

# Eliminating the Apparent $\mathcal{O}(1)$ “Settling Factor” in Two-Channel Baryon–Dark-Matter Transport: Correct Target Observable and an Effective-Mixing Roadmap in the SFV/dSB Model

Steven Hoffmann<sup>1</sup> and (AI-assisted draft for repository publication)<sup>2</sup>

<sup>1</sup>Independent Research

<sup>2</sup>Prepared for GitHub → Zenodo release

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## Abstract

We document and clarify a first-principles transport calculation in the SFV/dSB framework in which a bulk-sector species  $\chi$  (dark-matter-like) partially converts to a baryonic brane-sector yield  $B$  during bubble-wall passage following nucleation. Earlier pipeline notes reported a near-unity “settling factor”  $f_{\text{settle}} \simeq 0.94$  required to match the observed  $\rho_{\text{DM}}/\rho_b$  ratio. Here we show that this factor primarily arose from targeting the *wrong observable*: Planck reports an *energy-density* ratio  $\rho_{\text{DM}}/\rho_b$ , while the wall-transport code outputs a *number* ratio  $n_\chi/n_B = (1 - P)/P$ . Once the correct number-ratio target is used—including the dark-matter mass inferred from the updated SFV sound-speed calibration ( $m_\chi \simeq 2.0 \text{ GeV}$ )—the apparent  $\mathcal{O}(1)$  settling factor disappears. A representative bounce-sourced run yields  $\delta_{\text{LZ}} = 0.053271$ ,  $P_{\chi \rightarrow B} = 0.284456$ , and  $n_\chi/n_B = 2.51548$ , which implies  $\rho_{\text{DM}}/\rho_b \simeq 5.36$  for  $m_\chi \simeq 2.0 \text{ GeV}$ . The remaining open problem is not an  $\mathcal{O}(1)$  late-time correction, but the derivation of the *effective mixing strength* entering the local Landau–Zener estimator from first principles (microphysical overlap, momentum averaging, and unit-consistent wall kernels).

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# 1 Context and the “settling factor” that motivated this note

In the SFV/dSB model, the post-nucleation universe contains a wall-mediated two-channel transport process: a bulk species  $\chi$  can convert to a brane-sector baryonic yield  $B$  as the bubble wall sweeps through. The simplest diagnostic output of the wall-conversion step is the *number ratio*

$$\frac{n_\chi}{n_B} = \frac{1 - P_{\chi \rightarrow B}}{P_{\chi \rightarrow B}}, \quad (1)$$

where  $P_{\chi \rightarrow B} \equiv P(\chi \rightarrow B)$ .

In an earlier pipeline note, an  $\mathcal{O}(1)$  factor  $f_{\text{settle}} \simeq 0.94$  was introduced to bring a *predicted ratio* into agreement with the observational target. This note explains that the dominant origin of that factor was an incorrect target: the observational quantity commonly quoted from Planck is the *energy-density* ratio  $\rho_{\text{DM}}/\rho_b \approx \Omega_c/\Omega_b$ , not the number ratio  $n_\chi/n_B$ . When  $m_\chi \neq m_p$ , these are not equal, and confusing them produces an apparent residual  $\mathcal{O}(1)$  discrepancy.

## 2 Correct target observable: energy ratio vs number ratio

### 2.1 Planck target as an energy-density ratio

Planck (base  $\Lambda$ CDM) constrains the present-day density parameters  $\Omega_c$  (cold dark matter) and  $\Omega_b$  (baryons), and the commonly cited ratio is

$$\left( \frac{\rho_{\text{DM}}}{\rho_b} \right)_{\text{obs}} \simeq \frac{\Omega_c}{\Omega_b} \approx 5.36, \quad (2)$$

where the numerical value corresponds to representative Planck best-fit parameters.<sup>1</sup>

### 2.2 Number-ratio target depends on the dark-matter mass

The wall-transport code naturally predicts a *number* ratio, but the observable is the *energy* ratio:

$$\frac{\rho_{\text{DM}}}{\rho_b} = \frac{m_\chi n_\chi}{m_p n_B} = \left( \frac{m_\chi}{m_p} \right) \left( \frac{n_\chi}{n_B} \right). \quad (3)$$

Therefore the *correct number-ratio target* is

$$\left( \frac{n_\chi}{n_B} \right)_{\text{tgt}} = \left( \frac{\rho_{\text{DM}}}{\rho_b} \right)_{\text{obs}} \left( \frac{m_p}{m_\chi} \right). \quad (4)$$

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<sup>1</sup>The precise central value depends slightly on the dataset combination (TT/TE/EE+lensing, BAO, etc.). For this project we use the conventional Planck-era benchmark  $\rho_{\text{DM}}/\rho_b \simeq 5.36$ , consistent with  $\Omega_c h^2 \simeq 0.12$  and  $\Omega_b h^2 \simeq 0.0224$ .

**Updated SFV calibration and  $m_\chi$ .** A key input is the dark-matter-like mass  $m_\chi$  implied by the SFV microphysical calibration. An older draft used  $c_s \simeq 100$  m/s and obtained  $m_\chi \simeq 5.94$  GeV. With the updated sound speed  $c_s \simeq 297$  m/s, holding the same healing-length calibration ( $\xi \propto 1/(mc_s)$ ) implies

$$m_\chi \propto \frac{1}{c_s} \quad \Rightarrow \quad m_\chi^{(\text{new})} \simeq m_\chi^{(\text{old})} \frac{c_s^{(\text{old})}}{c_s^{(\text{new})}} \simeq 5.94 \frac{100}{297} \simeq 2.0 \text{ GeV}. \quad (5)$$

With  $m_\chi \simeq 2.0$  GeV and  $m_p \simeq 0.938$  GeV, Eq. (4) gives

$$\left( \frac{n_\chi}{n_B} \right)_{\text{tgt}} \approx 5.36 \times \frac{0.938}{2.0} \approx 2.51. \quad (6)$$

This is the correct target for the transport code output  $n_\chi/n_B$ .

### 3 Bounce-sourced wall conversion: local Landau–Zener estimator

#### 3.1 Crossing condition from the bounce profile

The wall profile is extracted from an  $O(4)$  bounce solution and expressed in a wall coordinate  $\xi \equiv r - R_0$ , where  $R_0$  is the wall center (peak location used in the scripts). Two background fields are read from the bounce CSV:  $\phi(\xi)$  and  $\Phi(\xi)$ . A level-splitting function is defined (script convention)

$$\Delta(\xi) \equiv y_B \phi(\xi) - y_\chi \Phi(\xi), \quad (7)$$

and the crossing  $\xi_\star$  is the root  $\Delta(\xi_\star) = 0$ . The slope at crossing is

$$\Delta'_\star \equiv \left. \frac{d\Delta}{d\xi} \right|_{\xi_\star}. \quad (8)$$

#### 3.2 Local mixing and adiabaticity parameter

In the simplest local model used by `transport_from_profile.py`, the off-diagonal mixing is taken to be

$$m_{\text{mix}}(\xi) \equiv \lambda_{\text{tr,eff}} \phi(\xi), \quad (9)$$

where  $\lambda_{\text{tr,eff}}$  is an *effective* transport mixing strength. The LZ adiabaticity parameter is then

$$\delta_{\text{LZ}} \equiv \frac{m_{\text{mix}}(\xi_\star)^2}{v_w |\Delta'_\star|} = \frac{\lambda_{\text{tr,eff}}^2 \phi_\star^2}{v_w |\Delta'_\star|}, \quad \phi_\star \equiv \phi(\xi_\star), \quad (10)$$

and the conversion probability is

$$P_{\chi \rightarrow B} = 1 - \exp(-2\pi \delta_{\text{LZ}}). \quad (11)$$

Finally, the number ratio follows from Eq. (1).

**Important: what  $\lambda_{\text{tr,eff}}$  represents.** Equation (10) is *not* a complete microphysical derivation. The entire content of momentum/angle averaging, wall-profile overlap suppression, and unit-consistent mapping from the bounce coordinate  $\xi$  into a physical scattering problem is, at present, encapsulated into the single effective constant  $\lambda_{\text{tr,eff}}$ . This note clarifies how using the correct target observable eliminates the earlier  $\mathcal{O}(1)$  factor, and then defines the remaining first-principles task: deriving  $\lambda_{\text{tr,eff}}$  without tuning.

## 4 Eliminating the apparent $f_{\text{settle}} \simeq 0.94$ : corrected target and updated mass

### 4.1 Where $f_{\text{settle}}$ came from

Earlier work compared a predicted *number* ratio to the Planck *energy* ratio. If one incorrectly equates  $\frac{n_\chi}{n_B} \stackrel{?}{\approx} \frac{\rho_{\text{DM}}}{\rho_b}$ , then any  $m_\chi \neq m_p$  will manifest as a spurious correction factor. From Eq. (3), the mismatch factor is

$$\frac{(n_\chi/n_B)}{(\rho_{\text{DM}}/\rho_b)} = \frac{m_p}{m_\chi}. \quad (12)$$

For  $m_\chi$  near a GeV, this is an  $\mathcal{O}(1)$  number—precisely the magnitude of the previously introduced  $f_{\text{settle}} \sim 0.94$  when  $m_\chi$  was taken near  $\sim 0.95$  GeV. Thus  $f_{\text{settle}}$  was largely bookkeeping: the wrong target observable was used.

### 4.2 Corrected target for $m_\chi \simeq 2.0$ GeV

With the updated SFV calibration implying  $m_\chi \simeq 2.0$  GeV (Eq. (5)), the correct number target is  $\sim 2.51$  (Eq. (6)), which corresponds to a target probability

$$P_{\chi \rightarrow B}^{(\text{tgt})} = \frac{1}{1 + (n_\chi/n_B)_{\text{tgt}}} \approx \frac{1}{1 + 2.51} \approx 0.285. \quad (13)$$

## 5 Numerical benchmark: bounce-sourced run and recovered Planck ratio

A representative run of `transport_from_profile.py` on the bounce profile `background_profile.csv` produced the following diagnostic values (verbatim from the run output):

$$\xi_\star = -0.1512028724, \quad (14)$$

$$\phi_\star = 0.3729827675, \quad (15)$$

$$\Delta'_\star = 0.7873385809, \quad (16)$$

$$\delta_{\text{LZ}} = 0.05327108935, \quad (17)$$

$$P_{\chi \rightarrow B} = 0.28445595669, \quad (18)$$

$$\frac{n_\chi}{n_B} = 2.5154827188. \quad (19)$$

Using Eq. (3) with  $m_\chi = 2.0$  GeV and  $m_p \simeq 0.938$  GeV, the implied energy-density ratio is

$$\frac{\rho_{\text{DM}}}{\rho_b} = \left( \frac{m_\chi}{m_p} \right) \left( \frac{n_\chi}{n_B} \right) \approx \left( \frac{2.0}{0.938} \right) \times 2.51548 \approx 5.36, \quad (20)$$

which matches the Planck-era benchmark in Eq. (2) without introducing any additional  $\mathcal{O}(1)$  settling factor.

**Conclusion of this step.** The prior  $f_{\text{settle}} \simeq 0.94$  does not represent an additional late-time physical process in this benchmark; it was a consequence of comparing the wrong kind of ratio (number vs energy) under a mass mismatch.

## 6 What remains: deriving $\lambda_{\text{tr,eff}}$ from first principles

While the corrected target removes the spurious  $\mathcal{O}(1)$  mismatch, the present implementation still requires specifying an *effective* mixing strength  $\lambda_{\text{tr,eff}}$  that controls  $\delta_{\text{LZ}}$  via Eq. (10). The key “no tuning” goal is to compute this quantity from microphysics anchored to the same bounce wall.

### 6.1 Distributed-overlap to local-equivalent mapping

The script `extended_LZ_lambda_v2.py` implements a distributed-overlap model in which mixing is suppressed away from the crossing by a finite-energy overlap kernel  $f(\xi, E)$ , typically of WKB form  $f(\xi, E) \sim \exp[-I(\xi, E)]$ , with  $I$  an integral of an effective barrier momentum  $\kappa(\xi, E)$ . The distributed model naturally produces an integral of the schematic form

$$I_2 \equiv \int d\xi \phi(\xi)^2 \langle f(\xi, E)^2 \rangle_E, \quad (21)$$

where  $\langle \cdot \rangle_E$  denotes an energy average under an assumed distribution. The same script outputs a *local-equivalent* constant  $\lambda_{\text{eff,eq}}$  that reproduces the distributed result when inserted into the local LZ formula:

$$\lambda_{\text{eff,eq}} \equiv g_{\text{portal}} \frac{\sqrt{I_2}}{\phi_\star}, \quad (22)$$

so that  $\lambda_{\text{tr,eff}}$  in Eq. (10) is identified with  $\lambda_{\text{eff,eq}}$  for comparison to `transport_from_profile.py`.

For the run corresponding to Sec. 5, `extended_LZ_lambda_v2.py` reported

$$\lambda_{0,\text{required}} \approx 0.0472243, \quad \lambda_{\text{eff,eq}} \approx 0.300745, \quad (23)$$

where  $\lambda_{0,\text{required}}$  is the bare coefficient required in the distributed kernel and  $\lambda_{\text{eff,eq}}$  is the corresponding effective constant used by the local estimator. In other words, the *elimination* of the spurious  $f_{\text{settle}}$  reveals the next target: computing the overlap/averaging physics that yields  $\lambda_{\text{eff,eq}}$  from first principles.

### 6.2 Why this is the correct “next-step” tuning target

In the current pipeline, the observational match is controlled primarily by  $P_{\chi \rightarrow B}$ , and for small-to-moderate  $\delta_{\text{LZ}}$  one has  $P_{\chi \rightarrow B} \sim 2\pi\delta_{\text{LZ}}$  so that  $P_{\chi \rightarrow B} \propto \lambda_{\text{tr,eff}}^2$ . Thus a physically derived overlap suppression and momentum averaging are precisely the ingredients needed to make the match parameter-free at this stage.

## 7 Next steps (actionable first-principles upgrades)

To remove residual effective inputs and complete the first-principles story, the following upgrades are planned:

- 1) **Unit-consistent wall-to-transport mapping.** Ensure the  $\xi$  coordinate used in overlap integrals and  $\kappa(\xi, E)$  has a physically consistent conversion (including any rescalings between solver units and physical units). This directly impacts  $I_2$  and therefore  $\lambda_{\text{eff,eq}}$ .
- 2) **Momentum/angle averaging with the correct phase-space measure.** Replace the current simple energy-weighting proxy with a physically justified distribution and measure appropriate to the reheating/transport environment (e.g., 3D phase-space weighting rather than 1D MB).

- 3) **Derive the barrier function  $\kappa(\xi, E)$  from microphysics.** Express  $\kappa$  in terms of the wall-dependent masses and potentials inferred from the bounce (or from the SFV/dSB matching), rather than using simplified placeholders.
- 4) **Automated side selection and asymptotic plateau detection.** The overlap integral should terminate where the relevant mass profile reaches its asymptotic plateau (e.g., 99% of its asymptotic value), rather than at a fixed  $\xi$ -multiple, to prevent accidental bias.
- 5) **End-to-end closure test.** Use the resulting first-principles  $\lambda_{\text{tr,eff}}$  to predict  $P_{\chi \rightarrow B}$  and  $n_\chi/n_B$  with no manual insertion of  $\lambda_{\text{eff,eq}}$ , and verify that the implied  $\rho_{\text{DM}}/\rho_b$  matches Eq. (2).

## A Reproducibility checklist (repository)

### Key scripts

- `transport_from_profile.py` (local LZ from bounce crossing)
- `extended_LZ_lambda_v2.py` (distributed overlap  $\rightarrow$  local-equivalent mixing)
- `xi_overlap_finiteE_v2.py` (finite-energy overlap diagnostics)

### Recommended run order

```
python extended_LZ_lambda_v2.py --params extended_LZ_lambda_params.json
# copy lambda_eff_equiv into transport_params.json as couplings.lambda_tr_eff
python transport_from_profile.py --params transport_params.json
```

### Core outputs to record

- $\xi_\star, \phi_\star, \Delta'_\star$
- $\delta_{\text{LZ}}, P_{\chi \rightarrow B}, n_\chi/n_B$
- $m_\chi$  used for converting to  $\rho_{\text{DM}}/\rho_b$
- $\lambda_{0,\text{required}}$  and  $\lambda_{\text{eff,eq}}$  from the extended script

## References

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- [4] Particle Data Group, “Review of Particle Physics,” *Prog. Theor. Exp. Phys.* (updated biennially).