

Number theory

Wilson's theorem

A natural number $n > 1$ is a prime number if and only if the product of all the positive integers less than n is one less than a multiple of n .

$$(n - 1)! \equiv -1 \pmod{n} \Leftrightarrow n \text{ is a prime number}$$

In other words, a number n is a prime number if, and only if, $(n - 1)! + 1$ is divisible by n .