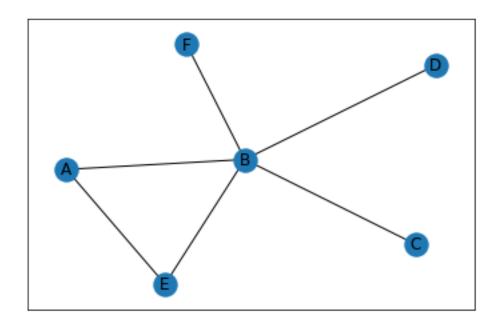
munity-detection-using-networkx-2

December 18, 2023

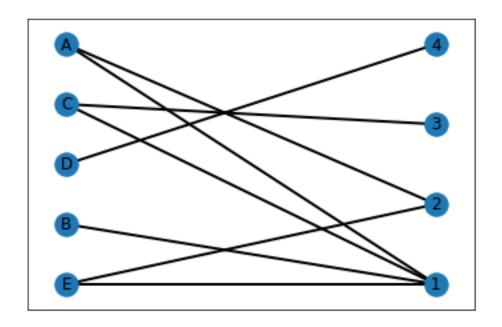
```
[1]: import numpy as np
     import matplotlib.pyplot as plt
     import networkx as nx
[2]: G = nx.Graph()
     G.add_edge('A','B',weight=13,relation='friend')
     G.add_edge('B','C',weight=9,relation='family')
     G.add_edge('B','D',weight=7,relation='friend')
     G.add_edge('E','B',weight=10,relation='friend')
     G.add edge('E','A',weight=1,relation='enemy')
     G.add_edge('F','B',weight=13,relation='family')
     G.edges(data=True)
[2]: EdgeDataView([('A', 'B', {'weight': 13, 'relation': 'friend'}), ('A', 'E',
     {'weight': 1, 'relation': 'enemy'}), ('B', 'C', {'weight': 9, 'relation':
     'family'}), ('B', 'D', {'weight': 7, 'relation': 'friend'}), ('B', 'E',
     {'weight': 10, 'relation': 'friend'}), ('B', 'F', {'weight': 13, 'relation':
     'family'})])
[3]: G.add node('A',role='Trader')
     G.add_node('B',role='Analyst')
     G.add_node('C',role='Manager')
     G.nodes(data=True)
[3]: NodeDataView({'A': {'role': 'Trader'}, 'B': {'role': 'Analyst'}, 'C': {'role':
     'Manager'}, 'D': {}, 'E': {}, 'F': {}})
[4]: nx.draw_networkx(G, with_labels=True)
```



[5]: True

```
[6]: edges = B.edges()
nx.draw_networkx(
    B,
    pos = nx.drawing.layout.bipartite_layout(B, ['A','B','C','D','E']),
    width = 2)
print(edges)
```

[('A', 1), ('A', 2), ('B', 1), ('C', 1), ('C', 3), ('D', 4), ('E', 1), ('E', 2)]



DOLPHINS NETWORK

This is a directed social network of bottlenose dolphins. The nodes are the bottlenose dolphins (genus Tursiops) of a bottlenose dolphin community living off Doubtful Sound, a fjord in New Zealand (spelled fiord in New Zealand). An edge indicates a frequent association. The dolphins were observed between 1994 and 2001. The network that has been used is Dolphin network [19]. Dolphin network contains 62 vertices and 159 links. After applying MFLM in Dolphin network, we receive 0.518 as modularity score and 5 communities.

Network Graph Generated using Gephi

```
[7]: import pandas as pd
    read_file = pd.read_excel ("dolphin.xlsx")
    read_file.to_csv ("dolphin.csv", index = None, header=True)
    df = pd.DataFrame(pd.read_csv("dolphin.csv"))
    df
```

[7]:		Node1	Node2
	0	0	35
	1	0	2
	2	0	6
	3	0	42
	4	0	7
		•••	•••

```
    154
    52
    56

    155
    53
    56

    156
    53
    61

    157
    55
    60

    158
    56
    61
```

[159 rows x 2 columns]

```
[8]: G = nx.Graph()
for index, row in df.iterrows():
    G.add_edge(row['Node1'], row['Node2'])
```

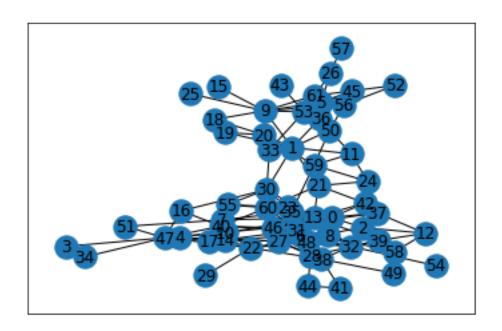
[9]: print(G.nodes)

[0, 35, 2, 6, 42, 7, 37, 1, 30, 36, 9, 11, 50, 19, 20, 21, 12, 22, 3, 47, 4, 27, 5, 45, 56, 61, 26, 53, 23, 28, 31, 32, 38, 8, 46, 48, 17, 40, 10, 51, 55, 13, 15, 18, 25, 14, 59, 24, 39, 58, 60, 16, 29, 57, 44, 33, 54, 34, 41, 49, 43, 52]

[10]: print(G.edges)

[(0, 35), (0, 2), (0, 6), (0, 42), (0, 7), (0, 37), (35, 6), (35, 7), (35, 27),(35, 30), (35, 31), (35, 59), (35, 48), (2, 12), (2, 37), (2, 22), (2, 42), (6, 37), (10, 10),23), (6, 27), (6, 28), (6, 31), (6, 32), (6, 38), (6, 8), (6, 46), (6, 48), (6, 17), (42, 13), (42, 21), (42, 24), (42, 37), (7, 40), (7, 10), (7, 51), (7, 17), (7, 55), (37, 12), (37, 24), (37, 46), (1, 30), (1, 36), (1, 9), (1, 11), (1, 55), (1, 12), (1, 12), (1, 13), (1, 14), (1, 15),50), (1, 19), (1, 20), (1, 21), (30, 13), (30, 16), (30, 31), (30, 33), (30, 55), (36, 5), (36, 61), (36, 53), (36, 50), (9, 5), (9, 56), (9, 61), (9, 15), (9, 53), (9, 18), (9, 20), (9, 25), (11, 59), (11, 50), (11, 24), (50, 5), (50, 50)56), (50, 59), (50, 53), (19, 18), (19, 20), (20, 18), (20, 59), (21, 13), (21, 60), (21, 24), (12, 39), (12, 58), (22, 10), (22, 14), (22, 17), (22, 29), (22, 38), (22, 40), (22, 47), (22, 48), (3, 47), (47, 10), (47, 14), (47, 16), (47, 17), (47, 34), (47, 40), (47, 46), (47, 51), (4, 27), (27, 8), (27, 14), (27, 28), (27, 31), (27, 32), (27, 38), (27, 46), (5, 45), (5, 56), (5, 61), (5, 26), (5, 53), (45, 52), (45, 61), (45, 53), (56, 52), (56, 53), (56, 61), (61, 26),(61, 53), (26, 57), (53, 33), (53, 43), (23, 60), (23, 55), (28, 39), (28, 31), (28, 44), (31, 8), (31, 14), (31, 60), (31, 38), (31, 40), (31, 58), (32, 8),(32, 13), (32, 38), (32, 39), (32, 48), (32, 54), (38, 41), (38, 49), (8, 46),(8, 13), (46, 13), (46, 40), (17, 10), (17, 40), (40, 10), (40, 14), (40, 16),(40, 60), (40, 55), (10, 13), (10, 14), (55, 60), (13, 60), (13, 39), (59, 24), (58, 49), (44, 41)]

[11]: nx.draw_networkx(G, with_labels=True)



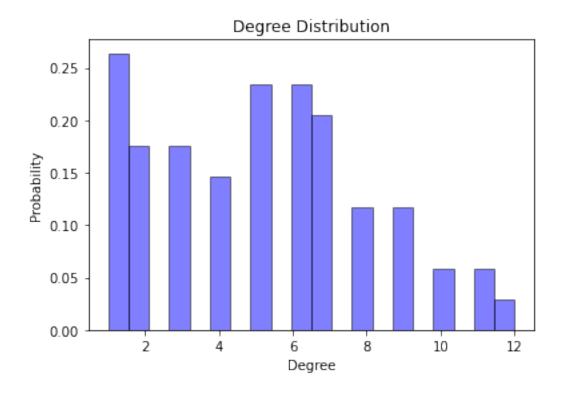
0.1 Network Type Prediction in Dolphin Newtork

```
[12]: import networkx as nx
      import matplotlib.pyplot as plt
      import numpy as np
      from collections import Counter
      from scipy.stats import norm, powerlaw, expon
      from scipy.optimize import curve_fit
      # Load your dataset as a NetworkX graph (replace this with your specific_
      \hookrightarrow dataset)
      G = nx.read_edgelist("dolphin.txt")
      # Compute the degree of each node
      degrees = dict(G.degree())
      degree_values = list(degrees.values())
      # Calculate the degree histogram
      hist, bin_edges = np.histogram(degree_values, bins=20, density=True)
      # Plot the degree distribution
      plt.hist(degree_values, bins=20, density=True, alpha=0.5, color='b', __
       ⇔edgecolor='black')
      plt.title("Degree Distribution")
      plt.xlabel("Degree")
      plt.ylabel("Probability")
```

```
# Define functions for fitting different distribution types
def power_law(x, a, b):
    return a * (x**b)
def exponential(x, scale):
    return scale * np.exp(-scale * x)
# Fit the degree distribution to different candidate distributions
params_powerlaw, _ = curve_fit(power_law, bin_edges[:-1], hist)
params_exponential, _ = curve_fit(exponential, bin_edges[:-1], hist)
# Determine the type of distribution based on the parameters
alpha_powerlaw = params_powerlaw[1]
scale_exponential = 1 / params_exponential[0]
if alpha_powerlaw > 2.0:
    print("The degree distribution appears to be closer to a power-law⊔
 ⇔(scale-free) distribution.")
elif scale_exponential < 2.0:</pre>
    print("The degree distribution appears to be closer to an exponential_

→distribution.")
else:
    print("The degree distribution does not seem to be a power-law or ⊔
 ⇔exponential distribution.")
plt.show()
```

The degree distribution does not seem to be a power-law or exponential distribution.



```
[13]: def network_describe(G):
          num_nodes = G.number_of_nodes()
          num_edges = G.number_of_edges()
          degree_sequence = [degree for (node, degree) in G.degree()]
          avg degree = sum(degree sequence) / num nodes
          degree_centrality = nx.degree_centrality(G)
          betweenness_centrality = nx.betweenness_centrality(G)
          eigenvector_centrality = nx.eigenvector_centrality(G)
          avg_clustering_coefficient = nx.average_clustering(G)
          degree_centrality = nx.degree_centrality(G)
          metric_values = list(degree_centrality.values())
          variance = np.var(metric_values)
          list_of_betw_tuples = list(betweenness_centrality.items())
          list_of_eigen_tuples = list(eigenvector_centrality.items())
          list_of_degree_tuples = list(degree_centrality.items())
          print("NETWORK STATISTICS :")
          print("Network Info : ",nx.info(G))
          print("Nodes : ",num_nodes)
          print("Edges : ",num_edges)
          print("Degree Centality : ")
          print(list_of_degree_tuples)
          print("Betweenness Centality : ")
          print(list_of_betw_tuples)
```

```
print("Eigenvector Centality : ")
print(list_of_eigen_tuples)
print("Average Clustering Coefficient : ")
print(avg_clustering_coefficient)
print("Variance : ")
print(variance)
```

[14]: network_describe(G)

```
NETWORK STATISTICS :
Network Info: Graph with 62 nodes and 159 edges
Nodes: 62
Edges: 159
Degree Centality:
[('0', 0.09836065573770492), ('40', 0.13114754098360656), ('10', 0.13114754098360656)]
0.0819672131147541), ('14', 0.19672131147540983), ('47', 0.09836065573770492),
('15', 0.11475409836065574), ('42', 0.09836065573770492), ('1',
0.13114754098360656), ('36', 0.11475409836065574), ('41', 0.0819672131147541),
('17', 0.14754098360655737), ('19', 0.06557377049180328), ('54',
0.11475409836065574), ('26', 0.04918032786885246), ('27', 0.0819672131147541),
('28', 0.0819672131147541), ('2', 0.06557377049180328), ('44', )
0.06557377049180328), ('61', 0.04918032786885246), ('3', 0.04918032786885246),
('8', 0.09836065573770492), ('59', 0.0819672131147541), ('4',
0.01639344262295082), ('51', 0.1639344262295082), ('5', 0.06557377049180328),
('56', 0.03278688524590164), ('9', 0.11475409836065574), ('13',
0.13114754098360656), ('57', 0.14754098360655737), ('6', 0.09836065573770492),
('7', 0.0819672131147541), ('30', 0.0819672131147541), ('37',
0.18032786885245902), ('45', 0.18032786885245902), ('20', 0.14754098360655737),
('32', 0.04918032786885246), ('29', 0.14754098360655737), ('11',
0.01639344262295082), ('12', 0.01639344262295082), ('33', 0.1639344262295082),
('34', 0.0819672131147541), ('38', 0.13114754098360656), ('43',
0.11475409836065574), ('16', 0.09836065573770492), ('50', 0.11475409836065574),
('52', 0.06557377049180328), ('24', 0.09836065573770492), ('18',
0.11475409836065574), ('55', 0.03278688524590164), ('22', 0.01639344262295082),
('25', 0.04918032786885246), ('31', 0.01639344262295082), ('21',
0.09836065573770492), ('23', 0.04918032786885246), ('35', 0.01639344262295082),
('60', 0.01639344262295082), ('49', 0.03278688524590164), ('39',
0.03278688524590164), ('58', 0.01639344262295082), ('46', 0.03278688524590164),
('53', 0.03278688524590164), ('48', 0.01639344262295082)]
Betweenness Centality:
[('0', 0.01908259621374376), ('40', 0.1431495183426175), ('10',
0.01609202091169304), ('14', 0.06197200484885411), ('47', 0.023201476119508912),
('15', 0.033292220982233216), ('42', 0.02915795194483718), ('1',
0.21332443553281097), ('36', 0.24823719602893804), ('41', 0.02325160067018617),
('17', 0.11430016291546972), ('19', 0.013314394166853186), ('54',
0.09912164676351941), ('26', 0.00436247723132969), ('27', 0.029236860493157973),
('28', 0.06675695466395656), ('2', 0.00907281243346817), ('44',
```

```
0.012037805849281259), ('61', 0.014194982613015399), ('3',
0.0023737965131407756), ('8', 0.022365737598409235), ('59',
0.02033277469038459), ('4', 0.0), ('51', 0.08467725475022556), ('5',
0.004380300179480506), ('56', 0.0001366120218579235), ('9',
0.02089438036159347), ('13', 0.05284632843869151), ('57', 0.08420468343495603),
('6', 0.029372536747686688), ('7', 0.11823861926938345), ('30',
0.033050460771772254), ('37', 0.13856978865859435), ('45',
0.040670440596470195), ('20', 0.10264573972090967), ('32', 0.03278688524590164),
('29', 0.06552928249649562), ('11', 0.0), ('12', 0.0), ('33',
0.0571664401172598), ('34', 0.032694759702956426), ('38', 0.045352238835845396),
('43', 0.06283060442896508), ('16', 0.0033047098620869113), ('50',
0.03341103492742837), ('52', 0.01923434489008259), ('24', 0.007383043489600867),
('18', 0.014854899716954898), ('55', 0.0008774695250105086), ('22', 0.0), ('25',
0.0016441148408361526), ('31', 0.0), ('21', 0.012700653930162124), ('23',
0.04218278563875617), ('35', 0.0), ('60', 0.0), ('49', 0.0009289617486338798),
('39', 0.07051677853993399), ('58', 0.0), ('46', 0.0030084669428931724), ('53',
0.0011930783242258653), ('48', 0.0)]
Eigenvector Centality:
[('0', 0.12850351911087213), ('40', 0.20787263130203706), ('10',
0.07525346435103512), ('14', 0.3157810764804676), ('47', 0.08037195763313358),
('15', 0.16417491138339663), ('42', 0.08095068341031325), ('1',
0.042091441435724804), ('36', 0.13276550630017522), ('41',
0.015262103099078309), ('17', 0.01753496833868234), ('19',
0.020682545955984934), ('54', 0.023022376520473394), ('26',
0.008949192287688038), ('27', 0.016326687320731025), ('28',
0.06822697202643722), ('2', 0.039757133098010516), ('44', 0.07780212964010047),
('61', 0.05199117201156754), ('3', 0.07933447607445519), ('8',
0.1431022167512096), ('59', 0.1118186569975593), ('4', 0.029287057142628192),
('51', 0.21068020892089806), ('5', 0.006572752164517532), ('56',
0.0026123141901086854), ('9', 0.012220169764468426), ('13',
0.015030415487480686), ('57', 0.017401973681970617), ('6',
0.012211980286547347), ('7', 0.04290802005630266), ('30', 0.04075065098782636),
('37', 0.30056092847049554), ('45', 0.28500310473240426), ('20',
0.18447787335323973), ('32', 0.003864343758966286), ('29', 0.21176109464474216),
('11', 0.029287057142628192), ('12', 0.03907586116163528), ('33',
0.2810970171605869), ('34', 0.1388272511035687), ('38', 0.19661653892836548),
('43', 0.19033796034550665), ('16', 0.20799316926734232), ('50',
0.21769051331081496), ('52', 0.1295635910153738), ('24', 0.19321180983300903),
('18', 0.20249300124247616), ('55', 0.05210934393071285), ('22',
0.0024382375398253426), ('25', 0.005952326426510383), ('31',
0.0024382375398253426), ('21', 0.20734961722376982), ('23',
0.08736202260403907), ('35', 0.029437314009677567), ('60',
0.0005374384753918982), ('49', 0.02342956700211971), ('39',
0.02087597074555255), ('58', 0.02733206208697855), ('46', 0.029716244849600233),
('53', 0.03368665459890722), ('48', 0.0024198473930088903)]
Average Clustering Coefficient :
0.2589582460550202
Variance:
```

0.0023101999199637803

Modularity Score

Modularity is a measure of the structure of networks or graphs which measures the strength of division of a network into modules (also called groups, clusters or communities). Networks with high modularity have dense connections between the nodes within modules but sparse connections between nodes in different modules. Modularity is often used in optimization methods for detecting community structure in networks. Biological networks, including animal brains, exhibit a high degree of modularity.

```
[16]: def calculate_community_mod(G1,n,a):
    x=[]
    for i in a:
        x.append(list(i))

comm_mod = 0
    for k in range(0,n):
        H=G1.subgraph(x[0])
    for i in x[0]: #
        #neighbours
        i_neighbours = list(H.adj[i])
        for j in i_neighbours:
            comm_mod = comm_mod + modularity_score(H, i, j)
```

```
import networkx as nx

def girvan_newman(G, num_communities):
    communities = [list(G.nodes())]

while len(communities) < num_communities:
    edge_betweenness = nx.edge_betweenness_centrality(G)

max_edge_betweenness = max(edge_betweenness.values())
    edges_to_remove = [edge for edge, centrality in edge_betweenness.

items() if centrality == max_edge_betweenness]
    G.remove_edges_from(edges_to_remove)</pre>
```

```
new_communities = list(nx.connected_components(G))

if len(new_communities) > len(communities):
        communities = new_communities

return communities
```

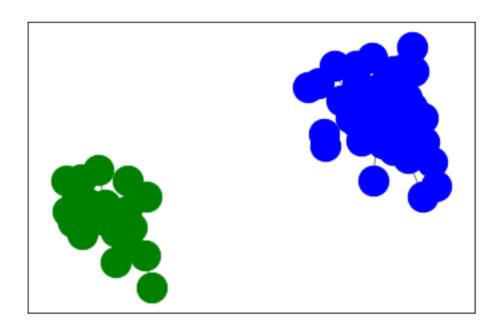
COMMUNITY DETECTION IN FOOTBALL NETWORK

Network Graph Generated using Gephi

```
[19]: a = girvan_newman(G, 2)
print(a)
```

```
[{'37', '11', '2', '34', '24', '8', '47', '52', '45', '0', '59', '18', '49', '12', '16', '21', '50', '38', '55', '14', '30', '43', '23', '29', '44', '42', '28', '46', '36', '3', '40', '15', '51', '58', '33', '35', '20', '10', '61', '53', '4'}, {'54', '56', '26', '9', '48', '25', '22', '1', '57', '17', '7', '39', '41', '6', '5', '32', '60', '27', '13', '19', '31'}]
```

```
[20]: draw_communities(G,a)
```



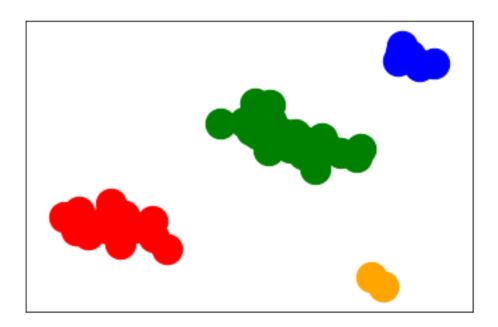
```
[21]: mod_G_2 = calculate_community_mod(G,2,a)
print(mod_G_2)
```

1.5522262435821903

[22]: a = girvan_newman(G, 4)
print(a)

[{'42', '28', '2', '10', '47', '30', '0'}, {'37', '11', '34', '24', '8', '52', '45', '59', '18', '49', '12', '16', '21', '38', '50', '55', '14', '43', '23', '29', '44', '46', '36', '3', '40', '15', '51', '58', '33', '35', '20', '4'}, {'54', '56', '26', '9', '48', '25', '22', '1', '57', '17', '7', '39', '41', '6', '5', '32', '60', '27', '13', '19', '31'}, {'61', '53'}]

[23]: draw_communities(G,a)



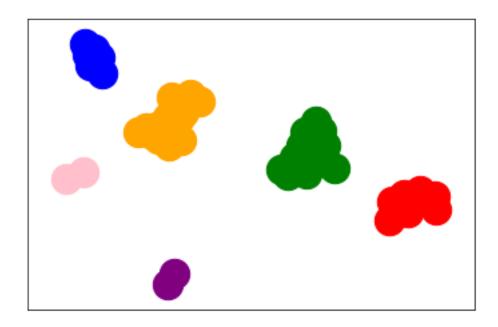
[24]: mod_G_4 = calculate_community_mod(G,4,a)
print(mod_G_4)

1.624999999999993

[25]: a = girvan_newman(G, 6)
print(a)

[{'42', '28', '2', '10', '47', '30', '0'}, {'37', '34', '8', '52', '59', '49', '12', '16', '38', '50', '14', '43', '44', '46', '36', '3', '40', '58', '33', '20'}, {'11', '18', '35', '24', '21', '55', '4', '23', '15', '29', '45', '51'}, {'54', '56', '26', '9', '48', '25', '22', '1', '57', '17', '7', '39', '41', '6', '5', '27', '13', '19', '31'}, {'61', '53'}, {'32', '60'}]

[26]: draw_communities(G,a)



```
[27]: mod_G_6 = calculate_community_mod(G,6,a)
print(mod_G_6)
```

2.437499999999987

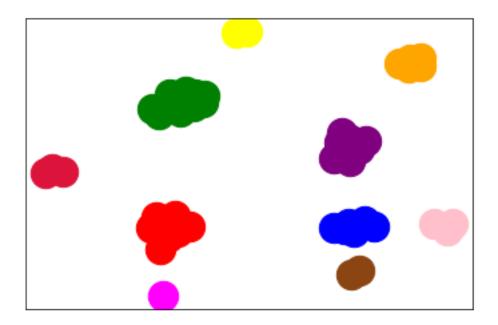
```
[28]: a = girvan_newman(G, 10)
print(a)
```

```
[{'42', '28', '2', '10', '47', '30', '0'}, {'37', '33', '49', '46', '20', '34', '16', '36', '43', '44', '38', '50', '14', '40', '52'}, {'11', '18', '35', '24', '21', '55', '4', '23', '15', '29', '45', '51'}, {'25', '7', '26', '1', '19', '27'}, {'54', '57', '39', '13', '41', '6', '56', '5', '9', '48'}, {'31', '17', '22'}, {'61', '53'}, {'8', '59', '3'}, {'32', '60'}, {'12'}, {'58'}]
```

[29]: draw_communities(G,a)

```
8
9 nx.draw_networkx_edges(G, pos, alpha=0.5)

IndexError: list index out of range
```



```
[30]: mod_G_10 = calculate_community_mod(G,10,a)
print(mod_G_10)
```

4.06249999999998

```
[31]: from networkx.algorithms import community from operator import itemgetter communities = community.greedy_modularity_communities(G)
```

```
[32]: betweenness_dict = nx.betweenness_centrality(G)
    eigenvector_dict = nx.eigenvector_centrality(G)

nx.set_node_attributes(G, betweenness_dict, 'betweenness')
nx.set_node_attributes(G, eigenvector_dict, 'eigenvector')
```

```
[33]: modularity_dict = {}
for i,c in enumerate(communities):
    for name in c:
        modularity_dict[name] = i

nx.set_node_attributes(G, modularity_dict, 'modularity')
class0 = [n for n in G.nodes() if G.nodes[n]['modularity'] == 0]
```

```
class0_eigenvector = {n:G.nodes[n]['eigenvector'] for n in class0}
class0_sorted_by_eigenvector = sorted(class0_eigenvector.items(),_
 →key=itemgetter(1), reverse=True)
for i,c in enumerate(communities):
    if len(c) > 2:
        print('Class '+str(i)+':', list(c))
        print('\n')
Class 0: ['37', '49', '33', '46', '20', '34', '16', '36', '40', '44', '50',
'38', '14', '43', '52']
Class 1: ['11', '18', '35', '24', '21', '55', '4', '23', '15', '29', '45', '51']
Class 2: ['54', '57', '39', '13', '41', '56', '6', '5', '9', '48']
Class 3: ['42', '10', '28', '47', '2', '0', '30']
Class 4: ['25', '7', '19', '1', '26', '27']
Class 5: ['59', '8', '3']
Class 6: ['31', '17', '22']
```

FOOTBALL NETWORK

The file football.gml contains the network of American football games between Division IA colleges during regular season Fall 2000, as compiled by M. Girvan and M. Newman. The nodes have values that indicate to which conferences they belong.

Network Graph Generated using Gephi

```
[34]: import pandas as pd

read_file = pd.read_excel ("football.xlsx")

read_file.to_csv ("football.csv", index = None, header=True)

df = pd.DataFrame(pd.read_csv("football.csv"))
```

df Node1 Node2

[613 rows x 2 columns]

```
[35]: G = nx.Graph()
for index, row in df.iterrows():
    G.add_edge(row['Node1'], row['Node2'])
```

[36]: print(G.nodes)

[0, 1, 44, 49, 77, 42, 7, 104, 23, 51, 31, 105, 108, 46, 6, 8, 55, 12, 103, 68, 33, 35, 4, 2, 60, 113, 10, 5, 85, 87, 13, 95, 98, 72, 3, 27, 71, 20, 22, 41, 48, 57, 76, 96, 114, 26, 37, 39, 62, 66, 69, 92, 109, 38, 50, 63, 83, 79, 101, 18, 74, 94, 9, 67, 107, 88, 102, 11, 82, 29, 30, 80, 90, 91, 15, 75, 112, 61, 32, 36, 81, 14, 56, 59, 64, 86, 97, 93, 16, 54, 78, 106, 111, 17, 24, 28, 70, 89, 110, 19, 43, 45, 47, 53, 21, 25, 99, 34, 84, 65, 52, 73, 40, 58, 100]

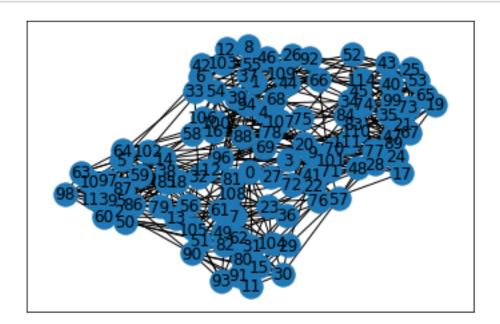
[37]: print(G.edges)

[(0, 1), (0, 44), (0, 49), (0, 77), (0, 42), (0, 7), (0, 104), (0, 23), (0, 51), (0, 31), (0, 105), (0, 108), (1, 42), (1, 46), (1, 6), (1, 8), (1, 55), (1, 12), (1, 103), (1, 68), (1, 33), (1, 35), (1, 4), (44, 4), (44, 26), (44, 37), (44, 39), (44, 43), (44, 54), (44, 92), (44, 109), (44, 66), (44, 107), (49, 7), (49, 11), (49, 23), (49, 31), (49, 36), (49, 60), (49, 104), (49, 51), (49, 108), (49, 81), (77, 17), (77, 24), (77, 28), (77, 35), (77, 67), (77, 75), (77, 111), (77, 78), (77, 83), (77, 101), (42, 6), (42, 8), (42, 12), (42, 26), (42, 33), (42, 46), (42, 55), (42, 103), (7, 104), (7, 13), (7, 23), (7, 31), (7, 51), (7, 79), (7, 85), (7, 101), (7, 108), (7, 18), (104, 11), (104, 23), (104, 30), (104, 31), (104, 51), (104, 76), (104, 93), (104, 108), (23, 79), (23, 47), (23, 95), (23, 24), (23, 51), (23, 31), (23, 108), (51, 31), (51, 50), (51, 93), (51, 79), (51, 108), (31, 15), (31, 30), (31, 91), (31, 105), (31, 108), (105, 13), (105, 32), (105, 36), (105, 60), (105, 61), (105, 81), (105, 93), (108, 94), (108, 96), (108, 106), (46, 6), (46, 8), (46, 12), (46, 33), (46, 45), (46, 55), (46, 94), (46, 103), (46, 110), (6, 5), (6, 33), (6, 55), (6, 83), (6, 103), (6,

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```

[38]: nx.draw_networkx(G, with_labels=True)



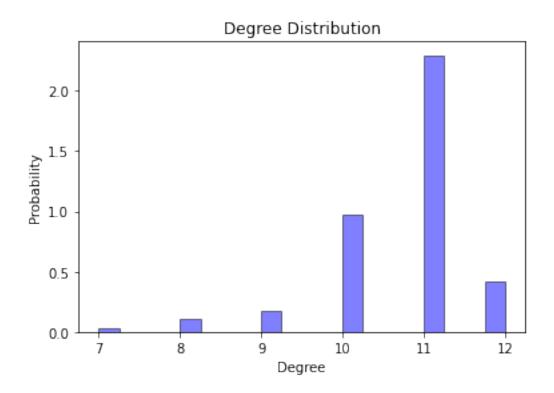
0.2 Network Type Prediction in Football Newtork

```
[39]: import networkx as nx import matplotlib.pyplot as plt import numpy as np from collections import Counter from scipy.stats import norm, powerlaw, expon from scipy.optimize import curve_fit
```

```
# Load your dataset as a NetworkX graph (replace this with your specific,
 \hookrightarrow dataset)
G = nx.read_edgelist("football.txt")
# Compute the degree of each node
degrees = dict(G.degree())
degree_values = list(degrees.values())
# Calculate the degree histogram
hist, bin edges = np.histogram(degree values, bins=20, density=True)
# Plot the degree distribution
plt.hist(degree_values, bins=20, density=True, alpha=0.5, color='b', __
 ⇔edgecolor='black')
plt.title("Degree Distribution")
plt.xlabel("Degree")
plt.ylabel("Probability")
# Define functions for fitting different distribution types
def power_law(x, a, b):
    return a * (x**b)
def exponential(x, scale):
    return scale * np.exp(-scale * x)
# Fit the degree distribution to different candidate distributions
params powerlaw, = curve fit(power law, bin edges[:-1], hist)
params_exponential, _ = curve_fit(exponential, bin_edges[:-1], hist)
# Determine the type of distribution based on the parameters
alpha_powerlaw = params_powerlaw[1]
scale_exponential = 1 / params_exponential[0]
if alpha_powerlaw > 2.0:
    print("The degree distribution appears to be closer to a power-law_{\sqcup}
 ⇔(scale-free) distribution.")
elif scale_exponential < 2.0:</pre>
    print("The degree distribution appears to be closer to an exponential_{\sqcup}

→distribution.")
else:
    print("The degree distribution does not seem to be a power-law or_{\sqcup}
 ⇔exponential distribution.")
plt.show()
```

The degree distribution appears to be closer to a power-law (scale-free) distribution.



[40]: network_describe(G)

```
NETWORK STATISTICS :
Network Info: Graph with 115 nodes and 613 edges
Nodes: 115
Edges: 613
Degree Centality:
[('0', 0.10526315789473684), ('1', 0.10526315789473684), ('35',
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Average Clustering Coefficient :
0.40321601104209814
Variance:
6.0067922600584965e-05
```

COMMUNITY DETECTION IN FOOTBALL NETWORK

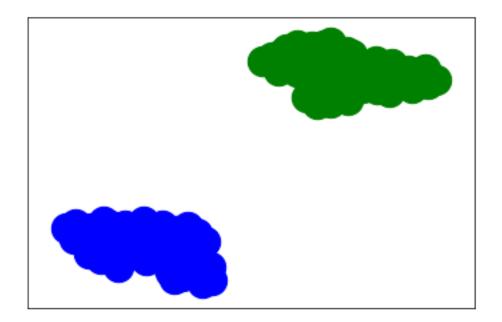
Network Graph Generated using Gephi

```
[41]: a = girvan_newman(G, 2) print(a)
```

[{'98', '11', '2', '24', '100', '8', '83', '84', '67', '74', '47', '72', '9',

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[42]: draw_communities(G,a)



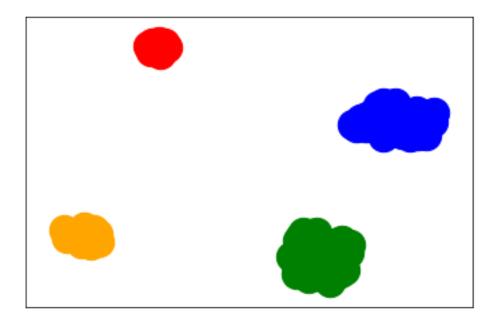
[43]: mod_G_2 = calculate_community_mod(G,2,a)
print(mod_G_2)

1.6448035815951454

[44]: a = girvan_newman(G, 4) print(a)

[{'98', '11', '24', '8', '83', '84', '67', '74', '72', '9', '73', '0', '52', '114', '102', '22', '49', '16', '82', '21', '50', '77', '23', '111', '28', '104', '110', '90', '7', '41', '69', '46', '5', '78', '88', '68', '3', '40', '51', '107', '81', '108', '10', '4', '53', '93'}, {'37', '103', '56', '89', '91', '113', '63', '86', '105', '65', '45', '48', '87', '25', '59', '66', '1', '79', '62', '55', '30', '109', '44', '29', '75', '57', '17', '94', '92', '76', '70', '112', '80', '27', '58', '97', '96', '33', '35', '20', '19', '101', '95'}, {'39', '13', '6', '2', '100', '32', '64', '47', '60', '106', '15'}, {'42', '54', '18', '12', '34', '26', '36', '38', '61', '14', '43', '31', '85', '71', '99'}]

[45]: draw_communities(G,a)



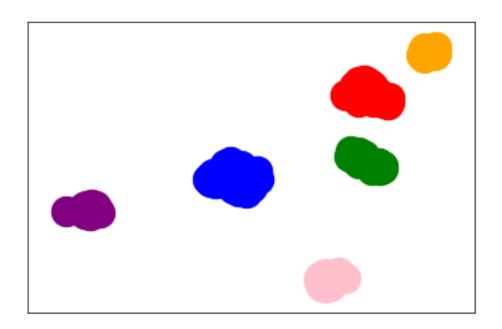
```
[46]: mod_G_4 = calculate_community_mod(G,4,a)
print(mod_G_4)
```

3.1349213029206444

[47]: a = girvan_newman(G, 6) print(a)

```
[{'11', '24', '8', '83', '67', '9', '73', '0', '114', '22', '49', '16', '21', '50', '77', '23', '111', '28', '104', '110', '90', '7', '41', '69', '46', '88', '78', '68', '51', '108', '4', '53', '93'}, {'37', '25', '33', '80', '103', '35', '94', '89', '1', '29', '79', '19', '101', '55', '109', '105', '45', '30'}, {'56', '113', '91', '63', '86', '65', '48', '87', '59', '66', '62', '44', '75', '57', '17', '92', '76', '70', '112', '27', '58', '97', '96', '20', '95'}, {'39', '102', '5', '109', '100', '106', '15'}, {'98', '107', '81', '102', '5', '31', '82', '84', '74', '10', '72', '40', '52'}, {'42', '54', '18', '12', '34', '26', '36', '38', '61', '14', '43', '31', '85', '71', '99'}]
```

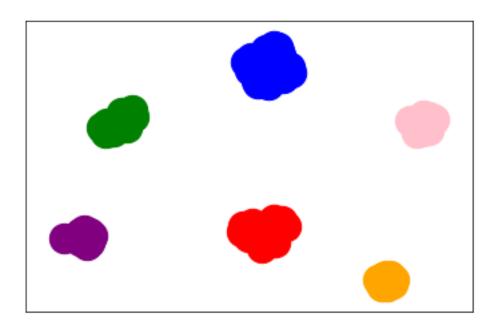
[48]: draw_communities(G,a)



[49]: a = girvan_newman(G, 6) print(a)

[{'11', '24', '8', '83', '67', '9', '73', '0', '114', '22', '49', '16', '21', '50', '77', '23', '111', '28', '104', '110', '90', '7', '41', '69', '46', '88', '78', '68', '51', '108', '4', '53', '93'}, {'37', '25', '33', '80', '103', '35', '94', '89', '1', '29', '79', '19', '101', '55', '109', '105', '45', '30'}, {'56', '113', '91', '63', '86', '65', '48', '87', '59', '66', '62', '44', '75', '57', '17', '92', '76', '70', '112', '27', '58', '97', '96', '20', '95'}, {'39', '102', '5', '102', '100', '32', '64', '47', '60', '106', '15'}, {'98', '107', '81', '102', '5', '3', '82', '84', '74', '10', '72', '40', '52'}, {'42', '54', '18', '12', '34', '26', '36', '38', '61', '14', '43', '31', '85', '71', '99'}]

[50]: draw_communities(G,a)



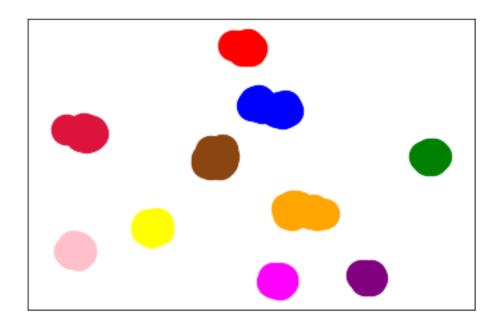
```
[51]: mod_G_6 = calculate_community_mod(G,6,a)
print(mod_G_6)
```

4.293072330973211

[52]: a = girvan_newman(G, 10)
print(a)

[{'104', '22', '7', '111', '41', '16', '8', '78', '68', '108', '21', '77', '4', '9', '23', '0', '93', '51'}, {'37', '25', '33', '103', '89', '1', '109', '105', '45'}, {'35', '80', '94', '79', '19', '101', '30', '55', '29'}, {'97', '58', '96', '17', '59', '20', '56', '113', '62', '63', '76', '27', '70', '95', '65', '87'}, {'28', '11', '90', '69', '24', '50'}, {'75', '57', '66', '92', '91', '112', '44', '86', '48'}, {'39', '13', '6', '2', '100', '32', '64', '47', '60', '106', '15'}, {'98', '107', '81', '102', '5', '3', '82', '84', '74', '10', '72', '40', '52'}, {'42', '54', '18', '12', '34', '26', '36', '38', '61', '14', '43', '31', '85', '71', '99'}, {'114', '110', '49', '46', '88', '83', '67', '53', '73'}]

[53]: draw_communities(G,a)



```
[54]: mod_G_10 = calculate_community_mod(G,10,a)
print(mod_G_10)
```

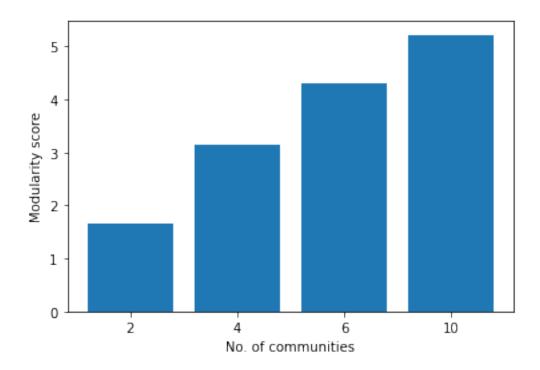
5.215111111111103

```
[55]: import matplotlib.pyplot as plt
import numpy as np

x = np.array(["2", "4", "6", "10"])
y = np.array([mod_G_2, mod_G_4, mod_G_6, mod_G_10])

plt.xlabel("No. of communities")
plt.ylabel("Modularity score")

plt.bar(x,y)
plt.show()
```



KARATE CLUB NETWORK

Zachary's karate club is a social network of a university karate club, described in the paper "An Information Flow Model for Conflict and Fission in Small Groups" by Wayne W. Zachary. The network became a popular example of community structure in networks after its use by Michelle Girvan and Mark Newman in 2002.[1]

Network Graph Generated using Gephi

```
[56]: import pandas as pd

read_file = pd.read_excel ("Karate.xlsx")

read_file.to_csv ("Karate.csv", index = None, header=True)

df = pd.DataFrame(pd.read_csv("Karate.csv"))

df
```

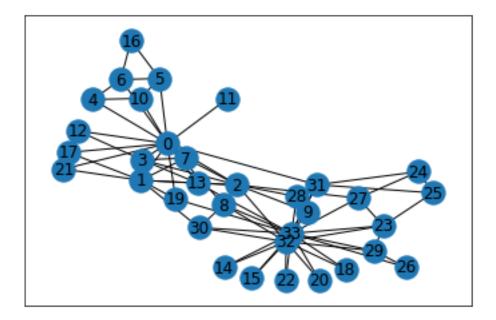
```
[56]:
            Node1
                    Node2
       0
                 0
                          1
                          2
       1
                 0
       2
                 0
                          3
       3
                 0
                          4
       4
                 0
                          5
```

```
73 30 33
74 30 32
75 31 32
76 31 33
77 32 33
```

[78 rows x 2 columns]

```
[57]: G = nx.Graph()
for index, row in df.iterrows():
        G.add_edge(row['Node1'], row['Node2'])

nx.draw_networkx(G, with_labels=True)
```

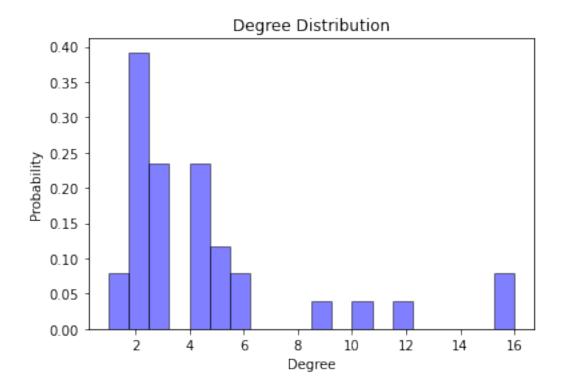


0.3 Network Type Prediction in Karate Club Newtork

```
# Compute the degree of each node
degrees = dict(G.degree())
degree_values = list(degrees.values())
# Calculate the degree histogram
hist, bin_edges = np.histogram(degree_values, bins=20, density=True)
# Plot the degree distribution
plt.hist(degree_values, bins=20, density=True, alpha=0.5, color='b', __
 ⇔edgecolor='black')
plt.title("Degree Distribution")
plt.xlabel("Degree")
plt.ylabel("Probability")
# Define functions for fitting different distribution types
def power_law(x, a, b):
    return a * (x**b)
def exponential(x, scale):
    return scale * np.exp(-scale * x)
# Fit the degree distribution to different candidate distributions
params_powerlaw, _ = curve_fit(power_law, bin_edges[:-1], hist)
params_exponential, _ = curve_fit(exponential, bin_edges[:-1], hist)
# Determine the type of distribution based on the parameters
alpha_powerlaw = params_powerlaw[1]
scale_exponential = 1 / params_exponential[0]
if alpha_powerlaw > 2.0:
    print("The degree distribution appears to be closer to a power-law⊔
 ⇔(scale-free) distribution.")
elif scale exponential < 2.0:</pre>
    print("The degree distribution appears to be closer to an exponential ⊔

→distribution.")
else:
    print("The degree distribution does not seem to be a power-law or ⊔
 ⇔exponential distribution.")
plt.show()
```

The degree distribution does not seem to be a power-law or exponential distribution.



[59]: network_describe(G)

```
NETWORK STATISTICS :
Network Info: Graph with 34 nodes and 77 edges
Nodes: 34
Edges: 77
Degree Centality :
[('0', 0.48484848484848486), ('9', 0.1515151515151515), ('14',
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('18', 0.06060606060606061), ('22', 0.06060606060606061), ('26',
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```

```
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('27', 0.0), ('28', 0.025365144115144116), ('29', 0.0035637973137973137), ('30',
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('1', 0.43960692085692077), ('3', 0.1741200928700929), ('4',
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('7', 0.02998737373737374), ('8', 0.0), ('10', 0.0), ('11', 0.0), ('11', 0.0), ('11', 0.0), ('10', 0.0), ('11', 0.0), ('11', 0.0), ('10', 0.0), ('11', 0.0), ('10', 0.0), ('10', 0.0), ('11', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('10', 0.0), ('
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Eigenvector Centality:
[('0', 0.36028869718137285), ('9', 0.2285824966102697), ('14',
0.22946890344377588), ('15', 0.10020390488798826), ('16', 0.10020390488798826),
('19', 0.10020390488798826), ('20', 0.14964911843723078), ('21',
0.10020390488798826), ('23', 0.10020390488798826), ('24', 0.1490309278297953),
('27', 0.07404311479213908), ('28', 0.1323105473918868), ('29',
0.13012948421188536), ('30', 0.1336439665192374), ('31', 0.17534431969032657),
('32', 0.19206726854315842), ('33', 0.3081600666425366), ('2',
0.2726760840775042), ('1', 0.36533721426632837), ('3', 0.31572719522124854),
('4', 0.21674854874719207), ('5', 0.0790098758057299), ('6',
0.08272774744850384), ('7', 0.08272774744850385), ('8', 0.17545978398577347),
('10', 0.047328600171325085), ('11', 0.07900987580572988), ('12',
0.05476507094052167), ('13', 0.08725625577574166), ('17', 0.024802115794733043),
('18', 0.09563999897922838), ('22', 0.09563999897922838), ('26',
0.05976459234511723), ('25', 0.057584792190228266)]
Average Clustering Coefficient :
0.5710710041592393
Variance:
0.01292255680428062
```

LES MISERABLES NETWORK

Network Graph Generated using Gephi

```
[60]: import pandas as pd
    read_file = pd.read_excel ("lesmis.xlsx")
    read_file.to_csv ("lesmis.csv", index = None, header=True)
    df = pd.DataFrame(pd.read_csv("lesmis.csv"))
    df
```

```
[60]: Node1 Node2
0 0 1
1 0 2
2 0 3
3 0 4
```

```
4
           0
                    5
249
          69
                   75
          70
250
                   71
          70
251
                   75
252
                   75
          71
253
          73
                   74
```

[254 rows x 2 columns]

```
[61]: G = nx.Graph()
for index, row in df.iterrows():
    G.add_edge(row['Node1'], row['Node2'])
```

[62]: print(G.edges)

```
[(0, 1), (0, 2), (0, 3), (0, 4), (0, 5), (0, 6), (0, 7), (0, 8), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0, 9), (0,
11), (2, 3), (2, 11), (3, 11), (11, 10), (11, 12), (11, 13), (11, 14), (11, 15),
(11, 23), (11, 24), (11, 25), (11, 26), (11, 27), (11, 28), (11, 29), (11, 31),
(11, 32), (11, 33), (11, 34), (11, 35), (11, 36), (11, 37), (11, 38), (11, 43),
(11, 44), (11, 48), (11, 49), (11, 51), (11, 55), (11, 58), (11, 64), (11, 68),
(11, 69), (11, 70), (11, 71), (11, 72), (12, 23), (23, 16), (23, 17), (23, 18),
(23, 19), (23, 20), (23, 21), (23, 22), (23, 24), (23, 25), (23, 27), (23, 29),
(23, 30), (23, 31), (24, 25), (24, 26), (24, 27), (24, 41), (24, 42), (24, 50),
(24, 68), (24, 69), (24, 70), (25, 26), (25, 27), (25, 39), (25, 40), (25, 41),
(25, 42), (25, 48), (25, 55), (25, 68), (25, 69), (25, 70), (25, 71), (25, 75),
(26, 16), (26, 27), (26, 43), (26, 49), (26, 51), (26, 54), (26, 55), (26, 72),
(27, 28), (27, 29), (27, 31), (27, 33), (27, 43), (27, 48), (27, 58), (27, 68),
(27, 69), (27, 70), (27, 71), (27, 72), (28, 44), (28, 45), (29, 34), (29, 35),
(29, 36), (29, 37), (29, 38), (31, 30), (34, 35), (34, 36), (34, 37), (34, 38),
(35, 36), (35, 37), (35, 38), (36, 37), (36, 38), (37, 38), (48, 47), (48, 55),
(48, 57), (48, 58), (48, 59), (48, 60), (48, 61), (48, 62), (48, 63), (48, 64),
(48, 65), (48, 66), (48, 68), (48, 69), (48, 71), (48, 73), (48, 74), (48, 75),
(48, 76), (49, 50), (49, 51), (49, 54), (49, 55), (49, 56), (51, 52), (51, 53),
(51, 54), (51, 55), (55, 16), (55, 39), (55, 41), (55, 54), (55, 56), (55, 57),
(55, 58), (55, 59), (55, 61), (55, 62), (55, 63), (55, 64), (55, 65), (58, 57),
(58, 59), (58, 60), (58, 61), (58, 62), (58, 63), (58, 64), (58, 65), (58, 66),
(58, 70), (58, 76), (64, 57), (64, 59), (64, 60), (64, 61), (64, 62), (64, 63),
(64, 65), (64, 66), (64, 76), (68, 41), (68, 69), (68, 70), (68, 71), (68, 75),
(69, 41), (69, 70), (69, 71), (69, 75), (70, 41), (70, 71), (70, 75), (71, 41),
(71, 75), (16, 17), (16, 18), (16, 19), (16, 20), (16, 21), (16, 22), (17, 18),
(17, 19), (17, 20), (17, 21), (17, 22), (18, 19), (18, 20), (18, 21), (18, 22),
(19, 20), (19, 21), (19, 22), (20, 21), (20, 22), (21, 22), (41, 42), (41, 57),
(41, 62), (41, 75), (39, 52), (57, 59), (57, 61), (57, 62), (57, 63), (57, 65),
(57, 67), (62, 59), (62, 60), (62, 61), (62, 63), (62, 65), (62, 66), (62, 76),
(46, 47), (59, 60), (59, 61), (59, 63), (59, 65), (59, 66), (60, 61), (60, 63),
(60, 65), (60, 66), (61, 63), (61, 65), (61, 66), (63, 65), (63, 66), (63, 76),
```

```
(65, 66), (65, 76), (66, 76), (73, 74)
```

PARTITIONED LES MISERABLES NETWORK

Network Graph Generated using Gephi

[63]: network_describe(G)

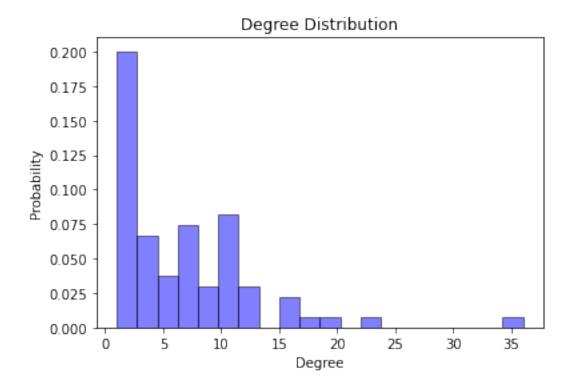
```
NETWORK STATISTICS :
Network Info: Graph with 77 nodes and 254 edges
Nodes: 77
Edges: 254
Degree Centality :
[(0, 0.13157894736842105), (1, 0.013157894736842105), (2, 0.039473684210526314),
(3, 0.039473684210526314), (4, 0.013157894736842105), (5, 0.013157894736842105),
(6, 0.013157894736842105), (7, 0.013157894736842105), (8, 0.013157894736842105),
(9, 0.013157894736842105), (11, 0.47368421052631576), (10,
0.013157894736842105), (12, 0.02631578947368421), (13, 0.013157894736842105),
(14, 0.013157894736842105), (15, 0.013157894736842105), (23,
0.19736842105263158), (24, 0.14473684210526316), (25, 0.21052631578947367), (26,
0.14473684210526316), (27, 0.22368421052631576), (28, 0.05263157894736842), (29,
0.10526315789473684), (31, 0.05263157894736842), (32, 0.013157894736842105),
(33, 0.02631578947368421), (34, 0.07894736842105263), (35, 0.07894736842105263),
(36, 0.07894736842105263), (37, 0.07894736842105263), (38, 0.07894736842105263),
(43, 0.039473684210526314), (44, 0.02631578947368421), (48, 0.2894736842105263),
(49, 0.09210526315789473), (51, 0.09210526315789473), (55, 0.25), (58,
0.19736842105263158), (64, 0.17105263157894735), (68, 0.13157894736842105), (69,
0.13157894736842105), (70, 0.13157894736842105), (71, 0.11842105263157894), (72,
0.039473684210526314), (16, 0.11842105263157894), (17, 0.09210526315789473),
(18, 0.09210526315789473), (19, 0.09210526315789473), (20, 0.09210526315789473),
(21, 0.09210526315789473), (22, 0.09210526315789473), (30, 0.02631578947368421),
(41, 0.14473684210526316), (42, 0.039473684210526314), (50,
0.02631578947368421), (39, 0.039473684210526314), (40, 0.013157894736842105),
(75, 0.09210526315789473), (54, 0.05263157894736842), (45,
0.013157894736842105), (52, 0.02631578947368421), (57, 0.14473684210526316),
(62, 0.17105263157894735), (46, 0.013157894736842105), (47,
0.02631578947368421), (59, 0.14473684210526316), (60, 0.11842105263157894), (61,
0.14473684210526316), (63, 0.15789473684210525), (65, 0.15789473684210525), (66,
0.13157894736842105), (73, 0.02631578947368421), (74, 0.02631578947368421), (76,
0.09210526315789473), (56, 0.02631578947368421), (53, 0.013157894736842105),
(67, 0.013157894736842105)]
Betweenness Centality:
[(0, 0.17684210526315788), (1, 0.0), (2, 0.0), (3, 0.0), (4, 0.0), (5, 0.0), (6, 0.0)]
(0.0), (7, 0.0), (8, 0.0), (9, 0.0), (11, 0.5699890527836186), (10, 0.0), (12, 0.0)
0.0), (13, 0.0), (14, 0.0), (15, 0.0), (23, 0.12964454098819425), (24,
0.02900241873046176), (25, 0.07490122123424227), (26, 0.023796253454148184),
(27, 0.05433155966478437), (28, 0.026491228070175437), (29,
0.008040935672514618), (31, 0.008640295033483887), (32, 0.0), (33, 0.0), (34,
(0.0), (35, 0.0), (36, 0.0), (37, 0.0), (38, 0.0), (43, 0.0), (44, 0.0), (48, 0.0)
```

```
0.1651125024258477), (49, 0.020210621583197756), (51, 0.047598927875243655),
(55, 0.132032488621946), (58, 0.0425533568221771), (64, 0.030753650179957816),
(68, 0.004960383978389518), (69, 0.004960383978389518), (70,
0.0048618041955992095), (71, 0.0038738298738298736), (72, 0.0), (16,
0.04062934817733579), (17, 0.0), (18, 0.0), (19, 0.0), (20, 0.0), (21, 0.0),
(22, 0.0), (30, 0.0), (41, 0.011487550654163002), (42, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50, 0.0), (50
0.00021720969089390142), (39, 0.006925438596491229), (40, 0.0), (75,
0.00043859649122807013), (54, 0.0), (45, 0.0), (52, 0.0003508771929824561), (57,
0.027661236424394314), (62, 0.005267029881988332), (46, 0.0), (47,
0.02631578947368421), (59, 0.0012501455659350393), (60, 0.0), (61,
0.0012501455659350393), (63, 0.0021854883087570063), (65,
0.0021854883087570063), (66, 0.00015037593984962405), (73, 0.0), (74, 0.0), (76,
0.0), (56, 0.0), (53, 0.0), (67, 0.0)]
Eigenvector Centality:
[(0, 0.028134336026755365), (1, 0.0023434559950116173), (2,
0.026872999836996418), (3, 0.026872999836996418), (4, 0.0023434559950116173),
(5, 0.0023434559950116173), (6, 0.0023434559950116173), (7,
0.0023434559950116173), (8, 0.0023434559950116173), (9, 0.0023434559950116173),
(11, 0.26761817598853926), (10, 0.022291152877501864), (12,
0.029767714740768846), (13, 0.022291152877501864), (14, 0.022291152877501864),
(15, 0.02291152877501864), (23, 0.08975922949834111), (24,
0.12228242172143362), (25, 0.1878077051550094), (26, 0.11103702398134034), (27,
0.184225163210257), (28, 0.04004860673568995), (29, 0.06227506194694945), (31,
0.046055011005835665), (32, 0.022291152877501864), (33, 0.03763613953656061),
(34, 0.04120828302958653), (35, 0.04120828302958653), (36, 0.04120828302958653),
(37, 0.04120828302958653), (38, 0.04120828302958653), (43,
0.046884942434314236), (44, 0.025627007259539696), (48, 0.31783893977497674),
(49, 0.06539729702430212), (51, 0.063169051443388), (55, 0.2591111453417876),
(58, 0.26717863282356663), (64, 0.24213078637474134), (68, 0.14543155406624994),
(69, 0.14543155406624994), (70, 0.14153627306562788), (71, 0.13602919446668402),
(72, 0.046884942434314236), (16, 0.04814615586401206), (17,
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(20, 0.019685736709537924), (21, 0.019685736709537924), (22,
0.019685736709537924), (30, 0.011312731565893446), (41, 0.14193827361489467),
(42, 0.03765154186582524), (50, 0.015632758907497154), (39,
0.03792696672003668), (40, 0.01564337736411263), (75, 0.1012869150267418), (54,
0.04153983995608888), (45, 0.0033358543820378303), (52, 0.008420710184175471),
(57, 0.19502891203664752), (62, 0.232467197170214), (46, 0.0022204916389402625),
(47, 0.026658767697788018), (59, 0.21073457488115607), (60,
0.17581635449396724), (61, 0.21073457488115607), (63, 0.22155360926119957), (65,
0.22155360926119957), (66, 0.1866353888740108), (73, 0.02887925933672828), (74,
0.02887925933672828), (76, 0.14071116072806059), (56, 0.027029413866137036),
(53, 0.005261623192198204), (67, 0.01624446552014877)]
Average Clustering Coefficient :
0.5731367499320135
Variance:
0.006233855003506406
```

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```
[64]: import networkx as nx
      import matplotlib.pyplot as plt
      import numpy as np
      from collections import Counter
      from scipy.stats import norm, powerlaw, expon
      from scipy.optimize import curve_fit
      # Load your dataset as a NetworkX graph (replace this with your specificu
       \rightarrow dataset)
      G = nx.read_edgelist("lesmis (1).txt")
      # Compute the degree of each node
      degrees = dict(G.degree())
      degree_values = list(degrees.values())
      # Calculate the degree histogram
      hist, bin edges = np.histogram(degree values, bins=20, density=True)
      # Plot the degree distribution
      plt.hist(degree_values, bins=20, density=True, alpha=0.5, color='b', __
       ⇔edgecolor='black')
      plt.title("Degree Distribution")
      plt.xlabel("Degree")
      plt.ylabel("Probability")
      # Define functions for fitting different distribution types
      def power_law(x, a, b):
          return a * (x**b)
      def exponential(x, scale):
          return scale * np.exp(-scale * x)
      # Fit the degree distribution to different candidate distributions
      params_powerlaw, _ = curve_fit(power_law, bin_edges[:-1], hist)
      params_exponential, _ = curve_fit(exponential, bin_edges[:-1], hist)
      # Determine the type of distribution based on the parameters
      alpha_powerlaw = params_powerlaw[1]
      scale_exponential = 1 / params_exponential[0]
      if alpha_powerlaw > 2.0:
          print("The degree distribution appears to be closer to a power-law⊔
       ⇔(scale-free) distribution.")
      elif scale_exponential < 2.0:</pre>
          print("The degree distribution appears to be closer to an exponential ⊔
       ⇔distribution.")
      else:
```

The degree distribution does not seem to be a power-law or exponential distribution.



[]: