## Resolução da <u>Lista 5</u> da disciplina de Matemática Discreta

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## 3. Formas disjuntivas mínimas

1.

a. 
$$\{\alpha = ab' + abc' + a'bc', \pi = ac' : \alpha = abc + ab'c' + abc' + a'bc' \}$$

Mapa de Karnaugh:

\	bc	bc'	b'c'	b'c
a		$\checkmark$	V	$\checkmark$
a'		V		

Logo, 
$$\alpha = ab' + bc' : \pi \not\subset \alpha$$

**b.** 
$$\{\alpha = ab + ab'c' + a'b'c', \pi = ab' : \alpha = abc + abc' + ab'c' + a'b'c' \}$$

\	bc	bc'	b'c'	b'c
a	<b>V</b>	$\checkmark$	V	
a'				V

Logo, 
$$\alpha = ab + ac' + a'b'c$$
  $\therefore \pi \not\subset \alpha$ 

c. 
$$\{\alpha = c + abc + abc', \pi = ab$$
  
 $\therefore \alpha = ab'c + a'bc + a'b'c + abc + abc'$ 

	bc	bc'	b'c'	b'c
a	<b>V</b>	$\checkmark$		$\checkmark$
a'	V			V

Logo, 
$$\alpha = c + ab = c + \pi$$
 . .  $\pi \subset \alpha$ 

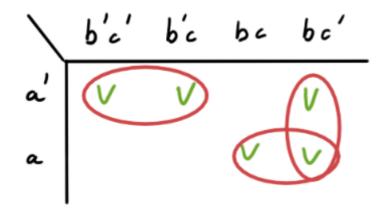
d. 
$$\{lpha=a'bc+ab'c+abc,\pi=abc:\pi\subsetlpha$$

2.

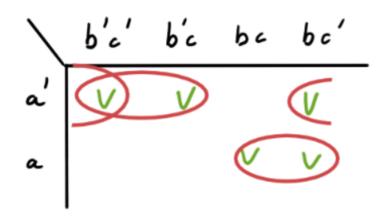
a. 
$$\alpha = abc + abc' + a'c' + a'b'c + a'bc'$$

$$= abc + abc' + a'b'c' + a'b'c + a'bc'$$

São **duas** as possíveis formas disjuntivas mínimas:



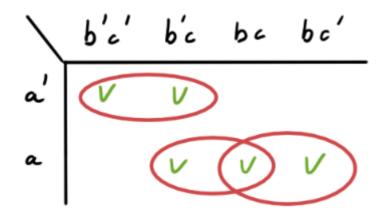
$$\alpha = b'c' + a'b' + ab$$



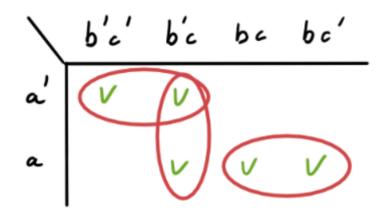
$$\alpha = ab + ac' + a'b'$$

$$\mathbf{b.}\,\beta = ab + a'(b'+c') + bc' = \underline{ab + a'b' + a'c' + bc'} = abc + abc' + a'b'c + a'b'c' + a'bc'$$

São **duas** as possíveis formas disjuntivas mínimas:



$$\beta = a'b' + ac + ab$$



$$\beta = a'b' + b'c + ab$$

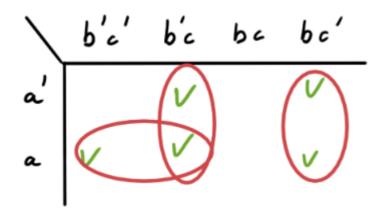
c. 
$$\gamma=a+bc+a'b'c'=abc+abc'+ab'c+ab'c'+a'bc+a'b'c'$$

	bc	bc'	b'c'	b'c
a		$\checkmark$		$\checkmark$
a'	<b>V</b>		V	

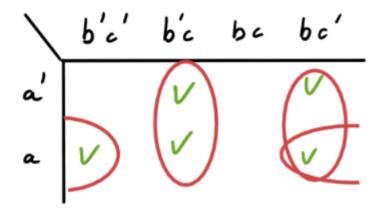
$$\gamma = a + bc + b'c'$$

d. 
$$\delta = abc' + ab'c + ab'c' + a'bc' + a'b'c$$

Existem duas formas disjuntivas mínimas possíveis:



$$\delta = ab' + bc' + b'c$$



$$\delta = ac' + bc' + b'c$$

e. 
$$\eta = abc + abc' + ab'c' + a'b'c$$

	bc	bc'	b'c'	b'c
a	<b>V</b>	$\checkmark$		
a'				V

$$\eta = ab + ac' + a'b'c$$

f. 
$$\mu=abc+abc'+ab'c+ab'c'+a'bc+a'bc'+a'b'c+a'b'c'$$

\	bc	bc'	b'c'	b'c
a	<b>V</b>	V		<b>\</b>
a'	<b>V</b>	V	$\checkmark$	

Existe apenas **uma** forma disjuntiva mínima possível:

$$\mu = 1$$

g. 
$$\nu = ab + a'bc' + a'b'c = abc + abc' + a'bc' + a'b'c$$

\	bc	bc'	b'c'	b'c
a	V			
a'				

$$\therefore \nu = ab + bc' + a'b'c$$

h. 
$$ho=ac+abc'+a'bc+a'b'c=abc+ab'c+abc'+a'bc+a'b'c$$

\	bc	bc'	b'c'	b'c
a	V		V	V
a'	V			

Existe apenas **uma** forma disjuntiva mínima possível:

$$\rho = ab' + c$$

## 3.

a. 
$$lpha = \sum m(3,5,7,13,14,15) = 0011,0101,0111,1101,1110,1111$$

\	*00 (z'w') *	01 (z'w)	11 (zw)	10 (zw')
00 (x'y')			<b>V</b>	
01(x'y)		<b>V</b>	<b>V</b>	
11 (xy)		<b>V</b>	<b>V</b>	<b>V</b>
10 (xy')				

Existe apenas **uma** forma disjuntiva mínima possível:

$$\alpha(x, y, z, w) = yw + x'zw + xyz$$

**b.** 
$$\beta = \sum m(3,4,5,6,7,8,12) = 0011,0100,0101,0110,0111,1000,1100$$

\	00 (z'w')	01 (z'w)	11 (zw)	10 (zw')
00 (x'y')			<b>V</b>	
01 (x'y)	<b>V</b>	<b>V</b>	<b>V</b>	<b>V</b>
11 (xy)	<b>V</b>			
10 (xy')	<b>V</b>			

Existe apenas **uma** forma disjuntiva mínima possível:

$$eta(x,y,z,w) = xz'w' + x'y + x'zw$$

c. 
$$\gamma = \sum m(0,1,2,3,4,5,6,7) = 000,001,010,011,100,101,110,111$$

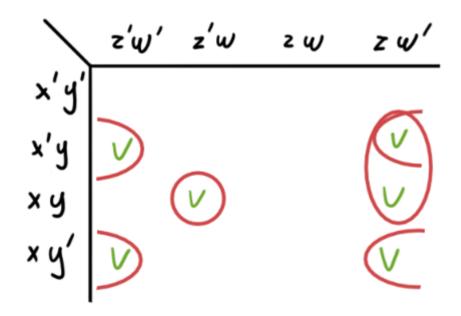
\	00 (y'z')	01 (y'z)	11 (yz)	10 (yz')
0 (x')	V	$\checkmark$	V	<b>~</b>
1 (x)	V	V	V	V

$$\gamma(x,y,z,w)=1$$

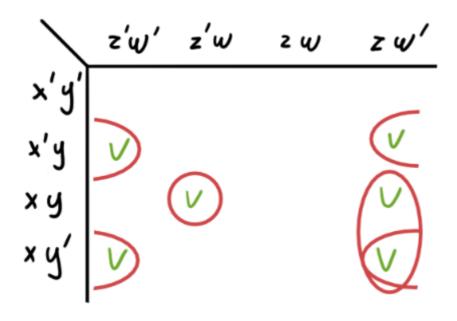
d. 
$$\delta = \sum m(4,6,8,10,13,14) = 0100,0110,1000,1010,1101,1110$$

\	00 (z'w')	01 (z'w)	11 (zw)	10 (zw')
00 (x'y')				
01 (x'y)	V			
11 (xy)		V		V
10 (x'y)	V			V

Existem **duas** formas disjuntivas mínimas possíveis:



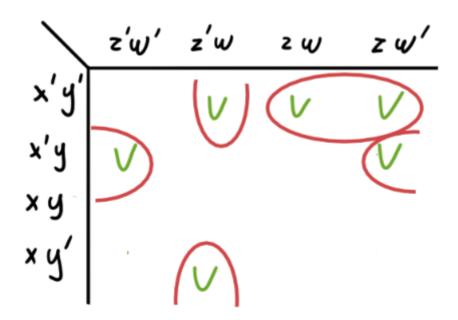
$$\delta(x,y,z,w) = xyz'w + xy'w' + x'yw' + yzw'$$



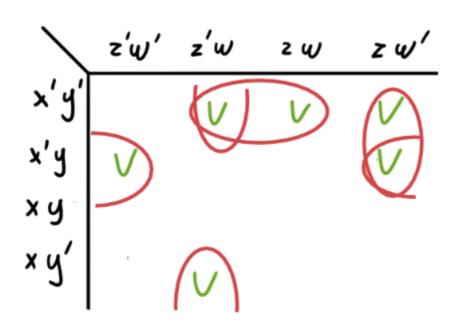
$$\delta(x,y,z,w)=xyz'w+xy'w'+x'yw'+xzw'$$
 e.  $\eta=\sum m(1,2,3,4,6,9)=0001,0010,0011,0100,0110,1001$ 

\	00 (z'w')	01 (z'w)	11 (zw)	10 (zw')
00 (x'y')		<b>V</b>	<b>V</b>	
01 (x'y)	V			<b>V</b>
11 (xy)				
10 (xy')		V		

Existem **duas** formas disjuntivas mínimas possíveis:



 $\eta(x,y,z,w) = x'yw' + x'y'z + y'z'w$ 



$$\eta(x,y,z,w) = x'yw' + x'y'w + x'zw' + y'z'w$$

f. 
$$\mu = \sum m(0,1,2,4,8) = 0000,0001,0010,0100,1000$$

\	00 (z'w')	01 (z'w)	11 (zw)	10 (zw')
00 (x'y')	V	<b>V</b>		<b>V</b>
01 (x'y)	V			
11 (xy)				
10 (xy')	V			

Existe apenas **uma** forma disjuntiva mínima possível:

$$\mu(x,y,z,w)=y'z'w'+x'y'w'+x'y'z'+x'z'w'$$

4.

$$\mathbf{a.}~ab'+c$$

**b.** 
$$ab + b'c' + a'b'$$

c. 
$$bc + a'b + ab'$$

$$\mathbf{d}. a' + c$$

**5.** 

a. 
$$a'c + abc + ac'd' + a'b'$$

**b.** 
$$a'cd + b'cd' + ab'd' + abc'd$$

c. 
$$a'c + a'd' + cd' + ab'c'$$

d. 
$$bc + ab' + b'c'$$

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