

# QUESTION : 12.13.3.7

ROLL NO:EE22BTECH11027

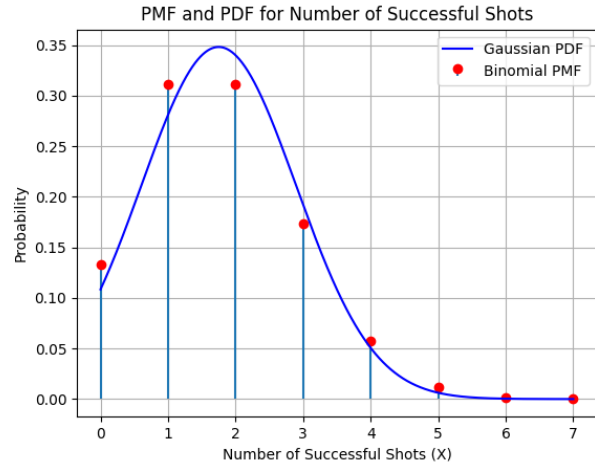
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9.3.27.The probability of a man hitting the target is 0.25. He shoots 7 times.What is the probability of his hitting the target atleast twice?

**Solution: :**

TABLE 0  
VARIABLES

Variable	Value	Description
n	7	Number of trails
p	0.25	The probability of man hitting the target
q	0.75	The probability of man not hitting the target
$\mu = np$	1.75	mean of distribution
$\sigma = \sqrt{npq}$	1.145	variance of distribution
X	$X \geq 2$	Number of times man hits the target



From gaussian,

$$Y \sim \mathcal{N}(\mu, \sigma^2) \quad (1)$$

CDF of Y is defined as:

$$F_Y(X) = \Pr(Y < X) \quad (2)$$

$$= \Pr\left(\frac{Y - \mu}{\sigma} \leq \frac{X - \mu}{\sigma}\right) \quad (3)$$

$$\Rightarrow \frac{Y - \mu}{\sigma} \sim N(0, 1) \quad (4)$$

$$= 1 - \Pr\left(\frac{Y - \mu}{\sigma} > \frac{X - \mu}{\sigma}\right) \quad (5)$$

$$= \begin{cases} 1 - Q\left(\frac{X - \mu}{\sigma}\right) & X \geq \mu \\ Q\left(\frac{\mu - X}{\sigma}\right) & X < \mu \end{cases} \quad (6)$$

Hence, the probability of hitting target atleast twice using gaussian distribution is:

without correction:

$$\Pr(Y \geq 2) = 1 - \Pr(Y < 2) \quad (7)$$

$$= 1 - F_Y(2) \quad (8)$$

$$\Rightarrow \Pr(Y \geq 2) = Q\left(\frac{X - \mu}{\sigma}\right) \quad (9)$$

$$= Q(0.218) \quad (10)$$

$$\Pr(Y \geq 2) = 0.4137 \quad (11)$$

Fig. 0. gaussian and binomial

with correction:

$$\Pr(Y \geq 2) = Q\left(\frac{X - 0.5 - \mu}{\sigma}\right) \quad (12)$$

$$= Q(-0.218) \quad (13)$$

$$\Pr(Y \geq 2) = 0.5862 \quad (14)$$

Hence, the probability of hitting target atleast twice using binomial distribution is:

$$\Pr(X \geq 2) = 1 - \Pr(X < 2) \quad (15)$$

$$= 1 - \sum_{k=0}^1 {}^nC_k p^k (1-p)^{n-k} \quad (16)$$

$$= 0.55 \quad (17)$$