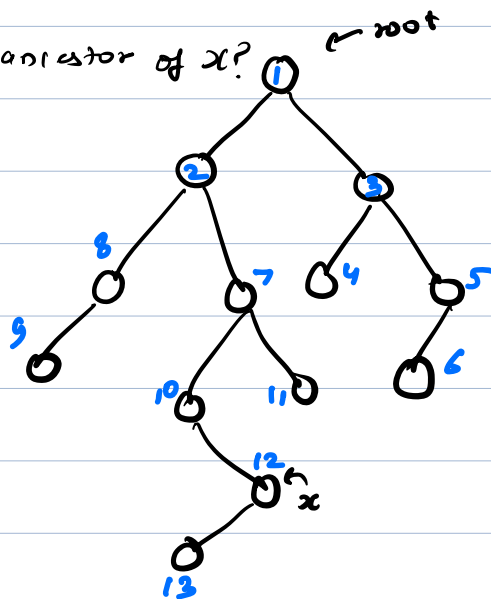


3rd Oct
Mon
Articulation

6th Oct
Thursday
AVL Trees

Binary lifting.

What is k^{th} ancestor of x ?



$par[]$

10^5

```
while(k--){
    x = par[x];
}
```

Tc $O(N)$

Sc $O(N)$

Maintain 1st par, 2nd par, 3rd par, ..., n^{th} par

Tc: $O(1)$

Sc: $O(N^2)$

1-50



1 2 4 8 16 32

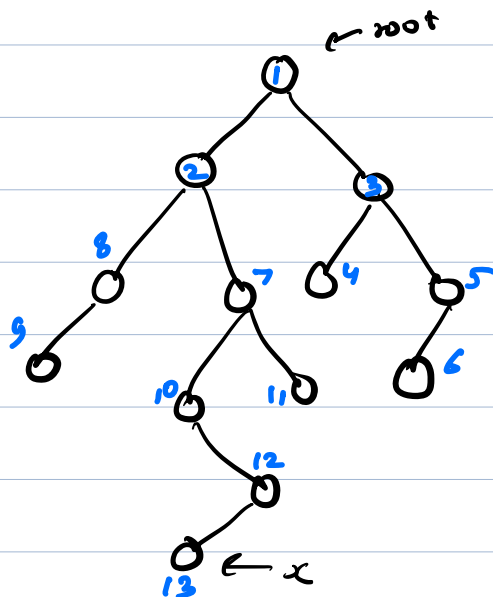
$$\log 50 = 6$$

$$\begin{array}{r} 50 \\ -32 \\ \hline 18 \\ -16 \\ \hline 2 \\ -2 \\ \hline 0 \end{array}$$

110010

Maintain

1st pow, 2nd pow, 4th pow, 8th pow, 16th pow,
32 powⁿ, 64 powⁿ



10th ancestor.

TC: $(\log N)$

SC: $N \log N$

$up[N][\log N]$

$up[i][0]$

$up[i][1]$

$up[i][2]$

$up[i][j]$

2^0 par of i

2^1 par of i

2^2 par of i

2^j par of i

void dfs (int curr, int par)

$up[curr][0] = par$

$up[curr][1] = up[up[curr][0]][0]$
 $up[curr][2] = up[up[curr][1]][1]$
 $up[curr][3] = up[up[curr][2]][2]$

for ($j=1, j < \log N; j++$)

$up[curr][j] = up[up[curr][j-1]][j-1]$

for (auto j : adj[curr])

if ($j \neq par$)

dfs ($j, curr$)

$up[curr][2]$

↑

$up[curr][0]$

↑

curr

↑ No of nodes

```
int kthanc (x, kth, N)
```

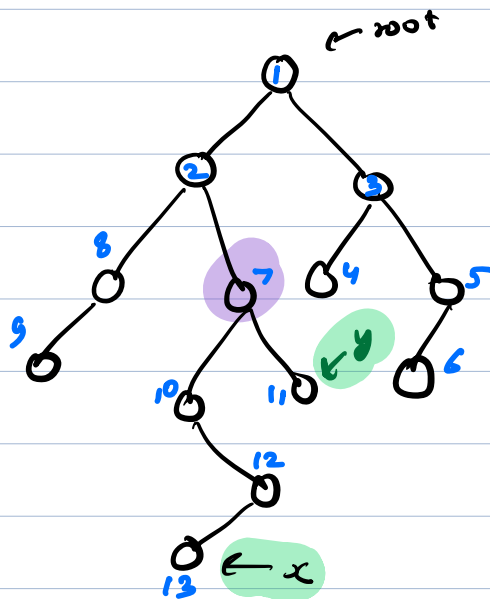
```
for ( i = logN - 1 ; i ≥ 0 ; i-- )
```

```
if ( (k & (1 << i)) != 0 )
```

```
    x = up[x][i]
```

```
return x
```

LCA = Lowest common ancestor.



$LCA(x, y) = 7$

$LCA(11, 9) = 2$

$LCA(8, 6) = 1$

check if x is a ancestor of y or not



If y is in subtree of x
then x is ancestor.

→ If x is an ancestor of y

bool isAncestor(x, y)

{

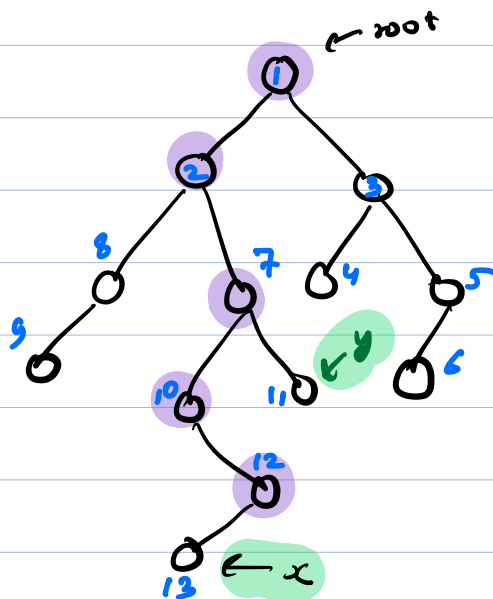
if ($intime[y] \geq intime[x]$

$\&\& outime[y] \leq outime[x]$

return True

else

return False



12 → X

10 → X

7 → ✓

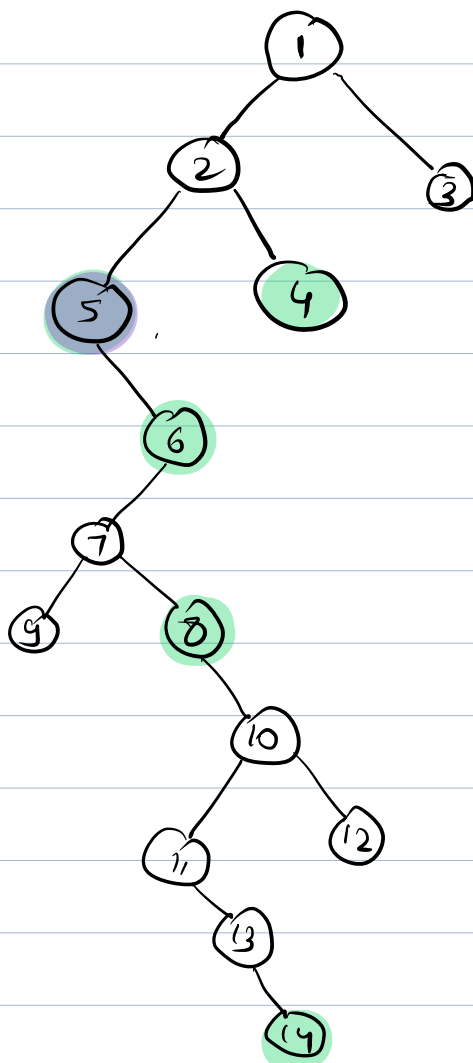
2 → ✓

1 → ✓

Goal is go as much up as you can

S.T node is not an ancestor of.

Once this is done, you are standing at
child of LCA,



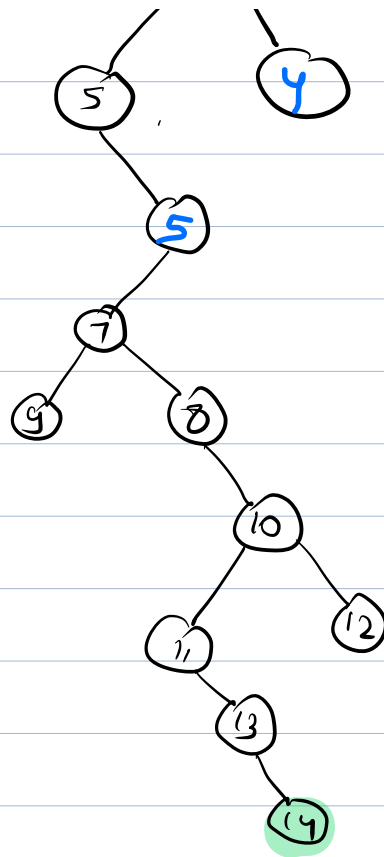
LCA (14,4)

$$2^3 = 8 \quad \times$$

$$2^2 = 4 \quad \checkmark$$

$$2^1 = 2 \quad \checkmark$$

$$2^0 = 1$$



$LCA(2, 14)$

$= 2$

```
int lca ( int x, int y )
```

```
    if ( is_ancestor ( x, y ) )
```

```
        return x
```

```
    if ( is_ancestor ( y, x ) )
```

```
        return y.
```

```
    for ( i = log N - 1 ; i ≥ 0 ; i-- )
```

```
    {
        temp = up[x][i]
```

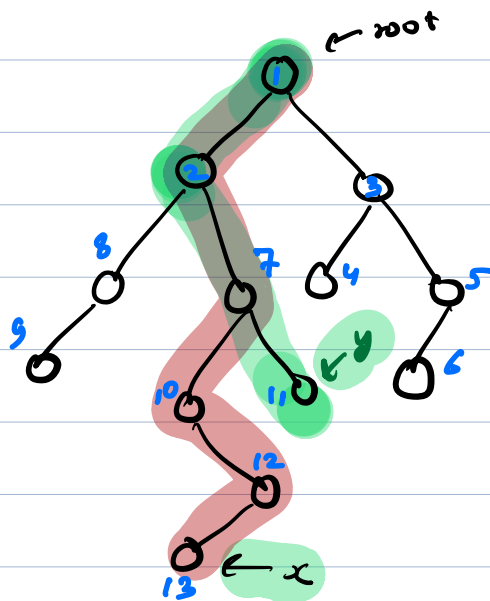

If (is_ancestor (temp, y) == 0)

$x = \text{up}[x][i]$

return $\text{up}[x][0]$

TC: $\log N$.

Q. Tree, calculate distance b/w x & y .



$\text{dist}(x, y) = 5$

$$6 + 4 - 2 \times 3 = 4$$

level[] + distance from root.

$$\text{level}[x] + \text{level}[y] - 2 \text{level}[\text{LCA}] + 1$$

↓

root → x

↓

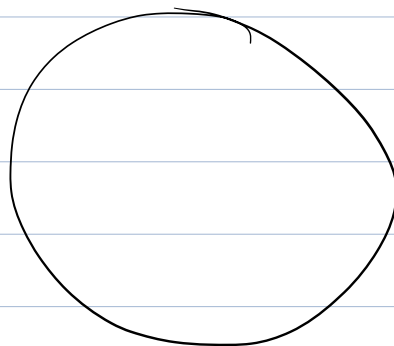
root → y

Doubt.

void dfs (curr, par)

{

$$\text{level}[\text{curr}] = 1 + \text{level}[\text{par}]$$



3rd

mon

5th oct

Thur

Articulation
points

AVL Tree