

Inducer**geometry.py**

$$\begin{aligned}
 c_{m1i} &= \text{arange}(lower, higher, step) \\
 c_{\theta1i} &= c_{m1i} \tan(\alpha_1) \\
 T_{1i} &= T_{00} - \frac{c_{1i}^2}{2c_p} \\
 M_{1i} &= \frac{c_{1i}}{\sqrt{\gamma RT}} \\
 P_{1i} &= P_{00} \left(\frac{T_{1i}}{T_{00}} \right)^{\frac{\gamma}{\gamma-1}} \\
 \rho_{1i} &= \frac{P_{1i}}{RT_{1i}} \\
 A_{1i} &= \frac{\dot{m}}{\rho c_1 (1-B_1)} \\
 U_{t1i} &= \frac{2\pi r}{60} N \\
 w_{1i} &= \sqrt{c_{\theta1i}^2 + c_{m1i}^2}
 \end{aligned}$$

$$dh_{0s} = \frac{\gamma RT_{00}}{\gamma-1} \left(\Pr \left(\frac{\gamma-1}{\gamma} \right) - 1 \right)$$

$$U_{crit} = \sqrt{\frac{2\sigma_{max}}{\rho_{material}}}$$

$$U_2 = U_{crit}$$

Evaluating for given rotational speed N:

$$U_{t1i} = \frac{2\pi r}{60} N$$

$$w_{1i} = \sqrt{c_{\theta1i}^2 + c_{m1i}^2}$$

w_{1i} is minimized. All arrays are evaluated at index of smallest w_1 in w_{1i} . This index is called $w1ti_index_min$:

$$c_{m1} = c_{m1i}[w1ti_index_min]$$

$$c_{\theta1} = c_{\theta1i}[w1ti_index_min]$$

:

$$w_1 = w_{1i}[w1ti_index_min]$$

$$U_2 = U_1 \frac{r_1}{r_2}$$

If $U_2 > U_{crit}$ rotational speed is adjusted

For all β :

Impeller, diffuser

For all Z_B :

$\sigma = \text{checkSlipFactorSigma}(\dots)$

$\psi, c_{\theta2}, c_{m2}, c_2 = \text{impellerOutletVelocities}(\dots)$

while Pressure ratio not converging:

$$w_x = \frac{dh_{0s}}{\eta}$$

$$T_{02} = T_{00} + w_x \frac{1}{c_p}$$

$$P_{02} = P_{00} \left(\eta w_x \frac{\gamma-1}{\gamma RT_{00}} + 1 \right)^{\frac{\gamma}{\gamma-1}}$$

$$T_2 = T_{02} - \frac{\gamma-1}{2\gamma R} c_2^2$$

$$P_2 = P_{02} \left(\frac{T_2}{T_{02}} \right)^{\frac{\gamma}{\gamma-1}}$$

$$\rho_2, A_2, b_2, M_2 \dots$$

$$P_3, P_{03}, C_3 = \text{diffuserFlow}(\dots)$$

$$\eta_{isen}, PressureEstimate = \text{systemTotalPerformance}(\dots)$$

if pressure ratio not converging

Plotting