

# QUESTION : 12.13.3.7

ROLL NO:EE22BTECH11027

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12.13.3.7.A and  $B$  are two events such that 4)

$\Pr(A) = \frac{1}{2}$ ,  $\Pr(B) = \frac{1}{3}$  and  $\Pr(A \cap B) = \frac{1}{4}$ .

Find:

- i  $\Pr(A|B)$
- ii  $\Pr(B|A)$
- iii  $\Pr(A'|B)$
- iv  $\Pr(A'|B')$

**Solution:** : Given,  $\Pr(A) = \frac{1}{2}$ ,  $\Pr(B) = \frac{1}{3}$  and  $\Pr(A \cap B) = \frac{1}{4}$ . Then,

$$\begin{aligned}\Pr(A') &= 1 - \Pr(A) = \frac{1}{2} \\ \Pr(B') &= 1 - \Pr(B) = \frac{2}{3}\end{aligned}\quad (1)$$

$$\begin{aligned}\Pr(A \cup B) &= \Pr(A) + \Pr(B) - \Pr(A \cap B) \\ &= \frac{7}{12}\end{aligned}$$

1)

$$\begin{aligned}\Pr(A|B) &= \frac{\Pr(A \cap B)}{\Pr(B)} \\ &= \frac{3}{4}\end{aligned}\quad (2)$$

2)

$$\begin{aligned}\Pr(B|A) &= \frac{\Pr(A \cap B)}{\Pr(A)} \\ &= \frac{1}{2}\end{aligned}\quad (3)$$

3)

$$\Pr(A'|B) = \frac{\Pr(A' \cap B)}{\Pr(B)}$$

Since,

$$\begin{aligned}\Pr(A \cap B) \Pr(A' \cap B) &= \Pr(B) - \Pr(A \cap B) \\ &= \frac{1}{12}\end{aligned}$$

We have,

$$\Pr(A'|B) = \frac{1}{4}\quad (4)$$

$$\Pr(A'|B') = \frac{\Pr(A' \cap B')}{\Pr(B')}$$

Since,

$$\begin{aligned}\Pr(A' \cap B') &= \Pr(A \cup B)' \\ &= 1 - \Pr(A \cup B) \\ &= \frac{5}{12}\end{aligned}\quad (5)$$

We have,

$$\Pr(A'|B') = \frac{5}{8}$$