dep\_delay

The departure delays variable is highly right-skewed.

```
range(fl$dep_delay)
```

```
## [1] -43 1301
```

```
fivenum(fl$dep_delay)
```

```
## [1] -43 -5 -2 11 1301
```

```
quantile(fl$dep_delay, probs = c(0.01, 0.05, 0.1, 0.25, .5, .75, .90, .95, .99))
```

```
## 1% 5% 10% 25% 50% 75% 90% 95% 99%
```

```
## -12 -9 -7 -5 -2 11 49 88 193
```

```
mean(fl$dep_delay >= 60) # about 15,000 or 8% of flights
```

```
## [1] 0.08210356
```

Top 10 delays.

```
fl %>% arrange(desc(dep_delay)) %>% head(10)
```

```
## # A tibble: 10 x 33
```

```
##   year.x month   day dep_time sched_dep_time dep_delay arr_time
##   <dbl> <dbl> <dbl>   <dbl>         <dbl>         <dbl>   <dbl>
## 1  2013     1     9     641             900           1301   1242
## 2  2013     9    20    1139            1845           1014   1457
## 3  2013     3    17    2321             810            911    135
## 4  2013     7    22    2257             759            898    121
## 5  2013    12     5     756            1700            896   1058
## 6  2013     5    19     713            1700            853   1007
## 7  2013     2    10    2243             830            853    100
## 8  2013    12    19     734            1725            849   1046
## 9  2013    12    17     705            1700            845   1026
## 10 2013    12    14     830            1845            825   1210
## # ... with 26 more variables: sched_arr_time <dbl>, arr_delay <dbl>,
## #   carrier <fct>, flight <dbl>, tailnum <fct>, origin <fct>, dest <fct>,
## #   air_time <dbl>, distance <dbl>, hour <dbl>, minute <dbl>,
## #   time_hour <dtm>, temp <dbl>, dewp <dbl>, humid <dbl>, wind_dir <dbl>,
## #   wind_speed <dbl>, precip <dbl>, visib <dbl>, name <fct>, lat <dbl>,
## #   lon <dbl>, alt <dbl>, tz <dbl>, dst <fct>, tzone <fct>
```

Summaries of departure delay by NYC airport:

```
Q3 <- function(x) { quantile(x, probs=.75) }
fl %>% group_by(origin) %>%
  summarize(n=n(), med_d = median(dep_delay), Q3_d = Q3(dep_delay), max_d = max(dep_delay)) %>%
  arrange(desc(Q3_d)) %>% head(10)
```

```
## # A tibble: 3 x 5
```

```
##   origin      n med_d  Q3_d max_d
##   <fct> <int> <dbl> <dbl> <dbl>
## 1 EWR    65512    -1    15   896
## 2 JFK    60327    -1    10  1301
```

```
## 3 LGA      58477      -3      7      911
```

Summaries of departure delay by airline (carrier).

```
fl %>% group_by(carrier) %>%  
  summarize(n=n(),med_d = median(dep_delay),Q3_d = Q3(dep_delay), max_d = max(dep_delay)) %>%  
  arrange(desc(Q3_d)) %>% head(10)
```

```
## # A tibble: 10 x 5  
##   carrier      n med_d  Q3_d max_d  
##   <fct>   <int> <dbl> <dbl> <dbl>  
## 1 EV      29137   -1    25    536  
## 2 WN       6897    1    18    471  
## 3 F9        388    0   17.2   853  
## 4 9E      10179   -2    16    430  
## 5 FL       1832    1    16    602  
## 6 YV        312   -3    13    387  
## 7 B6      29282   -1    12    502  
## 8 UA      32252    0    11    483  
## 9 MQ      14382   -3     9    486  
## 10 VX       2991    0     7    653
```

```
fl %>% group_by(origin,carrier) %>%  
  summarize(n=n(),med_d = median(dep_delay),Q3_d = Q3(dep_delay), max_d = max(dep_delay)) %>%  
  arrange(desc(Q3_d)) %>% head(10)
```

```
## # A tibble: 10 x 6  
## # Groups:   origin [3]  
##   origin carrier      n med_d  Q3_d max_d  
##   <fct> <fct>   <int> <dbl> <dbl> <dbl>  
## 1 EWR   00         3     4  67.5   131  
## 2 EWR   EV     23565   -1   26    443  
## 3 LGA   EV     4769   -2   22    473  
## 4 JFK   9E     8126   -1   20    430  
## 5 JFK   EV      803   -2   19    536  
## 6 EWR   WN     3487    2   18    440  
## 7 LGA   WN     3410    1   18    471  
## 8 LGA   F9       388    0  17.2   853  
## 9 EWR   MQ     1156   -2   17    381  
## 10 LGA  FL     1832    1   16    602
```

```
fl %>% group_by(dest,carrier) %>%  
  summarize(n=n(),med_d = median(dep_delay),Q3_d = Q3(dep_delay), max_d = max(dep_delay)) %>%  
  arrange(desc(Q3_d)) %>% head(10)
```

```
## # A tibble: 10 x 6  
## # Groups:   dest [10]  
##   dest carrier      n med_d  Q3_d max_d  
##   <fct> <fct>   <int> <dbl> <dbl> <dbl>  
## 1 STL   UA         2  77.5 116.   155  
## 2 DTW   00         2   61   96    131  
## 3 TYS   EV     183    8  68.5   285  
## 4 PBI   EV         3   50  67.5    85  
## 5 ORD   00         1   67   67     67  
## 6 RDU   UA         1   60   60     60  
## 7 TUL   EV     185    3   53    251  
## 8 OKC   EV     184   8.5  51.5   207
```

```
## 9 BHM EV 175 3 50 325
## 10 CAE EV 57 10 48 163
```

Summaries of departure delay by date:

```
f1 %>% group_by(month, day) %>%
  summarize(n=n(), med_d = mean(dep_delay), max_d = max(dep_delay)) %>%
  arrange(desc(med_d)) %>% head(10) # what happened on march 8?
```

```
## # A tibble: 10 x 5
## # Groups:   month [7]
##   month   day     n med_d max_d
##   <dbl> <dbl> <int> <dbl> <dbl>
## 1     3     8   461  79.5  470
## 2     7     1   505  58.1  363
## 3     7    10   471  56.6  576
## 4     9     2   438  53.7  696
## 5    12     5   458  52.2  896
## 6     5    23   453  51.5  410
## 7     4    19   511  50.4  812
## 8     9    12   444  50.4  602
## 9     6    13   469  50.3  388
## 10    7    22   476  49.9  898
```

Summaries of departure delay by precipitation:

```
f1 %>% mutate(haveprecip = factor(precip>0)) %>% group_by(haveprecip) %>%
  summarize(n=n(), med_d = median(dep_delay), Q3_d = Q3(dep_delay), max_d = max(dep_delay)) %>%
  arrange(desc(med_d)) %>% head(10)
```

```
## # A tibble: 2 x 5
##   haveprecip     n med_d  Q3_d max_d
##   <fct>       <int> <dbl> <dbl> <dbl>
## 1 TRUE      11804     5    41   853
## 2 FALSE   172512    -2     9  1301
```

## What can we predict?

Extremes seem to be caused by phenomena not in our data, such as snow storms, mechanical breakdowns (?), etc.

Perhaps we should map these extremes to something less extreme. Consider mapping to quantiles of the standard normal (like grading departure delays on a “curve”).

```
#f1 <- f1 %>% mutate(dep_delay = qqnorm(dep_delay)$x)
f1 <- f1 %>% mutate(dep_delay = rank(dep_delay))
```