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```
function alpha = rsp_alpha(chi_expt)

if chi_expt~=chi_expt'
    error('Input matrix is not a density matrix.')
else
    chi_expt=chi_expt/trace(chi_expt);
end

Not enough input arguments.

Error in rsp_alpha (line 2)
if chi_expt~=chi_expt'
```

## define SDP parameters

### define $v_\lambda$ and $\rho_\lambda$

```
for i = 1:2
for j = 1:2
for k = 1:2

    v{i,j,k} = [i,j,k];
    rho_lambda{i,j,k} = sdpvar(2,2,'hermitian','complex');

end
end
end
```

### define $p(v_{nm}|\lambda)$

```
for n=1:2
```

---

```

for m=1:3
for i=1:2
for j=1:2
for k=1:2
    P_lambda_vnm{i,j,k,n,m} = kronDel(n,v{i,j,k}(m));
end
end
end
end
end

```

**define**  $\tilde{\rho}_{c|v_{nm}} = \sum_{\lambda} p(\lambda|v_{nm})\rho_{\lambda}$

```

for n=1:2
for m=1:3
    rho_rcs{n,m} = 0*sdpvar(2,2);
for i=1:2
for j=1:2
for k=1:2
    rho_rcs{n,m} = rho_rcs{n,m} +
    P_lambda_vnm{i,j,k,n,m}*rho_lambda{i,j,k};
end
end
end
end
end

```

**construct**  $\tilde{\chi}_{\mathcal{E}_c}$

```

for i=1:2
for j=1:2

    rhoc{i,j}=0*sdpvar(2,2);

end
end

rhoc{1,1}=rho_rcs{1,3};
rhoc{1,2}=rho_rcs{1,1}+sqrt(-1)*rho_rcs{1,2}-
(1+sqrt(-1))*(rho_rcs{1,3}+rho_rcs{2,3})/2;
rhoc{2,1}=rho_rcs{1,1}-sqrt(-1)*rho_rcs{1,2}-(1-
sqrt(-1))*(rho_rcs{1,3}+rho_rcs{2,3})/2;
rhoc{2,2}=rho_rcs{2,3};

for i=1:2
    for j=1:2
        for k=1:2
            for l=1:2
                chi_Ec(i*2+j*1-2,k*2+l*1-2)=rhoc{i,k}(j,l);
            end
        end
    end
end

```

---

```

end
end

```

## contraints

```
F = [];
```

$$\tilde{\rho}_\lambda \geq 0, \forall \lambda$$

```

for i = 1:2
for j = 1:2
for k = 1:2
    F = [F, rho_lambda{i,j,k}>=0];
end
end
end

```

$$\tilde{\chi}_{\mathcal{E}_c} \geq 0$$

```
F = [F, chi_Ec >= 0];
```

$$\text{tr}(\tilde{\rho}_{c|v_{0m}}) = \text{tr}(\tilde{\rho}_{c|v_{1m}}), \quad \forall m$$

```

F =
[F,trace(rho_lambda{1,1,1}+rho_lambda{1,1,2}+rho_lambda{1,2,1}+rho_lambda{1,2,2})
F =
[F,trace(rho_lambda{1,1,1}+rho_lambda{1,1,2}+rho_lambda{2,1,1}+rho_lambda{2,1,2})
F =
[F,trace(rho_lambda{1,1,1}+rho_lambda{1,2,1}+rho_lambda{2,1,1}+rho_lambda{2,2,1})

```

$$\chi_{\mathcal{E}} - \tilde{\chi}_{\mathcal{E}_c} \geq 0$$

```
Fa_expt=[F , chi_expt-chi_Ec >= 0];
```

**minimize**  $\alpha \equiv \min_{\tilde{\chi}_{\mathcal{E}_c}} 1 - \text{tr}(\tilde{\chi}_{\mathcal{E}_c})$  **via SDP solver**

```

sums=1-trace(chi_Ec);
sol=solvesdp(Fa_expt ,sums)

alpha=double(sums);

```

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