

FuncComp Documentation

Daniel Garrett

Sibley School of Mechanical and Aerospace Engineering
Cornell University
Ithaca, NY 14850

ABSTRACT

This document describes the open source software package FuncComp. FuncComp contains two modules which calculate single-visit completeness for an assumed population of planets. The module Functional generates the single-visit completeness using an analytical function approach while MonteCarlo does the same using a Monte Carlo trial approach.

CONTENTS

1	Single-Visit Completeness	3
2	Python Packages	3
3	Supporting Modules	3
3.1	Population	3
3.1.1	Population Class Attributes	4
3.1.2	Population Class Methods	4
3.2	statsFun	4
3.2.1	simpSample Input/Output Description	4
3.3	util	5
3.3.1	maxdmag Input/Output Description	5
3.3.2	mindmag Input/Output Description	5
4	Functional Module	5
4.1	Functional Class Object	6
4.1.1	Initialization Input/Output Description	6
4.1.2	comp Input/Output Description	6
4.2	Jac Input/Output Description	7
4.3	onef_zeta Input/Output Description	7
4.4	onef_R2 Input/Output Description	7
4.5	onef_r Input/Output Description	8
4.6	onef_dmags Input/Output Description	8
4.7	onef_dmagsz Input/Output Description	9
5	MonteCarlo Module	9
5.1	MonteCarlo Class Object	10
5.1.1	Initialization Input/Output Description	10
5.1.2	comp Input/Output Description	10
5.2	oneMCsim Input/Output Description	11

1 Single-Visit Completeness

Obscurational completeness was introduced by Brown as a necessary, but not sufficient, condition for detection of an exoplanet [1]. Assuming distributions for semi-major axis and eccentricity of planetary orbits, Brown defined obscurational completeness as the probability of a planet falling outside a telescope’s central obscuration, thus becoming potentially observable. This concept was expanded to include selection effects due to photometric restrictions on exoplanet observability introduced by telescope optics [2]. Single-visit completeness is determined by the assumption that an exoplanet is observable if its angular separation from its star is greater than the observatory’s inner working angle (IWA) and less than the observatory’s outer working angle (OWA) while also being illuminated such that the difference in brightness between the star and planet (Δmag) is below a limiting value (Δmag_0). The IWA and OWA represent the minimum and maximum angular separation of the field of view. Δmag_0 is where unresolvable confusion between the planet signal and noise occur.

FuncComp provides two modules which calculate single-visit completeness along with other support modules and scripts. The module `MonteCarlo` calculates single-visit completeness using the procedure of Brown [2]. The module `Functional` calculates single-visit completeness using a functional approach (to be published).

2 Python Packages

The following Python packages are used for either `Functional` or `MonteCarlo`:

```
astropy
    astropy.units
copy_reg
matplotlib (optional)
numpy
pp (optional)
scipy
    scipy.integrate
    scipy.interpolate
sys
time (optional)
types
```

The packages `matplotlib` and `time` are used in the demonstration script `Plotting.py` included with FuncComp. The Parallel Python (`pp`) package, if installed, will utilize available cores of multicore processors to compute single-visit completeness.

3 Supporting Modules

FuncComp includes the following supporting modules: `Population`, `statsFun`, and `util`. The `Population` module contains a class object which when instantiated contains probability density functions of the planetary quantities needed for computing single-visit completeness. The `statsFun` module contains a sampling function. The `util` module contains functions calculating the minimum and maximum Δmag for a given separation value.

3.1 Population

The `Population` module contains a class object which when instantiated contains as attributes minimum and maximum values of needed quantities and methods which calculate the probability den-

sity of these quantities. These values and methods may be changed by the user to give the desired planetary population.

3.1.1 Population Class Attributes

The `Population` class object contains the following attributes giving the minimum and maximum values of the planetary population parameters:

arange

Semi-major axis range defined as $[a_{\min}, a_{\max}]$ (astropy Quantity initially set in *AU*)

erange

Eccentricity range defined as $[e_{\min}, e_{\max}]$ (ndarray)

Rrange

Planetary radius range defined as $[R_{\min}, R_{\max}]$ (astropy Quantity initially set in *km*)

prange

Planetary geometric albedo range defined as $[p_{\min}, p_{\max}]$ (ndarray)

3.1.2 Population Class Methods

The `Population` class object contains the following methods which calculate the probability density value for each quantity:

semi_axis

Semi-major axis probability density function (in AU^{-1})

eccentricity

Eccentricity probability density function

Radius

Planetary radius probability density function (in km^{-1})

albedo

Geometric albedo probability density function

3.2 statsFun

The `statsFun` module contains functions which utilize a rejection sampling method to generate samples from a given probability density function. The function used is `simpSample`.

3.2.1 simpSample Input/Output Description

Inputs

f

Probability density function (callable)

numTest

Number of samples desired (integer)

xMin

Minimum value of population (float)

xMax

Maximum value of population (float)

Outputs

X

Array of samples from the population (ndarray)

3.3 util

The `util` module contains two functions `maxdmag` and `mindmag` which calculate the maximum and minimum Δmag for a given separation value and maximum and minimum planet population values.

3.3.1 maxdmag Input/Output Description

Inputs

s

Array of apparent separation in *AU* (ndarray)

ranges

Tuple containing:

pmin : minimum geometric albedo (float)

Rmin : minimum planetary radius in *km* (float)

rmax : maximum planetary distance from star in *AU* (float)

x

Conversion factor for *AU* to *km* (float)

Output

maxdmag

Array of maximum Δmag values (ndarray)

3.3.2 mindmag Input/Output Description

Inputs

s

Array of apparent separation in *AU* (ndarray)

ranges

Tuple containing:

pmax : maximum geometric albedo (float)

Rmax : maximum planetary Radius in *km* (float)

rmin : minimum planetary distance from star in *AU* (float)

rmax : maximum planetary distance from star in *AU* (float)

x

Conversion factor for *AU* to *km* (float)

Output

mindmag

Array of minimum Δmag values (ndarray)

4 Functional Module

The `Functional` module contains the `Functional` class object which when instantiated contains the information for single-visit completeness. The module also contains functions `Jac`, `onef_zeta`, `onef_R2`, `onef_r`, `onef_dmags`, and `onef_dmagsz` which aid in the determination of the single-visit completeness joint probability density function $f_{\bar{s}, \Delta\text{mag}}(s, \Delta\text{mag})$.

4.1 Functional Class Object

4.1.1 Initialization Input/Output Description

Inputs

smin

Minimum apparent separation value in AU , default is zero (float)

smax

Maximum apparent separation value in AU , default is None and the maximum apparent separation is determined based on the assumed population values from the instantiated `Population` object (float)

ns

Number of points in separation to calculate, default is 400 (integer)

dmagmin

Minimum Δmag , default is None and minimum Δmag is determined based on the assumed population values from the instantiated `Population` object (float)

dmagmax

Maximum Δmag , default is None and maximum Δmag is determined based on the assumed population values from the instantiated `Population` object (float)

ndmag

Number of points in Δmag to calculate, default is 400 (integer)

Attributes

s

Points sampled in apparent separation in AU (ndarray)

dmag

Points sampled in Δmag (ndarray)

pc

Single-visit completeness joint probability density function evaluated at s and dmag in $[AU \cdot \text{mag}]^{-1}$ (ndarray)

grid

Interpolant of single-visit completeness joint probability density function $f_{\bar{s}, \overline{\Delta\text{mag}}}(s, \Delta\text{mag})$ in $[AU \cdot \text{mag}]^{-1}$ (callable($s, \Delta\text{mag}$))

pdf

Vectorized version of **grid** (callable($s, \Delta\text{mag}$))

4.1.2 comp Input/Output Description

The method `comp` belonging to the `Functional` class object calculates the single-visit completeness.

Inputs

smin

Array of minimum apparent separation in AU (ndarray)

smax

Array of maximum apparent separation in AU (ndarray)

dmagmin

Array of minimum Δmag values (ndarray)

dmagmax

Array of maximum Δmag values (ndarray)

Output

f

Array of completeness values (ndarray)

4.2 Jac Input/Output Description

The function `Jac` calculates the determinant of the Jacobian matrix of the change of variables necessary for calculating the joint probability density function.

Input

b

Phase angle in *rad* (ndarray)

Output

J

Determinant of Jacobian matrix (ndarray)

4.3 onef_zeta Input/Output Description

The function `onef_zeta` calculates the probability density function $f_{\bar{\zeta}}(\zeta)$ for $\zeta = pR^2$.

Inputs

zetai

Value of $\zeta = pR^2$ in km^2 (float)

pdfs

Tuple containing:

f_p : Probability density function for albedo (callable(p))

f_R : Probability density function for planetary radius in (callable(R))

ranges

Tuple containing:

pmin : minimum value of geometric albedo (float)

pmax : maximum value of geometric albedo (float)

Rmin : minimum value of planetary radius in km (float)

Rmax : maximum value of planetary radius in km (float)

Output

f

Probability density for given zetai in km^{-2} (float)

4.4 onef_R2 Input/Output Description

The function `onef_R2` calculates the probability density of planetary radius squared.

Inputs

R2

Value of planetary radius squared (float)

pdf

Probability density function of planetary radius (callable(R))

Output

f

Value of probability density function of planetary radius squared in km^{-2} (float)

4.5 onef_r Input/Output Description

The function `onef_r` calculates the probability density of orbital radius or distance from the star to the planet.

Inputs

ri

Value of orbital radius in AU (float)

pdfs

Tuple containing:

f_e : probability density function for eccentricity (callable(e))

f_a : probability density function for semi-major axis (callable(a))

ranges

Tuple containing:

amin : minimum semi-major axis in AU (float)

amax : maximum semi-major axis in AU (float)

emin : minimum eccentricity (float)

emax : maximum eccentricity (float)

Output

f

Value of probability density for orbital radius in AU^{-1} (float)

4.6 onef_dmag Input/Output Description

The function `onef_dmag` calculates the single-visit completeness joint probability density of separation and Δmag , $f_{\bar{s}, \Delta mag}(s, \Delta mag)$.

Inputs

dmag

Value of difference in magnitude, Δmag (float)

s

Value of apparent separation in AU (float)

ranges

Tuple containing:

pmin : minimum value of geometric albedo (float)

pmax : maximum value of geometric albedo (float)

Rmin : minimum value of planetary radius in km (float)

Rmax : maximum value of planetary radius in km (float)

rmin : minimum value of orbital radius in AU (float)

rmax : maximum value of orbital radius in AU (float)

zmin : minimum value of $\zeta = pR^2$ in km^2 (float)

zmax : maximum value of $\zeta = pR^2$ in km^2 (float)

val

Value of $\sin^2(\beta^*) \Phi(\beta^*)$ (float)

pdfs

Tuple containing:

f_z : probability density function for $\zeta = pR^2$ (callable(ζ))

f_r : probability density function for orbital radius (callable(r))

funcs

Tuple containing:

binv1 : inverse function of $\sin^2(\beta) \Phi(\beta)$ for $0 < \beta < \beta^*$ (callable(P))

binv2 : inverse function of $\sin^2(\beta) \Phi(\beta)$ for $\beta^* < \beta < \pi$ (callable(P))

x

Conversion factor between AU and km (float)

Output**f**

Joint probability density for given s and $dmag$ in $[AU \cdot mag]^{-1}$ (float)

4.7 onef_dmagsz Input/Output Description

The function `onef_dmagsz` calculates the joint probability density function $f_{\bar{s}, \overline{\Delta mag}, \bar{\zeta}}(s, \Delta mag, \zeta)$.

Inputs**z**

Value of $\zeta = pR^2$ in km^2 (float)

dmag

Value of difference in brightness magnitude, Δmag (float)

s

Value of apparent separation in AU (float)

val

Value of $\sin^2(\beta^*) \Phi(\beta^*)$ (float)

pdfs

Tuple containing:

f_z : probability density function for $\zeta = pR^2$ (callable(ζ))

f_r : probability density function for orbital radius (callable(r))

funcs

Tuple containing:

binv1 : inverse function of $\sin^2(\beta) \Phi(\beta)$ for $0 < \beta < \beta^*$ (callable(P))

binv2 : inverse function of $\sin^2(\beta) \Phi(\beta)$ for $\beta^* < \beta < \pi$ (callable(P))

x

Conversion factor between AU and km (float)

Output**f**

Joint probability density $f_{\bar{s}, \overline{\Delta mag}, \bar{\zeta}}(s, \Delta mag, \zeta)$ in $[AU \cdot mag \cdot km^2]^{-1}$ (float)

5 MonteCarlo Module

The `MonteCarlo` module contains the `MonteCarlo` class object which when instantiated contains the information for single-visit completeness using a Monte Carlo trial approach. The module also

contains the function `oneMCsim` which aids in the determination of the single-visit completeness joint probability density function $f_{\bar{s}, \Delta\text{mag}}(s, \Delta\text{mag})$.

5.1 MonteCarlo Class Object

5.1.1 Initialization Input/Output Description

Inputs

Nplanets

Number of planetary samples, default is 1e6 (float)

bins

Number of bins in apparent separation for 2-D histogram, default is 400 (integer)

bindmag

Number of bins in difference in magnitude for 2-D histogram, default is 400 (integer)

smin

Minimum value of apparent separation in *AU*, default is 0 (float)

smax

Maximum value of apparent separation in *AU*, default is None and maximum value is determined based on assumed planetary population from the instantiated `Population` object (float)

dmagmin

Minimum value of difference in magnitude, default is None and minimum value is determined based on assumed planetary population from the instantiated `Population` object (float)

dmagmax

Maximum value of difference in magnitude, default is None and maximum is determined based on assumed planetary population from the instantiated `Population` object (float)

Attributes

s

Points sampled in apparent separation in *AU* (ndarray)

dmag

Points sampled in Δmag (ndarray)

Hc

Normalized 2-D histogram representing single-visit completeness joint probability density function evaluated at *s* and *dmag* in $[AU \cdot \Delta\text{mag}]^{-1}$ (ndarray)

grid

Interpolant of single-visit completeness joint probability density function $f_{\bar{s}, \Delta\text{mag}}(s, \Delta\text{mag})$ in $[AU \cdot \Delta\text{mag}]^{-1}$ (callable(*s*, Δmag))

pdf

Vectorized version of **grid** (callable(*s*, Δmag))

5.1.2 comp Input/Output Description

The method `comp` belonging to the `MonteCarlo` class object calculates the single-visit completeness.

Inputs

smin

Array of minimum apparent separation in *AU* (ndarray)

smax

Array of maximum apparent separation in *AU* (ndarray)

dmagmin

Array of minimum Δmag values (ndarray)

dmagmax

Array of maximum Δmag values (ndarray)

Output

f

Array of single-visit completeness values (ndarray)

5.2 oneMCsim Input/Output Description

The function `oneMCsim` performs the Monte Carlo trials to help calculate the single-visit completeness joint probability density function $f_{\bar{s}, \Delta\text{mag}}(s, \Delta\text{mag})$.

Inputs

nplan

Number of sample planets (integer)

pdfs

Tuple containing:

f_e : probability density function for eccentricity (callable(e))

f_a : probability density function for semi-major axis (callable(a))

f_R : probability density function for planetary radius (callable(R))

f_p : probability density function for geometric albedo (callable(p))

ranges

Tuple containing:

emin : minimum eccentricity (float)

emax : maximum eccentricity (float)

amin : minimum semi-major axis in *AU* (float)

amax : maximum semi-major axis in *AU* (float)

Rmin : minimum planetary radius in *km* (float)

Rmax : maximum planetary radius in *km* (float)

pmin : minimum geometric albedo (float)

pmax : maximum geometric albedo (float)

smin : minimum apparent separation in *AU* (float)

smax : maximum apparent separation in *AU* (float)

dmagmin : minimum Δmag (float)

dmagmax : maximum Δmag (float)

binh

Tuple containing:

bins : number of bins in apparent separation for 2-D histogram (integer)

bindmag : number of bins in Δmag for 2-D histogram (integer)

x

Conversion factor of *AU* to *km* (float)

Outputs

hc

2-D histogram values for apparent separation and Δmag in $[AU \cdot \text{mag}]^{-1}$ (ndarray)

sedges

Edge values for 2-D histogram bins in apparent separation in AU (ndarray)

dmagedges

Edge values for 2-D histogram bins in Δmag (ndarray)

References

- [1] Brown, R. A., 2004. “Obscurational completeness”. *The Astrophysical Journal*, **607**(2), p. 1003.
- [2] Brown, R. A., 2005. “Single-visit photometric and obscurational completeness”. *The Astrophysical Journal*, **624**(2), p. 1010.