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## Table of Contents

.....	1
define SDP parameters .....	1
define $v_\lambda$ and $\rho_\lambda$ .....	1
define $p(v_{nm} \lambda)$ .....	1
define $\tilde{\rho}_{c v_{nm}} = \sum_\lambda p(\lambda v_{nm})\rho_\lambda$ .....	2
construct $\tilde{\chi}_{\mathcal{E}_c}$ .....	2
constraints .....	3
$\tilde{\rho}_\lambda \geq 0, \forall \lambda$ .....	3
$\tilde{\chi}_{\mathcal{E}_c} \geq 0$ .....	3
$\text{tr}(\tilde{\rho}_{c v_{0m}}) = \text{tr}(\tilde{\rho}_{c v_{1m}}), \forall m$ .....	3
$\text{tr}(\tilde{\chi}_{\mathcal{E}_c}) = 1$ .....	3
maximize $F_{\mathcal{E}_c} = \max_{\tilde{\chi}_{\mathcal{E}_c}} \text{tr}(\tilde{\chi}_{\mathcal{E}_c} \chi_{\text{RSP}})$ .....	3

```
function Fsc = rsp_Fsc(chi_RSP)

if chi_RSP~=chi_RSP' | trace(chi_RSP)<max(eig(chi_RSP))
    error('Input matrix is not a process matrix of an unitary.')
end

Not enough input arguments.

Error in rsp_Fsc (line 3)
if chi_RSP~=chi_RSP' | trace(chi_RSP)<max(eig(chi_RSP))
```

## define SDP parameters

### define $v_\lambda$ and $\rho_\lambda$

```
for i = 1:2
for j = 1:2
for k = 1:2

    v{i,j,k} = [i,j,k];
    rho_lambda{i,j,k} = sdpvar(2,2,'hermitian','complex');

end
end
end
```

### define $p(v_{nm}|\lambda)$

```
for n=1:2
for m=1:3
```

---

```

for i=1:2
for j=1:2
for k=1:2
    P_lambda_vnm{i,j,k,n,m} = kronDel(n,v{i,j,k}(m));
end
end
end
end
end

```

**define**  $\tilde{\rho}_{c|v_{nm}} = \sum_{\lambda} p(\lambda|v_{nm})\rho_{\lambda}$

```

for n=1:2
for m=1:3
    rho_rcs{n,m} = 0*sdpvar(2,2);
for i=1:2
for j=1:2
for k=1:2
    rho_rcs{n,m} = rho_rcs{n,m} +
    P_lambda_vnm{i,j,k,n,m}*rho_lambda{i,j,k};
end
end
end
end
end

```

**construct**  $\tilde{\chi}_{\mathcal{E}_c}$

```

for i=1:2
for j=1:2

    rhoc{i,j}=0*sdpvar(2,2);

end
end

rhoc{1,1}=rho_rcs{1,3};
rhoc{1,2}=rho_rcs{1,1}+sqrt(-1)*rho_rcs{1,2}-
(1+sqrt(-1))*(rho_rcs{1,3}+rho_rcs{2,3})/2;
rhoc{2,1}=rho_rcs{1,1}-sqrt(-1)*rho_rcs{1,2}-(1-
sqrt(-1))*(rho_rcs{1,3}+rho_rcs{2,3})/2;
rhoc{2,2}=rho_rcs{2,3};

for i=1:2
for j=1:2
for k=1:2
for l=1:2
    chi_Ec(i*2+j*1-2,k*2+l*1-2)=rhoc{i,k}(j,l);
end
end
end
end

```

---

end

## constraints

F = [];

$$\tilde{\rho}_\lambda \geq 0, \forall \lambda$$

```
for i = 1:2
for j = 1:2
for k = 1:2
    F = [F, rho_lambda{i,j,k}>=0];
end
end
end
```

$$\tilde{\chi}_{\mathcal{E}_c} \geq 0$$

F = [F, chi\_Ec >= 0];

$$\text{tr}(\tilde{\rho}_{c|v_{0m}}) = \text{tr}(\tilde{\rho}_{c|v_{1m}}), \quad \forall m$$

```
F =
[F,trace(rho_lambda{1,1,1}+rho_lambda{1,1,2}+rho_lambda{1,2,1}+rho_lambda{1,2,2})]
F =
[F,trace(rho_lambda{1,1,1}+rho_lambda{1,1,2}+rho_lambda{2,1,1}+rho_lambda{2,1,2})]
F =
[F,trace(rho_lambda{1,1,1}+rho_lambda{1,2,1}+rho_lambda{2,1,1}+rho_lambda{2,2,1})]
```

$$\text{tr}(\tilde{\chi}_{\mathcal{E}_c}) = 1$$

Fc\_t=[F , trace(chi\_Ec) <= 1];

**maximize**  $F_{\mathcal{E}_c} = \max_{\tilde{\chi}_{\mathcal{E}_c}} \text{tr}(\tilde{\chi}_{\mathcal{E}_c} \chi_{\text{RSP}})$

sums=trace(chi\_Ec\*chi\_RSP);

sol=solvesdp(Fc\_t , -1\*sums)

Fc=double(sums);

Fsc=(2\*Fc+1)/3; %convert process fidelity to average state fidelity

*Published with MATLAB® R2020b*