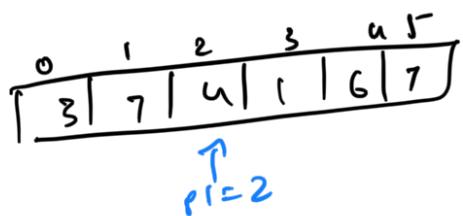


2 - Pointers

C++ address pointers?
int *a, *b;

⇒ Physical Representation:
variables which hold index values



2 Important Questions:

- 1) How (where) to initialize the pointers?
- 2) How to update the pointers?

Question: Given a sorted array of numbers such that $a[i] + a[j] = k$. Find all pairs (i, j) of distinct elements if there is a pair (i, j) of distinct elements such that $a[i] + a[j] = k$.

$A =$	-3	0	1	3	6	7	12	14	18	25
	0	1	2	3	4	5	6	7	8	9

$\boxed{(3, 14)}$ True

Brute Force:

Consider all pairs.

```
for(i=0; i<n; i++) {  
    for(j=i+1; j<n; j++) {  
        if(a[i]+a[j]==k)  
            cout << "Pair found" << endl;  
    }  
}
```

T.C: $O(n^2)$
 S.C: $O(1)$

Time - True;

False

Hashing:

T.C: $O(n)$
 S.C: $O(n)$

$k = 24$
 $a = 12$
 $b = 12$

$k = 17$

Binary Search:

$\begin{matrix} l & & d \\ -3 & 0 & 1 & 3 & 6 & 7 & 12 & 14 & 18 & 25 \\ o & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 \end{matrix}$

1) $a+b = 17$
 $a = -3 \Rightarrow b = 20$ Do B.S to check if there or not.

2) $a = 0$
 $b = 17 \rightarrow O(\log n)$

T.C: $O(n \log n)$
 S.C: $O(1)$

Edge Case:

$P_1: 0 \rightarrow P$ (P)
 $P_2: A \rightarrow P$ $(n-P)$

$P + n - P = n$

2 - Pointers:

$A = \begin{matrix} -2 & 0 & 1 & 3 & 6 & 7 & 12 & 14 & 18 & 25 \\ p_1 & 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 \end{matrix}$

$p_1 = 0$,

$p_2 = 9$

$p_1 = 3, p_2 = 7$

$k = 17$

p_2

Control

$(-3, 25) = 22$

$(cont++)$

$a[p_1] + a[p_2] = 22$

$n = 3 - 1$

$\dots - \dots = 15$

$R_1 = 1$

$$(0, 11) = 18 \rightarrow 17^*$$

$\leftarrow 10 \leftarrow 15$

$(0, 14)$

$(3, 14)$

$(1, 14)$

$\text{Count} = 1$

bool

$\text{checkSum}(\text{arr}[], n, k) \{$

$$\begin{aligned} p_1 &= 3 \\ p_2 &= 7 \\ k &= 1 \end{aligned}$$

$p_1 = 0, p_2 = n - 1$
while ($p_1 \leq p_2$) {

$\quad \text{if } (\text{arr}[p_1] + \text{arr}[p_2] \leq k) \quad \checkmark$

$\quad \text{else if } (\text{arr}[p_1] + \text{arr}[p_2] > k) \quad \times$

$\quad \quad p_1++;$

$\quad \quad p_2--;$

$\quad \quad \text{count}++;$

$\quad \quad p_1++;$

$\quad \quad p_2--;$

$\quad \quad \text{return false; return count;}$

}

T.C:

Question:

Count no of pairs

T.C: $O(n)$

S.C: $O(1)$

Question:

Duplicate

$K = 10$

A :



$$6 + 3 = 9$$

$$\begin{aligned} \# 4s &= 3 \\ \# 6s &= 2 \end{aligned} \quad \left\{ \begin{array}{l} 3 \times 2 \text{ pairs} \\ = 6 \text{ pairs} \end{array} \right.$$

$$\# 5s = 3$$

$$(5+5) = 10$$

$$3 \times 3 = 9 ?$$

$p_1 = 0$ $p_2 = n-1$ $\# \text{us} = 3$, $\# \text{bs} = 2$
 $\text{ans} = \frac{3+2}{2} = 2.5$ $(u_{c_2}) = \frac{n(n-1)}{2}$

$A = \begin{matrix} p_1 & p_1 & " & n & n & p_1 & p_2 & p_2 & p_2 \\ \downarrow & \downarrow \\ 1 & 4 & 4 & 4 & 5 & 5 & 6 & 6 & 11 \end{matrix}$ $k = 10$
 $\underbrace{(p_2 - p_1 + 1)}_{(1, 11) > 10}$ $\text{No } 8! \text{ s'}$
 $\underbrace{(1, 6) < 10}_{\text{count } c_2}$

Case 1: $(u, b) = 10$
 Case 2: $(s, b) = (\text{Do we have to break?})$

$\text{if } [a[p_1] + a[p_2]] == k \leftarrow$

$\text{if } [a[p_1] \neq a[p_2]] \leftarrow$

$\text{count_p1} = 0$, $\text{left} = p_1$
 $\text{while } [a[\text{left}] == a[p_1]] \leftarrow$
 $\text{left}++$
 $\text{count_p1}++$

$\text{right} = p_2$
 $\text{count_p2} = 0$, $\text{right} = p_2$
 $\text{while } [a[\text{right}] == a[p_2]] \leftarrow$
 $\text{right}--$
 $\text{count_p2}++$

$\text{count} = \text{count_p1} * \text{count_p2}$

$\text{else } [a[1] == a[p_2]] \leftarrow$

$\text{count} = \frac{(p_2 - p_1 + 1)}{2} \leftarrow$

$\left[\frac{n(n-1)}{2} \right]$

return count
 $}$

$T.C: O(n)$

$S.C: O(1)$

Question: Given sorted array elements, find a pair such that $a[j] - a[i] = k$ (such that $i < j$)

3) distinct pair (i, j)
 $a[i] - a[j] = k$
 $k = 11$

$A = \begin{matrix} -3 & 0 & 1 & 3 & 6 & 7 & 12 & 14 & 18 & 25 \\ 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 \end{matrix}$

$$(14, 3) = 11$$

\rightarrow If there is a pair with difference = k ,
 Is there a pair whose diff = $-k$

$(a, b) \Rightarrow a - b = \boxed{k}$

$(b, a) \Rightarrow b - a = -k$

$\boxed{\text{abs}(k)}$ $\boxed{-5} = \boxed{5}$

Brute Force:

T.C: $O(n^2)$

S.C: $O(1)$

Binary Search:

T.C: $O(n \log n)$

S.C: $O(1)$

Hashing:

T.C: $O(n)$

S.C: $O(n)$

2 - Pointers:

Ans to Initialize?

num

$$1) 0, n-1$$

$$2) \frac{n}{2}, \frac{n}{2}-1$$

$$3) 0, 1$$

$$4) 0, \frac{n}{2}$$

$$\{ n, n-1 \}$$

$$k=5$$

					p_1	p_2					
A =	-3	0	1	3	6	7	12	14	18	25	T'
	0	1	2	3	4	5	6	7	8	9	

$$1) p_1 = 0, p_2 = 9$$

$$25 - (-3) =$$

$$(25, -3) \Rightarrow 28 \Rightarrow$$

$$\begin{array}{l} p_1++ \Rightarrow \\ p_2-- \Rightarrow \end{array} \begin{array}{l} (0, 25) = 25 \\ (-3, 18) = 21 \end{array}$$

$\rightarrow p_1++$ } Brute force
 $\rightarrow p_2--$

$$2) p_1, p_2 \leq, p_2 = 4$$

$$\begin{array}{l} (7, 6) \Rightarrow 1 \\ \cancel{p_1--} \quad (7, 3) \Rightarrow 4 \\ \cancel{p_2++} \quad (12, 6) \Rightarrow 6 \end{array}$$

$$3) p_1 = 0, p_2 = 1$$

					p_1	p_2					
A =	-3	0	1	3	6	7	12	14	18	25	T'
	0	1	2	3	4	5	6	7	8	9	

$$K=5$$

$$(-3, 0) \Rightarrow 3$$

$$(-3, 1) = 4$$

$$(-3, 1) \Rightarrow 4$$

$$(-3, 3) \Rightarrow 6$$

$$(0, 3) \Rightarrow 3$$

$$(0, 6) \Rightarrow 6$$

$$(1, 6) \Rightarrow 5$$

→ No. of pairs ✓ }
→ Duplicates ✓ }

Takeaways

- 1) Initialization of Pointers:
Initialize pointers such that you can always make a decision and discard an element
- 2) Update the Pointers towards your decision making
Update when to stop
- 3)

Binary Search :

- 1) $\text{low} = 0, \text{high} = n-1$
 - 2) $\text{low} = \text{mid}$ or $\text{high} = \text{mid} - 1$
 p_1 p_2
 - 3) $\text{low} > \text{high}$
- Increment p_1 ↓ decrement p_2
- 2 Pointers ↗ Superior

Sum 9 3 nos

Question:

Given an array of 3 integers from the array A, find three integers, B, such that the sum of the three integers is closest to B.

the sum of these numbers
 \rightarrow Return $B = 14$

$A = [7, 0, -3, 16, -10, 12, -7, 3]$

$(7, 16, -10) \Rightarrow (13) \quad (14-3)$

$(-3, 0, 16) \Rightarrow 13 \quad (14-3)$

$(0, 3, 12) \Rightarrow 15 \quad (14-1)$

Simpler Problem: Find 2 numbers whose sum is closest to B .

$A = [7, 0, -3, 16, -10, 12, -7, 3]$

$(12, 3) \quad (16, -3)$

Brute Force:

Consider all pairs

T.C: $O(n^2)$

$$(0, 16) \Rightarrow 16, | -2 |$$

$$[, 16] \Rightarrow 16, | -5 |$$

2 Pointers:

\rightarrow Sort

$$(-10, 16) \quad (-10, 8)$$

$$(-10, 6) \quad (-10, 16) = 6$$

$$(-7, 16) = 9$$

$$(-3, 16) = 13$$

Array: $[7, -3, 16, -10, 0, 3, 12, 6, 5, 2, 1, -7, 14]$

P_1 P_2 $B = 14$

$D.H = 8$

$D.H = 5$

$D.H = 1$

$D.H = -2$

$D.H = -5$

$$(0, 16) = \textcircled{16} (19)$$

$$(0, 12) = 12$$

$$(3, 12) = 15$$

$$(3, 7) = 10$$

$$(7, 7)$$

$\min_diff = \text{INFINITY}, \text{sum} =$

$$p_1 = 0, p_2 = n-1$$

while ($p_1 < p_2$) {

if ($\text{abs}(a[p_1] + a[p_2]) - B < \min_diff$) {
 $\min_diff = \text{abs}(a[p_1] + a[p_2] - B)$
 $\text{sum} = a[p_1] + a[p_2]$;

if ($a[p_1] + a[p_2] < B$)
 p_1++

else p_2--

}

T.C: $O(n) + O(n \log n)$
S.C: $O(1)$

Left's Extend thy fo 3 numbers:



$$\min_{a+b+c} |a+b+c - B|$$

$$(a+b+c) = B$$

$$-10 + b+c = \frac{14}{2} = 7$$

Step1: $a = -10$

$$(b+c - 10)$$

such that sum

$$\begin{aligned} \text{diff} &= 4 \\ p1 &= -1 \\ p2 &= 4 \\ p1 &= p2 \end{aligned}$$

$$\begin{aligned} (0, 16) &= 16 \\ \text{sum} &= 18 \\ &\boxed{-2} \\ &\boxed{(-n)} \end{aligned}$$

→ Find 2 numbers
as close as possible to $\frac{10+10}{2} = 10$

Step 2: $a = -7$

$$b+c = 10+7 \\ = 21$$

for ($i=0$) $i < n$ $i++$ {
 $p_1 = i+1$, $p_2 = n-i$

$O(n)$ ← [← some code] }

3

T.C: $O(n \log n) + O(n^2)$
 $= \boxed{O(n^2)}$

Question: Given sorted array no. of rectangles that can be formed using area less than B.

whose lengths. Find area $(2,3) = (3,2)$

$B = 10$

$A = \{ 2 \quad 3 \quad 5 \}$

$\cancel{(3,2)} = (2,3)$ $2 < 10$
 $(2,3) = 6 < 10$

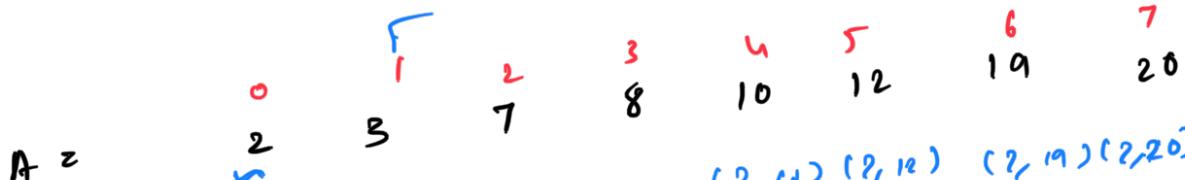
Y
Y
N

$\boxed{\text{Ans} = 5}$

$$\begin{aligned}(2, 5) &= 10 \\(3, 3) &= 9 < 10 \\(3, 5) &= 15 \\(5, 5) &= 25\end{aligned}$$

Y
N
N

$$B = 85$$



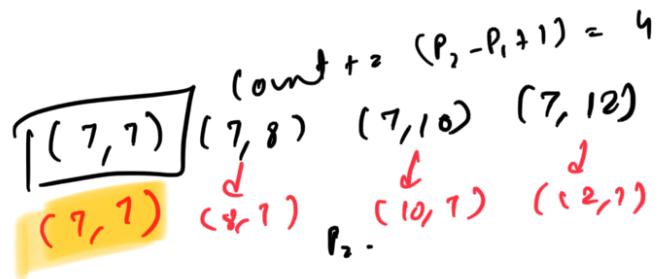
$$A =$$

$$\begin{aligned}2 &\Rightarrow (2, 2) (2, 3) (2, 7) (2, 8) (2, 10) (2, 12) (2, 19) (2, 20) = 8 \\3 &\Rightarrow (3, 5) (3, 7) (3, 8) (3, 10) (3, 12) \quad \text{Count} = 4 \\7 &\Rightarrow (7, 1) (7, 8) (7, 10) (7, 12) \quad \text{Count} = 2 \\8 &\Rightarrow (8, 6) (8, 10) \\10 &\Rightarrow\end{aligned}$$

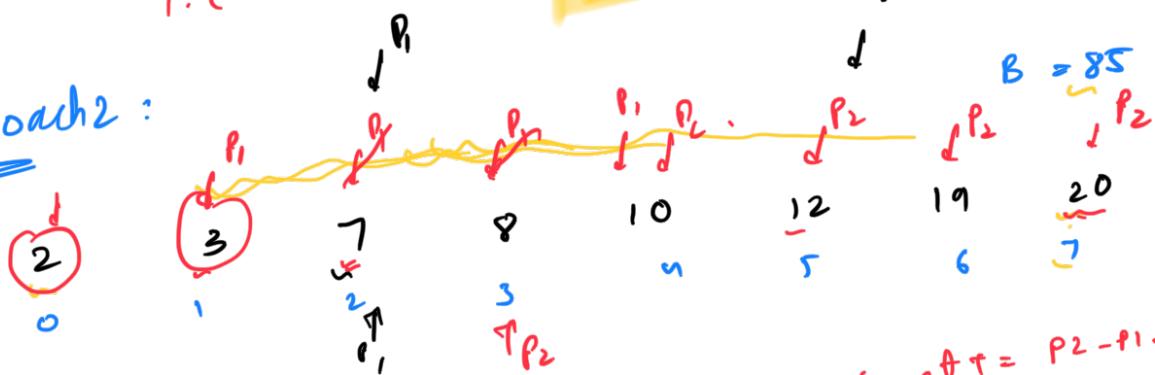
$$8 + 7 + 4 + 2 = \boxed{21}$$

B brute force:

Consider all pairs
T.C: $O(n^2)$



Approach 2:



$$(2, 20) = 40$$

$$(3, 20) = 60$$

$$(7, 20) = 140$$

$$(7, 19) = 133$$

$$(7, 12) = 84$$

$$\dots = 96$$

$(P_1 > P_2)$
break

$$\begin{aligned}\text{Count}^+ &= P_2 - P_1 + 1 \\ \text{Count}^- &= 8 + 7 \\ &= 15 + 4 \\ &= 19 + 2 \\ &= 21\end{aligned}$$

$$\begin{array}{ll} (9, 12) & 96 \\ (8, 10) & 100 \\ (10, 10) & \end{array}$$

```

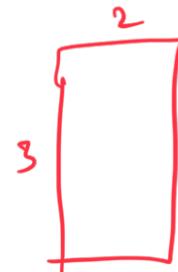
 $p_1 = 0$             $p_2 = n-1$ 
 $\text{count} = 0$ ;    $(p_1 \leq p_2) \leftarrow$ 
while
    if [ $a < p_1$ ]  $\times a \leq p_2]$        $\leftarrow B \leftarrow C$     $[2(p_2 - p_1 + 1) - 1]$ 
        count +=  $p_2 - p_1 + 1$ ;
        p1++;
    else
        p2--;
}
return count;

```

$O(n \log n)$

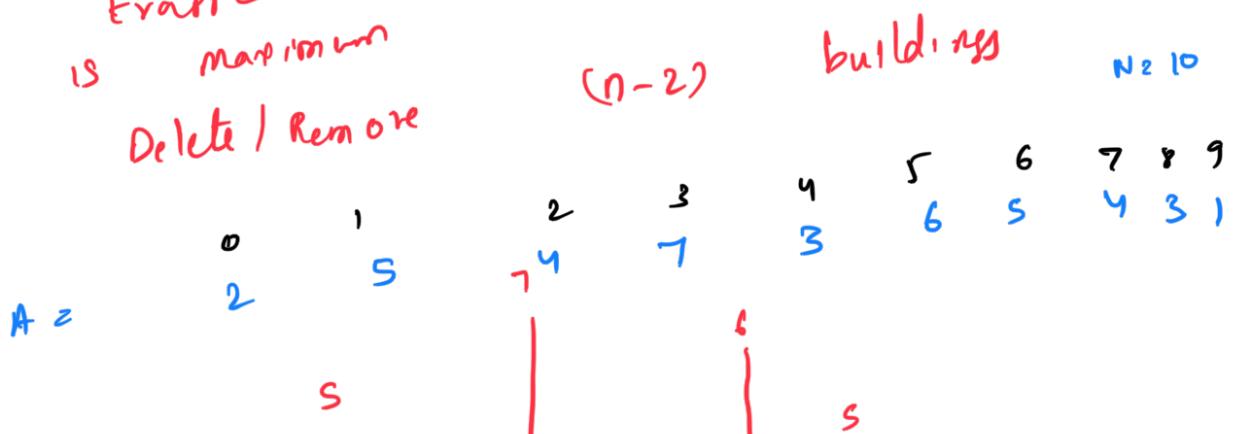
T.C: $O(n)$

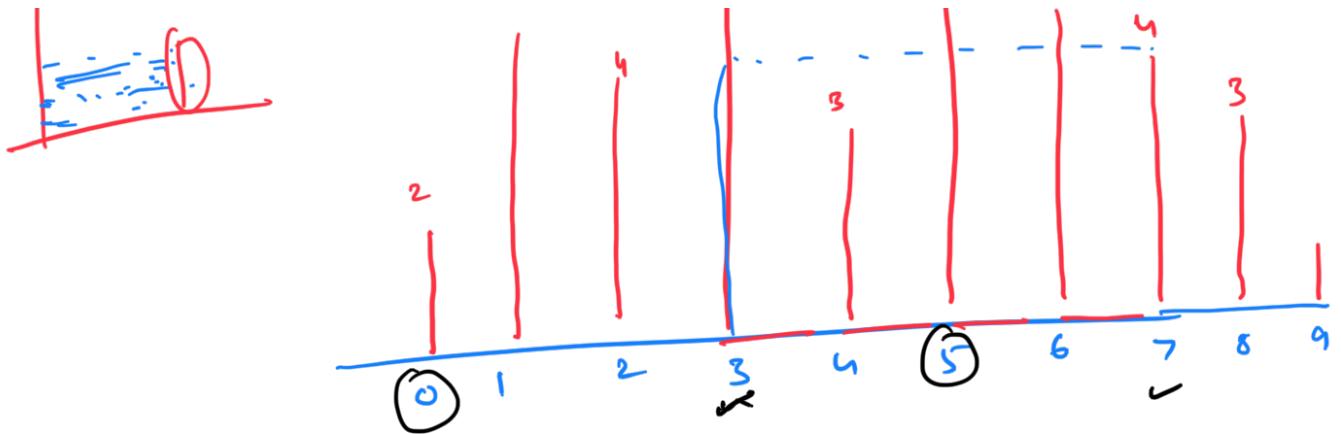
$$(a, b) \neq (b, a)$$



Question: Given an unsorted array of elements which represent height of buildings, choose 2 buildings such that water trapped between them is maximum.

→ Delete / Remove





$$\text{width} = (5-0) = 5$$

$$n = \min(2, 6) = 2$$

$$\text{Area} = 5 \times 2 = 10$$

$$\text{width} = 4$$

$$\text{height} = \min(7, 4)$$

$$\text{Area} = 4 \times 4 = 16$$

Given 2 building (i, j)

width $\leftarrow j-i$

height $= \min(a[i], a[j])$

$$\text{Area} = (j-i) \times \min(a[i], a[j])$$

Brute Force:

(on order all pairs of buildings)

for ($i=0$; $i < n$; $i++$) {

 for ($j=i+1$; $j < n$; $j++$) {

 ans = max(ans,)

T.C: $O(n^2)$, S.C: $O(1)$

$$n = \min(2, 1) = 1$$

$$\min(9, 1) = 1$$

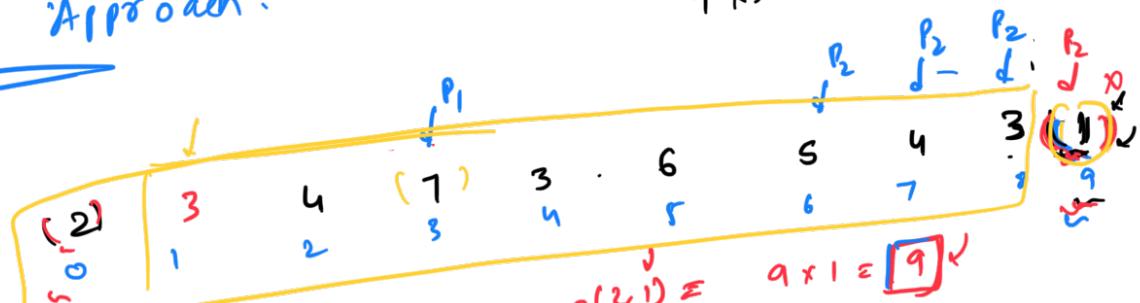
$$(2, 3) = \\ 8 \times 2 = 16$$

Better Approach:

$$w = 9$$

$$h = 1$$

A =



Observation:

$$\text{Area} = (0, 9) \approx$$

$$\frac{9 \times \min(2, 1)}{h=1, w=9} = 1 \times 9 = 9$$

1) can't get an area $> q$ with 1 as one of the built-in

$$\text{area} = \min(h, w)$$

$$\min(1, 7) = 1$$

$$\min(0, 1) = 1$$

$\boxed{\text{max_area} = 21}$

}

```

area = INT-MIN;
P1 = 0, P2 = n-1;
while (P1 < P2) {
    area = max (area, min(a[P1], a[P2]) * (P2 - P1));
    if (a[P1] < a[P2])
        P1++;
    else
        P2--;
}
return area;

```

T.C: $O(n)$

→ Median → Matrix of sorted rows
 → Sliding window Technique
 → B-S prob

$A = \begin{bmatrix} P_1 & -10 & -7 & -3 & 0 & 3 & 7 & 12 & 16 & P_2 \\ 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 \end{bmatrix}$

$$(16, -3, 0), (16, -10, 3)$$

hashset = $\{ -10, -7, -3, 0, 3, 7, 12, 16, 0, 1 \}$

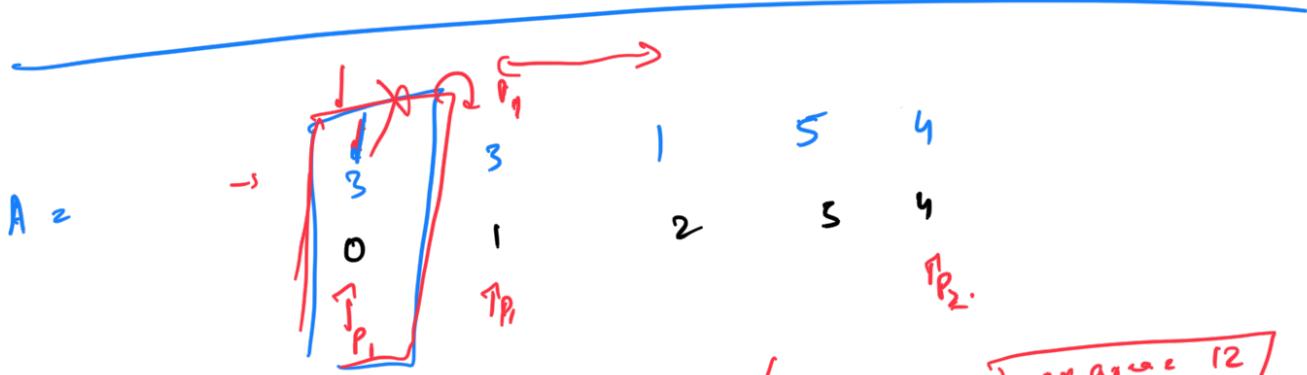
$$16 - 10 = 6 \quad 17 - 6 = 11$$

$$22 - 6 = 16$$

S.C: $O(n)$

\leftarrow \leftarrow
 f.c.: $\Theta(n)$
 s.c.: $\Theta(n)$

$(-10, 16, 16)$



Step 1: Area:

$$4 \times \min(3, n) = 12$$

Total area = 12

Step 2: Area:

$$3 \times \min(3, n) = 9$$