



• A model to assign a probability to a sentence

• Machine Translation:

• P(high winds tonight) • P(large winds tonight)

• Spell Correction

• The office is about fifteen minuets from my house!

• P(about fifteen minutes from) • P(about fifteen minuets from)

• Speech Recognition

• P(Isaw a van) >> P(eyes awe of an)

• + Summarization, question, answering, etc., etc.!!

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1 2

Probabilistic Language Modeling

• Goal: compute the probability of a sentence or sequence of words:

P(W) = P(w_1,w_2,w_3,w_4,w_5...w_e)

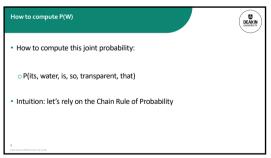
• Related task: probability of an upcoming word:

P(w_1|w_1,w_2,w_3,w_4)

• A model that computes either of these:

P(W) or P(w_1|w_1,w_2...w_e_1) is called a language model.

• Better: the grammar But language model or LM is standard



Reminder: The Chain Rule

Recall the definition of conditional probabilities

p(B|A) = P(A,B)/P(A) Rewriting: P(A,B) = P(A)P(B|A)

More variables:

P(A,B,C,D) = P(A)P(B|A)P(C|A,B)P(D|A,B,C)

The Chain Rule in General

P(x1,x2,x3,...,xn) = P(x1)P(x2|x1)P(x3|x1,x2)...P(xn|x1,...,xn·1)

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The Chain Rule applied to compute joint probability of words in sentence DEAKIN UNIVERSITY $P(w_1 w_2 ... w_n) = \prod P(w_i | w_1 w_2 ... w_{i-1})$ P("its water is so transparent") = P(its) × P(water | its) × P(is | its water) × P(so|its water is) × P(transparent|its water is so)

How to estimate these probabilities DEAKIN · Could we just count and divide? P(the |its water is so transparent that) =Count(its water is so transparent that the) Count(its water is so transparent that) No! Too many possible sentences! · We'll never see enough data for estimating these

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Markov Assumption · Simplifying assumption: $P(\text{the }|\text{ its water is so transparent that}) \approx P(\text{the }|\text{ that})$ Or maybe $P(\text{the }|\text{ its water is so transparent that}) \approx P(\text{the }|\text{transparent that})$

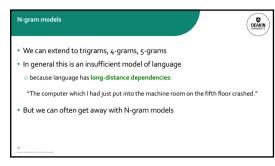
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Markov Assumption DEAKIN $P(w_1 w_2 ... w_n) \approx \prod P(w_i | w_{i-k} ... w_{i-1})$ • In other words, we approximate each component in the product $P(w_i | w_1 w_2 ... w_{i-1}) \approx P(w_i | w_{i-k} ... w_{i-1})$

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Simplest case: Unigram model $P(w_1 w_2 \dots w_n) \approx \prod P(w_i)$ Some automatically generated sentences from a unigram model fifth, an, of, futures, the, an, incorporated, a, a, the, inflation, most, dollars, quarter, in, is, mass thrift, did, eighty, said, hard, 'm, july, bullish that, or, limited, the 11

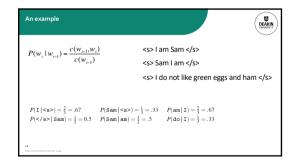
Bigram model DEAKIN · Condition on the previous word: $P(w_i | w_1 w_2 \dots w_{i-1}) \approx P(w_i | w_{i-1})$ texaco, rose, one, in, this, issue, is, pursuing, growth, in, a, boiler, house, said, mr., gurria, mexico, 's, motion, control, proposal, without, permission, from, five, hundred, fifty, five, yen outside, new, car, parking, lot, of, the, agreement, reached this, would, be, a, record, november





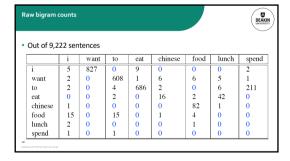
• The Maximum Likelihood Estimate $P(w_i \mid w_{i-1}) = \frac{count(w_{i-1}, w_i)}{count(w_{i-1})}$ $P(w_i \mid w_{i-1}) = \frac{c(w_{i-1}, w_i)}{c(w_{i-1})}$

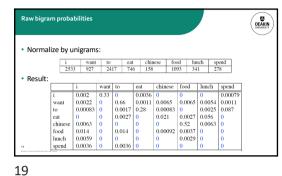
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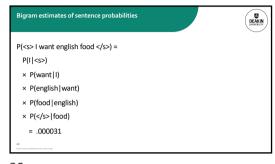


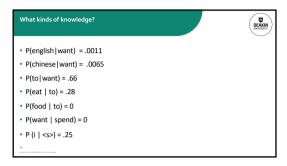
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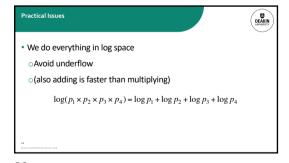


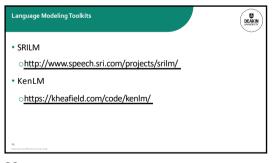






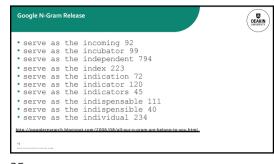
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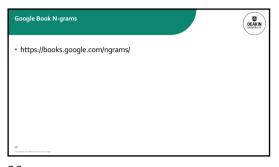


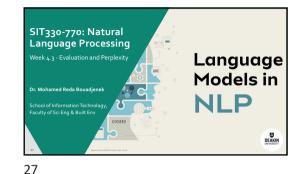




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"Extrinsic (in-vivo) Evaluation"

To compare models A and B

 Put each model in a real task
 Machine Translation, speech recognition, etc.

Run the task, get a score for A and for B
 How many words translated correctly
 How many words transcribed correctly

Compare accuracy for A and B

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Extrinsic (in-vitro) evaluation

Extrinsic evaluation not always possible

Expensive, time-consuming

Doesn't always generalize to other applications

Intrinsic evaluation: perplexity

Directly measures language model performance at predicting words.

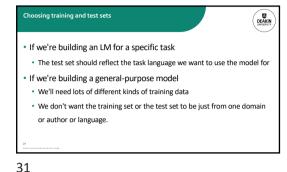
Doesn't necessarily correspond with real application performance

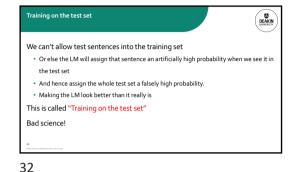
But gives us a single general metric for language models

Useful for large language models (LLMs) as well as n-grams

We train parameters of our model on a training set.
 We test the model's performance on data we haven't seen.
 A test set is an unseen dataset; different from training set.
 Intuition: we want to measure generalization to unseen data
 An evaluation metric (like perplexity) tells us how well our model does on the test set.

29 30





• If we test on the test set many times we might implicitly tune to its characteristics
• Noticing which changes make the model better.
• So we run on the test set only once, or a few times
• That means we need a third dataset:
• A development test set or, devset.
• We test our LM on the devset until the very end
• And then test our LM on the test set once

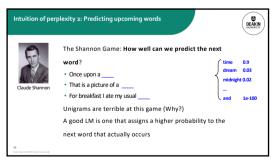
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Intuition of perplexity as evaluation metric: How good is our language model?

Intuition: A good LM prefers "real" sentences

Assign higher probability to "real" or "frequently observed" sentences

Assigns lower probability to "word salad" or "rarely observed" sentences?



Intuition of perplexity 3: The best language model is one that best predicts the entire unseen test set

* We said: a good LM is one that assigns a higher probability to the next word that actually occurs.

* Let's generalize to all the words!

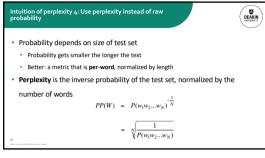
* The best LM assigns high probability to the entire test set.

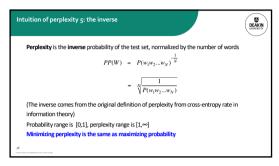
* When comparing two LMS, A and B

* We compute Px(test set) and Px(test set)

* The better LM will give a higher probability to (=be less surprised by) the test set than the other LM.

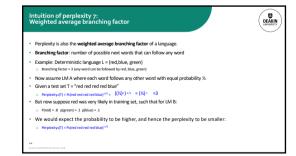
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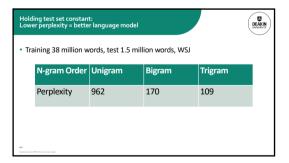


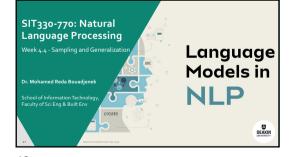
Intuition of perplexity 6: N-grams $PP(W) = P(w_iw_2 - w_N)^{\frac{1}{N}}$ $= \sqrt[N]{\frac{1}{P(w_iw_2 - w_N)}}$ Chain rule: $PP(W) = \sqrt[N]{\frac{1}{p-1}} \frac{1}{P(w_i|w_1 ... w_{i-1})}$ Bigrams: $PP(W) = \sqrt[N]{\frac{1}{p-1}} \frac{1}{P(w_i|w_{i-1})}$

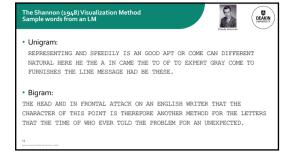
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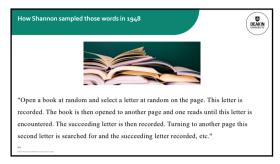


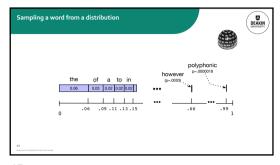
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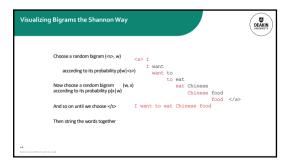


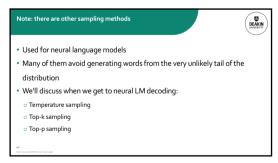


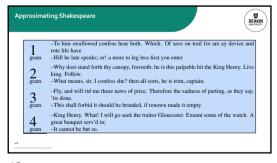




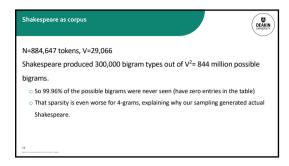
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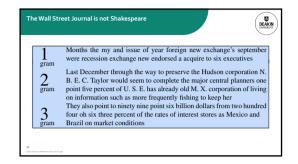






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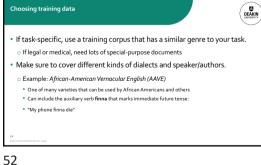


Can you guess the author? These 3-gram sentences are sampled from an LM trained on who?

1) They also point to ninety nine point six billion dollars from two hundred four oh six three percent of the rates of interest stores as Mexico and gram Brazil on market conditions
2) This shall forbid it should be branded, if renown made it empty.
3) "You are uniformly charming!" cried he, with a smile of associating and now and then I bowed and they perceived a chaise and four to wish for.

51

49 50



N-grams only work well for word prediction if the test corpus looks like the training corpus
But even when we try to pick a good training corpus, the test set will surprise us!
We need to train robust models that generalize!
One kind of generalization: Zeros
Things that don't ever occur in the training set
But occur in the test set

• Training set:

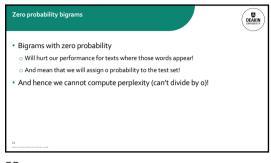
... ate lunch

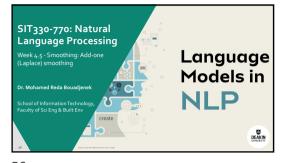
... ate dinner

... ate a

... ate the

P("breakfast" | ate) = 0





The intuition of smoothing (from Dan Klein)

• When we have sparse statistics:

File I denied the)

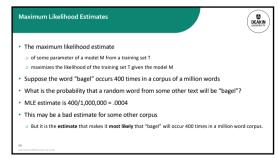
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1 reports
1 culms
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0 reports
1 culms
1 reports
1 report

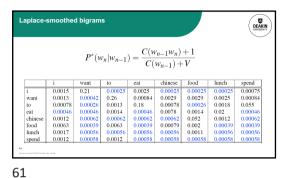
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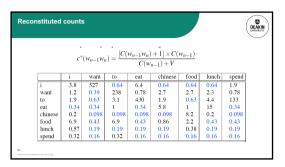
55 56

Add-one estimation $\begin{array}{c} \bullet \text{ Also called Laplace smoothing} \\ \bullet \text{ Pretend we saw each word one more time than we did} \\ \bullet \text{ Just add one to all the counts!} \\ \bullet \text{ MLE estimate: } P_{MLE}(w_i \mid w_{i-1}) = \frac{c(w_{i-1}, w_i)}{c(w_{i-1})} \\ \bullet \text{ Add-1 estimate: } P_{Add-1}(w_i \mid w_{i-1}) = \frac{c(w_{i-1}, w_i) + 1}{c(w_{i-1}) + V} \\ \end{array}$

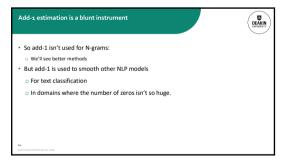
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1 62 63





Sometimes it helps to use less context
Condition on less context for contexts you haven't learned much about

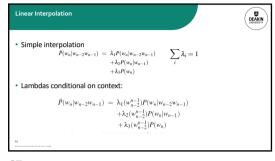
Backoff:
Use trigram if you have good evidence,
Otherwise bigram, otherwise unigram

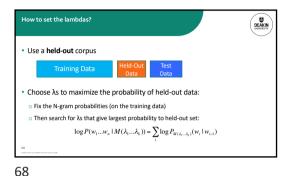
Interpolation:

mix unigram, bigram, trigram

Interpolation works better

64 65 66





If we know all the words in advanced

Verabulary via fixed

Closed verabulary visk

Offere we don't know this

Out of Verabulary - DOY words

Open verabulary ratik

Instead: create an unknown word token <UNIC>

Training of <UNIC probabilities

Context after fixed in a context of the contex

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67

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Huge web-scale n-grams

How to deal with, e.g., Google N-gram corpus
Pruning
Only store N-grams with count > threshold.

Remove singletons of higher-order n-grams
Entropy-based pruning
Efficiency
Efficiency
Efficient data structures like tries
Bloom filters: approximate language models
Store words as indexes, not strings
Use Nutfinan coding to fit large numbers of words into two bytes
Quantize probabilities (4-8 bits instead of 8-byte float)

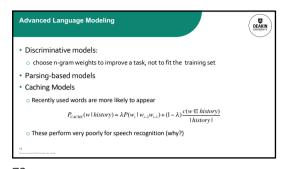
Smoothing for Web-scale N-grams * "Stupid backoff" (Brants \$et\$ \$al.\$ 2007) * No discounting, just use relative frequencies $S(w_i \mid w_{i-k+1}^{i-1}) = \begin{cases} \frac{\operatorname{count}(w_{i-k+1}^i)}{\operatorname{count}(w_{i-k+1}^i)} & \text{if } \operatorname{count}(w_{i-k+1}^i) > 0 \\ \frac{\operatorname{count}(w_{i-k+1}^i)}{\operatorname{count}(w_{i-k+2}^i)} & \text{otherwise} \end{cases}$ $S(w_i) = \frac{\operatorname{count}(w_i)}{N}$

N-gram Smoothing Summary

 Add-1 smoothing:
 OK for text categorization, not for language modeling

 The most commonly used method:
 Extended Interpolated Kneser-Ney

 For very large N-grams like the Web:
 Stupid backoff





DEAKIN Suppose we wanted to subtract a little from a count of 4 to save
 Italianing probability mass for the zeros .0000270 0.448 · How much to subtract ? 1.25 Church and Gale (1991)'s clever idea Divide up 22 million words of AP Newswire 3.23 Training and held-out set 4.21 o for each bigram in the training set 5.23 o see the actual count in the held-out set! 6.21 It sure looks like c* = (c - .75) 7.21 8.26

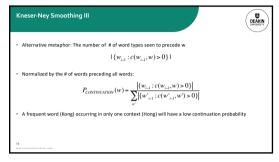
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73 74

* Save ourselves some time and just subtract 0.75 (or some d)! $P_{AbsoluteDiscounting}(w_i \mid w_{i-1}) = \frac{c(w_{i-1}, w_i) - d}{c(w_{i-1})} + \lambda(w_{i-1})P(w)$ * (Maybe keeping a couple extra values of d for counts 1 and 2) $P_{AbsoluteDiscounting}(w_i \mid w_{i-1}) = \frac{c(w_{i-1}, w_i) - d}{c(w_{i-1})} + \lambda(w_{i-1})P(w)$ * (Maybe keeping a couple extra values of d for counts 1 and 2) $P_{AbsoluteDiscounting}(w_i \mid w_{i-1}) = \frac{c(w_{i-1}, w_i) - d}{c(w_{i-1})} + \lambda(w_{i-1})P(w)$

76

 $\begin{aligned} & \text{Kneser-Ney Smoothing II} \\ & & \text{Power Smoothing II} \\ & & P_{CONTINUATION}(w) \times \left[\{w_{i-1} : c(w_{i-1}, w) > 0\} \right] \\ & & \text{Normalized by the total number of word bigram types} \\ & \left[\{(w_{j-1}, w_j) : c(w_{j-1}, w_j) > 0\} \right] \\ & & P_{CONTINUATION}(w) = \frac{\left[\{w_{j-1} : c(w_{i-1}, w) > 0\} \right]}{\left[\{(w_{j-1}, w_j) : c(w_{j-1}, w_j) > 0\} \right]} \end{aligned}$



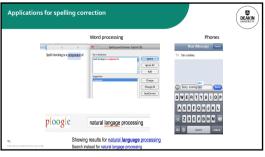
 $P_{EN}(w_i \, | \, w_{i:i}) = \frac{\max(c(w_{i:i}, w_i) - d, 0)}{c(w_{i:i})} + \lambda(w_{i:i})P_{CONTRVLATION}(w_i)$ $\lambda \text{ is a normalizing constant; the probability mass we've discounted}$ $\lambda(w_{i:i}) = \frac{d}{c(w_{i:i})} \left[\left\{ w : c(w_{i:i}, w) > 0 \right\} \right]$ The number of word spore that can follow we. = 8 of word spore we discounted = 8 of times we applied normalized discount

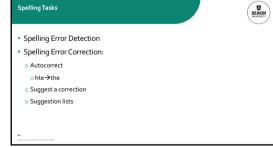
Kneser-Ney Smoothing: Recursive formulation $P_{KN}(w_i \mid w_{i-n+1}^{i-1}) = \frac{\max(c_{KN}(w_{i-n+1}^i) - d, 0)}{c_{KN}(w_{i-n+1}^i)} + \lambda(w_{i-n+1}^{i-1})P_{KN}(w_i \mid w_{i-n+2}^{i-1})$ $c_{KN}(\bullet) = \begin{cases} count(\bullet) & \text{for the highest order} \\ continuation count(\bullet) & \text{for lower order} \end{cases}$ Continuation count = Number of unique single word contexts for \bullet

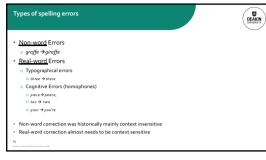
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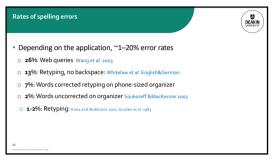


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Non-word spelling errors

• Non-word spelling error detection:

• Any word not in a dictionary is an error

• The larger the dictionary the better ... up to a point

• (The Web is full of mis-spellings, so the Web isn't necessarily a great dictionary ...)

• Non-word spelling error correction:

• Generate candidates: real words that are similar to error

• Choose the one which is best:

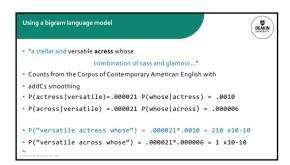
• Shortest weighted edit distance

• Highest noisy channel probability

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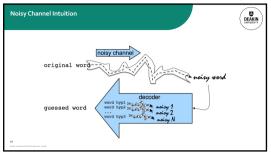
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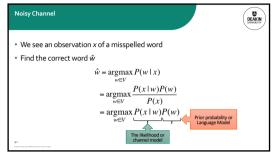
For each word w, generate candidate set:
For each word w, generate candidate set:
Find candidate words with similar pronunciations
Find candidate words with similar spellings
Include win candidate set
Choose best candidate
Noisy Channel view of spell errors
Context-sensitive – so have to consider whether the surrounding words "make sense"
Flying form Heathrow to LAX → Flying from Heathrow to LAX

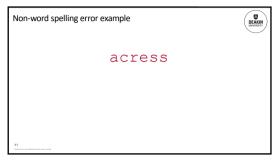


SIT330-770: Natural Language Processing
Week 4.9 – The Noisy Channel Model of Spelling
Dr. Mohamed Reda Bouadjenek
School of Information Technology, Faculty of Sci Eng & Butt Env

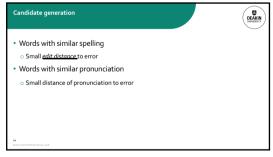
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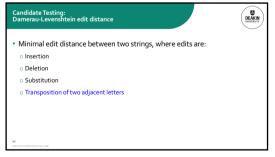


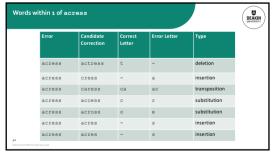




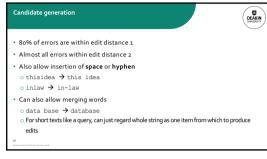
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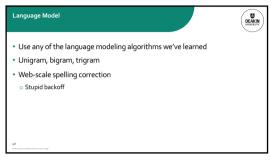






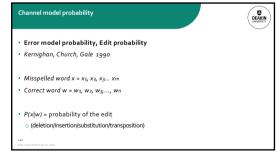
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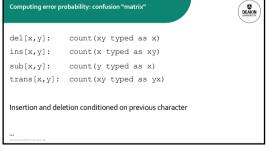




Unigram Prior probability DEAKIN UNIVERSITY • Counts from 404,253,213 words in Corpus of Contemporary English (COCA) Frequency of word P(w) 9,321 .0000230573 actress 220 .0000005442 cress 686 .0000016969 caress 37,038 .0000916207 access 120,844 .0002989314 across 12,874 .0000318463 acres

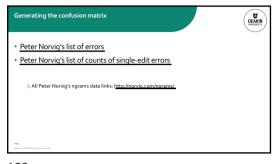
97 98 99

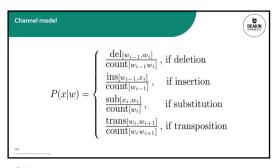






100 101 102





	1	1		
Candidate Correction	Correct Letter	Error Letter	x/w	P(x w)
actress	t	-	c ct	.000117
cress	-	a	a #	.00000144
caress	ca	ac	ac ca	.00000164
access	С	r	r c	.000000209
across	0	е	elo	.0000093
acres	-	s	es e	.0000321
acres	-	s	ss s	.0000342

103 104 105

Noisy channel probability for acress						
Candidate Correction	Correct Letter	Error Letter	x/w	P(x w)	P(w)	109* P(x w)* P(w)
actress	t	-	c ct	.000117	.0000231	2.7
cress	-	a	a #	.00000144	.000000544	.00078
caress	ca	ac	ac ca	.00000164	.00000170	.0028
access	С	r	r c	.000000209	.0000916	.019
across	0	е	elo	.0000093	.000299	2.8
acres	-	s	es e	.0000321	.0000318	1.0
acres	-	s	ss s	.0000342	.0000318	1.0



Using a bigram language model

• "a stellar and versatile acress whose combination of sass and glamour..."

• Counts from the Corpus of Contemporary American English with add-1 smoothing

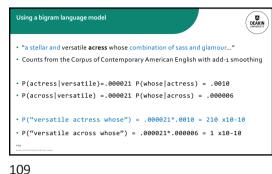
• P(actress|versatile)=.000021 P(whose|actress)=.0010

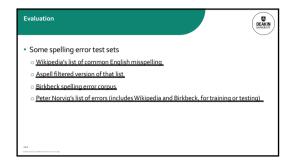
• P(across|versatile)=.000021 P(whose|across)=.000006

• P("versatile actress whose")=.000021*.0010=210 x10-10

• P("versatile across whose")=.000021*.000006=1 x10-10

106 107 108





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SIT330-770: Natural Language Processing

Week 4.10 - Real-word spelling errors

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School of Information Technology, Faculty of Sci Eng & Built Env

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109

• ...leaving in about fifteen *minuets* to go to her house.
• The design *an* construction of the system...
• Can they *lave* him my messages?
• The study was conducted mainly *be* John Black.
• 25-40% of spelling errors are real words Kukich 1992

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• For each word in sentence (phrase, query ...)

• Generate candidate set

• the word itself

• all single-letter edits that are English words

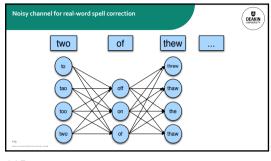
• words that are homophones

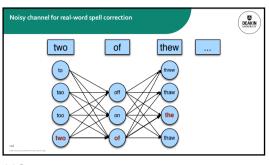
• (all of this can be pre-computed!)

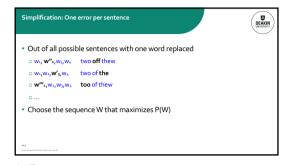
• Choose best candidates

• Noisy channel model

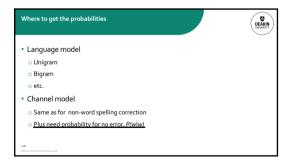
• Given a sentence $w_{s_{2}}w_{2},w_{3},...,w_{n}$ • Generate a set of candidates for each word w_{n} • Candidate(w_{n}) = [$w_{n},w_{n},w_{n},w_{n},w_{n}$]
• Candidate(w_{n}) = [$w_{n},w_{n},w_{n},w_{n},w_{n}$]
• Choose the sequence W that maximizes P(W)







115 116 117



• What is the channel probability for a correctly typed word?

• P("the"|"the")

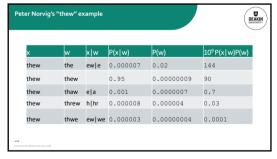
olf you have a big corpus, you can estimate this percent correct

• But this value depends strongly on the application

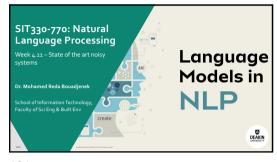
ole of cerror in 10 words)

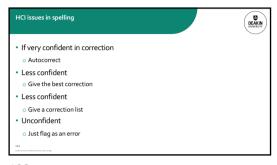
ole of cerror in 20 words)

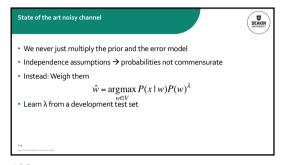
ole of cerror in 100 words)



118 119 120

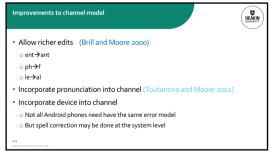


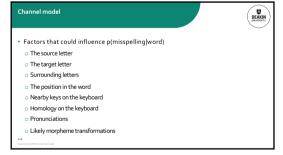




121 122 123







124 125 126



