

Package ‘SGDinference’

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Type Package

Title Inference with Stochastic sub-Gradient Descent

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Author SGDinference-Lab

Maintainer Youngki Shin <yshin12@gmail.com>, Sokbae ``Simon" Lee <sokbae@gmail.com>

Description This package provides R code to apply the S-subGD method. The algorithm is developed for fast and robust inference with large-scale quantile regression.

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Imports Rcpp (>= 1.0.5)

LinkingTo Rcpp, RcppArmadillo

RoxygenNote 7.2.1

Encoding UTF-8

Suggests knitr,
rmarkdown

VignetteBuilder knitr

R topics documented:

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sgdi

*Averaged SGD and its Inference via Random Scaling***Description**

Compute the averaged SGD estimator and the variance-covariance matrix via random scaling method.

Usage

```
sgdi(
  x,
  y,
  gamma_0 = 1,
  alpha = 0.667,
  burn = 1,
  model = "lm",
  inference = "rs",
  bt_start = NULL,
  path_output = NULL,
  qt = 0.5,
  studentize = TRUE,
  intercept = TRUE,
  rss_idx = c(1)
)
```

Arguments

| | |
|--------------------------|--|
| <code>x</code> | numeric. (n x p) matrix of regressors. Should not include 1 (the intercept) |
| <code>y</code> | numeric. (n x 1) vector of a dependent variable. |
| <code>gamma_0</code> | numeric. A tuning parameter for the learning rate ($\gamma_0 \times t^\alpha$). Default is 1. |
| <code>alpha</code> | numeric. A tuning parameter for the learning rate ($\gamma_0 \times t^\alpha$). Default is 0.667. |
| <code>burn</code> | numeric. A tuning parameter for "burn-in" observations. We burn-in up to (burn-1) observations and use observations from (burn) for estimation. Default is 1, i.e. no burn-in. |
| <code>model</code> | character specifying the model to be used: "lm" (linear mean regression model), "qr" (quantile regression) |
| <code>inference</code> | character. Specifying the inference method. Default is "rs" (random scaling). "rss" is for random scaling subset inference. Then, "rss_idx" should be provided. |
| <code>bt_start</code> | numeric. (p x 1) vector. User-provided starting value Default is NULL. |
| <code>path_output</code> | numeric specifying the sequence that print out the output paths |
| <code>qt</code> | numeric. Quantile. Default is 0.5. |

| | |
|------------|--|
| studentize | logical. Studentize regressors. Default is TRUE |
| intercept | logical. Use the intercept term for regressors. Default is TRUE |
| rss_idx | numeric. Index of x for random scaling subset inference. Default is 1, the first regressor of x. For example, if we want to infer the 1st, 3rd covariate of x, then set it to be c(1,3). |

Value

An object of class "sgdi", which is a list containing the following

- beta_hat A (p + 1)-vector of estimated parameter values including the intercept.
- V_hat A (p+1)x (p+1) variance-covariance matrix of beta_hat
- V_hat_sub A variance-covariance sub-matrix of beta_hat. If the subset size is not provided, it returns 0.

Examples

```
n = 1e05
p = 5
bt0 = rep(5,p)
x = matrix(rnorm(n*(p-1)), n, (p-1))
y = cbind(1,x) %*% bt0 + rnorm(n)
sgdi.out = sgdi(x,y)
```

| | |
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| SGDinference | <i>SGDinference</i> |
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Description

ADD DESCRIPTION LATER

Author(s)

SGDinference-Lab

sgdi_boot_qr

*Inference of quantile regression with SGD and random scaling***Description**

Compute the averaged SGD estimator of quantile regression and the confidence intervals via random scaling method.

Usage

```
sgdi_boot_qr(
  x,
  y,
  gamma_0 = 1,
  alpha = 0.667,
  burn = 1,
  inference = "boot",
  bt_start = NULL,
  path_output = NULL,
  qt = 0.5,
  studentize = TRUE,
  intercept = TRUE,
  n_boot = 1000
)
```

Arguments

| | |
|-------------|---|
| x | numeric. (n x p) matrix of regressors. Should not include 1 (the intercept) |
| y | numeric |
| gamma_0 | numeric. Tuning parameter for the learning rate: $\gamma_0 * n^{(\alpha)}$ (default is 1) |
| alpha | numeric. Tuning parameter for the learning rate: $\gamma_0 * n^{(\alpha)}$ (default is 0.667) |
| burn | numeric. Number of burn-in observations (default is 1, no burn-in) |
| inference | character specifying the inference method. Default is "rs" (random scaling) |
| bt_start | numeric. |
| path_output | numeric specifying the sequence that print out the output paths |
| qt | numeric. Quantile. Default is 0.5. |
| studentize | logical. Studentize regressors. Default is TRUE |
| intercept | logical. Use the intercept term for regressors. Default is TRUE |
| n_boot | numeric. The number of bootstrap samples. Default is 1000. |

Value

#' An object of class "sgdi", which is a list containing the following components:

Examples

```

n = 1e05
p = 5
bt0 = rep(5,p)
x = matrix(rnorm(n*(p-1)), n, (p-1))
y = cbind(1,x) %*% bt0 + rnorm(n)
sgdi.out = sgdi_qr(x,y)

```

sgdi_lm

*Averaged SGD and its Inference via Random Scaling***Description**

Compute the averaged SGD estimator and the confidence intervals via random scaling method.

Usage

```

sgdi_lm(
  x,
  y,
  gamma_0 = 1,
  alpha = 0.667,
  burn = 1,
  inference = "rs",
  bt_start = NULL,
  path_output = NULL,
  studentize = TRUE,
  intercept = TRUE
)

```

Arguments

| | |
|-------------|---|
| x | numeric. (n x p) matrix of regressors. Should not include 1 (the intercept) |
| y | numeric |
| gamma_0 | numeric |
| alpha | numeric |
| burn | numeric |
| inference | character specifying the inference method. Default is "rs" (random scaling) |
| bt_start | numeric |
| path_output | numeric specifying the sequence that print out the output paths |
| studentize | logical. Studentize regressors. Default is TRUE |
| intercept | logical. Use the intercept term for regressors. Default is TRUE |

Value

#' An object of class "sgdi", which is a list containing the following components:

Examples

```
n = 1e05
p = 5
bt0 = rep(5,p)
x = matrix(rnorm(n*(p-1)), n, (p-1))
y = cbind(1,x) %*% bt0 + rnorm(n)
sgdi.out = sgdi(x,y)
```

| | |
|-------------|-------------------|
| sgdi_lm_cpp | <i>Leading NA</i> |
|-------------|-------------------|

Description

Explanation

Usage

```
sgdi_lm_cpp(x, y, burn, gamma_0, alpha, bt_start, inference)
```

Arguments

| | |
|-----------|---|
| x | numeric. (n x p) matrix of regressors. Should not include 1 (the intercept) |
| y | numeric |
| burn | numeric |
| gamma_0 | numeric |
| alpha | numeric |
| bt_start | numeric |
| inference | character specifying the inference method. Default is "rs" (random scaling) |

Description

Compute the averaged SGD estimator of quantile regression and the confidence intervals via random scaling method.

Usage

```
sgdi_qr(
  x,
  y,
  gamma_0 = 1,
  alpha = 0.667,
  burn = 1,
  inference = "rs",
  bt_start = NULL,
  path_output = NULL,
  qt = 0.5,
  studentize = TRUE,
  intercept = TRUE,
  rss_idx = c(1)
)
```

Arguments

| | |
|-------------|--|
| x | numeric. (n x p) matrix of regressors. Should not include 1 (the intercept) |
| y | numeric |
| gamma_0 | numeric. Tuning parameter for the learning rate: $\gamma_0 * n^{\alpha}$ (default is 1) |
| alpha | numeric. Tuning parameter for the learning rate: $\gamma_0 * n^{\alpha}$ (default is 0.667) |
| burn | numeric. Number of burn-in observations (default is 1, no burn-in) |
| inference | character specifying the inference method. Default is "rs" (random scaling). |
| bt_start | numeric. |
| path_output | numeric specifying the sequence that print out the output paths |
| qt | numeric. Quantile. Default is 0.5. |
| studentize | logical. Studentize regressors. Default is TRUE |
| intercept | logical. Use the intercept term for regressors. Default is TRUE |
| rss_idx | numeric. Index of x for random scaling subset inference. Default is 1, the first regressor of x. |

Value

#' An object of class "sgdi", which is a list containing the following components:

Examples

```
n = 1e05
p = 5
bt0 = rep(5,p)
x = matrix(rnorm(n*(p-1)), n, (p-1))
y = cbind(1,x) %*% bt0 + rnorm(n)
sgdi.out = sgdi_qr(x,y)
```

sgd_qr

*Averaged SsubGD estimator for quantile regression***Description**

Compute the averaged SGD estimator for quantile regression. This function computes only the point estimate.

Usage

```
sgd_qr(
  x,
  y,
  gamma_0 = 1,
  alpha = 0.667,
  burn = 1,
  bt_start = NULL,
  path_output = NULL,
  qt = 0.5,
  studentize = TRUE,
  intercept = TRUE
)
```

Arguments

| | |
|---------|--|
| x | numeric. (n x p) matrix of regressors. Should not include 1 (the intercept) |
| y | numeric. (n x 1) vector of a dependent variable. |
| gamma_0 | numeric. A tuning parameter for the learning rate ($\text{gamma}_0 \times t^\alpha$). Default is 1. |
| alpha | numeric. A tuning parameter for the learning rate ($\text{gamma}_0 \times t^\alpha$). Default is 0.667. |
| burn | numeric. A tuning parameter for "burn-in" observations. We burn-in up to (burn-1) observations and use observations from (burn) for estimation. Default is 1, i.e. no burn-in. |

| | |
|-------------|--|
| bt_start | numeric. (p x 1) vector. User-provided starting value Default is NULL. |
| path_output | numeric specifying the sequence that print out the output paths |
| qt | numeric. Quantile. Default is 0.5. |
| studentize | logical. Studentize regressors. Default is TRUE |
| intercept | logical. Use the intercept term for regressors. Default is TRUE |

Value

An object of class "sgd_qr", which is a list containing the following

beta_hat A (p + 1)-vector of estimated parameter values including the intercept.

beta_hat_path A (p+1) x P matrix. The path of estimated coefficient values, where P is the length of the path

Examples

```
n = 1e05
p = 5
bt0 = rep(5,p)
x = matrix(rnorm(n*(p-1)), n, (p-1))
y = cbind(1,x) %*% bt0 + rnorm(n)
sgd.out = sgd_qr(x,y)
```

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