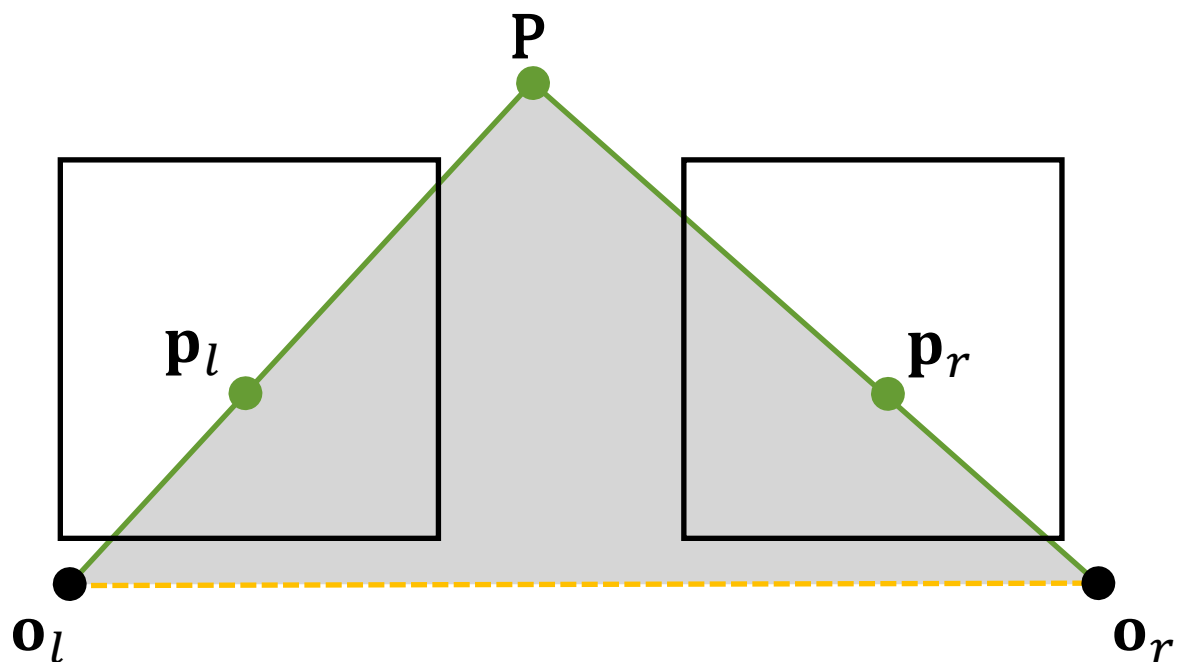


图像矫正



$$\mathbf{R} = \mathbf{I}_{3 \times 3}$$

$$\mathbf{T} = (B, 0, 0)^T$$

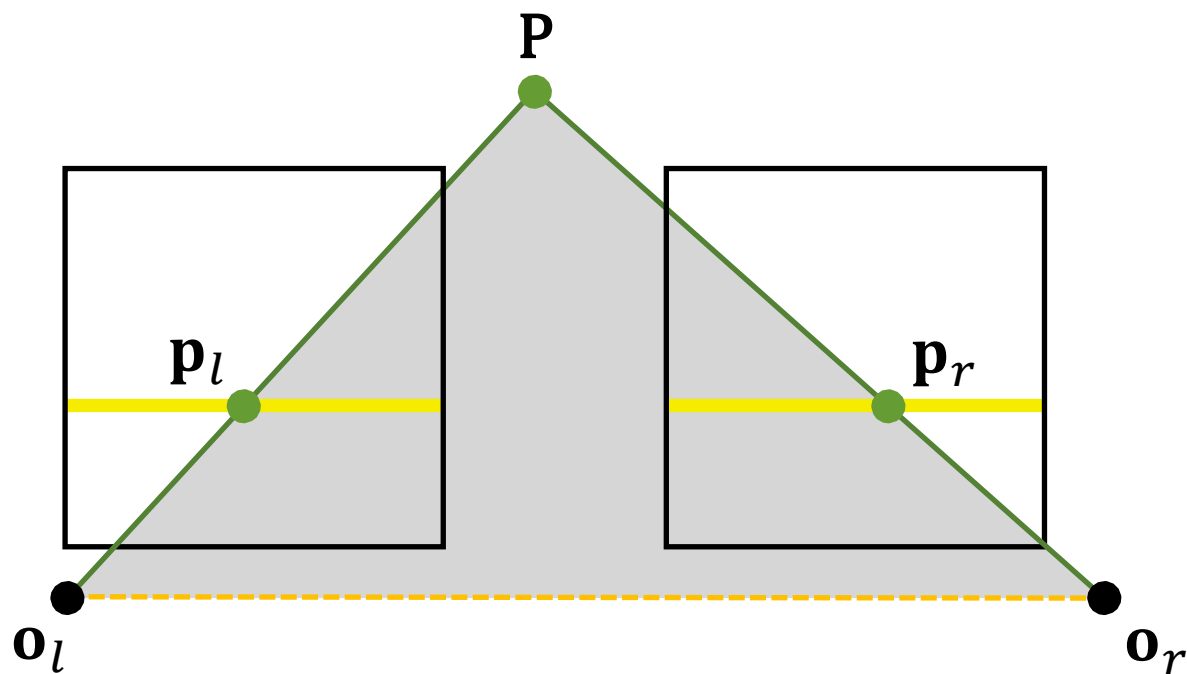
$$\mathbf{p}_r^T \mathbf{E} \mathbf{p}_l = 0$$

$$(x_r, y_r, 1) [\mathbf{T}_\times] (x_l, y_l, 1)^T = 0$$

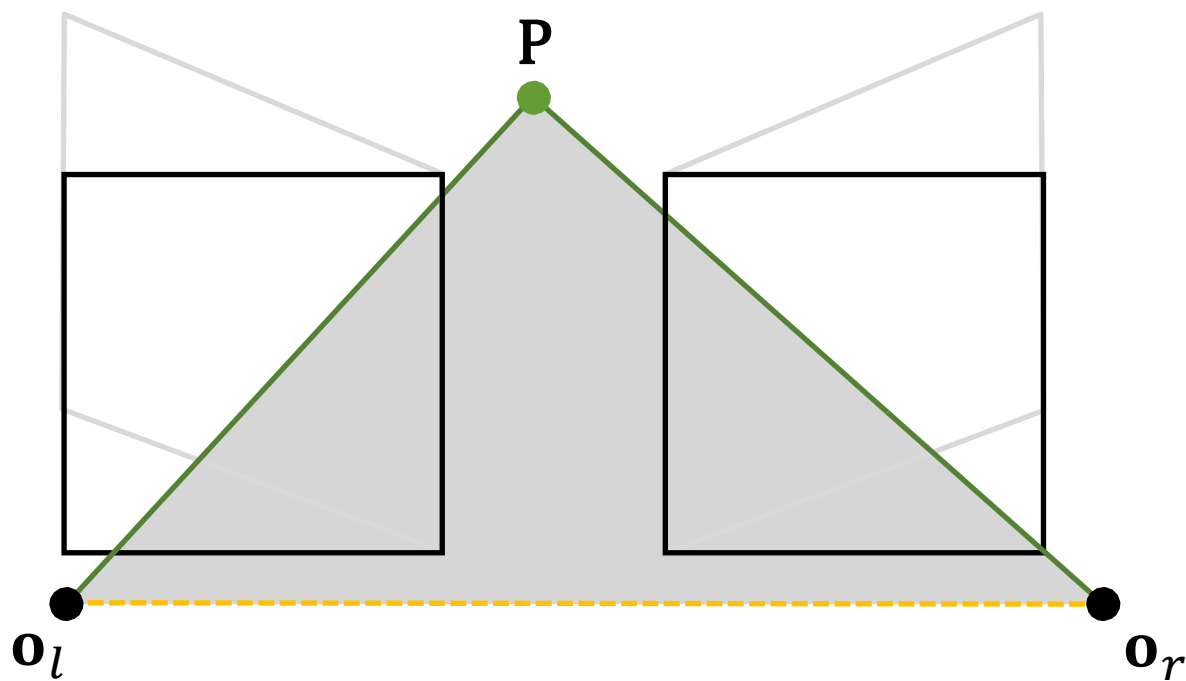
展开并化简

$$y_r = y_l$$

对应点位于同一条水平直线上



平行的像平面可以简化立体匹配问题



将图像重投影到与基线平行的公共平面上

对每幅图像应用单应变换

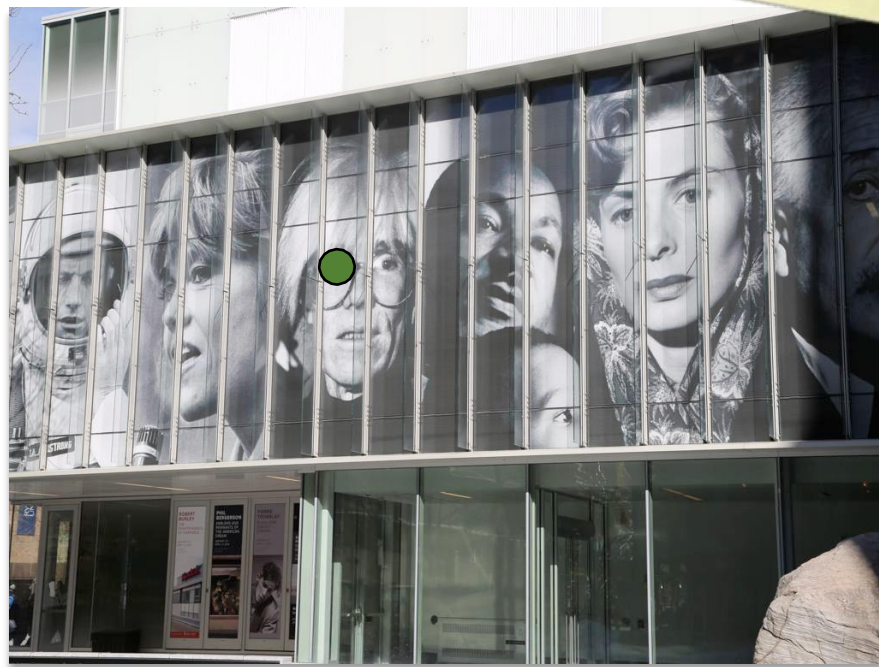
原始
图像对



原始
图像对



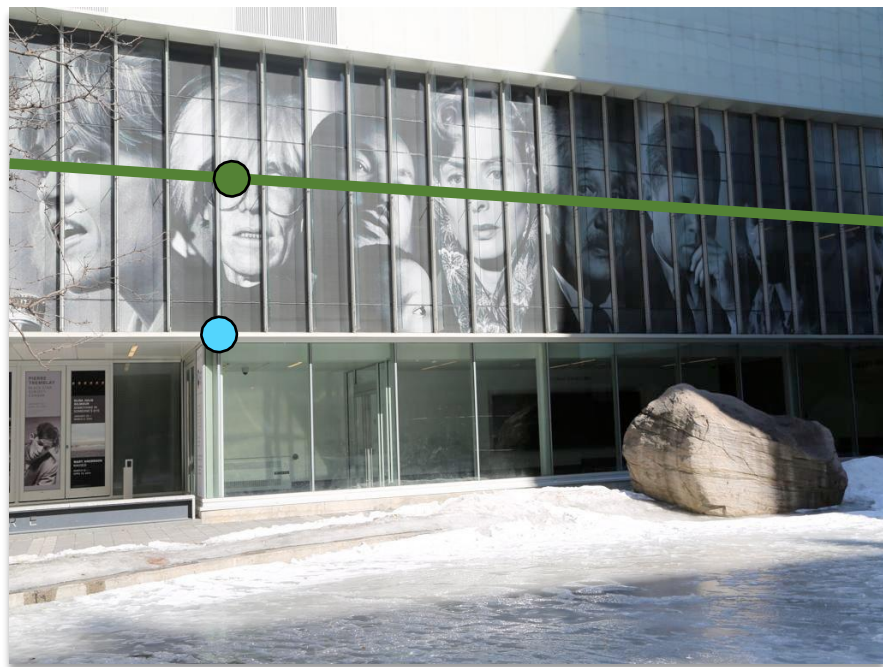
原始
图像对



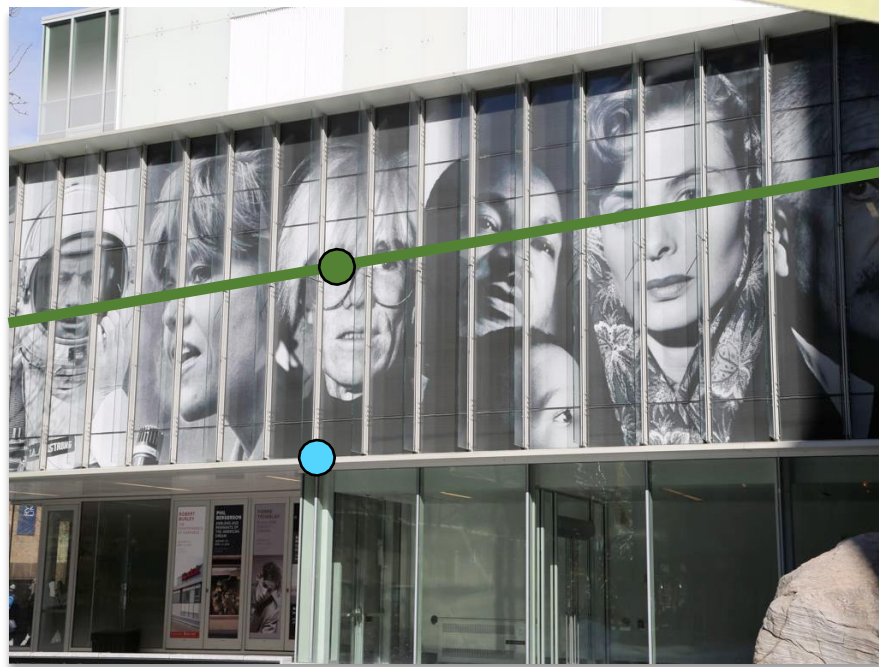
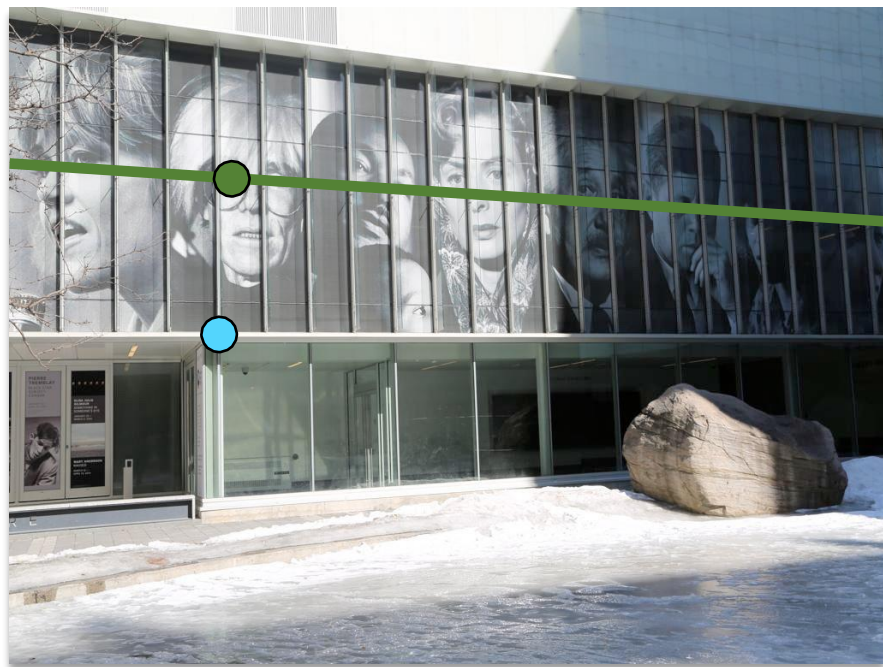
原始
图像对



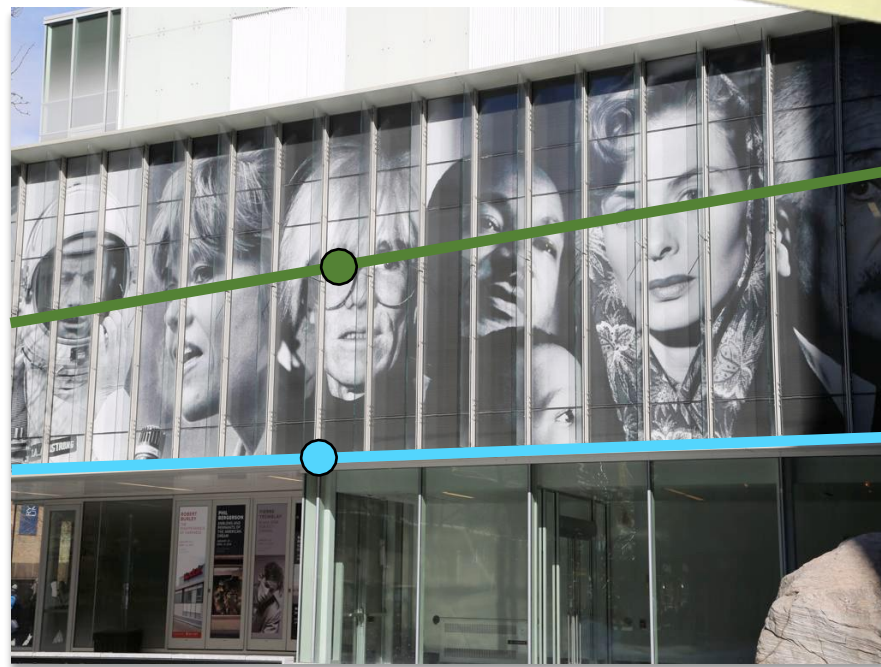
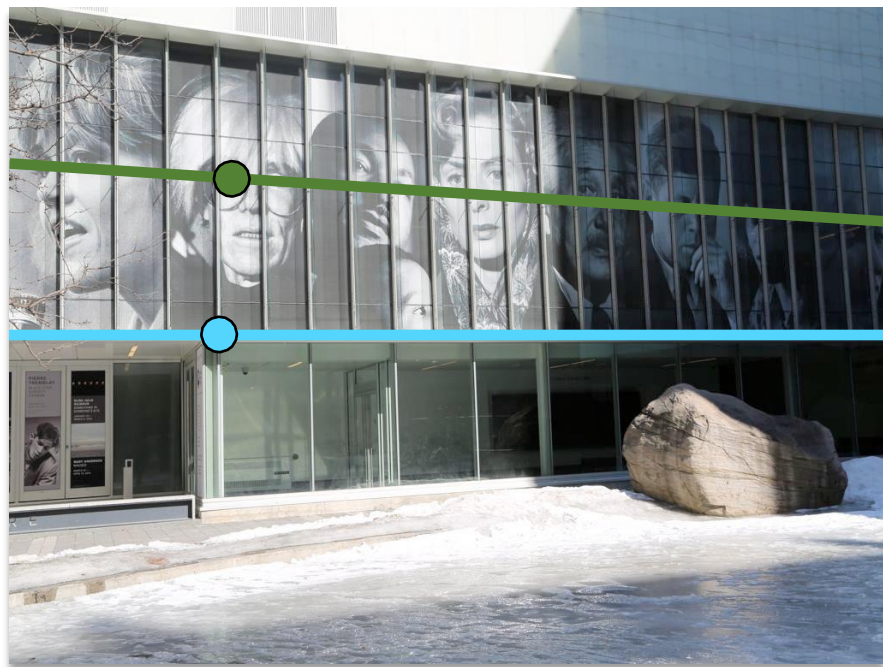
原始
图像对



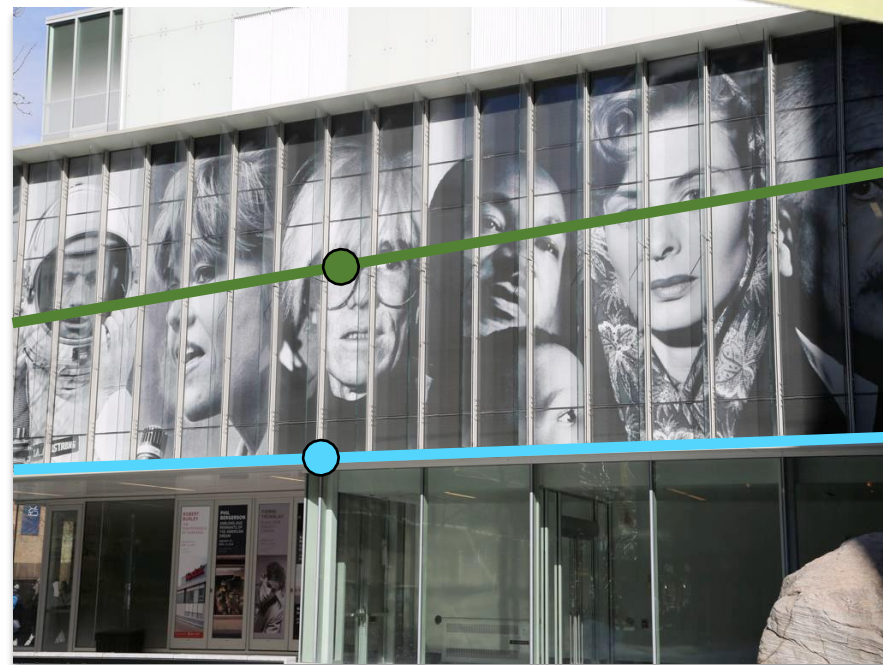
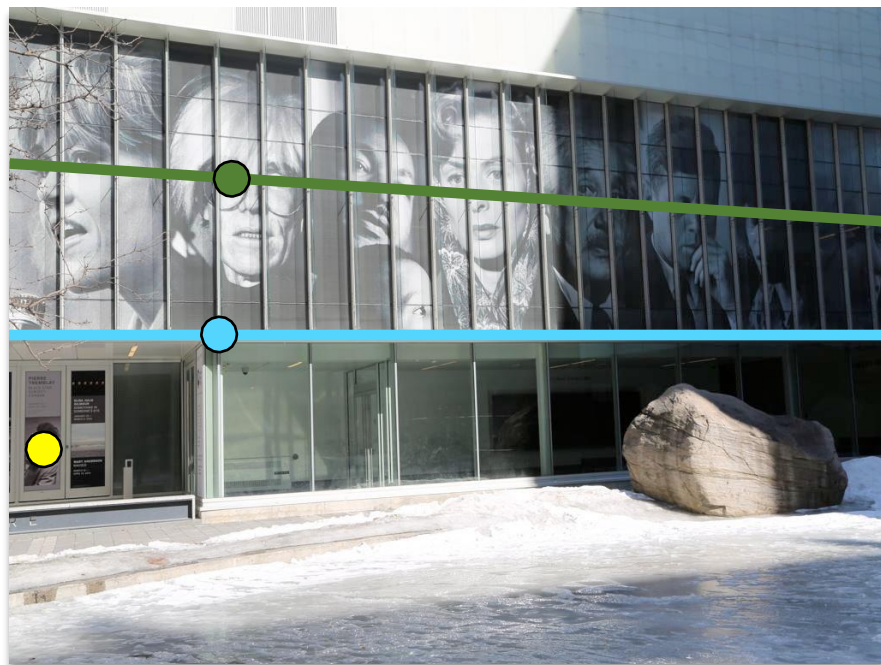
原始
图像对



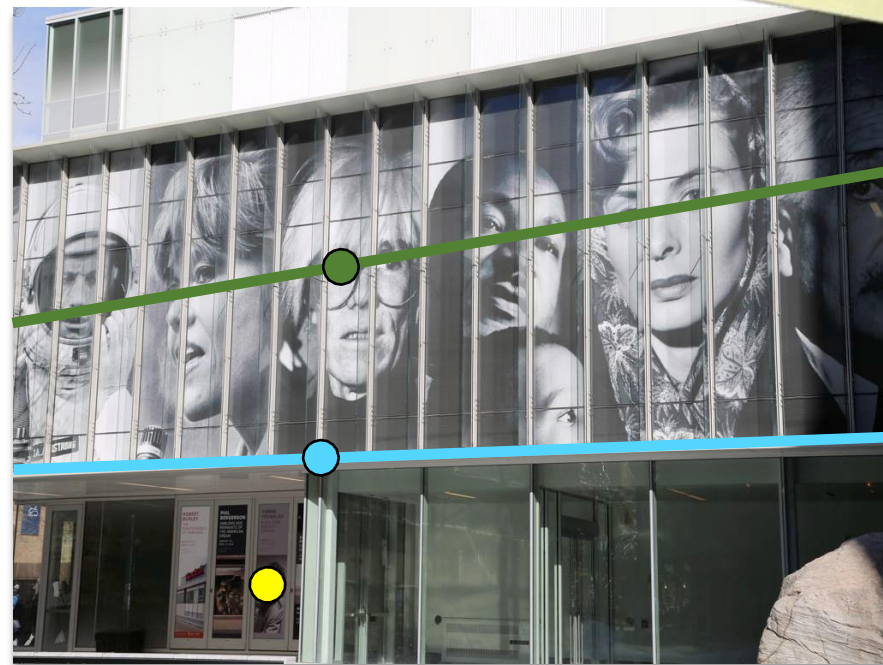
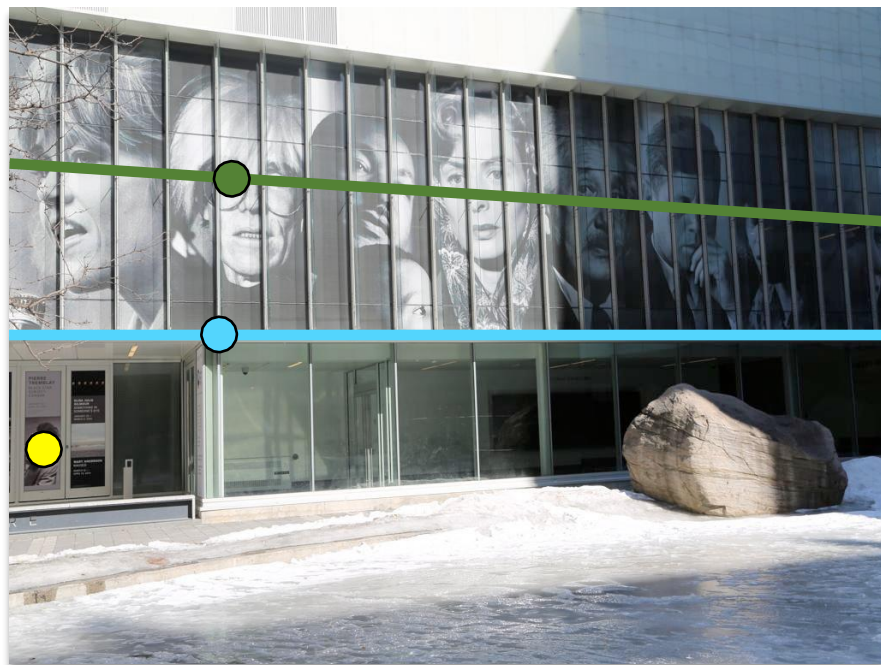
原始
图像对



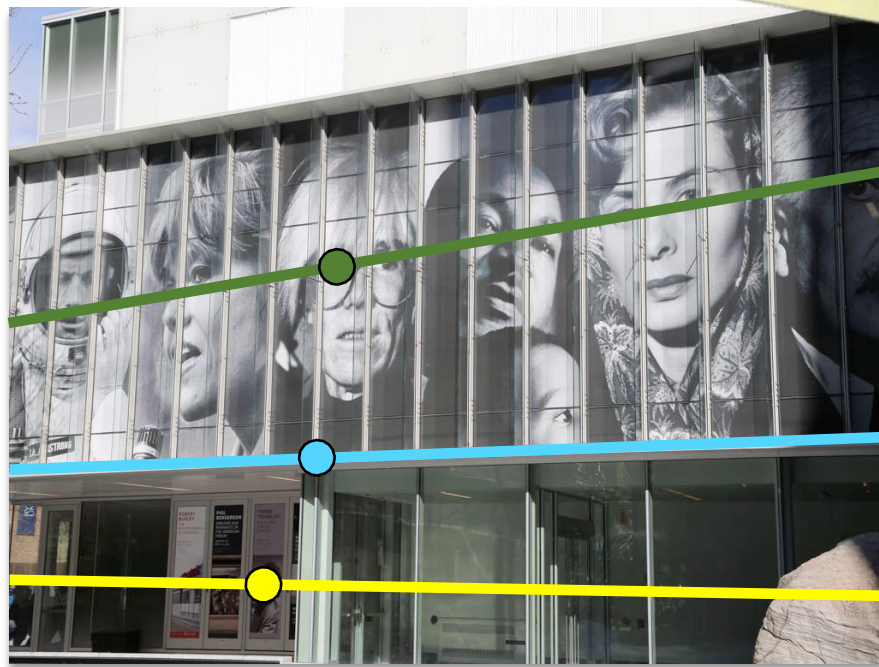
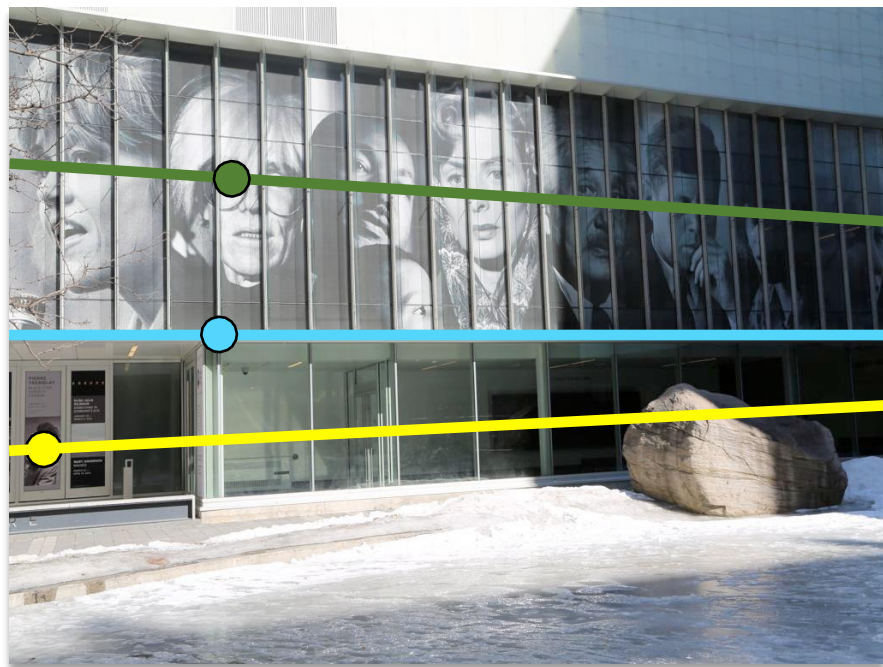
原始
图像对



原始
图像对



原始
图像对



矫正后
图像对

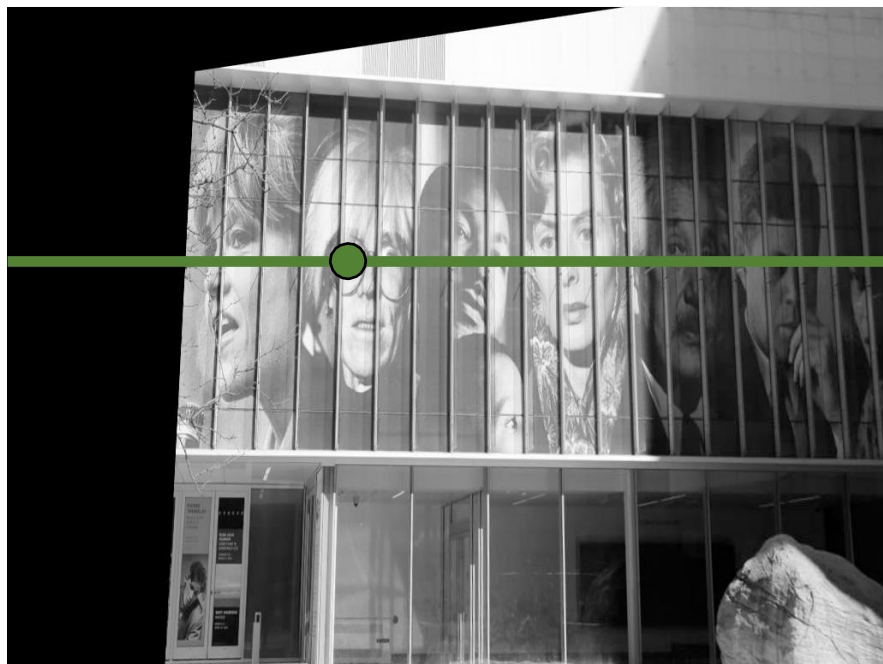


矫正后
图像对



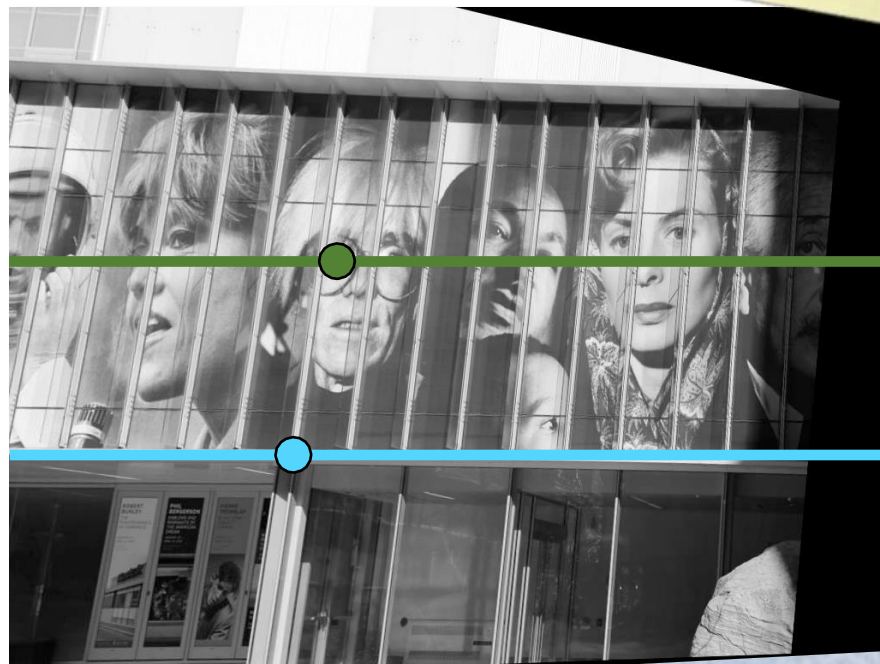
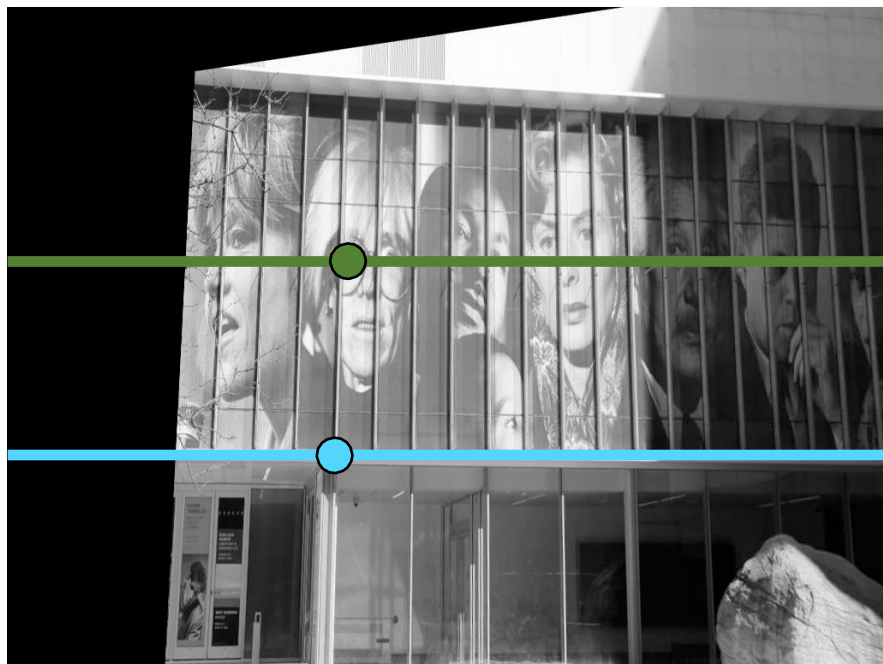
对应点在**同一条扫描线**上

矫正后
图像对



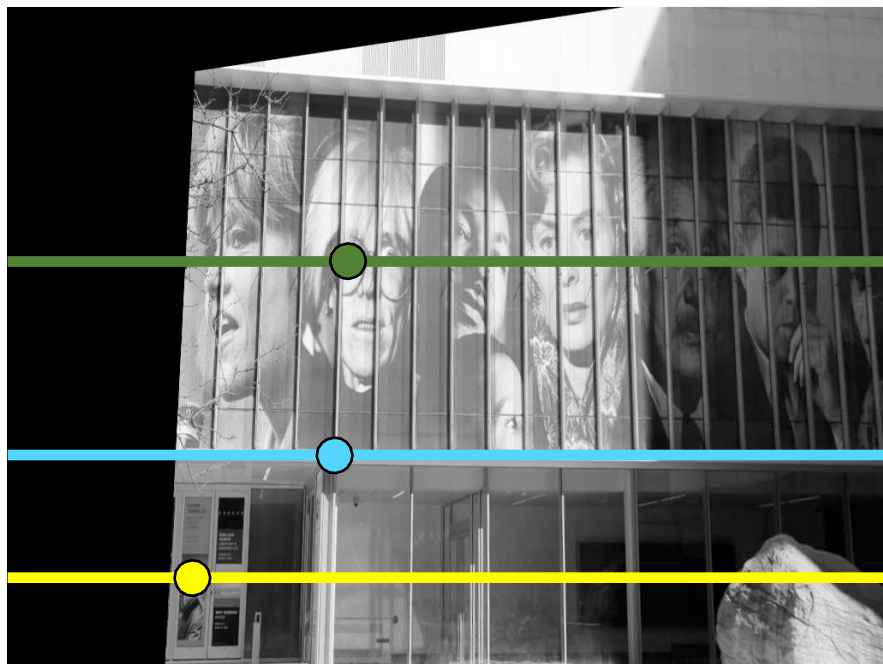
对应点在**同一条扫描线**上

矫正后
图像对



对应点在**同一条扫描线**上

矫正后
图像对



对应点在**同一条扫描线**上

Python时间

图像矫正

Load stereo image pair and convert to grayscale

```
I1 = cv2.imread('left.png', cv2.IMREAD_GRAYSCALE)
```

```
I2 = cv2.imread('right.png', cv2.IMREAD_GRAYSCALE)
```

Find the keypoints and descriptors with SIFT

```
sift = cv2.SIFT_create()
```

```
kp1, des1 = sift.detectAndCompute(I1, None)
```

```
kp2, des2 = sift.detectAndCompute(I2, None)
```

Visualize keypoints

```
I1_sift = cv2.drawKeypoints(I1, kp1, None,  
    flags=cv2.DRAW_MATCHES_FLAGS_DRAW_RICH_KEYPOINTS)
```

```
I2_sift = cv2.drawKeypoints(I2, kp2, None,  
    flags=cv2.DRAW_MATCHES_FLAGS_DRAW_RICH_KEYPOINTS)
```

```
I1_I2_sift = np.concatenate((I1_sift, I2_sift), axis=1)
```

```
cv2.imshow('Image SIFT keypoints', I1_I2_sift)
```

```
# Load stereo image pair and convert to grayscale
```

```
I1 = cv2.imread('left.png', cv2.IMREAD_GRAYSCALE)
```

```
I2 = cv2.imread('right.png', cv2.IMREAD_GRAYSCALE)
```

```
# Find the keypoints and descriptors with SIFT
```

```
sift = cv2.SIFT_create()
```

```
kp1, des1 = sift.detectAndCompute(I1, None)
```

```
kp2, des2 = sift.detectAndCompute(I2, None)
```

```
# Visualize keypoints
```

```
I1_sift = cv2.drawKeypoints(I1, kp1, None,  
    flags=cv2.DRAW_MATCHES_FLAGS_DRAW_RICH_KEYPOINTS)
```

```
I2_sift = cv2.drawKeypoints(I2, kp2, None,  
    flags=cv2.DRAW_MATCHES_FLAGS_DRAW_RICH_KEYPOINTS)
```

```
I1_I2_sift = np.concatenate((I1_sift, I2_sift), axis=1)
```

```
cv2.imshow('Image SIFT keypoints', I1_I2_sift)
```

```
# Load stereo image pair and convert to grayscale
```

```
I1 = cv2.imread('left.png', cv2.IMREAD_GRAYSCALE)
```

```
I2 = cv2.imread('right.png', cv2.IMREAD_GRAYSCALE)
```

```
# Find the keypoints and descriptors with SIFT
```

```
sift = cv2.SIFT_create()
```

```
kp1, des1 = sift.detectAndCompute(I1, None)
```

```
kp2, des2 = sift.detectAndCompute(I2, None)
```

```
# Visualize keypoints
```

```
I1_sift = cv2.drawKeypoints(I1, kp1, None,  
    flags=cv2.DRAW_MATCHES_FLAGS_DRAW_RICH_KEYPOINTS)
```

```
I2_sift = cv2.drawKeypoints(I2, kp2, None,  
    flags=cv2.DRAW_MATCHES_FLAGS_DRAW_RICH_KEYPOINTS)
```

```
I1_I2_sift = np.concatenate((I1_sift, I2_sift), axis=1)
```

```
cv2.imshow('Image SIFT keypoints', I1_I2_sift)
```

```
# Load stereo image pair and convert to grayscale
```

```
I1 = cv2.imread('left.png', cv2.IMREAD_GRAYSCALE)
```

```
I2 = cv2.imread('right.png', cv2.IMREAD_GRAYSCALE)
```

```
# Find the keypoints and descriptors with SIFT
```

```
sift = cv2.SIFT_create()
```

```
kp1, des1 = sift.detectAndCompute(I1, None)
```

```
kp2, des2 = sift.detectAndCompute(I2, None)
```

关键点

```
# visualize keypoints
```

```
I1_sift = cv2.drawKeypoints(I1, kp1, None,  
    flags=cv2.DRAW_MATCHES_FLAGS_DRAW_RICH_KEYPOINTS)
```

```
I2_sift = cv2.drawKeypoints(I2, kp2, None,  
    flags=cv2.DRAW_MATCHES_FLAGS_DRAW_RICH_KEYPOINTS)
```

```
I1_I2_sift = np.concatenate((I1_sift, I2_sift), axis=1)
```

```
cv2.imshow('Image SIFT keypoints', I1_I2_sift)
```



```
# Load stereo image pair and convert to grayscale
```

```
I1 = cv2.imread('left.png', cv2.IMREAD_GRAYSCALE)
```

```
I2 = cv2.imread('right.png', cv2.IMREAD_GRAYSCALE)
```

```
# Find the keypoints and descriptors with SIFT
```

```
sift = cv2.SIFT_create()
```

```
kp1, des1 = sift.detectAndCompute(I1, None)
```

```
kp2, des2 = sift.detectAndCompute(I2, None)
```

特征描述子

```
# Visualize keypoints
```

```
I1_sift = cv2.drawKeypoints(I1, kp1, None,  
    flags=cv2.DRAW_MATCHES_FLAGS_DRAW_RICH_KEYPOINTS)
```

```
I2_sift = cv2.drawKeypoints(I2, kp2, None,  
    flags=cv2.DRAW_MATCHES_FLAGS_DRAW_RICH_KEYPOINTS)
```

```
I1_I2_sift = np.concatenate((I1_sift, I2_sift), axis=1)
```

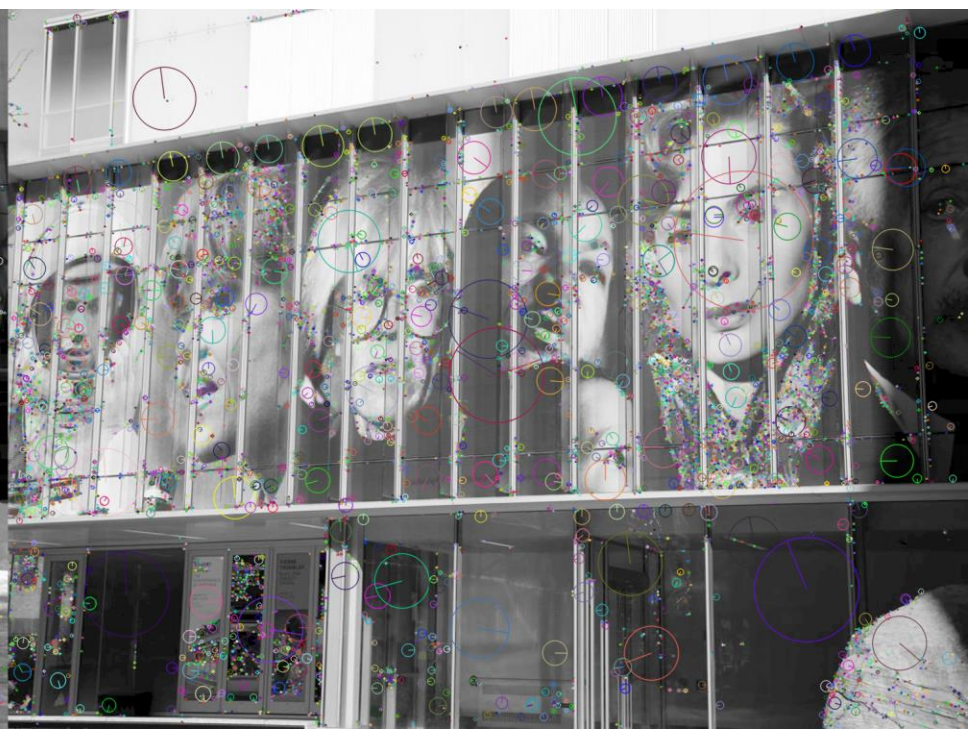
```
cv2.imshow('Image SIFT keypoints', I1_I2_sift)
```

```
# Load stereo image pair and convert to grayscale
I1 = cv2.imread('left.png', cv2.IMREAD_GRAYSCALE)
I2 = cv2.imread('right.png', cv2.IMREAD_GRAYSCALE)
```

```
# Find the keypoints and descriptors with SIFT
sift = cv2.SIFT_create()
kp1, des1 = sift.detectAndCompute(I1, None)
kp2, des2 = sift.detectAndCompute(I2, None)
```

```
# Visualize keypoints
```

```
I1_sift = cv2.drawKeypoints(I1, kp1, None,
    flags=cv2.DRAW_MATCHES_FLAGS_DRAW_RICH_KEYPOINTS)
I2_sift = cv2.drawKeypoints(I2, kp2, None,
    flags=cv2.DRAW_MATCHES_FLAGS_DRAW_RICH_KEYPOINTS)
I1_I2_sift = np.concatenate((I1_sift, I2_sift), axis=1)
cv2.imshow('Image SIFT keypoints', I1_I2_sift)
```



寻找
对应点

```
# Match keypoints in both images
```

```
FLANN_INDEX_KDTREE = 1
```

```
index_params = dict(algorithm=FLANN_INDEX_KDTREE, trees=10)
```

```
flann = cv2.FlannBasedMatcher(index_params, {})
```

```
matches = flann.knnMatch(des1, des2, k=2)
```

```
# Keep good matches: calculate distinctive image features
```

```
good, pts1, pts2 = [], [], []
```

```
for i, (m, n) in enumerate(matches):
```

```
    if m.distance < 0.7 * n.distance:
```

```
        good.append([m])
```

```
        pts1.append(kp1[m.queryIdx].pt)
```

```
        pts2.append(kp2[m.trainIdx].pt)
```

```
keypoint_matches = cv2.drawMatchesKnn(I1, kp1, I2, kp2, good, None,  
    flags=cv2.DRAW_MATCHES_FLAGS_NOT_DRAW_SINGLE_POINTS)
```

```
cv2.imshow('Keypoint matches', keypoint_matches)
```

```
# Match keypoints in both images
```

```
FLANN_INDEX_KDTREE = 1
```

```
index_params = dict(algorithm=FLANN_INDEX_KDTREE, trees=5)
```

```
flann = cv2.FlannBasedMatcher(index_params, {})
```

```
matches = flann.knnMatch(des1, des2, k=2)
```

```
# Keep good matches: calculate distinctive image features
```

```
good, pts1, pts2 = [], [], []
```

```
for i, (m, n) in enumerate(matches):
```

```
    if m.distance < 0.7 * n.distance:
```

```
        good.append([m])
```

```
        pts1.append(kp1[m.queryIdx].pt)
```

```
        pts2.append(kp2[m.trainIdx].pt)
```

```
keypoint_matches = cv2.drawMatchesKnn(I1, kp1, I2, kp2, good, None,  
    flags=cv2.DRAW_MATCHES_FLAGS_NOT_DRAW_SINGLE_POINTS)
```

```
cv2.imshow('Keypoint matches', keypoint_matches)
```

```
# Match keypoints in both images
```

```
FLANN_INDEX_KDTREE = 1
```

```
index_params = dict(algorithm=FLANN_INDEX_KDTREE, trees=5)
```

```
flann = cv2.FlannBasedMatcher(index_params, {})
```

```
matches = flann.knnMatch(des1, des2, k=2)
```

```
# Keep good matches: calculate distinctive image features
```

```
good, pts1, pts2 = [], [], []
```

```
for i, (m, n) in enumerate(matches):
```

```
    if m.distance < 0.7 * n.distance:
```

```
        good.append([m])
```

```
        pts1.append(kp1[m.queryIdx].pt)
```

```
        pts2.append(kp2[m.trainIdx].pt)
```

```
keypoint_matches = cv2.drawMatchesKnn(I1, kp1, I2, kp2, good, None,  
    flags=cv2.DRAW_MATCHES_FLAGS_NOT_DRAW_SINGLE_POINTS)
```

```
cv2.imshow('Keypoint matches', keypoint_matches)
```



```
# Match keypoints in both images
```

```
FLANN_INDEX_KDTREE = 1
```

```
index_params = dict(algorithm=FLANN_INDEX_KDTREE, trees=5)
```

```
flann = cv2.FlannBasedMatcher(index_params, {})
```

```
matches = flann.knnMatch(des1, des2, k=2)
```

```
# Keep good matches: calculate distinctive image features
```

```
good, pts1, pts2 = [], [], []
```

```
for i, (m, n) in enumerate(matches):
```

```
    if m.distance < 0.7 * n.distance:
```

```
        good.append([m])
```

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        pts1.append(kp1[m.queryIdx].pt)
```

```
        pts2.append(kp2[m.trainIdx].pt)
```

```
keypoint_matches = cv2.drawMatchesKnn(I1, kp1, I2, kp2, good, None,  
    flags=cv2.DRAW_MATCHES_FLAGS_NOT_DRAW_SINGLE_POINTS)
```

```
cv2.imshow('Keypoint matches', keypoint_matches)
```

```
# Match keypoints in both images
```

```
FLANN_INDEX_KDTREE = 1
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index_params = dict(algorithm=FLANN_INDEX_KDTREE, trees=5)
```

```
flann = cv2.FlannBasedMatcher(index_params, {})
```

```
matches = flann.knnMatch(des1, des2, k=2)
```

```
# Keep good matches: calculate distinctive image features
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good, pts1, pts2 = [], [], []
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```
for i, (m, n) in enumerate(matches):
```

```
    if m.distance < 0.7 * n.distance:
```

```
        good.append([m])
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        pts1.append(kp1[m.queryIdx].pt)
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```
keypoint_matches = cv2.drawMatchesKnn(I1, kp1, I2, kp2, good, None,  
    flags=cv2.DRAW_MATCHES_FLAGS_NOT_DRAW_SINGLE_POINTS)
```

```
cv2.imshow('Keypoint matches', keypoint_matches)
```

Match keypoints in both images

FLANN_INDEX_KDTREE = 1

index_params = dict(algorithm=FLANN_INDEX_KDTREE, trees=5)

flann = cv2.FlannBasedMatcher(index_params, {})

matches = flann.knnMatch(des1, des2, k=2)

Keep good matches: calculate distinctive image features

good, pts1, pts2 = [], [], []

for i, (m, n) in enumerate(matches):

if m.distance < 0.7 * n.distance:

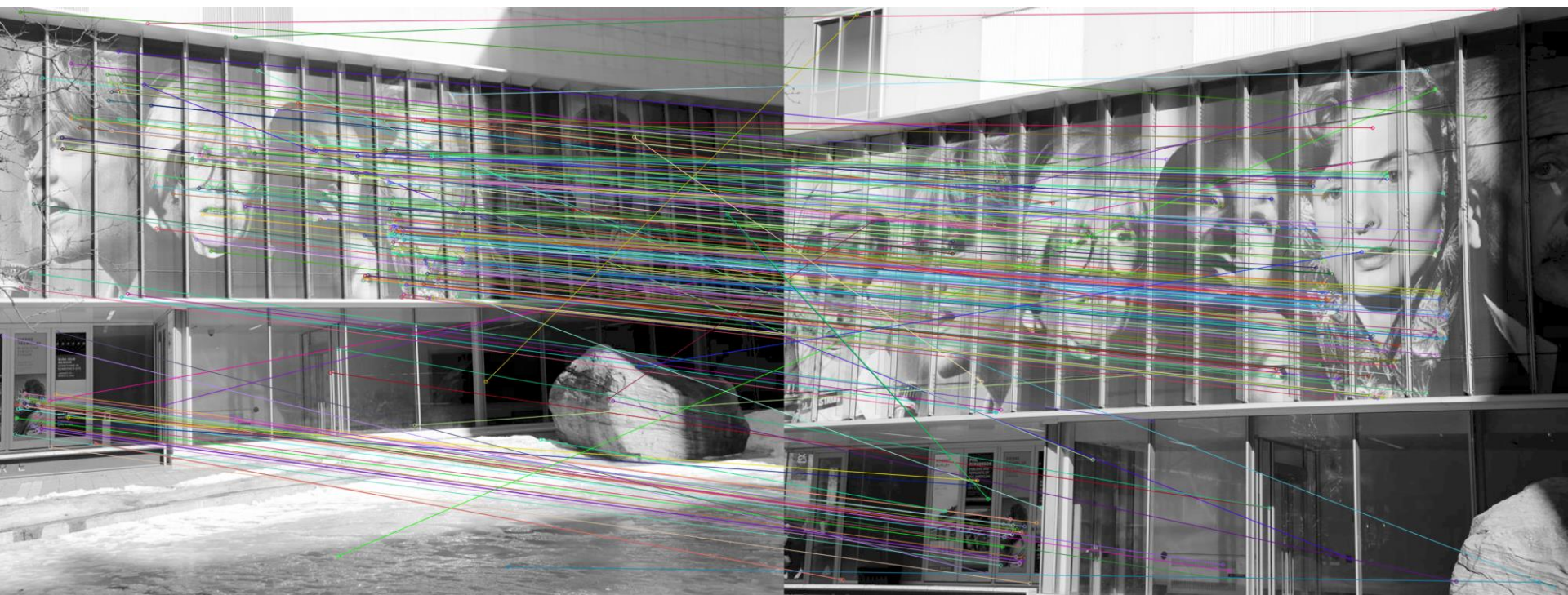
good.append([m])

pts1.append(kp1[m.queryIdx].pt)

pts2.append(kp2[m.trainIdx].pt)

keypoint_matches = cv2.drawMatchesKnn(I1, kp1, I2, kp2, good, None,
 flags=cv2.DRAW_MATCHES_FLAGS_NOT_DRAW_SINGLE_POINTS)

cv2.imshow('Keypoint matches', keypoint_matches)



Calculate the fundamental matrix for the cameras

```
pts1 = np.float32(pts1)
```

```
pts2 = np.float32(pts2)
```

```
fundamental_matrix, inliers = cv2.findFundamentalMat(  
    pts1, pts2, cv2.FM_RANSAC,  
    ransacReprojThreshold=0.9, confidence=0.99  
)
```

Select only inlier points

```
pts1 = pts1[inliers.ravel() == 1]
```

```
pts2 = pts2[inliers.ravel() == 1]
```

计算
基础矩阵

Calculate the fundamental matrix for the cameras

```
pts1 = np.float32(pts1)
```

```
pts2 = np.float32(pts2)
```

```
fundamental_matrix, inliers = cv2.findFundamentalMat(  
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Select only inlier points

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pts1 = pts1[inliers.ravel() == 1]
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pts2 = pts2[inliers.ravel() == 1]
```

```
# Calculate the fundamental matrix for the cameras
```

```
pts1 = np.float32(pts1)
```

```
pts2 = np.float32(pts2)
```

```
fundamental_matrix, inliers = cv2.findFundamentalMat(  
    pts1, pts2, cv2.FM_RANSAC,  
    ransacReprojThreshold=0.9, confidence=0.99  
)
```

```
# Select only inlier points
```

```
pts1 = pts1[inliers.ravel() == 1]
```

```
pts2 = pts2[inliers.ravel() == 1]
```



```
# Calculate the fundamental matrix for the cameras
```

```
pts1 = np.float32(pts1)
```

```
pts2 = np.float32(pts2)
```

```
fundamental_matrix, inliers = cv2.findFundamentalMat(  
    pts1, pts2, cv2.FM_RANSAC,  
    ransacReprojThreshold=0.9, confidence=0.99  
)
```

```
# Select only inlier points
```

```
pts1 = pts1[inliers.ravel() == 1]
```

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```

```
# Calculate the fundamental matrix for the cameras
```

```
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```

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```

```
fundamental_matrix, inliers = cv2.findFundamentalMat(  
    pts1, pts2, cv2.FM_RANSAC,  
    ransacReprojThreshold=0.9, confidence=0.99  
)
```

```
# Select only inlier points
```

```
pts1 = pts1[inliers.ravel() == 1]
```

```
pts2 = pts2[inliers.ravel() == 1]
```

Stereo rectification (uncalibrated variant)

h1, w1 = img1.shape

h2, w2 = img2.shape

_, H1, H2 = cv2.stereoRectifyUncalibrated(
 pts1, pts2, fundamental_matrix, imgSize=(w1, h1)
)

Rectify the images

I1_rect = cv2.warpPerspective(I1, H1, (w1, h1))

I2_rect = cv2.warpPerspective(I2, H2, (w2, h2))

Visualize rectified images

I1_I2_rect = np.concatenate((I1_rect, I2_rect), axis=1)

cv2.imshow('Rectified images', I1_I2_rect), cv2.waitKey(0)

矫正图像

```
# Stereo rectification (uncalibrated variant)
```

```
h1, w1 = img1.shape
```

```
h2, w2 = img2.shape
```

```
_, H1, H2 = cv2.stereoRectifyUncalibrated(  
    pts1, pts2, fundamental_matrix, imgSize=(w1, h1)  
)
```

```
# Rectify the images
```

```
I1_rect = cv2.warpPerspective(I1, H1, (w1, h1))
```

```
I2_rect = cv2.warpPerspective(I2, H2, (w2, h2))
```

```
# Visualize rectified images
```

```
I1_I2_rect = np.concatenate((I1_rect, I2_rect), axis=1)
```

```
cv2.imshow('Rectified images', I1_I2_rect), cv2.waitKey(0)
```



```
# Stereo rectification (uncalibrated variant)
```

```
h1, w1 = img1.shape
```

```
h2, w2 = img2.shape
```

```
_, H1, H2 = cv2.stereoRectifyUncalibrated(  
    pts1, pts2, fundamental_matrix, imgSize=(w1, h1)  
)
```

```
# Rectify the images
```

```
I1_rect = cv2.warpPerspective(I1, H1, (w1, h1))
```

```
I2_rect = cv2.warpPerspective(I2, H2, (w2, h2))
```

```
# Visualize rectified images
```

```
I1_I2_rect = np.concatenate((I1_rect, I2_rect), axis=1)
```

```
cv2.imshow('Rectified images', I1_I2_rect), cv2.waitKey(0)
```

```
# Stereo rectification (uncalibrated variant)
```

```
h1, w1 = img1.shape
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h2, w2 = img2.shape
```

```
_, H1, H2 = cv2.stereoRectifyUncalibrated(  
    pts1, pts2, fundamental_matrix, imgSize=(w1, h1)  
)
```

```
# Rectify the images
```

```
I1_rect = cv2.warpPerspective(I1, H1, (w1, h1))
```

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I2_rect = cv2.warpPerspective(I2, H2, (w2, h2))
```

```
# Visualize rectified images
```

```
I1_I2_rect = np.concatenate((I1_rect, I2_rect), axis=1)
```

```
cv2.imshow('Rectified images', I1_I2_rect), cv2.waitKey(0)
```



