625.661 Statistical Models and Regression Module 2 Discussion Questions

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Please discuss all the following questions.

- 1. A typical simple linear regression model is $y = \beta_0 + \beta_1 x + \varepsilon$, where y is a response variable (also often called dependent variable), x is an independent variable (also often called regressor), and ε is a random error with mean (also called expectation) zero. Thus y and ε are random variables. The regressor x is either a random variable or a non-random (also often called fixed) variable. A set of n independent paired data $(y_1, x_1), \dots, (y_n, x_n)$ follow this model. Before the n paired data values are available, we construct the ordinary least squares (OLS) estimators for β_0 and β_1 as described in Chapter 2 of the Textbook.
 - a) Discuss whether the assumption of "the constant variance σ^2 " (see (2.1) in the Textbook) is required for the construction of the OLS estimators.
 - b) Discuss whether the constant variance assumption in (2.1) of the Textbook is required for unbiasedness of OLS estimators.