

Name: Swapnil

Group: 2CS12

Roll Number: 102016108

Artificial Intelligence (AI)

UCS411

Assignment-3

Question-1: If the initial and final states are as below, find the value of Heuristic function, by taking

- Euclidean Distance

Initial:

2		3
1	8	4
7	6	5

Goal:

1	2	3
8		4
7	6	5

Code:

```
from copy import deepcopy

class Puzzle:

    def __init__(self, initial_state):
        self.initial = initial_state
        self.queue = []
        self.visited = []

    def _find_pos(self, state):
        for i in range(3):
            for j in range(3):
                if state[i][j] == 0:
                    return i, j

    def _right(self, state, pos):
        i, j = pos

        if j != 2:
            t = deepcopy(state)
```

```

        t[i][j], t[i][j+1] = t[i][j+1], t[i][j]

        return t

    else:

        return state

def _left(self, state, pos):

    i, j = pos

    if j != 0:

        t = deepcopy(state)

        t[i][j], t[i][j-1] = t[i][j-1], t[i][j]

        return t

    else:

        return state

def _up(self, state, pos):

    i, j = pos

    if i != 0:

        t = deepcopy(state)

        t[i][j], t[i-1][j] = t[i-1][j], t[i][j]

```

```

        return t

    else:

        return state

def _down(self, state, pos):

    i, j = pos

    if i != 2:

        t = deepcopy(state)

        t[i][j], t[i+1][j] = t[i+1][j], t[i][j]

        return t

    else:

        return state

def _enqueue(self, new_state):

    x = self._heu_el(new_state)

    if len(self.queue) == 0:

        self.queue.append(new_state)

```

```

elif x < self._heu_el(self.queue[0]):
    self.queue.insert(0, new_state)
else:
    for i in range(1, len(self.queue)):
        if self._heu_el(self.queue[i]) > x:
            self.queue.insert(i-1, new_state)

def _deque(self):
    self.visited.append(self.queue[0])

    ele = self.queue.pop(0)

    return ele

def _heu_el(self, state):
    val = 0

    for x in range(3):
        for i in range(3):

```

```

        q = state[x][i]

        for j in range(3):
            for k in range(3):
                if q == self.goal[j][k] and not (x == j and i
== k):

                    val += pow(abs(x-j)+abs(i-k),2)

                    break

            return pow(val,1/2)

def _print(self, vis):
    for k in range(len(vis)-1):
        x = vis[k]

        for i in range(3):
            for j in range(3):
                print(x[i][j], end=" ")

            print("\n")

        print("  |")
        print("  |")
        print("  V")

    x = vis[-1]

    for i in range(3):

```

```
for j in range(3):  
    print(x[i][j], end=" ")  
print("\n")
```

```
def Solve(self, goal_state):
```

```
    current_state = deepcopy(self.initial)  
    self.goal = goal_state  
    if current_state == goal_state:  
        return
```

```
    while 1:  
        pos = self._find_pos(current_state)  
        new_state = self._down(current_state, pos)  
        if new_state != current_state:  
            if new_state == goal_state:  
                print("Goal State Reached!!")  
                self.visited.append(new_state)  
                self._print(self.visited)  
                return  
            else:
```

```

        if new_state not in self.visited:
            self._enqueue(new_state)

new_state = self._left(current_state, pos)
if new_state != current_state:
    if new_state == goal_state:
        print("Goal State Reached!!")
        self.visited.append(new_state)

        self._print(self.visited)
        return
    else:
        if new_state not in self.visited:
            self._enqueue(new_state)

new_state = self._right(current_state, pos)
if new_state != current_state:
    if new_state == goal_state:
        print("Goal State Reached!!")
        self.visited.append(new_state)

```



```
        self._print(self.visited)
        return
    else:
        if new_state not in self.visited:
            self._enqueue(new_state)

new_state = self._up(current_state, pos)
if new_state != current_state:
    if new_state == goal_state:
        print("Goal State Reached!!")
        self.visited.append(new_state)

        self._print(self.visited)
        return
    else:
        if new_state not in self.visited:
            self._enqueue(new_state)
```

```
if len(self.queue) > 0:
    current_state = self._deque()
else:
    print("Not Found!")
    return
```

```
if __name__ == '__main__':
    P = Puzzle([[2, 0, 3], [1, 8, 4], [7, 6, 5]])
    P.Solve([[1, 2, 3], [8, 0, 4], [7, 6, 5]])
```

Output:

Goal State Reached!!

2 8 3

1 0 4

7 6 5

|

|

V

2 0 3

1 8 4

7 6 5

|

|

V

0 2 3

1 8 4

7 6 5

|

|

V

1 2 3

0 8 4

7 6 5

|

|

V

1 2 3

8 0 4

7 6 5

...Program finished with exit code 0

Press ENTER to exit console.

- **Manhattan Distance**

Initial:

2		3
1	8	4
7	6	5

Goal:

1	2	3
8		4
7	6	5

Code:

```
from copy import deepcopy

class Puzzle:

    def __init__(self, initial_state):
        self.initial = initial_state
        self.queue = []
        self.visited = []

    def _find_pos(self, state):
        for i in range(3):
            for j in range(3):
```

```

        if state[i][j] == 0:
            return i,j

def _right(self,state,pos):
    i,j = pos

    if j != 2:
        t = deepcopy(state)
        t[i][j],t[i][j+1] = t[i][j+1],t[i][j]
        return t
    else:
        return state

def _left(self,state,pos):
    i,j = pos

    if j!=0:
        t= deepcopy(state)
        t[i][j],t[i][j-1] = t[i][j-1],t[i][j]
        return t
    else:
        return state

```

```

def _up(self, state, pos):
    i, j = pos

    if i != 0:
        t= deepcopy(state)
        t[i][j],t[i-1][j] = t[i-1][j],t[i][j]
        return t
    else:
        return state

def _down(self, state, pos):
    i, j = pos

    if i != 2:
        t=deepcopy(state)
        t[i][j],t[i+1][j] = t[i+1][j],t[i][j]
        return t
    else:
        return state

def _enqueue(self, new_state):

```

```
x =self._heu_man(new_state)
```

```
if len(self.queue) == 0:
```

```
    self.queue.append(new_state)
```

```
elif x < self._heu_man(self.queue[0]):
```

```
    self.queue.insert(0,new_state)
```

```
else:
```

```
    for i in range(1,len(self.queue)):
```

```
        if self._heu_man(self.queue[i]) > x:
```

```
            self.queue.insert(i-1,new_state)
```

```
def _deque(self):
```

```
    self.visited.append(self.queue[0])
```

```
    ele = self.queue.pop(0)
```

```
    return ele
```

```

def _heu_man(self, state):
    val = 0

    for x in range(3):
        for i in range(3):
            q = state[x][i]

            for j in range(3):
                for k in range(3):
                    if q == self.goal[j][k] and not (x == j and
i==k):
                        val += abs(x-j)+abs(i-k)
                        break

    return val

```

```

def _print(self, vis):
    for k in range(len(vis)-1):
        x = vis[k]

        for i in range(3):
            for j in range(3):
                print(x[i][j], end=" ")

```



```
        print("\n")
    print("  |")
    print("  |")
    print("  V")
x = vis[-1]
for i in range(3):
    for j in range(3):
        print(x[i][j],end=" ")
    print("\n")
```

```
def Solve(self,goal_state):
```

```
    current_state = deepcopy(self.initial)
```

```
    self.goal = goal_state
```

```
    if current_state == goal_state:
```

```
        return
```

```
    while 1:
```

```
        pos = self._find_pos(current_state)
```

```
        new_state = self._down(current_state,pos)
```

```

if new_state != current_state:
    if new_state == goal_state:
        print("Goal State Reached!!")
        self.visited.append(new_state)

        self._print(self.visited)
        return
    else:
        if new_state not in self.visited:
            self._enqueue(new_state)

new_state = self._left(current_state,pos)
if new_state != current_state:
    if new_state == goal_state:
        print("Goal State Reached!!")
        self.visited.append(new_state)

        self._print(self.visited)
        return
    else:
        if new_state not in self.visited:

```

```

        self._enqueue(new_state)

new_state = self._right(current_state,pos)
if new_state != current_state:
    if new_state == goal_state:
        print("Goal State Reached!!")
        self.visited.append(new_state)

        self._print(self.visited)
        return
    else:
        if new_state not in self.visited:
            self._enqueue(new_state)

new_state = self._up(current_state,pos)
if new_state != current_state:
    if new_state == goal_state:
        print("Goal State Reached!!")
        self.visited.append(new_state)

        self._print(self.visited)

```

```
        return
    else:
        if new_state not in self.visited:
            self._enqueue(new_state)
```

```
if len(self.queue) > 0:
    current_state = self._deque()
else:
    print("Not Found!")
    return
```

```
if __name__ == '__main__':
    P = Puzzel([[2,0,3],[1,8,4],[7,6,5]])
    P.Solve([[1,2,3],[8,0,4],[7,6,5]])
```

Output:

```
Goal State Reached!!
2 8 3

1 0 4

7 6 5

  |
  |
  v
2 0 3

1 8 4

7 6 5

  |
  |
  v
0 2 3

1 8 4

7 6 5

  |
  |
  v
1 2 3

0 8 4

7 6 5

  |
  |
  v
1 2 3

8 0 4

7 6 5

...Program finished with exit code 0
Press ENTER to exit console.
```

- **Minkowski Distance**

Initial:

2		3
1	8	4
7	6	5

Goal:

1	2	3
8		4
7	6	5

Code:

```
from copy import deepcopy

class Puzzel:

    def __init__(self, initial_state):
        self.initial = initial_state
        self.queue = []
        self.visited = []

    def _find_pos(self, state):
        for i in range(3):
```

```
    for j in range(3):
        if state[i][j] == 0:
            return i, j
```

```
def _right(self, state, pos):
```

```
    i, j = pos
```

```
    if j != 2:
```

```
        t = deepcopy(state)
```

```
        t[i][j], t[i][j+1] = t[i][j+1], t[i][j]
```

```
        return t
```

```
    else:
```

```
        return state
```

```
def _left(self, state, pos):
```

```
    i, j = pos
```

```
    if j != 0:
```

```
        t = deepcopy(state)
```

```
        t[i][j], t[i][j-1] = t[i][j-1], t[i][j]
```

```
        return t
```

```

        else:
            return state

def _up(self, state, pos):
    i, j = pos

    if i != 0:
        t = deepcopy(state)
        t[i][j], t[i-1][j] = t[i-1][j], t[i][j]
        return t
    else:
        return state

def _down(self, state, pos):
    i, j = pos

    if i != 2:
        t = deepcopy(state)
        t[i][j], t[i+1][j] = t[i+1][j], t[i][j]
        return t
    else:

```



```
    return state
```

```
def _enqueue(self, new_state):
```

```
    x = self._heu_mok(new_state)
```

```
    if len(self.queue) == 0:
```

```
        self.queue.append(new_state)
```

```
    elif x < self._heu_mok(self.queue[0]):
```

```
        self.queue.insert(0, new_state)
```

```
    else:
```

```
        for i in range(1, len(self.queue)):
```

```
            if self._heu_mok(self.queue[i]) > x:
```

```
                self.queue.insert(i-1, new_state)
```

```
def _deque(self):
```

```
    self.visited.append(self.queue[0])
```

```

        ele = self.queue.pop(0)

    return ele

def _heu_mok(self, state):
    val = 0

    for x in range(3):
        for i in range(3):
            q = state[x][i]

            for j in range(3):
                for k in range(3):
                    if q == self.goal[j][k] and not (x == j and i
== k):
                        val += pow(abs(x-j)+abs(i-k),3)
                        break

    return pow(val,1/3)

def _print(self, vis):
    for k in range(len(vis)-1):

```

```

x = vis[k]
for i in range(3):
    for j in range(3):
        print(x[i][j], end=" ")
    print("\n")
print("  |")
print("  |")
print("  V")
x = vis[-1]
for i in range(3):
    for j in range(3):
        print(x[i][j], end=" ")
    print("\n")

```

```

def Solve(self, goal_state):

```

```

    current_state = deepcopy(self.initial)
    self.goal = goal_state
    if current_state == goal_state:
        return

```

```

while 1:

    pos = self._find_pos(current_state)

    new_state = self._down(current_state, pos)

    if new_state != current_state:

        if new_state == goal_state:

            print("Goal State Reached!!!")

            self.visited.append(new_state)


            self._print(self.visited)

            return

        else:

            if new_state not in self.visited:

                self._enqueue(new_state)


    new_state = self._left(current_state, pos)

    if new_state != current_state:

        if new_state == goal_state:

            print("Goal State Reached!!!")

            self.visited.append(new_state)

```

```
        self._print(self.visited)
        return
    else:
        if new_state not in self.visited:
            self._enqueue(new_state)

new_state = self._right(current_state, pos)
if new_state != current_state:
    if new_state == goal_state:
        print("Goal State Reached!!")
        self.visited.append(new_state)

        self._print(self.visited)
        return
    else:
        if new_state not in self.visited:
            self._enqueue(new_state)
```

```
new_state = self._up(current_state, pos)
if new_state != current_state:
    if new_state == goal_state:
        print("Goal State Reached!!")
        self.visited.append(new_state)

        self._print(self.visited)
        return
    else:
        if new_state not in self.visited:
            self._enqueue(new_state)
```

```
if len(self.queue) > 0:
    current_state = self._deque()
else:
    print("Not Found!")
    return
```

```
if __name__ == '__main__':
```

```
P = Puzzle([[2, 0, 3], [1, 8, 4], [7, 6, 5]])  
P.Solve([[1, 2, 3], [8, 0, 4], [7, 6, 5]])
```

Output:

```

Goal State Reached!!
2 8 3

1 0 4

7 6 5

  |
  |
  v
2 0 3

1 8 4

7 6 5

  |
  |
  v
0 2 3

1 8 4

7 6 5

  |
  |
  v
1 2 3

0 8 4

7 6 5

  |
  |
  v
1 2 3

8 0 4

7 6 5

...Program finished with exit code 0
Press ENTER to exit console.

```

Question-2: If the initial and final states are as below and $H(n)$: number of misplaced tiles in the current state n as compared to the goal node need to be considered as the heuristic function. You need to use BestFirst Search algorithm.

Initial:

2		3
1	8	4
7	6	5

Goal:

1	2	3
8		4
7	6	5

Code:

```
import copy
```

```
class MyEightPuzzle:
```

```
    def __init__(self, startState, goalState):
```

```
        self.currentState=startState
```

```
        self.goalState=goalState
```

```
        self.emptyIndex=self.emptyTileIndex()
```

```
        self.prevState=None
```

```
    def up(self):
```

```
        if self.emptyIndex==6 or self.emptyIndex==7 or  
self.emptyIndex==8:
```

```
            return False
```

```
        else:
```

```
            self.prevState=copy.deepcopy(self)
```

```
self.currentState[self.emptyIndex]=self.currentState[self.emptyIndex+3]  
]
```

```
    self.currentState[self.emptyIndex+3]=0
```

```
    self.emptyIndex=self.emptyIndex+3
```

```
    return True
```

```
def down(self):
```

```
    if self.emptyIndex==0 or self.emptyIndex==1 or  
    self.emptyIndex==2:
```

```
        return False
```

```
    else:
```

```
        self.prevState=copy.deepcopy(self)
```

```
self.currentState[self.emptyIndex]=self.currentState[self.emptyIndex-  
3]
```

```
    self.currentState[self.emptyIndex-3]=0
```

```
    self.emptyIndex=self.emptyIndex-3
```

```
    return True
```

```
def left(self):
```

```
    if self.emptyIndex==2 or self.emptyIndex==5 or  
    self.emptyIndex==8:
```

```
        return False
```

```
    else:
```

```

        self.prevState=copy.deepcopy(self)

self.currentState[self.emptyIndex]=self.currentState[self.emptyIndex+1
]

        self.currentState[self.emptyIndex+1]=0

        self.emptyIndex=self.emptyIndex+1

        return True


def right(self):

    if self.emptyIndex==0 or self.emptyIndex==3 or
self.emptyIndex==6:

        #print("Cannot move")

        return False

    else:

        self.prevState=copy.deepcopy(self)

self.currentState[self.emptyIndex]=self.currentState[self.emptyIndex-
1]

        self.currentState[self.emptyIndex-1]=0

        self.emptyIndex=self.emptyIndex-1

        return True


def displayState(self):

    print("-----")

```

```
        for i in range(0, 8, 3):  
            print(self.currentState[i], self.currentState[i+1],  
self.currentState[i+2])
```

```
def emptyTileIndex(self):  
    for i in range(0, 9):  
        if self.currentState[i]==0:  
            return i
```

```
def isGoalReached(self):  
    if self.currentState==self.goalState:  
        return True  
    else:  
        return False
```

```
def _eq_(self, other):  
    return self.currentState==other.currentState
```

```
def possibleNextStates(self):  
    stateList=[]  
  
    up_state=copy.deepcopy(self)
```

```
if up_state.up():
    stateList.append(up_state)

down_state=copy.deepcopy(self)
if down_state.down():
    stateList.append(down_state)

left_state=copy.deepcopy(self)
if left_state.left():
    stateList.append(left_state)

right_state=copy.deepcopy(self)
if right_state.right():
    stateList.append(right_state)

return stateList
```

```
def heuristic(self):
    count=0
    for i in range(0, 9):
```

```
        if self.goalState[i]!=self.currentState[i] and  
self.goalState[i]!=0:
```

```
            count=count+1
```

```
    return count
```

```
def constructPath(goalState):
```

```
    print("The solution path from Goal to Start")
```

```
    while goalState is not None:
```

```
        goalState.displayState()
```

```
        goalState=goalState.prevState
```

```
def BestFirstSearch(startState):
```

```
    open=[]
```

```
    closed=[]
```

```
    open.append(startState)
```

```
    while open:
```

```
thisState=open.pop(0)
thisState.displayState()
closed.append(thisState)
```

```
if thisState.isGoalReached():
    print("Goal state found.. stopping search")
    constructPath(thisState)
    break
```

```
nextStates=thisState.possibleNextStates()
```

```
for eachState in nextStates:
    if eachState not in open and eachState not in closed:
        open.append(eachState)
        open.sort(key=heuristic)
```

```
start=[2, 0, 3, 1, 8, 4, 7, 6, 5]
goal= [1, 2, 3, 8, 0, 4, 7, 6, 5]
problem=MyEightPuzzle(start, goal)
BestFirstSearch(problem)
```

Output:


```
-----  
2 0 3  
1 8 4  
7 6 5  
-----
```

```
0 2 3  
1 8 4  
7 6 5  
-----
```

```
1 2 3  
0 8 4  
7 6 5  
-----
```

```
1 2 3  
8 0 4  
7 6 5
```

```
Goal state found.. stopping search  
The solution path from Goal to Start  
-----
```

```
1 2 3  
8 0 4  
7 6 5  
-----
```

```
1 2 3  
0 8 4  
7 6 5  
-----
```

```
0 2 3  
1 8 4  
7 6 5  
-----
```

```
2 0 3  
1 8 4  
7 6 5
```

```
...Program finished with exit code 0  
Press ENTER to exit console. 
```

Question-3: If the initial and final states are as below and $H(n)$: number of misplaced tiles in the current state n as compared to the goal node need to be considered as the heuristic function. You need to use Hill Climbing algorithm.

Initial:	2		3
	1	8	4
	7	6	5

Goal:	1	2	3
	8		4
	7	6	5

Code:

```
import copy

class MyEightPuzzle:

    def __init__(self, startState, goalState):

        self.currentState=startState

        self.goalState=goalState

        self.emptyIndex=self.emptyTileIndex()

        self.prevState=None

    def up(self):
```

```

        if self.emptyIndex==6 or self.emptyIndex==7 or
self.emptyIndex==8:

            return False

        else:

            self.prevState=copy.deepcopy(self)

self.currentState[self.emptyIndex]=self.currentState[self.emptyIndex+3
]

            self.currentState[self.emptyIndex+3]=0

            self.emptyIndex=self.emptyIndex+3

            return True


def down(self):

    if self.emptyIndex==0 or self.emptyIndex==1 or
self.emptyIndex==2:

        return False

    else:

        self.prevState=copy.deepcopy(self)

self.currentState[self.emptyIndex]=self.currentState[self.emptyIndex-
3]

            self.currentState[self.emptyIndex-3]=0

            self.emptyIndex=self.emptyIndex-3

            return True

```

```

def left(self):

    if self.emptyIndex==2 or self.emptyIndex==5 or
self.emptyIndex==8:

        return False

    else:

        self.prevState=copy.deepcopy(self)

self.currentState[self.emptyIndex]=self.currentState[self.emptyIndex+1
]

        self.currentState[self.emptyIndex+1]=0

        self.emptyIndex=self.emptyIndex+1

        return True


def right(self):

    if self.emptyIndex==0 or self.emptyIndex==3 or
self.emptyIndex==6:

        return False

    else:

        self.prevState=copy.deepcopy(self)

self.currentState[self.emptyIndex]=self.currentState[self.emptyIndex-
1]

        self.currentState[self.emptyIndex-1]=0

        self.emptyIndex=self.emptyIndex-1

        return True

```

```
def displayState(self):  
    print("-----")  
    for i in range(0, 8, 3):  
        print(self.currentState[i], self.currentState[i+1],  
self.currentState[i+2])
```

```
def emptyTileIndex(self):  
    for i in range(0, 9):  
        if self.currentState[i]==0:  
            return i
```

```
def isGoalReached(self):  
    if self.currentState==self.goalState:  
        return True  
    else:  
        return False
```

```
def _eq_(self, other):  
    return self.currentState==other.currentState
```

```
def possibleNextStates(self):
```

```
stateList=[]
```

```
up_state=copy.deepcopy(self)
```

```
if up_state.up():
```

```
    stateList.append(up_state)
```

```
down_state=copy.deepcopy(self)
```

```
if down_state.down():
```

```
    stateList.append(down_state)
```

```
left_state=copy.deepcopy(self)
```

```
if left_state.left():
```

```
    stateList.append(left_state)
```

```
right_state=copy.deepcopy(self)
```

```
if right_state.right():
```

```
    stateList.append(right_state)
```

```
return stateList
```

```
def heuristic(self):
```

```
        count=0

        for i in range(0, 9):

            if self.goalState[i]!=self.currentState[i] and
self.goalState[i]!=0:

                count=count+1

        return count
```

```
def constructPath(goalState):

    print("The solution path from Goal to Start")

    while goalState is not None:

        goalState.displayState()

        goalState=goalState.prevState
```

```
def HillClimbing(startState):

    open=[]

    closed=[]

    open.append(startState)
```

```
    while open:
```

```
thisState=open.pop(0)
```

```
thisState.displayState()
```

```
if thisState.isGoalReached():
```

```
    print("Goal state found.. stopping search")
```

```
    constructPath(thisState)
```

```
    break
```

```
nextStates=thisState.possibleNextStates()
```

```
for eachState in nextStates:
```

```
    if eachState not in open and eachState not in closed:
```

```
        if eachState.heuristic() < thisState.heuristic():
```

```
            open.append(eachState)
```

```
            closed.append(thisState)
```



```
start=[2, 0, 3, 1, 8, 4, 7, 6, 5]  
goal= [1, 2, 3, 8, 0, 4, 7, 6, 5]  
problem=MyEightPuzzle(start, goal)  
HillClimbing(problem)
```

Output:

```
-----  
2 0 3  
1 8 4  
7 6 5  
-----
```

```
0 2 3  
1 8 4  
7 6 5  
-----
```

```
1 2 3  
0 8 4  
7 6 5  
-----
```

```
1 2 3  
8 0 4  
7 6 5  
-----
```

```
Goal state found.. stopping search  
The solution path from Goal to Start  
-----
```

```
1 2 3  
8 0 4  
7 6 5  
-----
```

```
1 2 3  
0 8 4  
7 6 5  
-----
```

```
0 2 3  
1 8 4  
7 6 5  
-----
```

```
2 0 3  
1 8 4  
7 6 5  
-----
```

```
...Program finished with exit code 0  
Press ENTER to exit console. 
```

Question-4: If the initial and final states are as below and $H(n)$: Manhattan distance as the heuristic function. You need to use Best First Search algorithm.

2	8	3
1	5	4
7	6	

Initial State



1	2	3
8		4
7	6	5

Final State

Code:

```
import copy
```

```
class MyEightPuzzle:
```

```
    def __init__(self, startState, goalState):
```

```
        self.currentState=startState
```

```
        self.goalState=goalState
```

```
        self.emptyIndex=self.emptyTileIndex()
```

```
        self.prevState=None
```

```

def up(self):

    if self.emptyIndex==6 or self.emptyIndex==7 or
self.emptyIndex==8:

        return False

    else:

        self.prevState=copy.deepcopy(self)

self.currentState[self.emptyIndex]=self.currentState[self.emptyIndex+3
]

        self.currentState[self.emptyIndex+3]=0

        self.emptyIndex=self.emptyIndex+3

        return True


def down(self):

    if self.emptyIndex==0 or self.emptyIndex==1 or
self.emptyIndex==2:

        return False

    else:

        self.prevState=copy.deepcopy(self)

self.currentState[self.emptyIndex]=self.currentState[self.emptyIndex-
3]

```

```
self.currentState[self.emptyIndex-3]=0
```

```
self.emptyIndex=self.emptyIndex-3
```

```
return True
```

```
def left(self):
```

```
    if self.emptyIndex==2 or self.emptyIndex==5 or  
self.emptyIndex==8:
```

```
        return False
```

```
    else:
```

```
        self.prevState=copy.deepcopy(self)
```

```
self.currentState[self.emptyIndex]=self.currentState[self.emptyIndex+1  
]
```

```
self.currentState[self.emptyIndex+1]=0
```

```
self.emptyIndex=self.emptyIndex+1
```

```
return True
```

```
def right(self):
```

```
    if self.emptyIndex==0 or self.emptyIndex==3 or  
self.emptyIndex==6:
```

```
        return False
```

```
    else:
```

```
        self.prevState=copy.deepcopy(self)
```

```
self.currentState[self.emptyIndex]=self.currentState[self.emptyIndex-1]
```

```
    self.currentState[self.emptyIndex-1]=0
```

```
    self.emptyIndex=self.emptyIndex-1
```

```
    return True
```

```
def displayState(self):
```

```
    print("-----")
```

```
    for i in range(0, 8, 3):
```

```
        print(self.currentState[i], self.currentState[i+1],  
self.currentState[i+2])
```

```
def emptyTileIndex(self):
```

```
    for i in range(0, 9):
```

```
        if self.currentState[i]==0:
```

```
            return i
```

```
def isGoalReached(self):
```

```
    if self.currentState==self.goalState:
```

```
        return True
```

```
    else:
```

```
        return False
```

```
def _eq_(self, other):  
    return self.currentState==other.currentState  
  
def possibleNextStates(self):  
    stateList=[]  
  
    up_state=copy.deepcopy(self)  
    if up_state.up():  
        stateList.append(up_state)  
  
    down_state=copy.deepcopy(self)  
    if down_state.down():  
        stateList.append(down_state)  
  
    left_state=copy.deepcopy(self)  
    if left_state.left():  
        stateList.append(left_state)  
  
    right_state=copy.deepcopy(self)  
    if right_state.right():
```

```
stateList.append(right_state)
```

```
return stateList
```

```
def heuristic(self):
```

```
    sum=0
```

```
    for i in range(0, 9):
```

```
        goalNode=self.goalState[i]
```

```
        if goalNode==0:
```

```
            continue
```

```
        goalIndex=i
```

```
    for j in range(0, 9):
```

```
        currentNode=self.currentState[j]
```

```
        if currentNode==goalNode:
```

```
            currentIndex=j
```

```
            break
```

```
    difference=abs(goalIndex-currentIndex)
```

```
    if difference<3:
```



```
        moves=difference

    elif difference>=3 and difference<6:

        moves=difference%3 + 1

    elif difference>=6 and difference<8:

        moves=difference%3 + 2


    sum=sum+moves

    return sum
```

```
def constructPath(goalState):

    print("The solution path from Goal to Start")

    while goalState is not None:

        goalState.displayState()

        goalState=goalState.prevState
```

```
def BestFirstSearch(startState):

    open=[]

    closed=[]


    open.append(startState)
```

```
while open:
```

```
    thisState=open.pop(0)
```

```
    thisState.displayState()
```

```
    closed.append(thisState)
```

```
    if thisState.isGoalReached():
```

```
        print("Goal state found.. stopping search")
```

```
        constructPath(thisState)
```

```
        break
```

```
    nextStates=thisState.possibleNextStates()
```

```
    for eachState in nextStates:
```

```
        if eachState not in open and eachState not in closed:
```

```
open.append(eachState)

open.sort(key=heuristic)
```

```
start=[2, 0, 3, 1, 8, 4, 7, 6, 5]
goal= [1, 2, 3, 8, 0, 4, 7, 6, 5]
problem=MyEightPuzzle(start, goal)
BestFirstSearch(problem)
```

Output:

```
-----  
2 0 3  
1 8 4  
7 6 5  
-----
```

```
2 8 3  
1 0 4  
7 6 5  
-----
```

```
2 3 0  
1 8 4  
7 6 5  
-----
```

```
0 2 3  
1 8 4  
7 6 5  
-----
```

```
1 2 3  
0 8 4  
7 6 5  
-----
```

```
1 2 3  
7 8 4  
0 6 5  
-----
```

```
1 2 3  
8 0 4  
7 6 5  
-----
```

```
Goal state found.. stopping search  
The solution path from Goal to Start  
-----
```

```
1 2 3  
8 0 4  
7 6 5  
-----
```

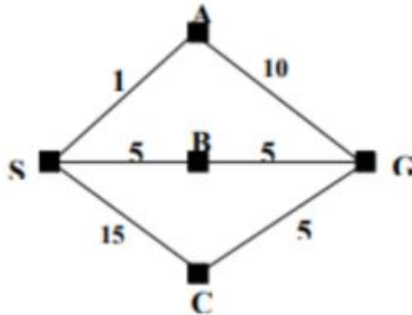
```
1 2 3  
0 8 4  
7 6 5  
-----
```

```
0 2 3  
1 8 4  
7 6 5  
-----
```

```
2 0 3  
1 8 4  
7 6 5  
-----
```

```
...Program finished with exit code 0  
Press ENTER to exit console.
```

Question-5: Solve this given problem using Uniform Cost search. A is the initial state and G is the goal state



Code:

```
import copy
```

```
class MyShortestPath:
```

```
    def __init__(self, map, startCity, goalCity):
```

```
        MyShortestPath.map=map
```

```
        self.currentCity=startCity
```

```
        self.goalCity=goalCity
```

```
        self.visitedList=[]
```

```
        self.cost=0
```

```
        self.visitedList=[]
```

```
        self.visitedList.append(self.currentCity)
```

```
self.prevState=None
```

```
def displayState(self):  
    print("-----")  
    print(f"Current city:{self.currentCity}      Visited  
cities={self.visitedList}      Cost={self.cost}")
```

```
def __gt__(self, other):  
    return self.cost>other.cost
```

```
def __lt__(self, other):  
    return self.cost<other.cost
```

```
def __eq__(self, other):  
    return self.visitedList==other.visitedList
```

```
def isGoalReached(self):  
    if self.goalCity in self.visitedList:  
        return True  
    else:  
        return False
```

```

def move(self, city):

    if city!=self.currentCity and city not in self.visitedList and
MyShortestPath.map[self.currentCity][city]!=0:

        print(f"Moving from city {self.currentCity} to {city}")

        self.cost+=MyShortestPath.map[self.currentCity][city]

        self.currentCity=city

        self.visitedList.append(self.currentCity)

        return True

    else:

        print("Already visited")

        return False


def possibleNextStates(self):

    stateList=[]

    for i in range(0, len(MyShortestPath.map[0])):

        state=copy.deepcopy(self)

        if state.move(i):

            self.prevState=copy.deepcopy(self)

            stateList.append(state)

    return stateList

```

```

def constructPath(goalState):
    print("The solution path from Goal to Start")
    while goalState is not None:
        goalState.displayState()
        goalState=goalState.prevState

open=[]
closed=[]
def UCS(state):
    open.append(state)
    while(open):
        thisState=open.pop(0)
        thisState.displayState()
        if thisState not in closed:
            closed.append(thisState)
            if thisState.isGoalReached():
                print("Goal state found.. stopping search")
                constructPath(thisState)
                break
            else:
                nextStates=thisState.possibleNextStates()
                for eachState in nextStates:

```



```

        if eachState not in open and eachState not in
closed:

        open.append(eachState)

        open.sort()

    elif eachState in open:

        index=open.index(eachState)

        if open[index].cost>eachState.cost:

            open.pop(index)

            open.append(eachState)

            open.sort()

    elif eachState in closed:

        index=closed.index(eachState)

        if closed[index].cost>eachState.cost:

            closed.pop(index)

            closed.append(eachState)

            propagateImprovement(eachState)

```

```

def propagateImprovement(state):

    nextStates=state.possibleNextStates()

    for eachState in nextStates:

        if eachState in open:

            index=open.index(eachState)

            if open[index].cost>eachState.cost:

```

```

        open.pop(index)

        open.append(eachState)

        open.sort()

    if eachState in closed:

        index=closed.index(eachState)

        if closed[index].cost>eachState.cost:

            closed.pop(index)

            closed.append(eachState)

            propagateImprovement(eachState)

map=[[0, 1, 5, 15, 0], [1, 0, 0, 0, 10], [5, 0, 0, 0, 5], [15, 0, 0,
0, 5], [0, 10, 5, 5, 0]]

start=0

goal=4

problem=MyShortestPath(map, start, goal)

UCS(problem)

```

Output:

```
-----  
Current city:0      Visited cities=[0]      Cost=0  
Already visited  
Moving from city 0 to 1  
Moving from city 0 to 2  
Moving from city 0 to 3  
Already visited  
-----  
Current city:1      Visited cities=[0, 1]    Cost=1  
Already visited  
Already visited  
Already visited  
Already visited  
Moving from city 1 to 4  
-----  
Current city:2      Visited cities=[0, 2]    Cost=5  
Already visited  
Already visited  
Already visited  
Already visited  
Moving from city 2 to 4  
-----  
Current city:4      Visited cities=[0, 2, 4] Cost=10  
Goal state found.. stopping search  
The solution path from Goal to Start  
-----  
Current city:4      Visited cities=[0, 2, 4] Cost=10  
-----  
Current city:0      Visited cities=[0]      Cost=0  
  
...Program finished with exit code 0  
Press ENTER to exit console.
```

