Policy Evaluation The Big Picture

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Recap I: Markov Decision Process (MDP)

- Markov Decision Process is Markov Reward Process + actions
- Definition of MDP
 - ▶ S is a (finite) set of Markov states $s \in S$
 - ▶ A is a (finite) set of actions $a \in A$
 - ▶ P is dynamics/transition model for each action, that specifies $P(s_{t+1} = s' \mid s_t = s, a_t = a)$
 - R is a reward function $R(s_t = s, a_t = a) = \mathbb{E}[r_r \mid s_t = s, a_t = a]$
 - ***** Sometimes R is also defined based on (s) or on (s, a, s')
 - ▶ Discount factor $\gamma \in [0, 1]$
- MDP is tuple (S, A, P, R, γ)



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 - ▶ Discount factor $\gamma \in [0, 1]$
- MDP is tuple (S, A, P, R, γ)
- → Unfortunately, we often do not have access to true MDP models



Recap II

- Definition of Return G_t (for a MRP)
 - ▶ Discounted sum of rewards from time step t to horizon

$$G_t = r_t + \gamma r_{t+1} + \gamma^2 r_{t+2} + \gamma^3 r_{t+3} + \dots$$



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- Definition of State-Action Value Function $Q^{\pi}(s,a)$
 - \blacktriangleright Expected return from starting in state s, taking action a and then following policy π

$$Q^{\pi}(s, a) = \mathbb{E}_{\pi}[G_t \mid s_t = s, a_t = a]$$

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Goal for this week

- Assumption: We don't have the exact model of the environment (i.e., model-free), but we can query the environment ("playing roll-outs")
 - state space and action space are in principle known
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- ▶ If we first learn the MDP and then apply planning to the learned MDP, we do "model-based" RL (not today!)



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- Goal for this week: We want to learn $V^{\pi}(s)$ or $Q^{\pi}(s,a)$ (depending on the RL algorithm we want to use) by only querying the unknown MDP