

Genetic Algorithm for Optimization Problems:

→ A Genetic Algorithm is an adaptive heuristic search algorithm inspired by principle of natural selection and genetics. GAs are widely used for solving optimization and search problems.

Population size, mutation rate, crossover rate and number

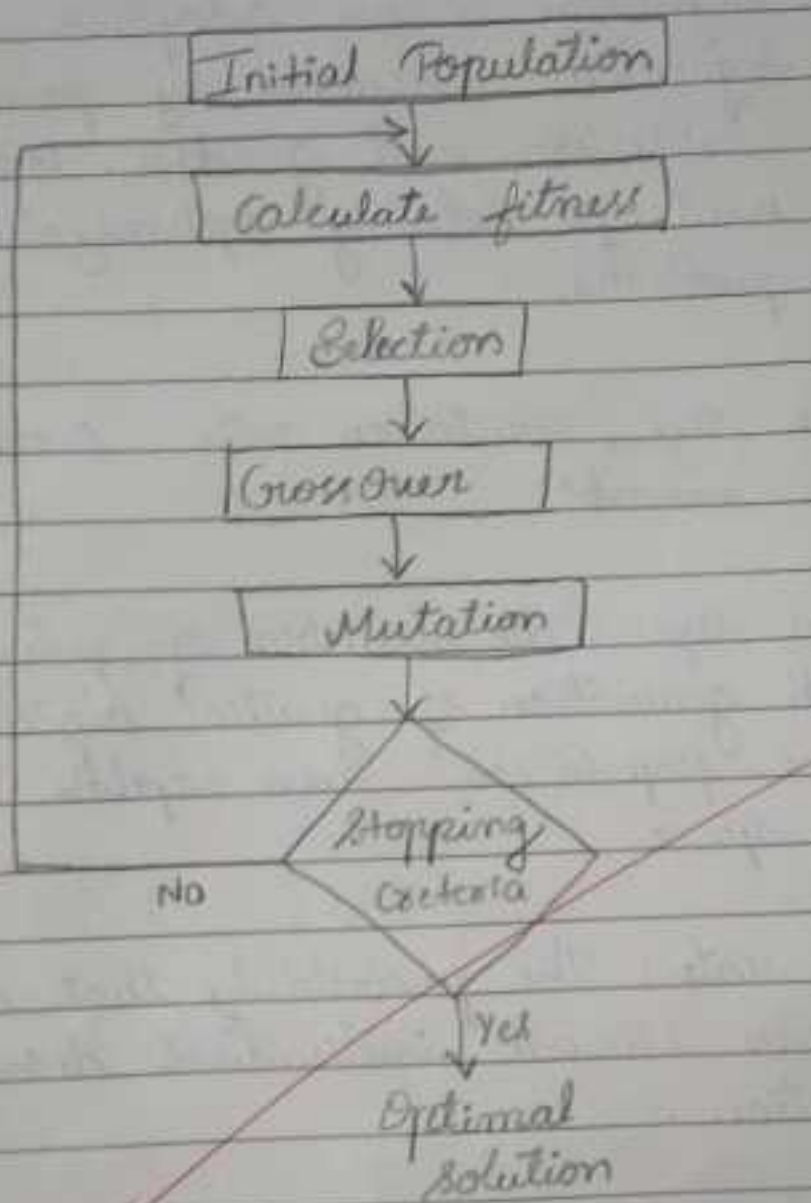
Population Size: The number of potential solutions in each generation of genetic algorithm. A larger population can explore a broader solution space.

Mutation rate: The probability that a mutation will occur in an individual during reproduction.

Crossover Rate: The probability that two parents solution will combine to produce offspring.

The best performing solution are selected to reproduce combining their attributes through crossover and mutation. Crossover mixes part of two parents solution to create offsprings, while mutation introduce random changes to promote diversity. This cycle of selection, reproduction and evaluation continues for multiple generations to generations.

The population tends to evolve towards better solution



8/19/24

[Genetic] Algorithm:

Step 1: Initialize Parameter: Set the population size, mutation rate, crossover rate, & number of generation.

Step 2: Generate Initial Population: Create a random population of potential solutions within given bounds.

Step 3: Evaluate Fitness: Calculate the fitness of each individual in the population by evaluating objective function.

Step 4: Select Parents: Select the fittest individuals from population to reproduce, based on their fitness.

Step 5: Crossover: Perform crossover between the selected parents to create new offspring, with a probability equal to the crossover rate.

Step 6: Mutate: Apply mutation to offspring, with a probability equal to the mutation rate, to introduce new traits.

Step 7: Replace Least Fit: Replace the least fit individuals in population with new offspring.

Step 8: Repeat: Repeat step 3-7 for a fixed no. of generations or until convergence criteria are met.

Step 9: Output Best Solution: Return the best solution found during the generations, which is the individual with highest fitness.

Applications of Genetic Algorithm:

- (i) Optimization problems: Finding the best solution to a problem under certain constraints ex. maximizing profit, minimum cost.
- (ii) Function maximization/minimization: GAs can be used to find maxima & minima of complex mathematical functions.
- (iii) Scheduling problems: GAs are useful in resource allocation, task scheduling problems.
- (iv) Machine learning & AI: GAs are sometimes used for optimizing hyperparameters in machine learning models.
- (v) Engineering design: GAs help in optimization design for efficiency, such as structures, circuits & aerodynamics.
- (vi) Robotics & control system: GAs can help in designing robots / optimizing control parameters for efficient performance.

Optimizing Techniques

- * Selection: Selecting the fittest individuals from population to reproduce.
- * Crossover: Combining the genetic information of two parents to create a new offspring.
- * Mutation: Randomly changing genetic information of an individual to introduce new traits.
- * Elitism: Preserving the best solution from previous generation to ensure that best solutions are not lost.
- * Tournament Selection: Selecting the fittest individuals having a higher chance of being selected from a subset of population to reproduce.
- * Roulette wheel selection: Selecting individuals based on their fitness, with higher fitness individual having a higher chance of being selected.
- * Simulated binary crossover: A crossover technique that simulates the process of binary crossover to create new offspring.

8/3/10/24

Implement the Genetic Algorithm

```
import random
import numpy as np
```

```
def objective_function(x):
    return x**2 + 2*x + 1
```

```
def generate_initial_population(population_size,
                                bounds):
```

```
    population = []
```

```
    for i in range(population_size):
```

```
        x = random.uniform(bounds[0], bounds[1])
```

```
        population.append(x)
```

```
    return population
```

```
def evaluate_fitness(population):
```

```
    fitness = []
```

```
    for x in population:
```

```
        fitness.append(objective_function(x))
```

```
    return fitness
```

```
def selection(population, fitness, num_parents):
```

```
    parents = []
```

```
    for i in range(num_parents):
```

```
        max_fitness_idx = np.argmax(fitness)
```

```
        parents.append(population[max_fitness_idx])
```

```
        fitness[max_fitness_idx] = -float("inf")
```

```
    return parents
```

```
def crossover(parents, crossover_rate):
```

```
    offspring = []
```

```
    for i in range(len(parents) // 2):
```

```
        parent1, parent2 = random.sample(parents, 2)
```

- to 2)


```

def mutation(offspring, mutation_rate, bounds):
    for i in range(len(offspring)):
        if random.random() < mutation_rate:
            offspring[i] += random.uniform(-0.1,
            0.1) * (bounds[i] - bounds[0])
            offspring[i] = max(bounds[0], min(offp-
            ring[i], bounds[i]))
    return offspring

```

```

def genetic_algorithm(population_size, mutation_size,
    crossover_rate, num_generations, bounds):
    population = generate_initial_population(popul-
    ation_size, bounds)
    for generation in range(num_generations):
        fitness = evaluate_fitness(population)
        parent = selection(population, fitness,
        population_size // 2)
        offspring = mutation(offspring, mutation-
        rate, bounds)
        offspring = crossover(parents, crossover_rate)
        offspring + population = offspring + parents
        best_solution = min(population, key=objective-
        function)
    return best_solution.

```

population_size = 100
 mutation_rate = 0.01
 crossover_rate = 0.5
 num_generation = 100
 bounds = (-10, 10)

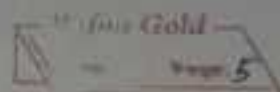
0.26
 3


```
best solution = genetic algorithm (population size,  
bounds, mutation rate, crossover rate, num generation)  
print("Best solution:", best solution)
```

Output:-

Best solution = 9.94691113423836

~~Solve~~
Solve



Practical Exam for Optimization

Pso is an Optimizer

```
import numpy as np
```

```
def SphereFunction(x):  
    return np.sum(x**2)
```

```
class PSO:
```

```
    def __init__(self, func, dim, numparticles=30,  
        max_iter=100, w=0.5, c1=1.5, c2=1.5, bound=  
        (-5.12, 5.12)):
```

```
        self.func = func
```

```
        self.dim = dim
```

```
        self.numparticles = numparticles
```

```
        self.max_iter = max_iter
```

```
        self.w = w
```

```
        self.c1 = c1
```

```
        self.c2 = c2
```

```
        self.bound = bound
```

```
        self.position = np.random.uniform(self.bound[0],  
            self.bound[1], (self.numparticles, self.dim))
```

```
        self.velocities = np.random.uniform(-1, 1, (self.  
            numparticles, self.dim))
```

```
        self.personal_best_position = np.copy(self.position)
```

```
        self.personal_best_score = np.array([self.func(p)  
            for p in self.position])
```

```
        self.global_best_position = self.personal_best_position  
            [np.argmin(self.personal_best_score)]
```

```
        self.global_best_position_score = np.min(self.  
            personal_best_score)
```



```

def update_velocity(self, i):
    r1, r2 = np.random.rand(2)
    cognitive_velocity = self.c1 * r1 * (self.personal_best_position[i] - self.position[i])
    social_velocity = self.c2 * r2 * (self.global_best_position - self.position[i])
    inertia_velocity = self.w * self.velocity[i]
    return inertia_velocity + cognitive_velocity + social_velocity

```

```

def update_position(self, i):
    self.position[i] += self.velocities[i]
    self.position[i] = np.clip(self.position[i], self.bounds[0], self.bounds[1])

```

```

def pso_optimize(self):
    for iteration in range(self.max_iter):
        for i in range(self.num_particles):
            fitness = self.funct(self.position[i])
            if fitness < self.personal_best[i]:
                self.personal_best[i] = fitness
                self.personal_best_position[i] = self.position[i]

```

```

        for i in range(self.num_particles):
            self.velocities[i] = self.update_velocity(i)
            self.update_position(i)

```

```

        print("Iteration < iteration + 1 / self.max_iter")
        BestScore = (self.global_best_score)

```

```

    best_position, best_score = pso_optimize

```

```
print(f"Optimal sol: {best_position}")
print(f"Optimal score (objective value): {best_score}
      {best_index}")
```

Q. output:-

Optimal solution: $(0.0010113, -0.00101066)$
 optimal score: 2.05903216466

[Signature]
 07-11-22

Ant Colony Optimization for Travelling
Salesman problem

```
import numpy as np
import random
import math
```

```
city cities = [(0,0), (1,2), (2,4), (5,6), (7,8), (8,0)]
```

```
def euclidean_distance(city1, city2):
    return math.sqrt((city1[0] - city2[0])**2 +
                      (city1[1] - city2[1])**2)
```

```
num_cities = len(cities)
```

```
distance_matrix = np.zeros((num_cities, num_cities))
for i in range(num_cities):
```

```
    for j in range(i+1, num_cities):
```

```
        dist = euclidean_distance(cities[i], cities[j])
```

```
        distance_matrix[i][j] = dist
```

```
        distance_matrix[j][i] = dist
```

```
num_ants = 10
```

```
iterations = 100
```

```
alpha = 1.0
```

```
beta = 2.0
```

```
rho = 0.5
```

```
tau0 = 1e-4
```

```
pheromone_matrix = np.ones((num_cities,
                             num_cities)) * tau0
```

```

def construct_sol():
    path = [random.randint(0, numcities-1)]
    visited = set(path)

    while len(path) < numcities:
        current_city = path[-1]
        probabilities = []

        for next_city in range(numcities):
            if next_city not in visited:
                pheromone = pheromone_matrix[current_city][next_city]**alpha
                heuristic = (1.0 / distance_matrix[current_city][next_city])**beta
                probabilities.append(pheromone * heuristic)
            else:
                probabilities.append(0)

        total_prob = sum(probabilities)
        probabilities = [p/total_prob for p in probabilities]

        next_city = np.random.choice(range(numcities),
                                     p=probabilities)
        path.append(next_city)
        visited.add(next_city)

    return path

def update_pheromones(all_paths, all_lengths,
                      global_pheromone_matrix):
    pheromone_matrix *= (1-rho)

```



```
for path, length in zip(all_paths, all_lengths):  
    pheromone_deposits = 1.0 / length
```

best_path = None

best_length = float('inf')

```
for iteration in range(iterations):
```

all_paths = []

all_lengths = []

```
for _ in range(num_ants):
```

path = construct_sol()

all_paths.append(path)

all_lengths.append(length)

if length < best_length:

best_length = length

best_path = path

update_pheromones(all_paths, all_lengths)

```
print(f"Iteration {iteration + 1} / {iterations} :  
      best_length = {best_length}")
```

```
print(f"Best path found: ", best_path)
```

```
print(f"Best length: ", best_length)
```

O/P

Iteration 1/3 : Best length = 26.96837

Iteration 2/3 : Best length = 26.96837

Iteration 3/3 : Best length = 26.96837

Best path found: [0, 1, 3, 3, 4, 5]

Best length: 26.96837

Cuckoo Search Algorithm

```
import numpy as np
```

```
def objective_funt(x):  
    return np.sum(x**2)
```

```
def levy_flight(lambda, dim):  
    step = np.random.randn(1, dim) * np.power  
    (np.abs(np.random.randn(1, dim)), 1/  
    lambda)  
    return step
```

```
def cuckoo_search(objective_funt, num_nest=25,  
    max_iter=100, pa=0.25, lambda=1.5, dim=5):  
    nests = np.random.uniform(-10, 10, (num_nests,  
    dim))  
    fitness = np.apply_along_axis(objective_funt, 1, nests)  
    best_nest = nests[np.argmin(fitness)]  
    best_fitness = np.min(fitness)
```

```
    for iteration in range(max_iter):  
        new_nests = np.copy(nests)  
        for i in range(num_nests):  
            step = levy_flight(lambda, dim)  
            new_nests[i] = nests[i] + step  
            new_nests[i] = np.clip(new_nests[i], -10, 10)  
        new_fitness = np.apply_along_axis(objective_funt, 1,  
            new_nests)  
        for i in range(num_nests):
```



```

if (new_fitness[i] < fitness[i]):
    nests[i] = new_nests[i]
    fitness[i] = new_fitness[i]

```

```

for i in range(int(pa * num_nests)):
    random_index = np.random.randint(0,
                                       num_nests)
    nests[random_index] = np.random.uniform
    [-10, 10, dim]
    fitness[random_index] = objective_func(nests
    [random_index])

```

```

current_best = np.min(fitness)
if current_best < best_fitness:
    best_fitness = current_best
    best_nest = nests[np.argmin(fitness)]

```

```

print(f"Iteration {iteration+1} : Best fitness = {best_fitness}")

```

```

return best_nest, best_fitness

```

```

best_sol, best_fitness = cuckoo_bsearch(objective_func)
print("\n Best solution found: ", best_sol)
print("Best fitness value: ", best_fitness)

```

O/p

```

Iteration 1 : Best fitness : 58.03326
Iteration 2 : Best " : 44.467699
Iteration 3 : " : 44.497991
Iteration 4 : " : 36.590403

```

Best solution found: [-1.26757 -0.24478 1.64976 4.67124
3.1715907D

Best fitness value: 36.5904034066528

Grey Wolf Optimizer (GWO):

GWO is nature-inspired optimization algorithm based on hunting behaviour and social hierarchy of grey wolves. The algorithm mimics the roles of wolves in a pack: alpha, beta, delta & Omega.

```
import numpy as np
```

```
def objfun(x):  
    return np.sum(x**2)
```

```
def gwo(no_wolves, no_itera, dim):  
    wolves = np.random.uniform(-10, 10, (no_wolves, dim))
```

```
    alpha_pos = np.zeros(dim)  
    beta_pos = np.zeros(dim)  
    delta_pos = np.zeros(dim)  
    alpha_score = float('inf')  
    beta_score = float('inf')  
    delta_score = float('inf')
```

```
    for i in range(no_itera):  
        for j in range(no_wolves):  
            fitness = objfun(wolves[j])
```

```
            if fitness < alpha_score:  
                delta_score = beta_score  
                delta_pos = beta_pos  
                beta_score = alpha_score
```



```

beta_pos = alpha_pos
alpha_score = fitness
alpha_pos = wolves[i]

```

```

elif fitness < beta_score:
    delta_score = beta_score
    delta_pos = beta_pos
    beta_score = beta_pos
    beta_pos = fitness

```

```

elif fitness < delta_score:
    delta_score = fitness
    delta_pos = wolves[i]

```

```

a = 2 - 2 * (-1 no-itera)

```

```

for i in range (no_wolves):

```

```

    r1, r2 = np.random.rand(2)

```

```

    A = 2 * a * r1 - a

```

```

    C = 2 * r2

```

```

    D_alpha = abs(C * alpha_pos - wolves[i])

```

```

    D_beta = abs(C * beta_pos - wolves[i])

```

```

    D_delta = abs(C * delta_pos - wolves[i])

```

```

    wolves[i] = wolves[i] - A * D_alpha - A * D_beta

```

```

    return alpha_pos, alpha_score

```

```

best_pos, best_score = gwo(30, 100, 2)

```

```

print("Best position:", best_pos)

```

```

print("Best Score:", best_score)

```

O/p: Best position: [3.19199700 30 5.77800777e-05]
 Best Score: 0.9931131132000192

Parallel cellular Algorithms and Programs

Parallel cellular algorithm are inspired by functioning of biological cells that operate in highly parallel and distributed manner.

These algorithms leverage the principles of cellular automata and parallel computing to solve complex optimization problems efficiently.

```
import numpy as np
```

```
def fitness_function(position):  
    return np.sum(position**2)
```

```
num_cells = 100
```

```
grid_size = (10, 10)
```

```
solution_dim = 2
```

```
iteration = 100
```

```
neighbor_radius = 1
```

```
search_space_bounds = [-5.0, 5.0]
```

```
def evaluate_fitness(population):
```

```
    fitness = np.zeros(grid_size[0], grid_size[0])
```

```
    for i in range(grid_size[0]):
```

```
        for j in range(grid_size[1]):
```

```
            fitness[i, j] = fitness_function(population[i, j])
```

```
    return fitness
```



```

def get_neighbors(grid_size, i, j, radius):
    neighbours = []
    for di in range(-radius, radius+1):
        for dj in range(-radius, radius+1):
            ni, nj = (i+di) % grid_size[0], (j+dj) % grid_size[1]
            if (di != 0 or dj != 0):
                neighbours.append((ni, nj))
    return neighbours

```

```

def update_population(population, fitness, grid_size, radius):
    new_population = np.copy(population)
    for i in range(grid_size[0]):
        for j in range(grid_size[1]):
            neighbours = get_neighbors(grid_size, i, j, radius)
            best_neighbor = population[i, j]
            best_fitness = fitness[i, j]
            for ni, nj in neighbours:
                if fitness[ni, nj] < best_fitness:
                    best_neighbor = population[ni, nj]
                    best_fitness = fitness[ni, nj]
            new_population[i, j] = (population[i, j] + best_neighbor) / 2.0
    return new_population

```

```

def parallel_cellular():
    population = initialize_population(grid_size,
                                       solution_dim, search_space_bounds)
    best_solution = None
    best_fitness = float('inf')

```

```
for iteration in range(iterations):
    fitness = evaluate_fitness(population)
    if min_fitness < best_fitness:
        best_fitness = min_fitness
        best_indices = np.unravel_index(np.argmin(
            fitness), fitness.shape)
        best_solution = population[best_indices]
```

```
population = update_population(population,
                                fitness, grid_size, neighborhood_radius)
```

```
print(f"Iteration {iteration+1}/{iterations},  
Best fitness: {best_fitness:.6f}")
```

```
print("\nBest Solution found:", best_solution)
print("Best fitness value:", best_fitness)
```

Output:-

```
Best Solution found: [4.52424603e-06 -3.90935704e-05]
Best fitness value: 3.575187462248841e-11
```


Optimization via Gene Expression Algorithm

GEA are inspired by biological process of gene expression in living organisms. This process involves the translation of genetic information encoded in DNA into functional proteins

```
import numpy as np
import random
```

```
def fitness(solution):
    return np.sum(np.array(solution)**2)
```

```
population = 20
num_gene = 10
mutation = 0.1
crossover = 0.7
generation = 25
gene_bound = [-5.0, 5.0]
```

```
def initialize_population(population_size, num_genes,
                          bounds):
```

```
    population = []
    for i in range(population_size):
        individual = [random.uniform(bounds[i][0], bounds[i][1]) for i in range(num_genes)]
        population.append(individual)
    return population
```

```
def evaluate_population(population):
    fitness_scores = [fitness_func(individual)
                       for individual in population]
    return fitness_scores
```

```
def tournament_sel(population, fitness_scores,
                   tournament_size=3):
    selected = []
    for i in range(len(population)):
        participants = random.sample(list(enumerate(
            fitness_scores)), tournament_size)
        winner = min(participants, key=lambda
            x: x[1])
        selected.append(population[winner[0]])
    return selected
```

```
def crossover(parent1, parent2):
    if random.random() < crossover_rate:
        point = random.randint(1, len(parent1)-1)
        offspring1 = parent1[:point] + parent2[point:]
        offspring2 = parent2[:point] + parent1[point:]
        return offspring1, offspring2
    return parent1, parent2
```

```
def mutate(individual, bounds, mutation_rate):
    for i in range(len(individual)):
        if random.random() < mutation_rate:
            individual[i] = random.uniform(
                bounds[0], bounds[1])
    return individual
```



```
def gene_expression():  
    population = initialize_population(population_size,  
                                     num_genes, gene_bounds)
```

```
    best_solution = None
```

```
    best_fitness = float('inf')
```

```
    for generation in range(generations):  
        fitness_scores = evaluate_population(population)
```

```
        curr_best = np.argmin(fitness_scores)
```

```
        if fitness_scores[curr_best] < best_fitness:
```

```
            best_fitness = fitness_scores[curr_best]
```

```
            best_sol = population[curr_best]
```

```
    selected_population = tournament(population,  
                                     fitness_scores)
```

```
    next_generation = []
```

```
    for i in range(0, population_size // 2):
```

```
        parent1 = selected_population[i]
```

```
        parent2 = selected_population[i+1]
```

```
        offspring1, offspring2 = crossover(parent1,  
                                           parent2)
```

```
        next_generation.append(mutate(offspring1,  
                                     gene_bounds, mutation_rate))
```

```
        next_generation.append(mutate(offspring2,  
                                     gene_bounds, mutation_rate))
```

```
    population = next_generation
```

```
    print(f"Generation {generation+1} / {generations}")
```

Best fitness: (best fitness: 6/3)

```
print("\Best solution found:", bestsolution)
print("Best fitness value:", bestfitness)
```

```
if __name__ == "__main__":
    gene expression()
```

Output:-

Best Solution found: [0.195663732022, 1.22774355284,
-0.8043843675228429, -0.709477394383185, 0.15407105
-0.271151235533, -0.1175746543343202, -0.8708068,
0.2980.51041 ...]

Best fitness value: 4.379193223001671

Signature
24-12-2