

Probabilistic Programming Reading List

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Abstract

Test

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1 Semantics

1. *Semantics of probabilistic programs*, [Kozen, 1981]: One of the original semantics papers on probabilistic programs, designed for verifying and representing randomized algorithms.
2. *PMAF: an algebraic framework for static analysis of probabilistic programs*, [Wang and Hoffmann, 2018]: Gives an algebraic semantics for manipulating probabilistic programs; very recent.
3. [Borgström et al., 2013]: Measure transformer semantics
4. [Ścibior et al., 2017]: Describe a semantics of recursive probabilistic programs, discrete inference
5. [Vákár et al., 2019]: Domain theory for higher-order probabilistic programs

2 Probabilistic Program Analysis

[Morgan et al., 1996]: Probabilistic predicate transformers

[Ferrer Fioriti and Hermanns, 2015]: Analysis of probabilistic termination.

3 Inference & Systems

In general, inference methods can be divided into several broad categories:

1. *Approximation* methods, which perform approximate inference either via sampling or optimization.
2. *Compilation-based* methods, which perform inference by compiling the probabilistic program into an alternative representation which supports the kinds of queries that we care about.
3. *Symbolic* methods, which operate directly on the program (i.e., enumeration and block-based analyses).

3.1 Approximation Methods

3.1.1 Sampling

1. [Hur et al., 2015]: Utilizes program analysis to improve Markov-Chain Monte Carlo.
2. [Nori et al., 2014]: R2 sampling method
3. [Goodman et al., 2012]: Church
4. [Wingate et al., 2011]: Sampling with program transformation
5. [Carpenter et al., 2017]: Stan

3.1.2 Variational Approximations

3.2 Compilation-based Methods

1. [Sampson et al., 2014]: Verifies that probabilistic assertions hold by compiling the program to a graphical model.
2. [McCallum et al., 2009]: Factorie, a language for specifying factor graphs.
3. [Minka et al., 2014]: Infer.NET, compiles probabilistic programs to factor graphs.
4. [Pfeffer, 2009]: Figaro, compiles to factor graphs
5. [Pfeffer, 2001]: Ibal, an early PPL which uses variable elimination
6. [Fierens et al., 2013]: ProbLog, compiles probabilistic logic programs to weighted Boolean formulae.

3.3 Symbolic Methods

1. [Claret et al., 2013]: Performs inference by compiling probabilistic programs to algebraic decision diagrams (ADDs).
2. [Sankaranarayanan et al., 2013]: Approximates the probability with analyzing a finite subset of paths
3. [Albarghouthi et al., 2017]: FairSquare, performs inference by approximating integrating under each path in the program.
4. [Belle et al., 2015]: Approximate weighted model integration, a generalization of SMT-solvers to perform integrals instead of just finding a satisfying assignment.
5. [Chistikov et al., 2015]: Performs inference using weighted model integration.

4 Program Transformations

In standard program analysis, a program transformation is a rewriting procedure which preserves the underlying semantics of the program; for example, the optimization phase of a compiler. In the context of probabilistic programs, the goal is to generalize well-known rewriting procedures to apply to programs with probabilistic semantics, in the hopes of easing analyses such as inference.

1. [Hur et al., 2014]: Generalizes program slicing to the setting of probabilistic programs with observations.
2. [McIver and Morgan, 2005]: Abstraction and refinement in probabilistic systems; extending the framework of program abstraction to verifying probabilistic properties.
3. [Wang et al., 2018]: PMAF, abstract interpretation for lower/upper bounds on Bayesian inference
4. [Narayanan et al., 2016]: Hakaru, compiles programs into posterior distributions

5 Probabilistic Model Checking

1. [Baier et al., 1997]: Early work on symbolic model checking for probabilistic systems.
2. [Hermanns et al., 2008]: Probabilistic CEGAR, generalizes CEGAR to probabilistic systems.
3. [Dehnert et al., 2017]: Storm model checker
4. [Kwiatkowska et al., 2002]: PRISM model checker

6 Applications

- [Foster et al., 2016]: Probabilistic network verification (ProbNetKat).
- [Gordon et al., 2014]: Using probabilistic programs to define probabilistic databases.
- [Schkufza et al., 2013]: Stochastic super-optimization; treats optimization as a search through a probability space over programs.

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