



# Module #7a:

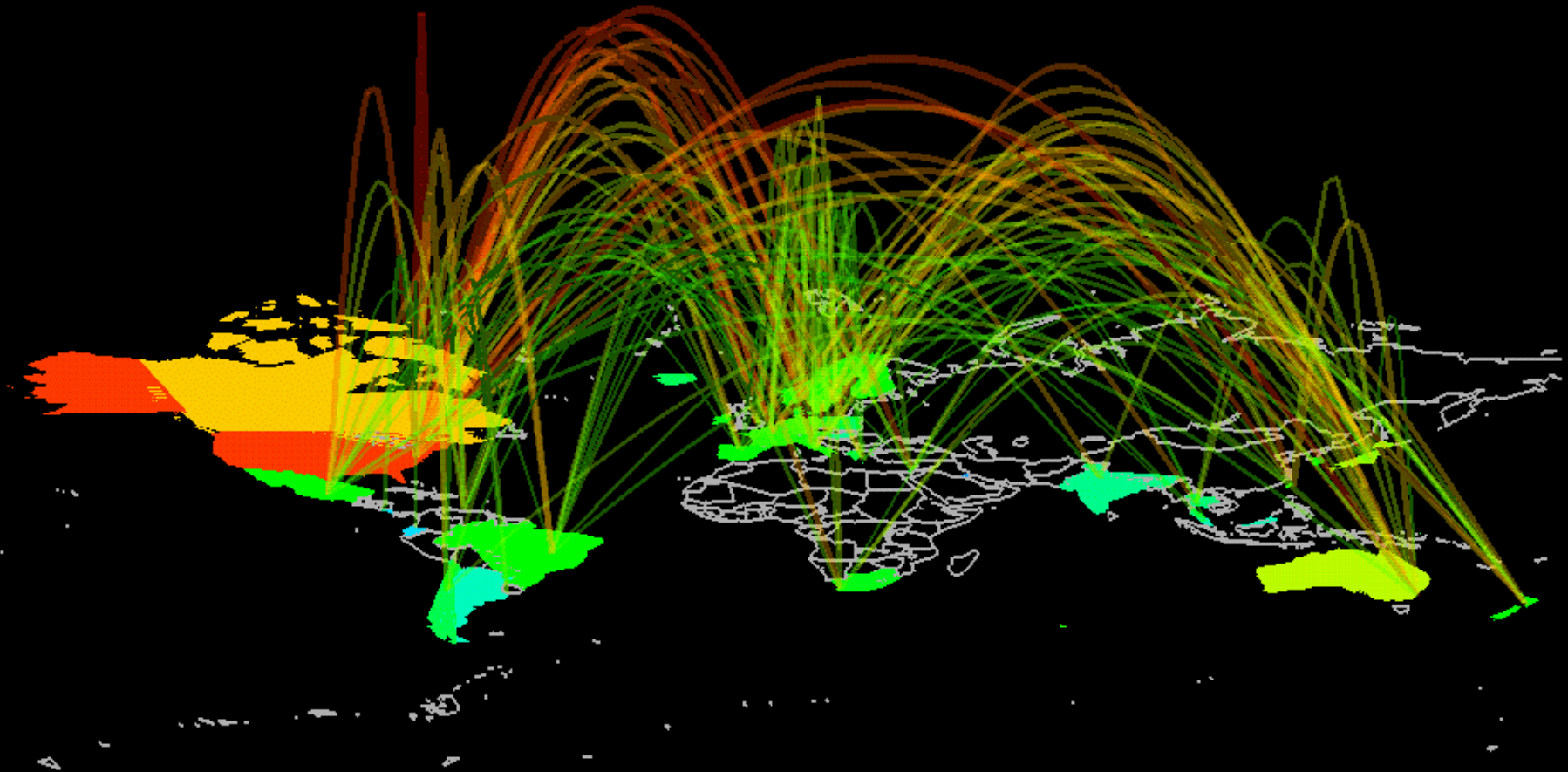
# Theory of Network Visualization



# Objective

- Define hierarchical data and related terms
- List example tasks for hierarchical and network data
- Understand approaches to draw 2D trees
- Describe treemap, SunBurst, and other techniques

# Connected World



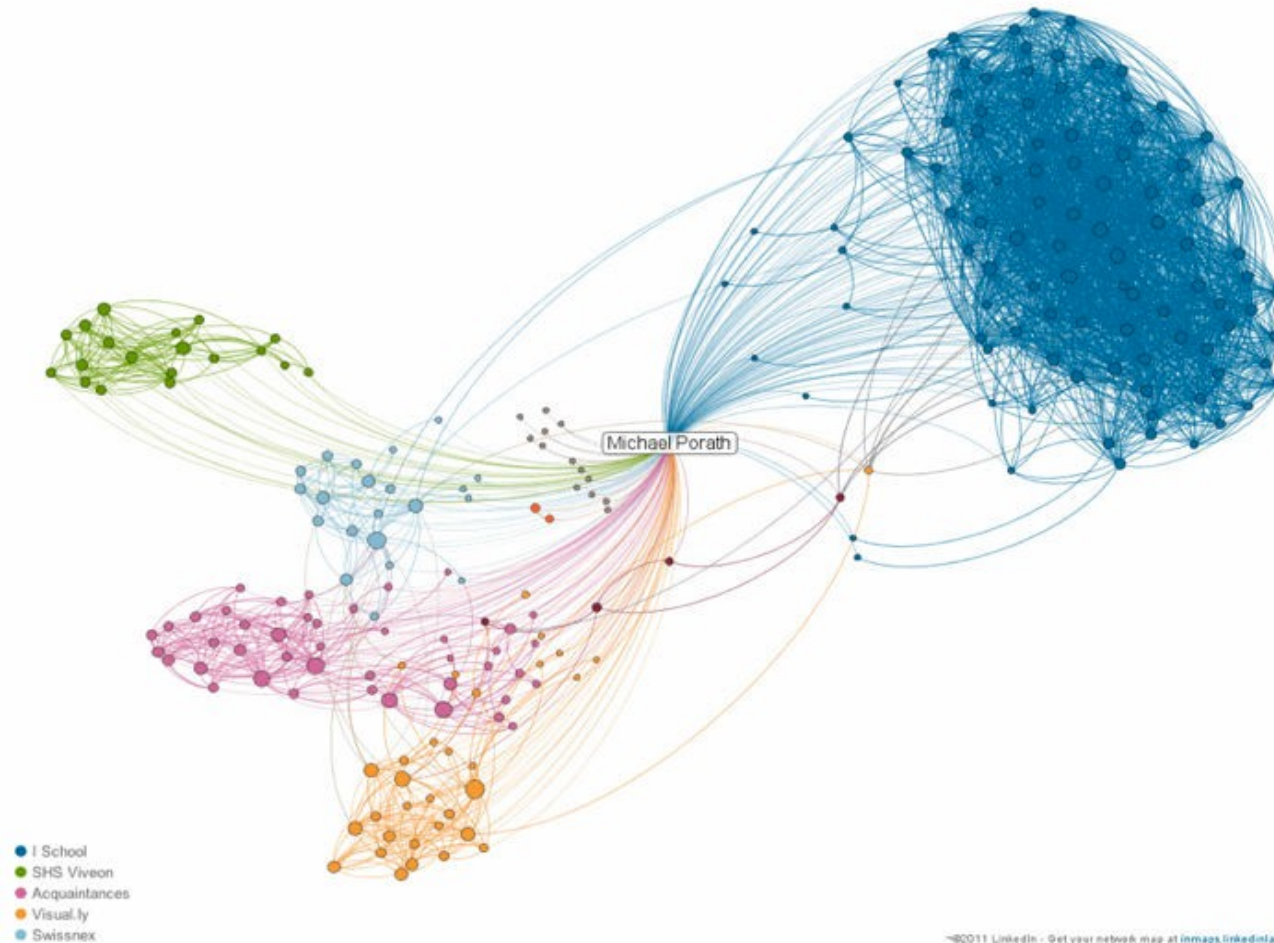


# Social Networks



# Social Networks

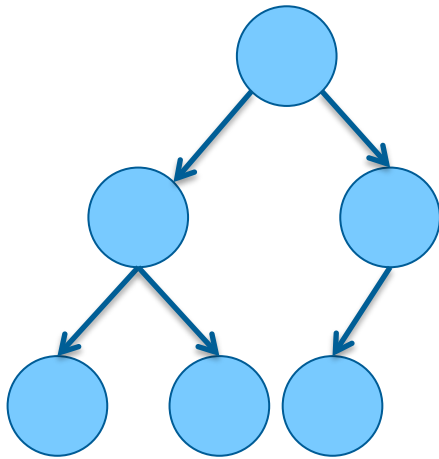
LinkedIn Maps Michael Porath's Professional Network  
as of April 8, 2012



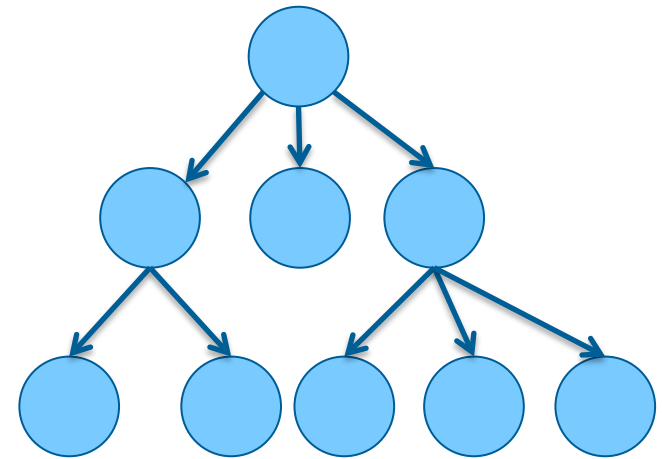
©2011 LinkedIn - Get your network map at [inmaps.linkedinlabs.com](http://inmaps.linkedinlabs.com/)



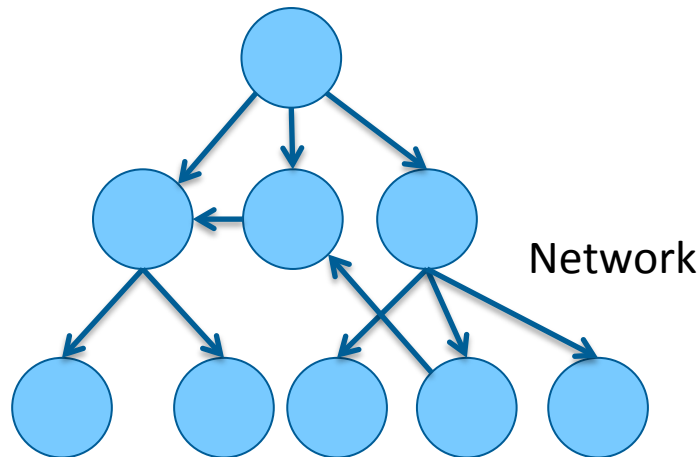
# Properties of networks



Tree



Tree



Network



# Properties



Undirected edges



Directed edges



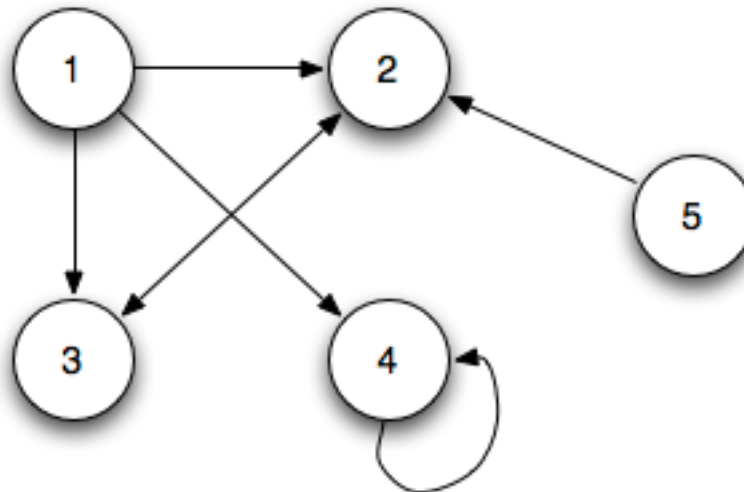
Bi-directional, symmetrical edges



Bi-directional, asymmetrical edges

# Graph terminology I

- A **graph** is a collection of **nodes** (or **vertices**, singular is **vertex**) and **edges** (or **arcs**)
  - Each node contains an **element**
  - Each edge connects two nodes together (or possibly the same node to itself) and may contain an **edge attribute**

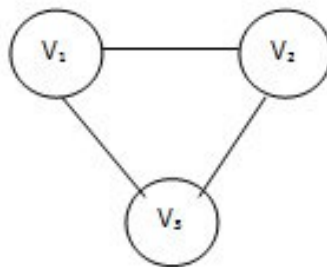




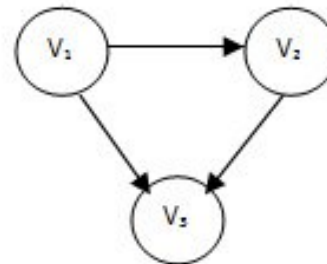
# Graph terminology I

- A **directed graph** is one in which the edges have a direction
- An **undirected graph** is one in which the edges do not have a direction

Undirected Graph

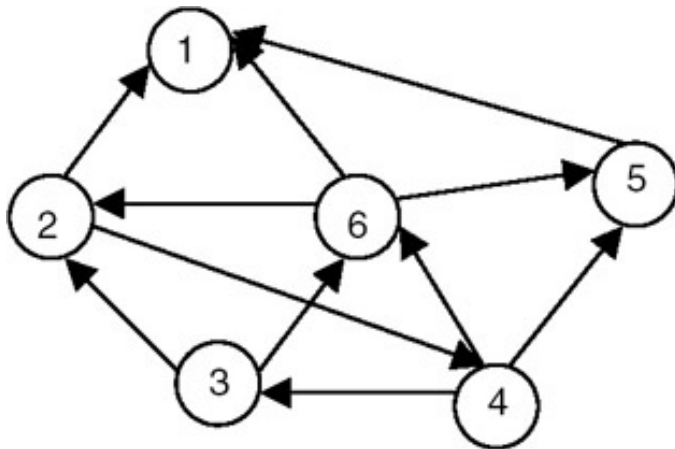


Directed Graph



# Graph terminology II

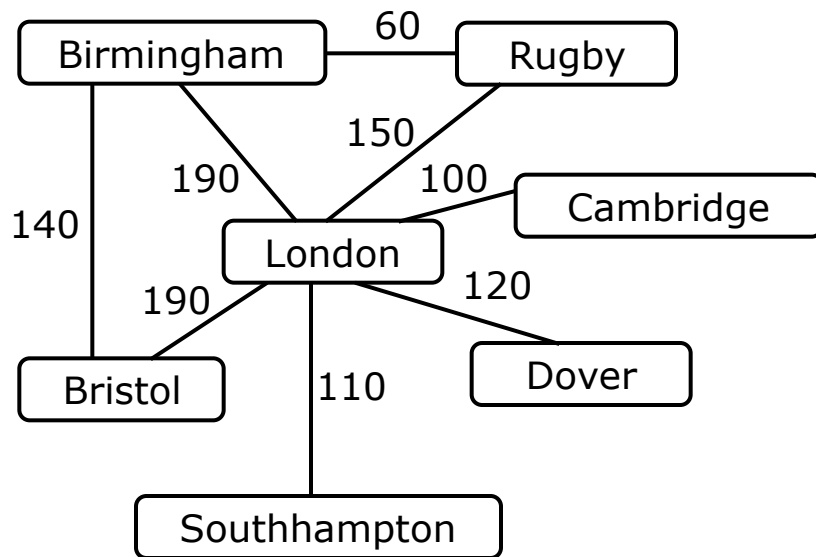
- The **size** of a graph is the number of *nodes* in it
- If two nodes are connected by an edge, they are **neighbors** (and the nodes are **adjacent** to each other)
- The **degree of a node** is the number of edges it has
- For directed graphs,
  - The **in-degree** of a node is the number of in-edges it has
  - The **out-degree** of a node is the number of out-edges it has



	Indegree	Outdegree
1	3	0
2	2	2
3	1	2
4	1	3
5	2	1
6	2	3

# Graph terminology III

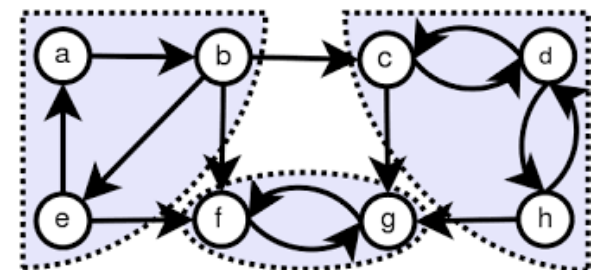
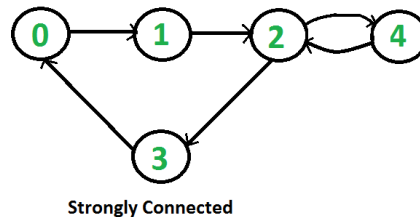
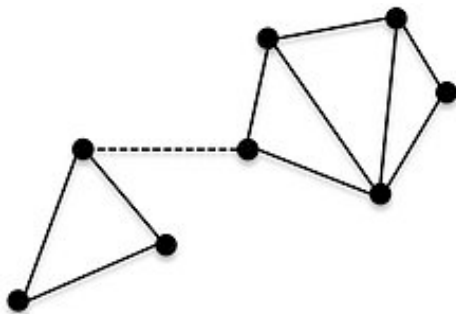
- A **path** is a list of edges such that each node (but the last) is the predecessor of the next node in the list
- A **cycle** is a path whose first and last nodes are the same



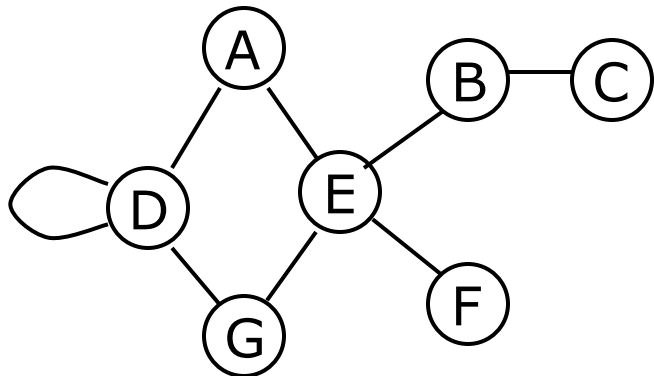
- Example: (London, Bristol, Birmingham, London, Dover) is a path
- Example: (London, Bristol, Birmingham, London) is a cycle
- A **cyclic graph** contains at least one cycle
- An **acyclic graph** does not contain any cycles

# Graph terminology IV

- An undirected graph is **connected** if there is a path from every node to every other node
- A *directed graph* is **strongly connected** if there is a path from every node to every other node
- Node  $X$  is **reachable** from node  $Y$  if there is a path from  $Y$  to  $X$
- A subset of the nodes of the graph is a **connected component** (or just a **component**) if there is a path from every node in the subset to every other node in the subset



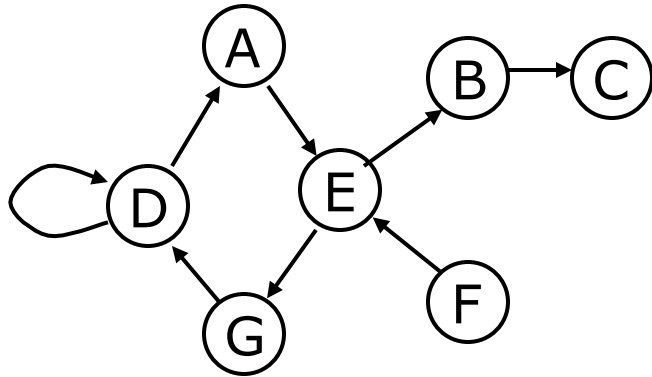
# Adjacency-matrix representation I



	A	B	C	D	E	F	G
A				●	●		
B			●		●		
C		●					
D	●			●			●
E	●	●				●	●
F					●		
G				●	●		

- One simple way of representing a graph is the **adjacency matrix**
- A 2-D array has a mark at  $[i][j]$  if there is an edge from node  $i$  to node  $j$
- The adjacency matrix is symmetric about the main diagonal

# Adjacency-matrix representation II



	A	B	C	D	E	F	G
A					●		
B			●				
C							
D	●			●			
E		●					●
F					●		
G				●			

- An **adjacency matrix** can equally well be used for digraphs (directed graphs)
- A 2-D array has a mark at  $[i][j]$  if there is an edge from node  $i$  to node  $j$
- Only suitable for *small* graphs!





# Pros and Cons of Adjacency Matrices

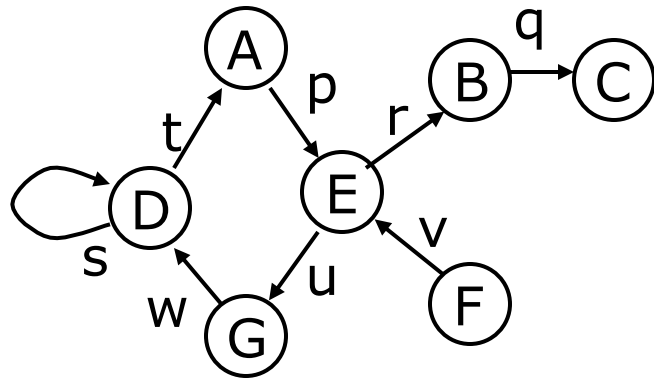
- Pros:
  - Simple to implement
  - Easy and fast to tell if a pair  $(i,j)$  is an edge: simply check if  $A[i][j]$  is 1 or 0
- Cons:
  - No matter how few edges the graph has, the matrix takes  $O(n^2)$  in memory



# Edge-set representation I

- An **edge-set** representation uses a *set* of nodes and a *set* of edges
  - The sets might be represented by, say, linked lists
  - The set links are stored in the nodes and edges themselves

# Edge-set representation II

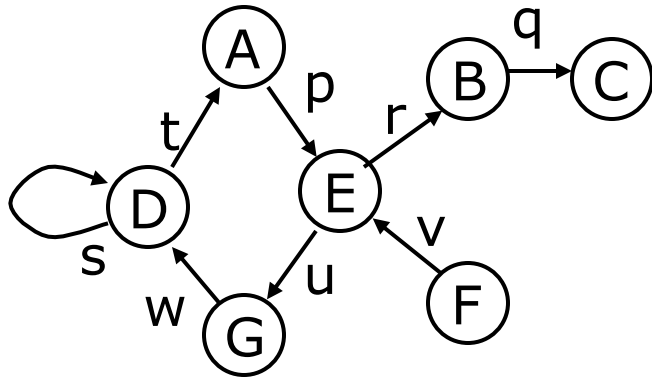


nodeSet = {A, B, C, D, E, F, G}

edgeSet = { p: (A, E),  
q: (B, C), r: (E, B),  
s: (D, D), t: (D, A),  
u: (E, G), v: (F, E),  
w: (G, D) }

- Here we have a set of nodes, and each node contains only its element (not shown)
- Each edge contains references to its source and its destination (and its attribute, if any)

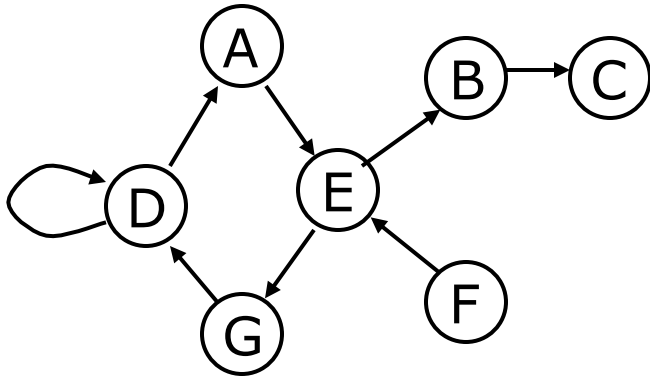
# Adjacency-set representation II



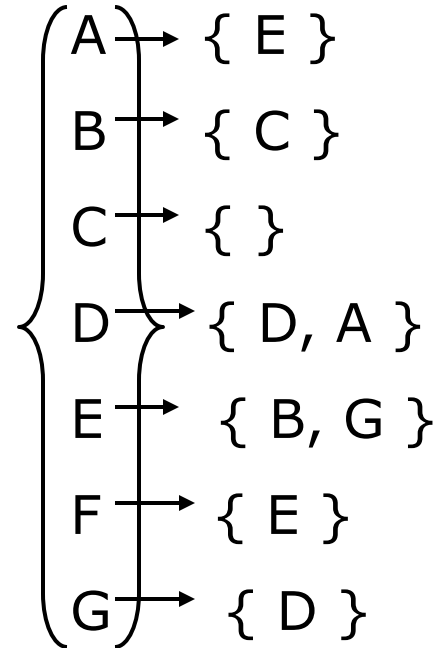
- Here we have a set of nodes, and each node refers to a set of edges
- Each edge contains references to its source and its destination (and its attribute, if any)

A	→	{ p }	p: (A, E)
B	→	{ q }	q: (B, C)
C	→	{ }	r: (E, B)
D	→	{ s, t }	s: (D, D)
E	→	{ r, u }	t: (D, A)
F	→	{ v }	u: (E, G)
G	→	{ w }	v: (F, E)
			w: (G, D)

# Adjacency-set representation II



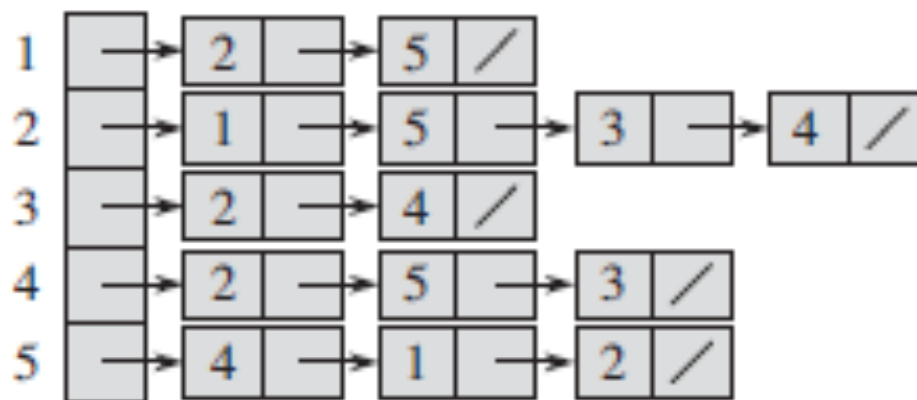
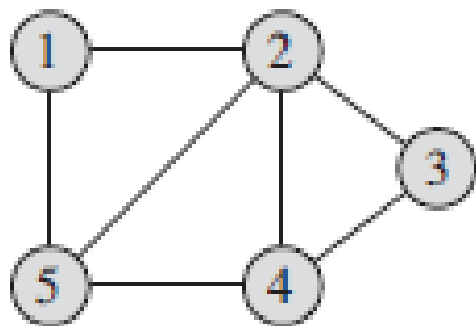
- Here we have a set of nodes, and each node refers to a set of other (pointed to) nodes
- The edges are *implicit*





# Graph representations: Adjacency List

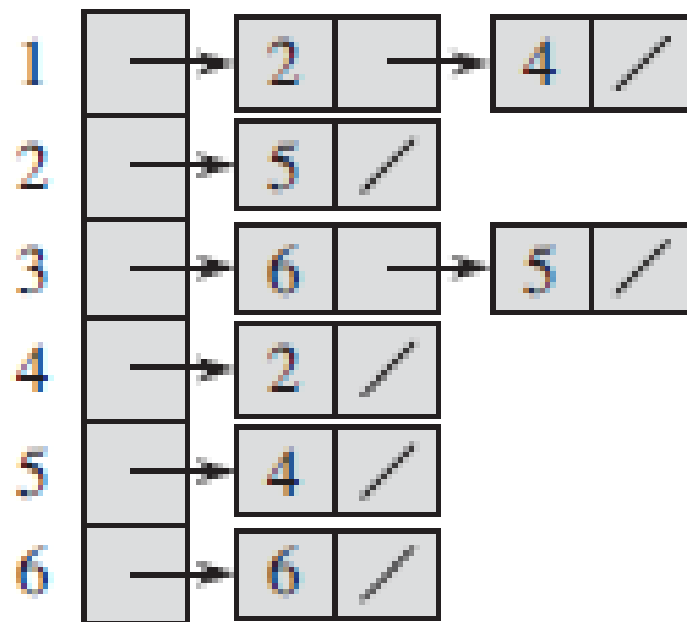
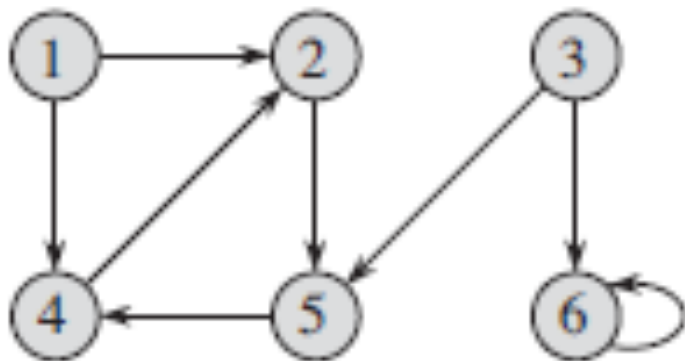
- **Undirected** weighted graph





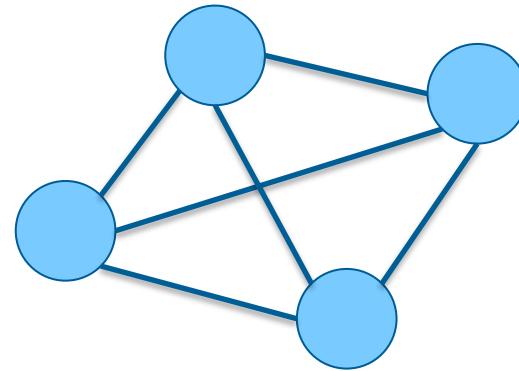
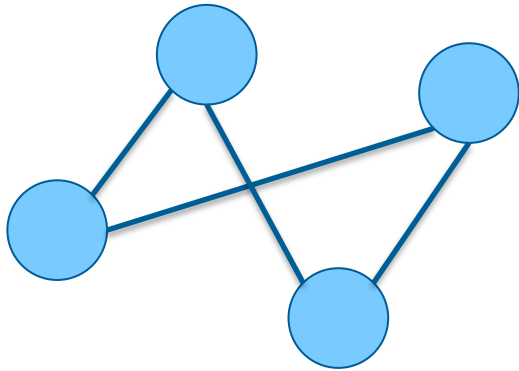
# Graph representations: Adjacency List

- **Directed** weighted graph



# Topology: Planar graphs

Graphs that can be laid out without edge crossing

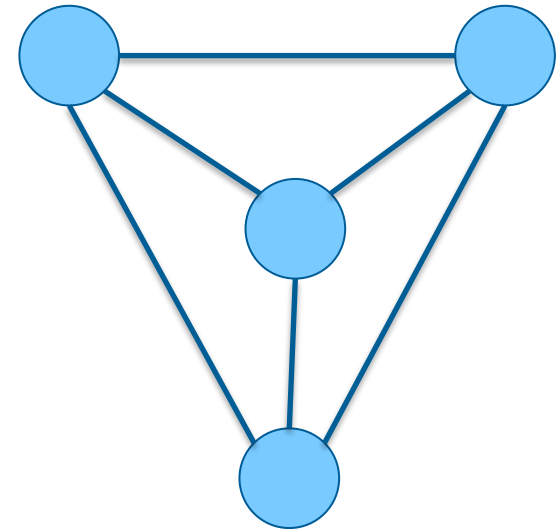
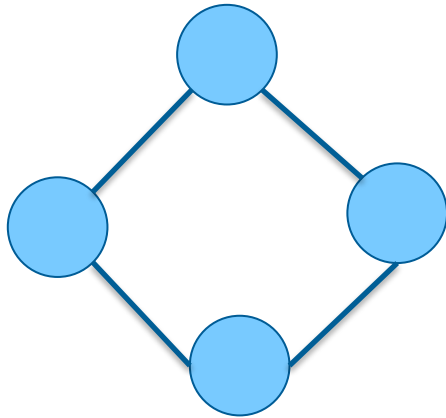


Which one is planar?



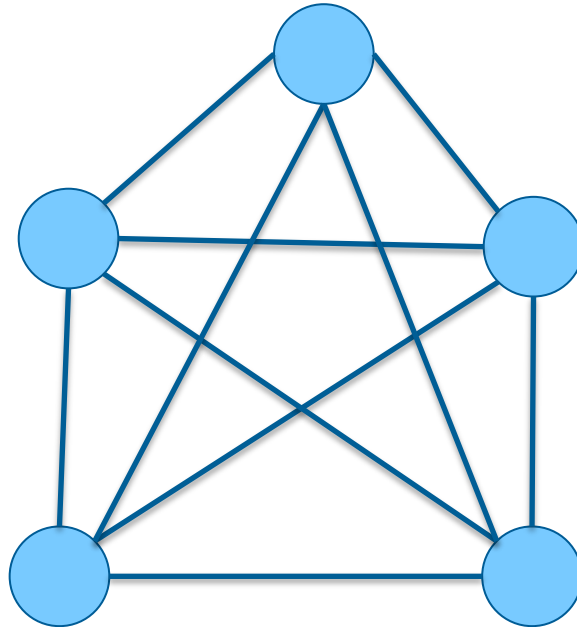
# Topology: Planar graphs

Graphs that can be laid out without edge crossing





# Topology: Planar graphs



Non-planar



JOHNS HOPKINS  
WHITING SCHOOL  
*of* ENGINEERING

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