

Splines

H.M. James Hung

In many practical problems, the expected value of the response variable y may follow a complex form of the regressor x . An example is that $E(y | x)$ is linear in x in one interval of x and quadratic in x in other intervals.

How to model $E(y | x)$?

Refer to Section 7.2.2 of Textbook

Use of splines is a powerful method.

Use subscript + to define the knot; for example, + in $(x - t)_+$ implies

when $x > t$, $(x - t)_+ = x - t$, which is positive.

when $x \leq t$, $(x - t)_+ = 0$

Use superscript “power” to define the degree of the polynomial function (e.g., linear, quadratic), as shown in Mod05.

Thus, when $x > t$, $(x - t)_+^0 = (x - t)^0 = 1$; that is, any positive number to the 0th power is 1.

Define $(x - t)_+^0 = 0$, when $x \leq t$.

When $x > t$, $(x - t)_+^1 = (x - t)^1 = (x - t)$.

When $x \leq t$, $(x - t)_+^1 = 0$.

Likewise, for any $j \geq 2$,

when $x > t$, $(x - t)_+^j = (x - t)^j$;

when $x \leq t$, $(x - t)_+^j = 0$.