Model Free Control SARSA and Q-Learning

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Model-free Policy Iteration with TD Methods

- Use temporal difference methods for policy evaluation step
- Initialize policy π
- Repeat:
 - \blacktriangleright Policy evaluation: compute Q^π using temporal difference updating with Q-greedy policy
 - Policy improvement: Same as Monte Carlo policy improvement, set π to ϵ -greedy (Q^{π})
- First consider SARSA, which is an on-policy algorithm



General Form of SARSA Algorithm

- Initialization:
 - ε-greedy policy
 - t = 0
 - ightharpoonup initial state $s_t = s_0$
- Loop
 - ▶ Take action $a_{t+1} \sim \pi(s_{t+1})$
 - ▶ Observe (r_{t+1}, s_{t+2})
 - ▶ Update Q given $(s_t, a_t, r_t, s_{t+1}, a_{t+1})$:

$$Q(s_t, a_t) \leftarrow Q(s_t, a_t) + \alpha(r_t + \gamma Q(s_{t+1}, a_{t+1}) - Q(s_t, a_t))$$

- ▶ $\pi(s_t) \in \arg\max_{a \in A} Q(s_t, a)$ with probability 1ϵ , else random
- ▶ t = t + 1



Convergence Properties of SARSA

- Theorem:
- SARSA for finite-state and finite-action MDPs converges to the optimal action-value, $Q(s,a) \rightarrow Q^*(s,a)$, under the following conditions:
 - **1** The policy sequence $\pi_t(a \mid s)$ satisfies the condition of GLIE
 - 2 The step-sizes α_t satisfy the Robbins-Munro sequence such that

$$\sum_{t=1}^{\infty} \alpha_t = \infty$$

$$\sum_{t=1}^{\infty} \alpha_t^2 < \infty$$

- \bullet For example $\alpha_t = \frac{1}{T}$ satisfies the above condition
- Would one want to use a step size choice that satisfies the above in practice? Likely not.

Q-Learning: Learning the Optimal State-Action Value

- SARSA is an on-policy learning algorithm
- SARSA estimates the value of the current behavior policy (policy using to take actions in the world)
- And then updates the policy trying to estimate
- Alternatively, can we directly estimate the value of π^* while acting with another behavior policy π_b ?
- Yes! Q-learning, an off-policy RL algorithm
- Key idea: Maintain state-action Q estimates and use to bootstrap use the value of the best future action
- Recall SARSA

$$Q(s_t, a_t) \leftarrow Q(s_t, a_t) + \alpha((r_t + \gamma Q(s_{t+1}, a_{t+1})) - Q(s_t, a_t))$$

• Q-Learning:

$$Q(s_t, a_t) \leftarrow Q(s_t, a_t) + \alpha((r_t + \gamma \max_{a' \in A} Q(s_{t+1}, a')) - Q(s_t, a_t))$$
Automated Macline Learning

Q-Learning with ϵ -greedy Exploration

- Initialization:
 - $ightharpoonup Q(s,a). \forall s \in S, a \in A$
 - ightharpoonup initial state $s_t = s_0$
- Loop
 - ▶ Take action $a_t \sim \pi_b(s_t)$
 - ▶ Observe (r_t, s_{t+1})
 - Update Q

$$Q(s_t, a_t) \leftarrow Q(s_t, a_t) + \alpha(r_t + \gamma \max_{a \in A} Q(s_{t+1}, a) - Q(s_t, a_t))$$

- \bullet $\pi(s_t) \in \arg \max_{a \in A} Q(s_t, a)$ with probability 1ϵ , else random
- ▶ t = t + 1



Q-Learning with ϵ -greedy Exploration

- Conditions for convergence to Q*?
 - ightharpoonup Visit all (s,a) pairs infinitely often
 - the step-sizes α_t satisfy the Robbins-Munro sequence
 - Note: the algorithm does not have to be greedy in the limit of infinite exploration (GLIE) to satisfy this
- ullet Conditions for convergence to optimal π^*
 - ▶ The above requirements to converge to optimal Q*
 - The algorithm is GLIE

