

QUESTION : 12.13.3.7

ROLL NO:EE22BTECH11027

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12.13.3.7.A and B are two events such that 4)

$$\Pr(A) = \frac{1}{2}, \Pr(B) = \frac{1}{3} \text{ and } \Pr(AB) = \frac{1}{4}.$$

Find:

- i $\Pr(A|B)$
- ii $\Pr(B|A)$
- iii $\Pr(A'|B)$
- iv $\Pr(A'|B')$

Solution: : Given, $\Pr(A) = \frac{1}{2}$, $\Pr(B) = \frac{1}{3}$ and $\Pr(AB) = \frac{1}{4}$. Then,

$$\Pr(A'|B') = \frac{\Pr(A'B')}{\Pr(B')}$$

$$\begin{aligned} \therefore \Pr(A'B') &= \Pr(A+B)' \\ &= 1 - \Pr(A+B) \end{aligned} \quad (5)$$

$$\Pr(A'B') = \frac{5}{12}$$

$$\therefore \Pr(A'|B') = \frac{5}{8}$$

$$\Pr(A') = 1 - \Pr(A) = \frac{1}{2}$$

$$\Pr(B') = 1 - \Pr(B) = \frac{2}{3} \quad (1)$$

$$\begin{aligned} \Pr(A+B) &= \Pr(A) + \Pr(B) - \Pr(AB) \\ &= \frac{7}{12} \end{aligned}$$

1)

$$\Pr(A|B) = \frac{\Pr(AB)}{\Pr(B)} = \frac{3}{4} \quad (2)$$

2)

$$\Pr(B|A) = \frac{\Pr(AB)}{\Pr(A)} = \frac{1}{2} \quad (3)$$

3)

$$\Pr(A'|B) = \frac{\Pr(A'B)}{\Pr(B)}$$

$$\begin{aligned} \Pr(A'B) &= \Pr(A'B) + \Pr(AB) - \Pr(AB) \\ &= \Pr(A'B + AB) - \Pr(AB) \end{aligned}$$

($\because \Pr(E_1 + E_2 + \dots) = \Pr(E_1) + \Pr(E_2) + \dots$, when mutually exclusive.)

$$\begin{aligned} \Pr(A'B) &= \Pr((A + A')B) - \Pr(AB) \\ &= \Pr(B) - \Pr(AB) \end{aligned}$$

$$= \frac{1}{12}$$

$$\therefore \Pr(A'|B) = \frac{1}{4}$$

(4)