if you keras is not using tensorflow as backend set "KERAS_BACKEND=tensorflow" use this command

Keras -- MLPs on MNIST (10 models trained)

from keras.utils import np_utils

```
from keras.datasets import mnist
import seaborn as sns
from keras.initializers import RandomNormal
            Using TensorFlow backend.
%matplotlib notebook
import matplotlib.pyplot as plt
import numpy as np
import time
# https://gist.github.com/greydanus/f6eee59eaf1d90fcb3b534a25362cea4
# https://stackoverflow.com/a/14434334
# this function is used to update the plots for each epoch and error
def plt_dynamic(x, vy, ty, ax, colors=['b']):
    ax.plot(x, vy, 'b', label="Validation Loss")
    ax.plot(x, ty, 'r', label="Train Loss")
         plt.legend()
         plt.grid()
         fig.canvas.draw()
    This file was updated remotely or in another tab. To force a save, overwriting the last update, select
   Save from the File menu
            Downloading data from <a href="https://s3.amazonaws.com/img-datasets/mnist.npz">https://s3.amazonaws.com/img-datasets/mnist.npz</a>
            print("Number of training examples :", X_train.shape[0], "and each image is of shape (%d, %d)"%(X
print("Number of training examples :", X_test.shape[0], "and each image is of shape (%d, %d)"%(X_
            Number of training examples: 60000 and each image is of shape (28, 28)
            Number of training examples: 10000 and each image is of shape (28, 28)
# if you observe the input shape its 2 dimensional vector
# for each image we have a (28*28) vector
# we will convert the (28*28) vector into single dimensional vector of 1 * 784
X_train = X_train.reshape(X_train.shape[0], X_train.shape[1]*X_train.shape[2])
X_{\text{test}} = X_{\text{test.reshape}}(X_{\text{test.shape}}[0], X_{\text{test.shape}}[1]*X_{\text{test.shape}}[2])
# after converting the input images from 3d to 2d vectors
 print("Number of training examples :", X_train.shape[0], "and each image is of shape (%d)"%(X_train.theorem of training examples :", X_test.shape[0], "and each image is of shape (%d)"%(X_test.theorem of training examples :", X_test.shape[0], "and each image is of shape (%d)"%(X_test.theorem of training examples :", X_test.shape[0], "and each image is of shape (%d)"%(X_test.theorem of training examples :", X_test.shape[0], "and each image is of shape (%d)"%(X_test.theorem of training examples :", X_test.shape[0], "and each image is of shape (%d)"%(X_test.theorem of training examples :", X_test.shape[0], "and each image is of shape (%d)"%(X_test.theorem of training examples :", X_test.shape[0], "and each image is of shape (%d)"%(X_test.theorem of training examples :", X_test.shape[0], "and each image is of shape (%d)"%(X_test.theorem of training examples :", X_test.shape[0], "and each image is of shape (%d)"%(X_test.theorem of training examples :", X_test.theorem of training examples :", X_
            Number of training examples: 60000 and each image is of shape (784)
            Number of training examples: 10000 and each image is of shape (784)
# An example data point
print(X_train[0])
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# if we observe the above matrix each cell is having a value between 0-255
# before we move to apply machine learning algorithms lets try to normalize the
# X => (X - Xmin)/(Xmax-Xmin) = X/255

X_train = X_train/255
X_test = X_test/255

# example data point after normlizing
print(X_train[0])
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# here we are having a class number for each image
print("Class label of first image :", y_train[0])

# lets convert this into a 10 dimensional vector
# ex: consider an image is 5 convert it into 5 => [0, 0, 0, 0, 0, 1, 0, 0, 0, 0]
# this conversion needed for MLPs

Y_train = np_utils.to_categorical(y_train, 10)
Y_test = np_utils.to_categorical(y_test, 10)

print("After converting the output into a vector : ",Y_train[0])

Chass label of first image : 5
    After converting the output into a vector : [0. 0. 0. 0. 0. 1. 0. 0. 0. 0.]
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Softmax classifier

```
# The Sequential model is a linear stack of layers.
# you can create a Sequential model by passing a list of layer instances to the constructor:
# model = Sequential([
#
      Dense(32, input_shape=(784,)),
#
      Activation('relu'),
#
      Dense(10),
      Activation('softmax'),
#])
# You can also simply add layers via the .add() method:
# model = Sequential()
# model.add(Dense(32, input dim=784))
# model.add(Activation('relu'))
# https://keras.io/layers/core/
# keras.layers.Dense(units, activation=None, use_bias=True, kernel_initializer='glorot_uniform',
# bias_initializer='zeros', kernel_regularizer=None, bias_regularizer=None, activity_regularizer=
# kernel_constraint=None, bias_constraint=None)
# Dense implements the operation: output = activation(dot(input, kernel) + bias) where
# activation is the element-wise activation function passed as the activation argument,
# kernel is a weights matrix created by the layer, and
# bias is a bias vector created by the layer (only applicable if use_bias is True).
# output = activation(dot(input, kernel) + bias) => y = activation(WT. X + b)
####
# https://keras.io/activations/
# Activations can either be used through an Activation layer, or through the activation argument
# from keras.layers import Activation, Dense
```

```
# model.add(Dense(64))
# model.add(Activation('tanh'))

# This is equivalent to:
# model.add(Dense(64, activation='tanh'))

# there are many activation functions ar available ex: tanh, relu, softmax

from keras.models import Sequential
from keras.layers import Dense, Activation
```

```
# some model parameters
output_dim = 10
input_dim = X_train.shape[1]
batch_size = 128
nb_epoch = 20
```

* 2 Hidden layers MLP + ReLU + ADAM without batch normalization and d

```
model1_1 = Sequential()
model1_1.add(Dense(512, activation='relu', input_shape=(input_dim,), kernel_initializer=RandomNor
model1 1.add(Dense(128, activation='relu', kernel initializer=RandomNormal(mean=0.0, stddev=0.125

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Save from the File menu
mistory = model1_1.fil(A_train, f_train, battn_size=battn_size, epochs=nb_epoch, verbose=1, varid
```

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Model: "sequential 8"

Layer (type)	Output Shape	Param #
dense_28 (Dense)	(None, 512)	401920
dense_29 (Dense)	(None, 128)	65664
dense_30 (Dense)	(None, 10)	1290
Total params: 468,874 Trainable params: 468,874		

Trainable params: 468,874 Non-trainable params: 0

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```
Epoch 7/20
Epoch 8/20
Epoch 9/20
Epoch 10/20
Epoch 11/20
Epoch 12/20
Epoch 13/20
60000/60000 [============== ] - 3s 54us/step - loss: 0.0108 - acc: 0.9
Epoch 14/20
60000/60000 [============== ] - 3s 56us/step - loss: 0.0102 - acc: 0.9
Epoch 15/20
Epoch 16/20
60000/60000 [============= ] - 3s 56us/step - loss: 0.0085 - acc: 0.9
Epoch 17/20
60000/60000 [============== ] - 3s 55us/step - loss: 0.0098 - acc: 0.9
Epoch 18/20
60000/60000 [============== ] - 3s 55us/step - loss: 0.0054 - acc: 0.9
Epoch 19/20
Epoch 20/20
60000/60000 [============== ] - 3s 55us/step - loss: 0.0081 - acc: 0.9
```

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```
print('Test score:', score[0])
print('Test accuracy:', score[1])
fig,ax = plt.subplots(1,1)
ax.set_xlabel('epoch'); ax.set_ylabel('Categorical Crossentropy Loss')
# list of epoch numbers
x = list(range(1,nb epoch+1))
# print(history.history.keys())
# dict_keys(['val_loss', 'val_acc', 'loss', 'acc'])
# history = model_drop.fit(X_train, Y_train, batch_size=batch_size, epochs=nb_epoch, verbose=1, v
# we will get val_loss and val_acc only when you pass the paramter validation_data
# val_loss : validation loss
# val_acc : validation accuracy
# loss: training loss
# acc : train accuracy
# for each key in histrory.histrory we will have a list of length equal to number of epochs
vy = history.history['val_loss']
ty = history.history['loss']
plt_dynamic(x, vy, ty, ax)
     Test score: 0.09645916890637461
     Test accuracy: 0.9819
score = model1_1.evaluate(X_test, Y_test, verbose=0)
print('Test score:', score[0])
print('Test accuracy:', score[1])
fig,ax = plt.subplots(1,1)
ax.set_xlabel('epoch'); ax.set_ylabel('Categorical Crossentropy Loss')
 This file was updated remotely or in another tab. To force a save, overwriting the last update, select
 Save from the File menu
# print(history.history.keys())
# dict_keys(['val_loss', 'val_acc', 'loss', 'acc'])
# history = model_drop.fit(X_train, Y_train, batch_size=batch_size, epochs=nb_epoch, verbose=1, v
# we will get val_loss and val_acc only when you pass the paramter validation_data
# val_loss : validation loss
# val_acc : validation accuracy
# loss: training loss
# acc : train accuracy
# for each key in histrory.histrory we will have a list of length equal to number of epochs
vy = history.history['val_loss']
ty = history.history['loss']
plt_dynamic(x, vy, ty, ax)
     Test score: 0.09645916890637461
     Test accuracy: 0.9819
%matplotlib inline
w_after = model1_1.get_weights()
h1_w = w_after[0].flatten().reshape(-1,1)
h2_w = w_after[2].flatten().reshape(-1,1)
out w = w after[4].flatten().reshape(-1,1)
fig = plt.figure()
plt.title("Weight matrices after model trained")
plt.subplot(1, 3, 1)
plt.title("Trained model Weights")
```

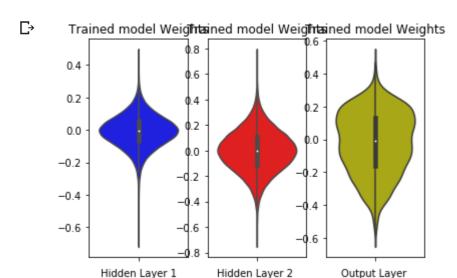
ax = sns.violinplot(y=h1_w,color='b')

plt.title("Trained model Weights")
ax = sns.violinplot(y=h2 w, color='r')

plt.xlabel('Hidden Layer 1')

plt.subplot(1, 3, 2)

```
plt.xlabel('Hidden Layer 2 ')
plt.subplot(1, 3, 3)
plt.title("Trained model Weights")
ax = sns.violinplot(y=out_w,color='y')
plt.xlabel('Output Layer ')
plt.show()
```



```
from keras.layers import Dense, Dropout, Flatten, Activation, BatchNormalization
model1 = Sequential()
model1.add(Dense(512, activation='relu', input_shape=(input_dim,), kernel_initializer=RandomNorma
model1.add(BatchNormalization())
model1.add(Dropout(0.5))
model1.add(Dense(128, activation='relu', kernel_initializer=RandomNormal(mean=0.0, stddev=0.125,
model1.add(Dense(output_dim, activation='softmax'))
model1.add(Dense(output_dim, activation='softmax'))
print(model1.summary())
model1.compile(optimizer='adam', loss='categorical_crossentropy', metrics=['accuracy'])
history = model1.fit(X_train, Y_train, batch_size=batch_size, epochs=nb_epoch, verbose=1, validat
```

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Model: "sequential 9"

Layer (type)	Output Shape	 Param #
=======================================	:========	.==========
dense_31 (Dense)	(None, 512)	401920
batch_normalization_14 (Batch_	(None, 512)	2048
dropout_11 (Dropout)	(None, 512)	0
dense_32 (Dense)	(None, 128)	65664
batch_normalization_15 (Batch_	(None, 128)	512
dropout_12 (Dropout)	(None, 128)	0
dense_33 (Dense)	(None, 10)	1290

Total params: 471,434 Trainable params: 470,154 Non-trainable params: 1,280

None

Train on 60000 samples, validate on 10000 samples

Epoch 1/20

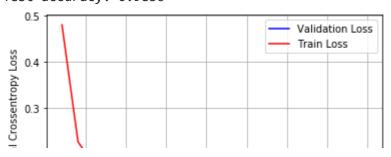
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```
9
Epoch 3/20
Epoch 4/20
Epoch 5/20
Epoch 6/20
60000/60000 [============== ] - 6s 94us/step - loss: 0.1156 - acc: 0.9
Epoch 7/20
Epoch 8/20
Epoch 9/20
60000/60000 [============== ] - 5s 89us/step - loss: 0.0927 - acc: 0.9
Epoch 10/20
60000/60000 [============== ] - 6s 93us/step - loss: 0.0870 - acc: 0.9
Epoch 11/20
Epoch 12/20
60000/60000 [============= ] - 5s 89us/step - loss: 0.0813 - acc: 0.9
Epoch 13/20
Epoch 14/20
Epoch 15/20
Epoch 16/20
60000/60000 [============== ] - 6s 92us/step - loss: 0.0647 - acc: 0.9
Epoch 17/20
60000/60000 [=============== ] - 6s 93us/step - loss: 0.0616 - acc: 0.9
Epoch 18/20
60000/60000 [============== ] - 5s 91us/step - loss: 0.0570 - acc: 0.9
Epoch 19/20
```

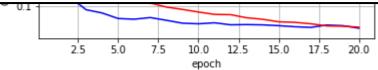
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```
score = model1.evaluate(X_test, Y_test, verbose=0)
print('Test score:', score[0])
print('Test accuracy:', score[1])
fig,ax = plt.subplots(1,1)
ax.set_xlabel('epoch'); ax.set_ylabel('Categorical Crossentropy Loss')
# list of epoch numbers
x = list(range(1,nb_epoch+1))
vy = history.history['val_loss']
ty = history.history['loss']
plt_dynamic(x, vy, ty, ax)
```

Test score: 0.052021935435730846 Test accuracy: 0.9836

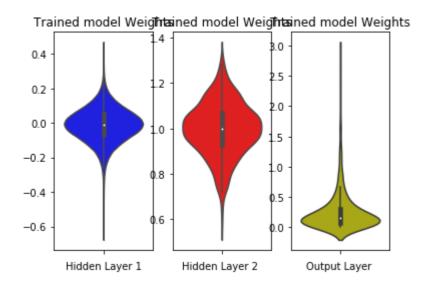


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```
%matplotlib inline
w_after = model1.get_weights()
h1_w = w_after[0].flatten().reshape(-1,1)
h2_w = w_after[2].flatten().reshape(-1,1)
out_w = w_after[4].flatten().reshape(-1,1)
fig = plt.figure()
plt.title("Weight matrices after model trained")
plt.subplot(1, 3, 1)
plt.title("Trained model Weights")
ax = sns.violinplot(y=h1_w,color='b')
plt.xlabel('Hidden Layer 1')
plt.subplot(1, 3, 2)
plt.title("Trained model Weights")
ax = sns.violinplot(y=h2_w, color='r')
plt.xlabel('Hidden Layer 2
plt.subplot(1, 3, 3)
plt.title("Trained model Weights")
ax = sns.violinplot(y=out_w,color='y')
plt.xlabel('Output Layer ')
plt.show()
```

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* 2 Hidden layers MLP + SIGMOID + SGD + Batch Normalization + Dropout



WARNING:tensorflow:From /usr/local/lib/python3.6/dist-packages/keras/backend/tensorfl

WARNING:tensorflow:From /usr/local/lib/python3.6/dist-packages/keras/backend/tensorfl

WARNING:tensorflow:From /usr/local/lib/python3.6/dist-packages/keras/backend/tensorfl

WARNING:tensorflow:From /usr/local/lib/python3.6/dist-packages/keras/backend/tensorfl

WARNING:tensorflow:From /usr/local/lib/python3.6/dist-packages/keras/backend/tensorfl Instructions for updating:

Please use `rate` instead of `keep_prob`. Rate should be set to `rate = 1 - keep_prob WARNING:tensorflow:From /usr/local/lib/python3.6/dist-packages/keras/backend/tensorfl

Model: "sequential_1"

Layer (type)	Output	Shape	Param #
dense_1 (Dense)	(None,	512)	401920
batch_normalization_1 (Batch	(None,	512)	2048
dropout_1 (Dropout)	(None,	512)	0
dense_2 (Dense)	(None,	128)	65664

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dense_3 (Dense) (None, 10) 1290

Total params: 471,434 Trainable params: 470,154 Non-trainable params: 1,280

None

WARNING:tensorflow:From /usr/local/lib/python3.6/dist-packages/keras/optimizers.py:79

WARNING:tensorflow:From /usr/local/lib/python3.6/dist-packages/tensorflow/python/ops/Instructions for updating:

Use tf.where in 2.0, which has the same broadcast rule as np.where

Train on 60000 samples, validate on 10000 samples

Epoch 1/20

Epoch 9/20

https://colab.research.google.com/drive/1DRS5Bc89zMQaEbcYU8hS6cW8QmVfzXtS#scrollTo=J5pc4W 9QKcw&printMode=true

```
60000/60000 [============== ] - 4s 73us/step - loss: 0.3863 - acc: 0.8
Epoch 11/20
60000/60000 [============== ] - 4s 73us/step - loss: 0.3762 - acc: 0.8
Epoch 12/20
Epoch 13/20
Epoch 14/20
Epoch 15/20
Epoch 16/20
Epoch 17/20
Epoch 18/20
Epoch 19/20
60000/60000 [============== ] - 4s 74us/step - loss: 0.3329 - acc: 0.9
Epoch 20/20
60000/60000 [============== ] - 4s 74us/step - loss: 0.3312 - acc: 0.9
```

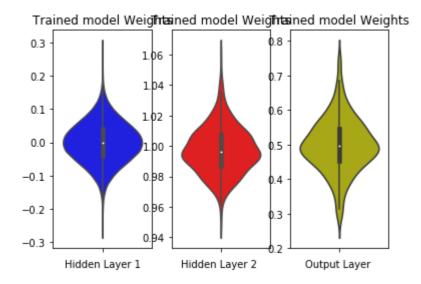
```
score = model1.evaluate(X_test, Y_test, verbose=0)
print('Test score:', score[0])
print('Test accuracy:' score[1])
```

x = list(range(1,nb_epoch+1))

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```
vy = history.history['val_loss']
ty = history.history['loss']
plt_dynamic(x, vy, ty, ax)
     Test score: 0.23021167929247022
     Test accuracy: 0.9338
%matplotlib inline
w_after = model1.get_weights()
h1_w = w_after[0].flatten().reshape(-1,1)
h2_w = w_after[2].flatten().reshape(-1,1)
out_w = w_after[4].flatten().reshape(-1,1)
fig = plt.figure()
plt.title("Weight matrices after model trained")
plt.subplot(1, 3, 1)
plt.title("Trained model Weights")
ax = sns.violinplot(y=h1_w,color='b')
plt.xlabel('Hidden Layer 1')
plt.subplot(1,3,2)
plt.title("Trained model Weights")
ax = sns.violinplot(y=h2_w, color='r')
plt.xlabel('Hidden Layer 2 ')
plt.subplot(1, 3, 3)
plt.title("Trained model Weights")
ax = sns.violinplot(y=out_w,color='y')
plt.xlabel('Output Layer ')
plt.show()
```

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* 2 Hidden layers MLP + tanh + SGD + Batch Normalization + Dropout



Model: "sequential 2"

Layer (type)	Output	Shape	Param #
dense_4 (Dense)	(None,	512)	401920
batch_normalization_3 (Batch	(None,	512)	2048
dropout_3 (Dropout)	(None,	512)	0
dense_5 (Dense)	(None,	128)	65664
batch_normalization_4 (Batch	(None,	128)	512
dropout_4 (Dropout)	(None,	128)	0
dense_6 (Dense)	(None,	10)	1290
	======	===========	=======

Total params: 471,434 Trainable params: 470,154 Non-trainable params: 1,280

None

Train on 60000 samples, validate on 10000 samples

Epoch 1/20

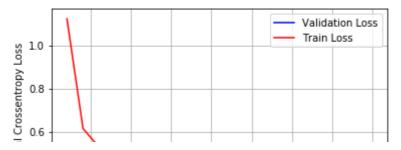
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```
8
Epoch 3/20
Epoch 4/20
Epoch 5/20
Epoch 6/20
Epoch 7/20
Epoch 8/20
Epoch 9/20
Epoch 10/20
Epoch 11/20
Epoch 12/20
Epoch 13/20
Epoch 14/20
Epoch 15/20
Epoch 16/20
60000/60000 [============== ] - 4s 72us/step - loss: 0.3312 - acc: 0.9
Epoch 17/20
60000/60000 [=============] - 4s 72us/step - loss: 0.3258 - acc: 0.9
Epoch 18/20
60000/60000 [=============== ] - 4s 72us/step - loss: 0.3224 - acc: 0.9
Epoch 19/20
```

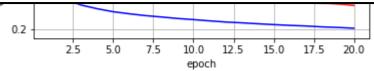
.6

```
score = model1.evaluate(X_test, Y_test, verbose=0)
print('Test score:', score[0])
print('Test accuracy:', score[1])
fig,ax = plt.subplots(1,1)
ax.set_xlabel('epoch'); ax.set_ylabel('Categorical Crossentropy Loss')
# list of epoch numbers
x = list(range(1,nb_epoch+1))
vy = history.history['val_loss']
ty = history.history['loss']
plt_dynamic(x, vy, ty, ax)
```

Test score: 0.20571986180469393 Test accuracy: 0.9393

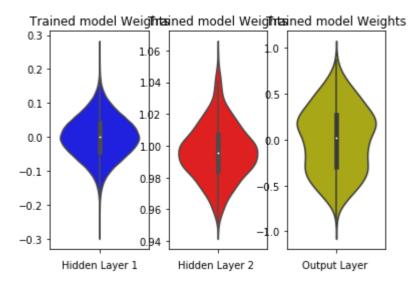


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```
%matplotlib inline
w_after = model1.get_weights()
h1_w = w_after[0].flatten().reshape(-1,1)
h2_w = w_after[2].flatten().reshape(-1,1)
out_w = w_after[4].flatten().reshape(-1,1)
fig = plt.figure()
plt.title("Weight matrices after model trained")
plt.subplot(1, 3, 1)
plt.title("Trained model Weights")
ax = sns.violinplot(y=h1_w,color='b')
plt.xlabel('Hidden Layer 1')
plt.subplot(1,3,2)
plt.title("Trained model Weights")
ax = sns.violinplot(y=h2_w, color='r')
plt.xlabel('Hidden Layer 2
plt.subplot(1, 3, 3)
plt.title("Trained model Weights")
ax = sns.violinplot(y=out_w,color='y')
plt.xlabel('Output Layer ')
plt.show()
```

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```
from keras.layers import Dense, Dropout, Flatten, Activation, BatchNormalization
model1 = Sequential()
model1.add(Dense(512, activation='sigmoid', input_shape=(input_dim,), kernel_initializer=RandomNormodel1.add(BatchNormalization())
model1.add(Dropout(0.4))
model1.add(Dense(128, activation='sigmoid', kernel_initializer=RandomNormal(mean=0.0, stddev=0.12
model1.add(BatchNormalization())
model1.add(Dropout(0.4))
model1.add(Dense(output_dim, activation='softmax'))
```

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Model: "sequential 3"

Layer (type)	Output	Shape	Param #
dense_7 (Dense)	(None,	512)	401920
batch_normalization_5 (Batch	(None,	512)	2048
dropout_5 (Dropout)	(None,	512)	0
dense_8 (Dense)	(None,	128)	65664
batch_normalization_6 (Batch	(None,	128)	512
dropout_6 (Dropout)	(None,	128)	0
dense_9 (Dense)	(None,	10)	1290
	=====		

Total params: 471,434 Trainable params: 470,154 Non-trainable params: 1,280

None

Train on 60000 samples, validate on 10000 samples

Epoch 1/20

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```
9
Epoch 3/20
Epoch 4/20
Epoch 5/20
Epoch 6/20
Epoch 7/20
Epoch 8/20
Epoch 9/20
60000/60000 [============== ] - 5s 83us/step - loss: 0.1276 - acc: 0.9
Epoch 10/20
60000/60000 [============== ] - 5s 83us/step - loss: 0.1197 - acc: 0.9
Epoch 11/20
Epoch 12/20
60000/60000 [============= ] - 5s 84us/step - loss: 0.1003 - acc: 0.9
Epoch 13/20
Epoch 14/20
60000/60000 [============== ] - 5s 83us/step - loss: 0.0894 - acc: 0.9
Epoch 15/20
Epoch 16/20
60000/60000 [============== ] - 5s 85us/step - loss: 0.0805 - acc: 0.9
Epoch 17/20
60000/60000 [=============] - 5s 82us/step - loss: 0.0754 - acc: 0.9
Epoch 18/20
60000/60000 [============== ] - 5s 83us/step - loss: 0.0711 - acc: 0.9
Epoch 19/20
```

.8

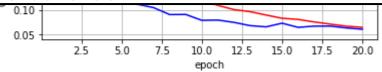
```
60000/60000 [===============] - 5s 82us/step - loss: 0.0669 - acc: 0.9 Epoch 20/20 60000/60000 [================ ] - 5s 80us/step - loss: 0.0646 - acc: 0.9
```

```
score = model1.evaluate(X_test, Y_test, verbose=0)
print('Test score:', score[0])
print('Test accuracy:', score[1])
fig,ax = plt.subplots(1,1)
ax.set_xlabel('epoch'); ax.set_ylabel('Categorical Crossentropy Loss')
# list of epoch numbers
x = list(range(1,nb_epoch+1))
vy = history.history['val_loss']
ty = history.history['loss']
plt_dynamic(x, vy, ty, ax)
```

Test score: 0.06078589027107228 Test accuracy: 0.9818

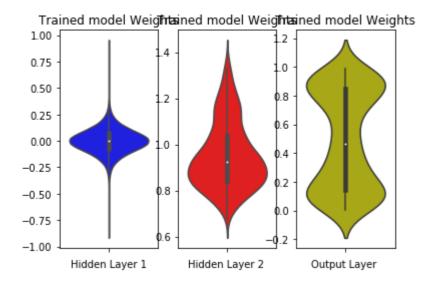


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```
%matplotlib inline
w_after = model1.get_weights()
h1_w = w_after[0].flatten().reshape(-1,1)
h2_w = w_after[2].flatten().reshape(-1,1)
out_w = w_after[4].flatten().reshape(-1,1)
fig = plt.figure()
plt.title("Weight matrices after model trained")
plt.subplot(1, 3, 1)
plt.title("Trained model Weights")
ax = sns.violinplot(y=h1_w,color='b')
plt.xlabel('Hidden Layer 1')
plt.subplot(1,3,2)
plt.title("Trained model Weights")
ax = sns.violinplot(y=h2_w, color='r')
plt.xlabel('Hidden Layer 2
plt.subplot(1, 3, 3)
plt.title("Trained model Weights")
ax = sns.violinplot(y=out_w,color='y')
plt.xlabel('Output Layer ')
plt.show()
```

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2 layer + ADAM + DROPOUT + BATCH NORMALIZATION + TANH

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Model: "sequential 4"

Layer (type)	Output	Shape	Param #
dense_10 (Dense)	(None,	512)	401920
batch_normalization_7 (Batch	(None,	512)	2048
dropout_7 (Dropout)	(None,	512)	0
dense_11 (Dense)	(None,	128)	65664
batch_normalization_8 (Batch	(None,	128)	512
dropout_8 (Dropout)	(None,	128)	0
dense_12 (Dense)	(None,	10)	1290

Total params: 471,434
Trainable params: 470,154
Non-trainable params: 1,280

None

Train on 60000 samples, validate on 10000 samples

Epoch 1/20

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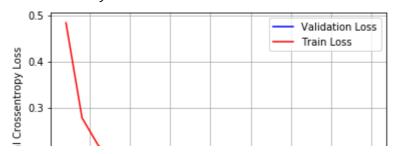
```
Epoch 3/20
Epoch 4/20
Epoch 5/20
Epoch 6/20
Epoch 7/20
Epoch 8/20
Epoch 9/20
60000/60000 [============== ] - 5s 85us/step - loss: 0.1008 - acc: 0.9
Epoch 10/20
60000/60000 [============== ] - 5s 85us/step - loss: 0.0911 - acc: 0.9
Epoch 11/20
Epoch 12/20
60000/60000 [============== ] - 5s 86us/step - loss: 0.0811 - acc: 0.9
Epoch 13/20
Epoch 14/20
60000/60000 [=============== ] - 5s 85us/step - loss: 0.0725 - acc: 0.9
Epoch 15/20
60000/60000 [============= ] - 5s 85us/step - loss: 0.0695 - acc: 0.9
Epoch 16/20
60000/60000 [============== ] - 5s 85us/step - loss: 0.0663 - acc: 0.9
Epoch 17/20
60000/60000 [=============] - 5s 89us/step - loss: 0.0613 - acc: 0.9
Epoch 18/20
60000/60000 [============== ] - 5s 84us/step - loss: 0.0561 - acc: 0.9
Epoch 19/20
```

Э.

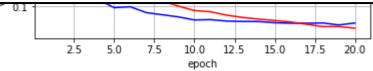
9

```
score = model1.evaluate(X_test, Y_test, verbose=0)
print('Test score:', score[0])
print('Test accuracy:', score[1])
fig,ax = plt.subplots(1,1)
ax.set_xlabel('epoch'); ax.set_ylabel('Categorical Crossentropy Loss')
# list of epoch numbers
x = list(range(1,nb_epoch+1))
vy = history.history['val_loss']
ty = history.history['loss']
plt_dynamic(x, vy, ty, ax)
```

Test score: 0.0640238022508216 Test accuracy: 0.9822

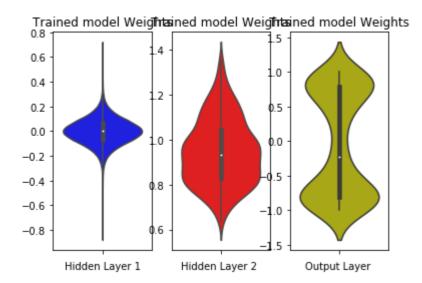


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```
%matplotlib inline
w_after = model1.get_weights()
h1_w = w_after[0].flatten().reshape(-1,1)
h2_w = w_after[2].flatten().reshape(-1,1)
out_w = w_after[4].flatten().reshape(-1,1)
fig = plt.figure()
plt.title("Weight matrices after model trained")
plt.subplot(1, 3, 1)
plt.title("Trained model Weights")
ax = sns.violinplot(y=h1_w,color='b')
plt.xlabel('Hidden Layer 1')
plt.subplot(1,3,2)
plt.title("Trained model Weights")
ax = sns.violinplot(y=h2_w, color='r')
plt.xlabel('Hidden Layer 2
plt.subplot(1, 3, 3)
plt.title("Trained model Weights")
ax = sns.violinplot(y=out_w,color='y')
plt.xlabel('Output Layer ')
plt.show()
```

Гэ



3 hidden layer MLP + Batch-Norm on hidden Layers + AdamOptimizer but

С⇒

Model: "sequential_10"

Layer (type) Output Shape Param # dense_34 (Dense) (None, 512) 401920 batch_normalization_16 (Batc (None, 512) 2048 dense_35 (Dense) (None, 256) 131328 batch_normalization_17 (Batc (None, 256) 1024 dense_36 (Dense) (None, 128) 32896 batch_normalization_18 (Batc (None, 128) 512					
batch_normalization_16 (Batc (None, 512) 2048 dense_35 (Dense) (None, 256) 131328 batch_normalization_17 (Batc (None, 256) 1024 dense_36 (Dense) (None, 128) 32896	Layer (type)		Output	Shape	Param #
dense_35 (Dense) (None, 256) 131328 batch_normalization_17 (Batc (None, 256) 1024 dense_36 (Dense) (None, 128) 32896	dense_34 (Dense)	========	(None,	512)	401920
batch_normalization_17 (Batc (None, 256) 1024 dense_36 (Dense) (None, 128) 32896	batch_normalizati	on_16 (Batc	(None,	512)	2048
dense_36 (Dense) (None, 128) 32896	dense_35 (Dense)		(None,	256)	131328
	batch_normalizati	on_17 (Batc	(None,	256)	1024
batch_normalization_18 (Batc (None, 128) 512	dense_36 (Dense)		(None,	128)	32896
	batch_normalizati	on_18 (Batc	(None,	128)	512
dense_37 (Dense) (None, 10) 1290	dense_37 (Dense)	========	(None,	10)	1290

Total params: 571,018 Trainable params: 569,226 Non-trainable params: 1,792

model 2 commile(ontimizer-'adam' loss-'categorical crossentrony' metrics-['acduracy'])

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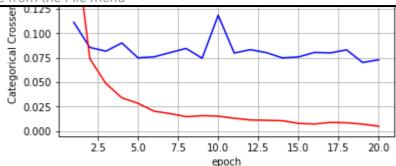
da

```
Train on 60000 samples, validate on 10000 samples
  Epoch 1/20
  Epoch 2/20
  60000/60000 [=============== ] - 7s 116us/step - loss: 0.0741 - acc: 0.
  Epoch 3/20
  60000/60000 [============== - 7s 112us/step - loss: 0.0487 - acc: 0.
  Epoch 4/20
  60000/60000 [============== ] - 7s 114us/step - loss: 0.0341 - acc: 0.
  Epoch 5/20
  60000/60000 [============= ] - 7s 118us/step - loss: 0.0285 - acc: 0.
  Epoch 6/20
  60000/60000 [============= - 7s 117us/step - loss: 0.0205 - acc: 0.
  Epoch 7/20
  60000/60000 [=============== ] - 7s 117us/step - loss: 0.0180 - acc: 0.
  Epoch 8/20
  Epoch 9/20
  Epoch 10/20
  60000/60000 [============= ] - 7s 115us/step - loss: 0.0154 - acc: 0.
  Epoch 11/20
  Epoch 12/20
  60000/60000 [============= ] - 7s 114us/step - loss: 0.0115 - acc: 0.
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  Epoch 15/20
  60000/60000 [============== - 7s 114us/step - loss: 0.0080 - acc: 0.
  Epoch 16/20
  60000/60000 [=============== ] - 7s 115us/step - loss: 0.0073 - acc: 0.
  Epoch 17/20
  60000/60000 [============== ] - 7s 113us/step - loss: 0.0090 - acc: 0.
  Epoch 18/20
  60000/60000 [============= ] - 7s 113us/step - loss: 0.0086 - acc: 0.
  Epoch 19/20
  Epoch 20/20
  60000/60000 [=============== ] - 6s 108us/step - loss: 0.0051 - acc: 0.
```

```
print('Test score:', score[0])
print('Test accuracy:', score[1])
fig,ax = plt.subplots(1,1)
ax.set_xlabel('epoch'); ax.set_ylabel('Categorical Crossentropy Loss')
# list of epoch numbers
x = list(range(1,nb_epoch+1))
# print(history.history.keys())
# dict_keys(['val_loss', 'val_acc', 'loss', 'acc'])
# history = model_drop.fit(X_train, Y_train, batch_size=batch_size, epochs=nb_epoch, verbose=1, v
# we will get val loss and val acc only when you pass the paramter validation data
# val_loss : validation loss
# val_acc : validation accuracy
# loss: training loss
# acc : train accuracy
# for each key in histrory.histrory we will have a list of length equal to number of epochs
vy = history.history['val_loss']
ty = history.history['loss']
plt_dynamic(x, vy, ty, ax)
```

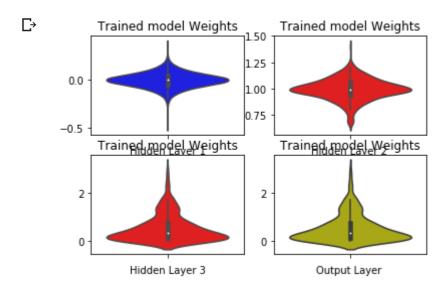
Test score: 0.07286385818796771 Test accuracy: 0.9821





```
w_after = model_2.get_weights()
h1_w = w_after[0].flatten().reshape(-1,1)
h2_w = w_after[2].flatten().reshape(-1,1)
h3_w = w_after[4].flatten().reshape(-1,1)
out w= w after[4].flatten().reshape(-1,1)
fig = plt.figure()
plt.title("Weight matrices after model trained")
plt.subplot(2, 2, 1)
plt.title("Trained model Weights")
ax = sns.violinplot(y=h1_w,color='b')
plt.xlabel('Hidden Layer 1')
plt.subplot(2, 2, 2)
plt.title("Trained model Weights")
ax = sns.violinplot(y=h2_w, color='r')
plt.xlabel('Hidden Layer 2 ')
plt.subplot(2, 2, 3)
plt.title("Trained model Weights")
ax = sns.violinplot(y=h3_w, color='r')
plt.xlabel('Hidden Layer 3'
plt.subplot(2, 2, 4)
```

```
plt.title("Trained model Weights")
ax = sns.violinplot(y=out_w,color='y')
plt.xlabel('Output Layer ')
plt.show()
```



3 HIDDEN LAYER AND RELU WITH DROPOUT AND BATCH NORMALIZATION

```
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model_2_1.add(Dropout(0.5))

model_2_1.add(Dense(256, activation='relu', input_shape=(input_dim,), kernel_initializer=RandomNc

model_2_1.add(BatchNormalization())

model_2_1.add(Dense(128, activation='relu', input_shape=(input_dim,), kernel_initializer=RandomNc

model_2_1.add(Dense(128, activation='relu', input_shape=(input_dim,), kernel_initializer=RandomNc

model_2_1.add(Dropout(0.5))

model_2_1.add(Dense(output_dim, activation='softmax'))

model_2_1.summary()
```

₽

Model: "sequential_11"

Layer (type)		Output	Shape	Param #
dense_38 (Dense)	=====	(None,	 512)	 401920
	<u> </u>	· · ·		
<pre>batch_normalization_19 (</pre>	(Batc	(None,	512)	2048
dropout_13 (Dropout)		(None,	512)	0
dense_39 (Dense)		(None,	256)	131328
	<u> </u>			1004
batch_normalization_20 ((ватс	(None,	256)	1024
dropout_14 (Dropout)		(None,	256)	0
dense_40 (Dense)		(None,	128)	32896
batch_normalization_21 ((Batc	(None,	128)	512
dropout_15 (Dropout)		(None,	128)	0
dense_41 (Dense)		(None,	10)	1290
	=====		· ====================================	

Total params: 571,018

```
model_2_1.compile(optimizer='adam', loss='categorical_crossentropy', metrics=['accuracy'])
history = model_2_1.fit(X_train, Y_train, batch_size=batch_size, epochs=nb_epoch, verbose=1, vali
```

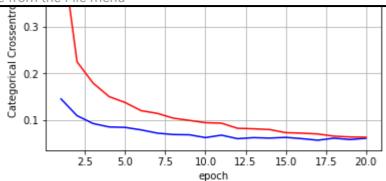
```
Train on 60000 samples, validate on 10000 samples
  Epoch 1/20
  Epoch 2/20
  60000/60000 [=============== ] - 7s 112us/step - loss: 0.2249 - acc: 0.
  Epoch 3/20
  60000/60000 [============== - 7s 111us/step - loss: 0.1794 - acc: 0.
  Epoch 4/20
  60000/60000 [============== ] - 7s 111us/step - loss: 0.1506 - acc: 0.
  Epoch 5/20
  60000/60000 [============= ] - 7s 111us/step - loss: 0.1379 - acc: 0.
  Epoch 6/20
  60000/60000 [============= - 7s 113us/step - loss: 0.1205 - acc: 0.
  Epoch 7/20
  60000/60000 [=============== ] - 7s 112us/step - loss: 0.1148 - acc: 0.
  Epoch 8/20
  Epoch 9/20
  Epoch 10/20
  60000/60000 [============= ] - 7s 115us/step - loss: 0.0949 - acc: 0.
  Epoch 11/20
  Epoch 12/20
  This file was updated remotely or in another tab. To force a save, overwriting the last update, select
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  Epoch 15/20
  60000/60000 [============== - 7s 120us/step - loss: 0.0736 - acc: 0.
  Epoch 16/20
  60000/60000 [=============== ] - 7s 117us/step - loss: 0.0726 - acc: 0.
  Epoch 17/20
  60000/60000 [=============== ] - 7s 119us/step - loss: 0.0708 - acc: 0.
  Epoch 18/20
  60000/60000 [============= ] - 7s 120us/step - loss: 0.0662 - acc: 0.
  Epoch 19/20
  Epoch 20/20
  60000/60000 [=============== ] - 7s 122us/step - loss: 0.0639 - acc: 0.
```

```
print('Test score:', score[0])
print('Test accuracy:', score[1])
fig,ax = plt.subplots(1,1)
ax.set_xlabel('epoch'); ax.set_ylabel('Categorical Crossentropy Loss')
# list of epoch numbers
x = list(range(1,nb_epoch+1))
# print(history.history.keys())
# dict_keys(['val_loss', 'val_acc', 'loss', 'acc'])
# history = model_drop.fit(X_train, Y_train, batch_size=batch_size, epochs=nb_epoch, verbose=1, v
# we will get val loss and val acc only when you pass the paramter validation data
# val_loss : validation loss
# val_acc : validation accuracy
# loss: training loss
# acc : train accuracy
# for each key in histrory.histrory we will have a list of length equal to number of epochs
vy = history.history['val_loss']
ty = history.history['loss']
plt_dynamic(x, vy, ty, ax)
```

```
Test score: 0.061630533440283033
Test accuracy: 0.9821

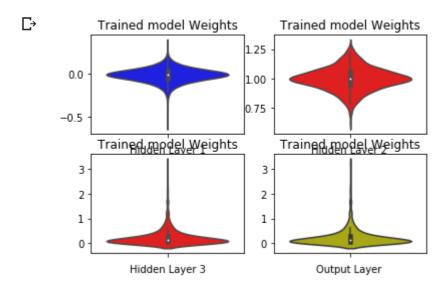
O.5

Validation Loss
```



```
w_after = model_2_1.get_weights()
h1_w = w_after[0].flatten().reshape(-1,1)
h2_w = w_after[2].flatten().reshape(-1,1)
h3_w = w_after[4].flatten().reshape(-1,1)
out w= w after[4].flatten().reshape(-1,1)
fig = plt.figure()
plt.title("Weight matrices after model trained")
plt.subplot(2, 2, 1)
plt.title("Trained model Weights")
ax = sns.violinplot(y=h1_w,color='b')
plt.xlabel('Hidden Layer 1')
plt.subplot(2, 2, 2)
plt.title("Trained model Weights")
ax = sns.violinplot(y=h2_w, color='r')
plt.xlabel('Hidden Layer 2 ')
plt.subplot(2, 2, 3)
plt.title("Trained model Weights")
ax = sns.violinplot(y=h3_w, color='r')
plt.xlabel('Hidden Layer 3')
```

```
plt.subplot(2, 2, 4)
plt.title("Trained model Weights")
ax = sns.violinplot(y=out_w,color='y')
plt.xlabel('Output Layer ')
plt.show()
```



* 5 Hidden layer MLP + ReLu + AdamOptimizer

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```
model_3_1.add(Dense(512, activation='relu', input_shape=(input_dim,), kernel_initializer=RandomNo
model_3_1.add(Dense(256, activation='relu', input_shape=(input_dim,), kernel_initializer=RandomNo
model_3_1.add(Dense(128, activation='relu', input_shape=(input_dim,), kernel_initializer=RandomNo
model_3_1.add(Dense(64, activation='relu', input_shape=(input_dim,), kernel_initializer=RandomNor
model_3_1.add(Dense(32, activation='relu', input_shape=(input_dim,), kernel_initializer=RandomNor
model_3_1.add(Dense(output_dim, activation='softmax'))
model_3_1.summary()
```

Model: "sequential_12"

Layer (type)		Output	Shape	Param #
dense_42 (Der	nse)	(None,	512)	401920
dense_43 (Dei	nse)	(None,	256)	131328
dense_44 (Dei	nse)	(None,	128)	32896
dense_45 (Dei	ıse)	(None,	64)	8256
dense_46 (Dei	nse)	(None,	32)	2080
dense_47 (Dei	nse)	(None,	10)	330

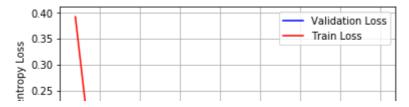
Total params: 576,810 Trainable params: 576,810 Non-trainable params: 0

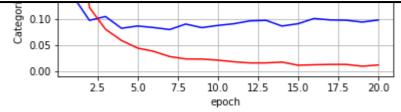
```
model_3_1.compile(optimizer='adam', loss='categorical_crossentropy', metrics=['accuracy'])
history = model_3_1.fit(X_train, Y_train, batch_size=batch_size, epochs=nb_epoch, verbose=1, vali
https://colab.research.google.com/drive/1DRS5Bc89zMQaEbcYU8hS6cW8QmVfzXtS#scrollTo=J5pc4W 9QKcw&printMode=true
32/41
```

```
Train on 60000 samples, validate on 10000 samples
Гэ
 Epoch 1/20
 Epoch 2/20
 60000/60000 [============== ] - 4s 71us/step - loss: 0.1226 - acc: 0.9
 Epoch 3/20
 60000/60000 [============== ] - 4s 71us/step - loss: 0.0807 - acc: 0.9
 Epoch 4/20
 Epoch 5/20
 Epoch 6/20
 Epoch 7/20
 Epoch 8/20
 Epoch 9/20
 Epoch 10/20
 Epoch 11/20
 Epoch 12/20
                                  ^,9
This file was updated remotely or in another tab. To force a save, overwriting the last update, select
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 Epocn 14/20
 60000/60000 [============== ] - 4s 72us/step - loss: 0.0172 - acc: 0.9
 Epoch 15/20
 Epoch 16/20
 Epoch 17/20
 60000/60000 [============== ] - 4s 71us/step - loss: 0.0127 - acc: 0.9
 Epoch 18/20
 60000/60000 [============== ] - 4s 70us/step - loss: 0.0127 - acc: 0.9
 Epoch 19/20
 Epoch 20/20
```

```
score = model_3_1.evaluate(X_test, Y_test, verbose=0)
print('Test score:', score[0])
print('Test accuracy:', score[1])
fig,ax = plt.subplots(1,1)
ax.set_xlabel('epoch'); ax.set_ylabel('Categorical Crossentropy Loss')
# list of epoch numbers
x = list(range(1,nb_epoch+1))
# print(history.history.keys())
# dict_keys(['val_loss', 'val_acc', 'loss', 'acc'])
# history = model_drop.fit(X_train, Y_train, batch_size=batch_size, epochs=nb_epoch, verbose=1, v
# we will get val_loss and val_acc only when you pass the paramter validation_data
# val_loss: validation loss
# val_acc: validation accuracy
# loss: training loss
# acc: train accuracy
# for each key in histrory.histrory we will have a list of length equal to number of epochs
vy = history.history['val_loss']
ty = history.history['loss']
plt_dynamic(x, vy, ty, ax)
```

Test score: 0.09843842560593985 Test accuracy: 0.9782



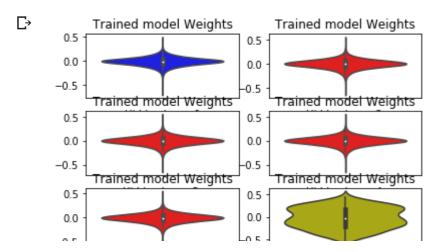


```
w_after = model_3_1.get_weights()
h1_w = w_after[0].flatten().reshape(-1,1)
h2_w = w_after[2].flatten().reshape(-1,1)
h3_w = w_after[4].flatten().reshape(-1,1)
h4_w = w_after[6].flatten().reshape(-1,1)
h5_w = w_after[8].flatten().reshape(-1,1)
out_w = w_after[10].flatten().reshape(-1,1)
fig = plt.figure()
plt.title("Weight matrices after model trained")
plt.subplot(3,2 , 1)
plt.title("Trained model Weights")
ax = sns.violinplot(y=h1 w,color='b')
plt.xlabel('Hidden Layer 1')
plt.subplot(3, 2, 2)
plt.title("Trained model Weights")
ax = sns.violinplot(y=h2_w, color='r')
plt.xlabel('Hidden Layer 2 ')
plt.subplot(3, 2, 3)
plt.title("Trained model Weights")
ax = sns.violinplot(y=h2_w, color='r')
plt.xlabel('Hidden Layer 3
plt.subplot(3,2, 4)
plt.title("Trained model Weights")
```

```
ax = sns.violinplot(y=h2_w, color='r')
plt.xlabel('Hidden Layer 4 ')

plt.subplot(3, 2, 5)
plt.title("Trained model Weights")
ax = sns.violinplot(y=h2_w, color='r')
plt.xlabel('Hidden Layer 5 ')

plt.subplot(3,2, 6)
plt.title("Trained model Weights")
ax = sns.violinplot(y=out_w,color='y')
plt.xlabel('Output Layer ')
plt.show()
```



* 5 Hidden layer MLP + Dropout + Batch Normalization + ReLu + AdamOpt

```
# https://stackoverflow.com/questions/34716454/where-do-i-call-the-batchnormalization-function-in
from keras.layers import Dropout
model_3 = Sequential()
model_3.add(Dense(512, activation='relu', input_shape=(input_dim,), kernel_initializer=RandomNorm
model_3.add(BatchNormalization())
model 3.add(Dropout(0.5))
model_3.add(Dense(256, activation='relu', input_shape=(input_dim,), kernel_initializer=RandomNorm
model_3.add(BatchNormalization())
model_3.add(Dropout(0.5))
model_3.add(Dense(128, activation='relu', input_shape=(input_dim,), kernel_initializer=RandomNorm
model_3.add(BatchNormalization())
model_3.add(Dropout(0.5))
model 3.add(Dense(64, activation='relu', input shape=(input dim,), kernel initializer=RandomNorma
model 3.add(BatchNormalization())
model 3.add(Dropout(0.5))
model_3.add(Dense(32, activation='relu', input_shape=(input_dim,), kernel_initia|izer=RandomNorma
model_3.add(BatchNormalization())
model_3.add(Dropout(0.5))
model_3.add(Dense(output_dim, activation='softmax'))
model_3.summary()
```

₽

Model: "sequential_13"

Layer (type)	Output	Shape	Param #
dense_48 (Dense)	(None,	512)	401920
batch_normalization_22 (E	Batc (None,	512)	2048
dropout_16 (Dropout)	(None,	512)	0
dense_49 (Dense)	(None,	256)	131328
batch_normalization_23 (E	Batc (None,	256)	1024
dropout_17 (Dropout)	(None,	256)	0
dense_50 (Dense)	(None,	128)	32896
batch_normalization_24 (E	Batc (None,	128)	512
dropout_18 (Dropout)	(None,	128)	0
dense_51 (Dense)	(None,	64)	8256
batch_normalization_25 (E	Batc (None,	64)	256

dense_52 (Dense)	(None,	32)	2080
batch_normalization_26 (Batc	(None,	32)	128
dropout_20 (Dropout)	(None,	32)	0
dense_53 (Dense)	(None,	10)	330
	======	=============	========

Total params: 580,778
Trainable params: 578,794
Non-trainable params: 1,984

model_3.compile(optimizer='adam', loss='categorical_crossentropy', metrics=['accuracy'])
history = model_3.fit(X_train, Y_train, batch_size=batch_size, epochs=nb_epoch, verbose=1, valida

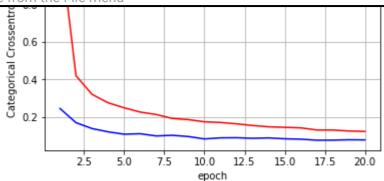
C→

```
Train on 60000 samples, validate on 10000 samples
Epoch 1/20
Epoch 2/20
Epoch 3/20
Epoch 4/20
Epoch 5/20
60000/60000 [============== ] - 9s 158us/step - loss: 0.2495 - acc: 0.
Epoch 6/20
Epoch 7/20
Epoch 8/20
Epoch 9/20
Epoch 10/20
Epoch 11/20
Epoch 12/20
0
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Save from the File menu
Epoch 15/20
Epoch 16/20
Epoch 17/20
Epoch 18/20
Epoch 19/20
Epoch 20/20
```

```
print('Test score:', score[0])
print('Test accuracy:', score[1])
fig,ax = plt.subplots(1,1)
ax.set_xlabel('epoch'); ax.set_ylabel('Categorical Crossentropy Loss')
# list of epoch numbers
x = list(range(1,nb_epoch+1))
# print(history.history.keys())
# dict_keys(['val_loss', 'val_acc', 'loss', 'acc'])
# history = model_drop.fit(X_train, Y_train, batch_size=batch_size, epochs=nb_epoch, verbose=1, v
# we will get val loss and val acc only when you pass the paramter validation data
# val_loss : validation loss
# val_acc : validation accuracy
# loss: training loss
# acc : train accuracy
# for each key in histrory.histrory we will have a list of length equal to number of epochs
vy = history.history['val_loss']
ty = history.history['loss']
plt_dynamic(x, vy, ty, ax)
```

Test score: 0.07888613095330074 Test accuracy: 0.9813





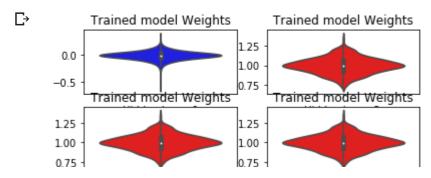
```
w_after = model_3.get_weights()
h1_w = w_after[0].flatten().reshape(-1,1)
h2_w = w_after[2].flatten().reshape(-1,1)
h3_w = w_after[4].flatten().reshape(-1,1)
h4_w = w_after[6].flatten().reshape(-1,1)
h5_w = w_after[8].flatten().reshape(-1,1)
out_w = w_after[10].flatten().reshape(-1,1)
fig = plt.figure()
plt.title("Weight matrices after model trained")
plt.subplot(3,2 , 1)
plt.title("Trained model Weights")
ax = sns.violinplot(y=h1_w,color='b')
plt.xlabel('Hidden Layer 1')
plt.subplot(3, 2, 2)
plt.title("Trained model Weights")
ax = sns.violinplot(y=h2_w, color='r')
plt.xlabel('Hidden Layer 2
plt.subplot(3, 2, 3)
plt.title("Trained model Weights")
```

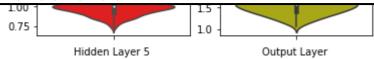
```
ax = sns.violinplot(y=h2_w, color='r')
plt.xlabel('Hidden Layer 3 ')

plt.subplot(3,2, 4)
plt.title("Trained model Weights")
ax = sns.violinplot(y=h2_w, color='r')
plt.xlabel('Hidden Layer 4 ')

plt.subplot(3, 2, 5)
plt.title("Trained model Weights")
ax = sns.violinplot(y=h2_w, color='r')
plt.xlabel('Hidden Layer 5 ')

plt.subplot(3,2, 6)
plt.title("Trained model Weights")
ax = sns.violinplot(y=out_w,color='y')
plt.xlabel('Output Layer ')
plt.show()
```





```
from prettytable import PrettyTable

x = PrettyTable()

x.field_names = ["Hiddden layers", "batch normalization","activation function","optimizer" ,"drop

x.add_row([2,'no',"relu",'adam','no',98.19])
x.add_row([2,'yes','relu',"adam",'yes', 98.36])
x.add_row([2,'yes',"sigmoid",'SGD','yes',93.38])
x.add_row([2,'yes',"sigmoid",'sGD",'yes',93.93])
x.add_row([2,'yes',"sigmoid",'adam','yes',98.18])
x.add_row([3,'yes','tanh',"adam','yes',98.22])
x.add_row([3,'no','relu','adam','no', 98.2])
x.add_row([5,'no','relu','adam','yes', 98.35])
x.add_row([5,'no','relu','adam','yes', 98.16])
print(x)
```

 \Box

_	L	L	L		
Hiddden layers	 batch normalization	activation function	optimizer	dropout	
2	no	relu	adam	no	
2	yes	relu	adam	yes	
2	yes	sigmoid	SGD	yes	
2	yes	tanh	SGD	yes	
2	yes	sigmoid	adam	yes	
2	yes	tanh	adam	yes	
3	l no	relu	adam	no	
3	yes	relu	adam	yes	
5	l no	relu	adam	no	
5	yes	relu	adam	yes	
+	L	L			- -

Conclusion: 1.We can see that 2 hidden layer with batch normalization and dropout gives higher accuracy. 2.If th models tend to overfit. 3.Without doing batch normalization the convergennce rate is slow, so batch normalizatic without dropout and only batch normalization we can see it performs better than a MLP which doent have both batch regulizer. 5.We can observe Adam as best optimizer as compared to SGD. 6.Tanh activation function with \$\frac{1}{2}\$ with SGD optimizer. 7.ReLu is best activation function. 8.So for MNIST dataset, a MLP works well when it has dropout and 2 hidden layers