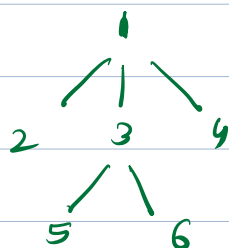


Given a tree, Q queries are asked:

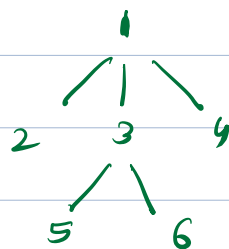
Each query have 2 int x & y.

If y belongs to subtree of x or not

Q = 7



|   |   |   |     |
|---|---|---|-----|
| 3 | 5 | → | Yes |
| 5 | 6 | → | NO  |
| 2 | 6 | → | NO  |
| 1 | 6 | → | Yes |
| 1 | 2 | → | Yes |
| 4 | 5 | → | NO  |



|   |   |   |       |
|---|---|---|-------|
| 3 | 6 | <span style="border: 1px solid green; border-radius: 50%; padding: 2px;">y</span> | True  |
| 3 | 4 |   | False |

```
void dfs (int curr, par)
```

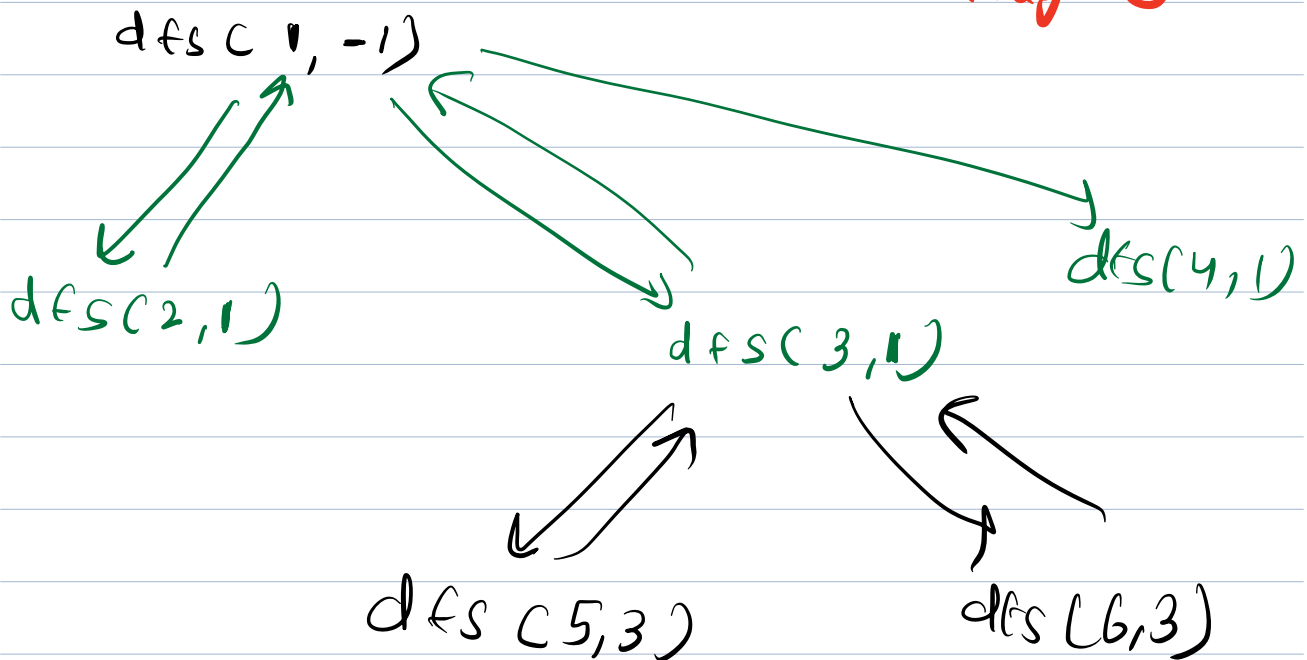
```
// curr is visiting right now
```

```
for( auto j: adj[curr]
```

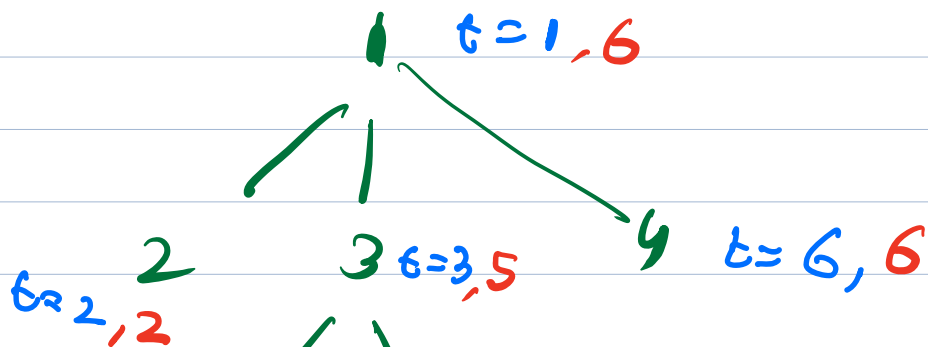
if ( $j \neq \text{par}$ ) dfs( $j, \text{cur}$ )

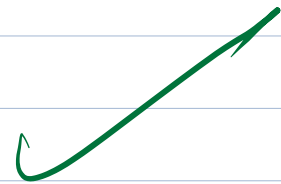
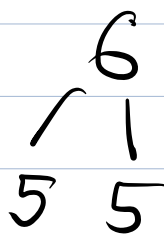
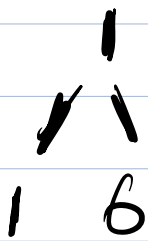
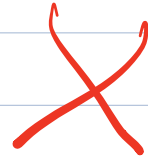
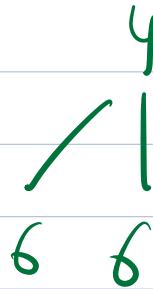
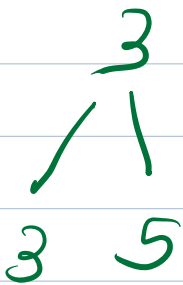
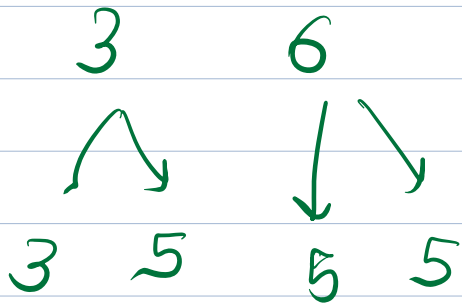
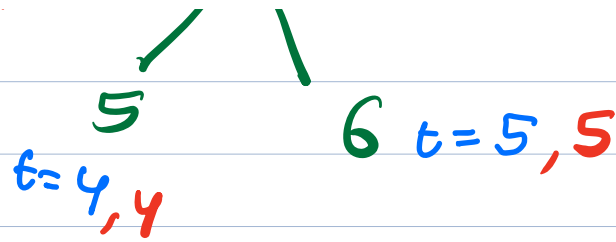
return

flag = 0



$t = 0$





Once start time & end time  
are recorded

1



Each query can be answered  
in  $O(1)$  time.

int timer

void dfs ( int curr, int par, intime[], outtime[] )

timer++

intime[curr] = timer

for ( auto j : adj[curr] )

{ if ( j != par ) dfs( j, curr, intime, outtime ) }

outtime[curr] = timer

timer = 0

int intime[N], outtime[N]

dfs( 1, -1, intime, outtime )

for( i = 0; i < q; i++ )

x y .

if ( intime[x] ≥ intime[y] && outtime[y] ≤ outtime[x] )

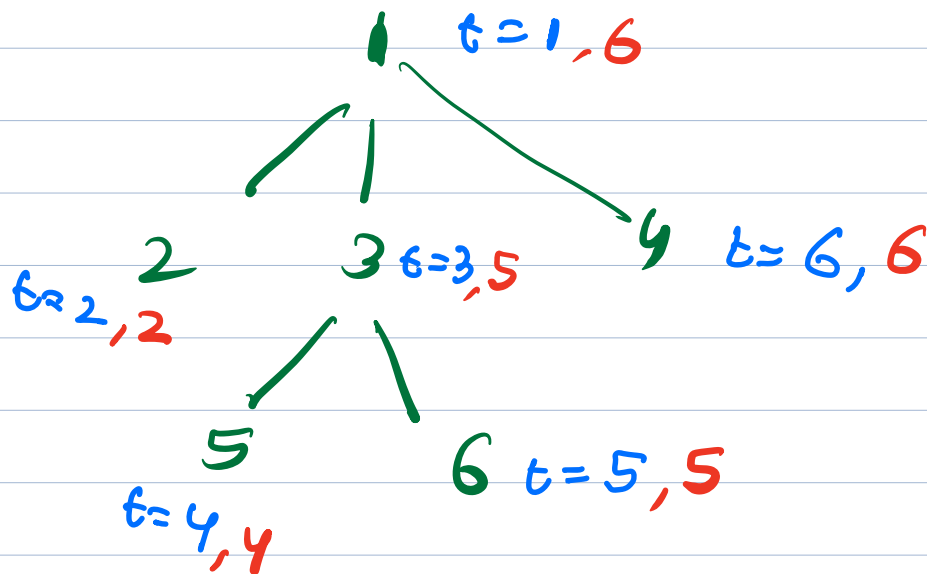
cout << "Yes" ;

else

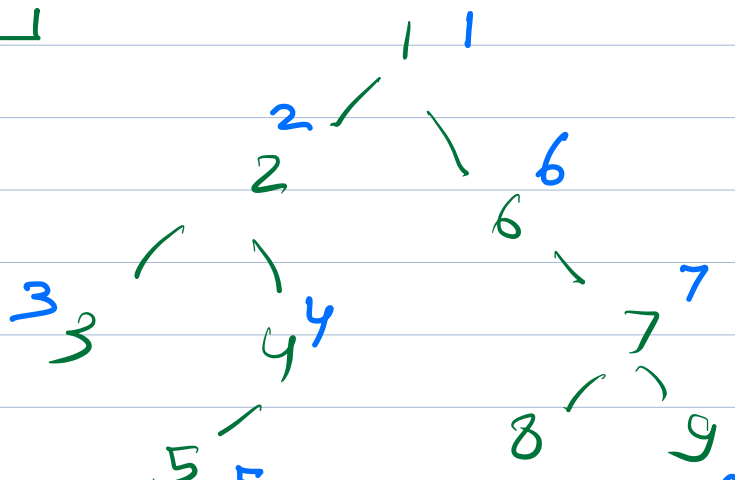
cout << "No" ;

$$T_C: O(V + E + Q)$$

$$S_C: O(V)$$



1, 2, 3, 5, 6, 4



→

8

9

1, 2, 3, 4, 5, 6, 7, 8, 9

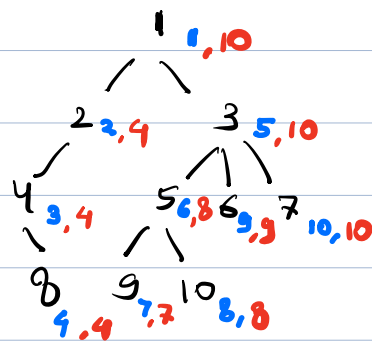
Q. Given a tree A nodes numbered from 1 to A, root at 1. Initially every one is 1.

Q queries x

Type1 All nodes in subtree of x, make them 1

Type2 All nodes in subtree of x, make them 0

Type3 Count no of nodes in subtree of x, which are one.



|   |   |     |
|---|---|-----|
| 2 | 5 |     |
| 3 | 3 | ⇒ 3 |
| 3 | 5 | ⇒ 0 |

2 6

1 1

3 3 ⇒ 5

2 4

3 1 ⇒ 8

1 2 3 4 5 6 7 8 9 10

1, 2, 4, 8, 3, 5, 9, 10, 6, 7

update curr subtree

update ( inTime[curr] + 1, outTime[curr] )

- Tree flattening
- Segment tree
- Lazy propagation

int timer

void dfs ( int curr, int par, int time[], outtime[] )

timer++

intime[curr] = timer

for ( auto j : adj[curr] )

{ if ( j != par ) dfs( j, curr, intime, outtime )

outtime[curr] = timer

void Build ( idx, start, end )

if ( start == end )

{ segtree[idx] = 0

return

mid = (start + end) / 2

Build ( 2\*idx+1, start, mid )

Build ( 2\*idx+2, mid+1, end )

segtree[idx] = segtree[2\*idx+1] + segtree[2\*idx+2]  
+ 2

// update

// Query

timer = 0

int intime[N], outtime[N]

dfs(1, -1, intime, outtime)

Build(0, 0, N-1)

for( i = 0; i < q; i++)

{  
    if (type1)  
    {  
        update(0, 0, N-1, intime[x] + 1, outtime[x], 1)  
    }  
    else if (type2)  
    {  
        update(0, 0, N-1, intime[x] + 1, outtime[x], 0)  
    }  
    else  
    {  
        printQuery(0, 0, N-1, intime[x] + 1, outtime[x])  
    }  
}

$T.C. O(V + E + Q \log V + V) : O(V + E + Q \log V)$



$$S_c: O(v + v + 4v) \Rightarrow O(v)$$

— x — x —