Introduction
Overview of the approach
Outline of the talk
Introduction to Kernel notation
Compilation
Verification

Kernel: functional notation for system description

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Introduction

- ▶ Kernel is a notation for describing computer systems
- Kernel is both a programing language which can be compiled into a highly optimized machine code, and a specification language for modeling and verification purposes
- ► Main features unique to *Kernel* are
 - the uniform and minimalistic syntax;
 - precise mathematical semantics in terms of relations;
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- 1 My Solidum/IDT Canada experience: PDL/PTL (Packet Description/Transformation Language)
 - for programming one-state push-down automaton implemented in hardware
- 2 Edgewater: RTEdge a real-time programming language with integrated verifier for "meeting deadlines"
- ▶ In both cases the proprietary languages were needed even though hundreds of programming languages had already existed...
- Kernel aims to become a common notation easily extensible ... to meet PTL or RTEdge requirements, for example.



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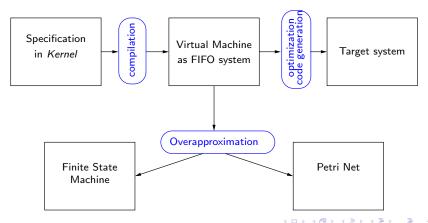
What Kernel is not...

- Kernel is not a full featured general purpose programming language for IT professionals ...
 Even though one could use Kernel to develop a Web site or a flashy graphical user interface, the notation was not designed for it ...
- You may be interested in Kernel if you want your program to be provably:
 - ▶ fast
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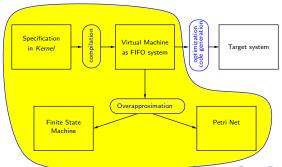
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Overview of the approach



Outline of the talk

- 1. Short introduction to Kernel notation
- 2. How do we compile a Kernel program into FIFO system
- 3. Verification by over-approximations



<type> nat <is> ['0 {}, '1 nat];

Values: '0, '1'0, '1'1'0, '1'1'1'0, ..., are trees!

A Kernel type is

- a set of values (finite tree automata = and-or graphs),
- ▶ a set of constructors (field names), and
- ▶ a set of *patterns* (initial parts of values).

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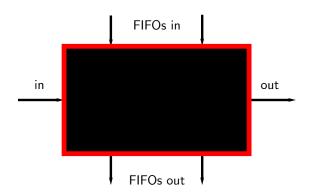
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- a set of patterns (initial parts of values).

Kernel components are relations



Every non-recursive *Kernel* component can be translated into one (possibly very big) state machine.

```
←□→ ←□→ ←□→ ←□→
```

```
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(pair \rightarrow nat) x-y =
   [ (\{ x ..., y '0 \} -> \$.x \},
     ({ (x '1 ..., 'y ... } \rightarrow { (x $.x.1, 'y $.y.1}) :: x-y)
   ] <by> FIRST_MATCH;
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(\{\} \rightarrow nat\}) main =
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   get_nat,
   get_pair :: x-y
   <longest> /* <shortest>, <unknown> */ get_nat
];
```

- Pattern matching
 - Every pattern corresponds to a regular tree language encoded by a "simple language" (one state push-down automaton).
 - Regular tree languages are closed by union, intersection, and complement.
- Product, Union, and Composition are variations of composition of relations - realized by corresponding state products
- Projection is relabeling





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An example...

Pattern {'x ..., 'y '0} of type pair: $(x/x)(1/1)^*(0/0)(y/y)(0/0)$

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FIFO system

- ▶ A FIFO system is a network of finite state machines connected by point-to-point FIFO channels.
- Since FIFOs are unbounded, even a single state machine with a couple of FIFOs is Turing Machine equivalent.
- Advantages of FIFO virtual machine representation are:
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- ▶ In theory, a finite state FIFO system (i.e., with bounded size channels) can be verified using SPIN/Promela tool set ... however, checking if FIFO system is "finite state" is undecidable!
- Over-approximation:
 - over-approximation of 5 consists in adding "executions" to the system creating its "over-approximation" S', hopefully simpler to analyze
 - ▶ to prove that every execution of S has a property ϕ , we prove that every execution of S' has the property ϕ
 - E.g., the over-approximation can be used in proving that a WCRT is bounded by a "deadline"



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- ► We have considered two over-approximations of a FIFO system *S*:
 - ► Transformation of *S* into a finite state machine: It can be done by a successive elimination of FIFO channels Question: How a FIFO channel can be eliminated?
 - Transformation of S into a Petri Net. If the FIFO channels are replaced by "any-order" containers then without loosing any possible execution of the initial FIFO system, we can replace every channel by a finite set of Places.

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- We propose a simple but powerful notation for describing computing systems
- Semantics of the notation is expressed in terms of multi-dimensional "relations" which can be effectively implemented as a FIFO system
- We mentioned two techniques which can transform FIFO system by over-approximation into:
 - a finite state machine
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- This is work in progress ... especially meaningful FIFO system construction



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the end