

# Policy Evaluation

## Monte Carlo Evaluation

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Automated  
Machine Learning  
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# Policy Evaluation without a model

- Goal: Policy Evaluation without a model
  - ▶ Given data and/or ability to interact with the environment
  - ▶ Efficiently compute a good estimate of a policy  $\pi$
- For example: Estimate expected total purchases during an online shopping session for a new automated product recommendation policy

# Monte Carlo (MC) Policy Evaluation

- $G_t = r_t + \gamma r_{t+1} + \gamma^2 r_{t+2} + \dots$  in MDP  $M$  under policy  $\pi$
- $V^\pi(s) \approx \mathbb{E}_{T \sim \pi}[G_t \mid s_t = s]$ 
  - ▶ Expectation over trajectories  $T$  generated by following  $\pi$
- Simple idea: Value = mean return
- If trajectories are all finite, sample set of trajectories & average returns

# Monte Carlo (MC) Policy Evaluation

- If trajectories are all finite, sample set of trajectories & average returns
- Does **not** require MDP dynamics/rewards
- No bootstrapping
- Does not assume state is Markov
- Can only be applied to episodic MDPs
  - ▶ Averaging over returns from a complete episode
  - ▶ Requires each episode to terminate

# Monte Carlo (MC) Policy Evaluation

- Aim: estimate  $V^\pi(s)$  given episodes generated under policy  $\pi$ 
  - ▶  $s_1, a_1, r_1, s_2, a_2, r_2, \dots$  where the actions are sampled from  $\pi$
- $G_t = r_t + \gamma r_{t+1} + \gamma^2 r_{t+2} + \dots$  in MDP  $M$  under policy  $\pi$
- $V^\pi(s) = \mathbb{E}[G_t \mid s_t = s]$
- MC computes empirical mean return
- Often do this in an incremental fashion
  - ▶ After each episode, update estimate of  $V^\pi$

# First-Visit Monte Carlo (MC) On Policy Evaluation

Initialize  $N(s) = 0$ ,  $G(s) = 0 \forall s \in S$

Loop

- Sample episode  $i = s_{i,1}, a_{i,1}, r_{i,1}, s_{i,2}, a_{i,2}, r_{i,2}, \dots, s_{i,n}$
- Define  $G_{i,t} = r_{i,t} + \gamma r_{i,t+1} + \gamma^2 r_{i,t+2} + \dots$
- For each state  $s$  visited in episode  $i$ 
  - ▶ for first time  $t$  that state  $s$  is visited in episode  $i$ 
    - ★ Increment counter of total first visits:  $N(s) = N(s) + 1$
    - ★ Increment total return  $G(s) = G(s) + G_{i,t}$
    - ★ Update estimate  $V^\pi(s) = G(s)/N(s)$