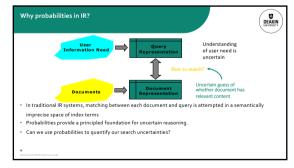
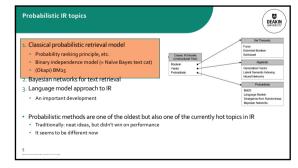


2





The document ranking problem

We have a collection of documents

User issues a query

A list of documents needs to be returned

Ranking method is the core of modern IR systems:

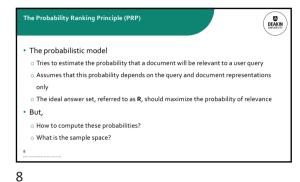
In what order do we present documents to the user?

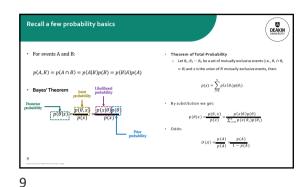
We want the "best" document to be first, second best second, etc.

Idea: Rank by probability of relevance of the document w.r.t. information need

P(R=a|document, query)





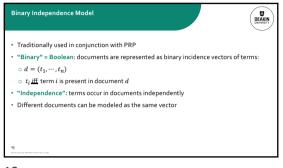


The Probability Ranking Principle (PRP) DEAKIN UNIVERSITY - Let $\ensuremath{\emph{d}}$ represent a document in the collection * Let $\it R$ represent relevance of a document w.r.t. given (fixed) query and let $\it R=1$ represent relevant and R = 1 not relevant Need to find p(R = 1|d) – probability that a document d is relevant • $p(R = 1|d) = \frac{p(d|R=1)p(R=1)}{2}$ p(R=1), p(R=0) - prior probability of retrieving a relevant or non-relevant document at random • $p(R = 0|d) = \frac{p(d|R=0)p(R=0)}{p(d)}$ p(d|R=1) , p(d|R=0) - probability that if a relevant (not relevant) document is retrieved, it is d• p(R = 0|d) + p(R = 1|d) = 1

Probabilistic Retrieval Strategy DEAKIN UMVERSITY · First, estimate how each term contributes to relevance o How do other things like term frequency and document length influence your judgments about document relevance? Not at all in BIM o A more nuanced answer is given by BM25 · Combine to find document relevance probability · Order documents by decreasing probability • Theorem: Using the PRP is optimal, in that it minimizes the loss (Bayes risk) under 1/o o Provable if all probabilities correct, etc. [e.g., Ripley 1996]

network office structure document search digital technology security The Binary Independence Model: BIM order software retrieve connection metadata service control record tracking service control enterprise analysis documentation DEAKIN online access consulting

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Binary Independence Model $\begin{array}{c} \text{DEAN} \\ \text$

Binary Independence Model $O(R|q,\vec{x}) = \frac{p(R=1|q,d)}{p(R=0|q,d)} \underbrace{\begin{array}{l} p(R=1|q) \\ p(R=0|q,d) \\ p(R=0|q,d) \end{array}}_{p(R=0|q)} \underbrace{\begin{array}{l} p(d|R=1,q) \\ p(d|R=0,q) \\ p(d|R=0,q) \end{array}}_{\text{Needs estimation}}$ $\cdot \text{ Using independence Assumption: } \underbrace{\begin{array}{l} \text{Constant for a} \\ \text{Evice nucey} \\ p(d|R=0,q) \\ \hline \end{array}}_{p(d|R=0,q)} \underbrace{\begin{array}{l} p(t_1|R=1,q) \\ p(d|R=0,q) \\ \hline \end{array}}_{n=1} \underbrace{\begin{array}{l} p(t_1|R=1,q) \\ p(t_1|R=0,q) \\ \hline \end{array}}_{p(t_1|R=0,q)}$ $O(R|q,d) = O(R|q) \times \prod_{i=1}^{n} \frac{p(t_i|R=1,q)}{p(t_i|R=0,q)}$

15

13 14

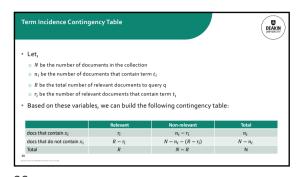
Binary Independence Model $O(R|q,d) = O(R|q) \times \prod_{i=1}^n \frac{p(t_i|R=1,q)}{p(t_i|R=0,q)}$ • Since x_i is either o or 1: $O(R|q,d) = O(R|q) \times \prod_{i=1}^n \frac{p(t_i|R=1,q)}{p(t_i|R=0,q)} \times \prod_{i=0}^n \frac{p(t_i|R=1,q)}{p(t_i|R=0,q)}$ • Let $x_i = p(t_i|R=1,q)$ and $y_i = p(t_i|R=0,q)$.
• Assume, for all terms not occurring in the query $(q_i=0)$ $p_i = u_i$: $O(R|q,d) = O(R|q) \times \prod_{i=1}^{p_i} \frac{1}{q_i} \times \prod_{i=1}^{q_i} \frac{1-p_i}{d_i}$

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Binary Independence Model $O(R|q,d) = O(R|q) \times \prod_{\substack{q=1\\q=1}}^{p_i} \prod_{\substack{q=1\\q=1}}^{(1-p_i)} \frac{(1-p_i)}{(1-u_i)}$ Non-matching query terms $O(R|q,\vec{x}) = O(R|q) \times \prod_{\substack{q=1\\q=1}}^{q} \prod_{u_i} \prod_{\substack{l_i=1\\l_i=1}}^{(1-u_i)} \frac{1-p_{l_i}}{1-u_l} \prod_{\substack{q=1\\q=1}}^{(1-p_i)} \frac{(1-p_i)}{(1-u_i)}$ $O(R|q,\vec{x}) = O(R|q) \times \prod_{\substack{q=1\\q=1}}^{q} \prod_{u_i} \prod_{\substack{l_i=1\\u_i=1}}^{(1-u_i)} \frac{1-p_{l_i}}{1-u_l} \prod_{\substack{l_i=1\\q=1}}^{(1-p_i)} \frac{1-p_{l_i}}{1-u_l}$ All matching terms

Binary Independence Model $O(R|q,d) = O(R|q) \times \underbrace{\prod_{\substack{l_l = q_l = 1 \\ l_l = q_l = 1}}^{p_l(1-u_l)} \underbrace{\prod_{\substack{u_l (1-p_l) \\ \text{only quuntity to be estimated} \\ \text{for rankings}}}^{(1-p_l)} \times \underbrace{\prod_{\substack{l_l = q_l = 1 \\ l_l = q_l = 1}}^{(1-p_l)} \underbrace{\prod_{\substack{l_l = q_l = 1 \\ l_l = q_l = 1}}^{(1-p_l)} \underbrace{\prod_{\substack{l_l = q_l = 1 \\ l_l = q_l = 1}}^{(1-p_l)} \underbrace{\prod_{\substack{l_l = q_l = 1 \\ l_l = q_l = 1}}^{(1-p_l)} \times \underbrace{\prod_{\substack{l_l = q_l = 1 \\ l_l = q_l = 1}}^{(1-p_l)} \times \underbrace{\prod_{\substack{l_l = q_l = 1 \\ l_l = q_l = 1}}^{(1-p_l)} \times \underbrace{\prod_{\substack{l_l = q_l = 1 \\ l_l = q_l = 1}}^{(1-p_l)} \times \underbrace{\prod_{\substack{l_l = q_l = 1 \\ l_l = q_l = 1}}^{(1-p_l)} \times \underbrace{\prod_{\substack{l_l = q_l = 1 \\ l_l = q_l = 1}}^{(1-p_l)} \times \underbrace{\prod_{\substack{l_l = q_l = 1 \\ l_l = q_l = 1}}^{(1-p_l)} \times \underbrace{\prod_{\substack{l_l = q_l = 1 \\ l_l = q_l = 1}}^{(1-p_l)} \times \underbrace{\prod_{\substack{l_l = q_l = 1 \\ l_l = q_l = 1}}^{(1-p_l)} \times \underbrace{\prod_{\substack{l_l = q_l = 1 \\ l_l = q_l = 1}}^{(1-p_l)} \times \underbrace{\prod_{\substack{l_l = q_l = 1 \\ l_l = q_l = 1}}^{(1-p_l)} \times \underbrace{\prod_{\substack{l_l = q_l = 1 \\ l_l = q_l = 1}}^{(1-p_l)} \times \underbrace{\prod_{\substack{l_l = q_l = 1 \\ l_l = q_l = 1}}^{(1-p_l)} \times \underbrace{\prod_{\substack{l_l = q_l = 1 \\ l_l = q_l = 1}}^{(1-p_l)} \times \underbrace{\prod_{\substack{l_l = q_l = 1 \\ l_l = q_l = 1}}^{(1-p_l)} \times \underbrace{\prod_{\substack{l_l = q_l = 1 \\ l_l = q_l = 1}}^{(1-p_l)} \times \underbrace{\prod_{\substack{l_l = q_l = 1 \\ l_l = q_l = 1}}^{(1-p_l)} \times \underbrace{\prod_{\substack{l_l = q_l = 1 \\ l_l = q_l = 1}}^{(1-p_l)} \times \underbrace{\prod_{\substack{l_l = q_l = 1 \\ l_l = 1}}^{(1-p_l)} \times \underbrace{\prod_{\substack{l_l = q_l = 1 \\ l_l = 1}}^{(1-p_l)} \times \underbrace{\prod_{\substack{l_l = q_l = 1 \\ l_l = 1}}^{(1-p_l)} \times \underbrace{\prod_{\substack{l_l = q_l = 1 \\ l_l = 1}}^{(1-p_l)} \times \underbrace{\prod_{\substack{l_l = q_l = 1 \\ l_l = 1}}^{(1-p_l)} \times \underbrace{\prod_{\substack{l_l = q_l = 1 \\ l_l = 1}}^{(1-p_l)} \times \underbrace{\prod_{\substack{l_l = q_l = 1 \\ l_l = 1}}^{(1-p_l)} \times \underbrace{\prod_{\substack{l_l = q_l = 1 \\ l_l = 1}}^{(1-p_l)} \times \underbrace{\prod_{\substack{l_l = q_l = 1 \\ l_l = 1}}^{(1-p_l)} \times \underbrace{\prod_{\substack{l_l = q_l = 1 \\ l_l = 1}}^{(1-p_l)} \times \underbrace{\prod_{\substack{l_l = q_l = 1 \\ l_l = 1}}^{(1-p_l)} \times \underbrace{\prod_{\substack{l_l = q_l = 1}}^{(1-p_l)} \times \underbrace{\prod_{\substack{l_l = 1 \\ l_l = 1}}^{(1-p_l)} \times \underbrace{\prod_{\substack{l_l = q_l = 1}}^{(1-p_l)} \times \underbrace{\prod_{\substack{l_l = q_l$





Ranking Formula DEAKIN UNIVERSITY · If information on the contingency table were available for a given query, we could write: · Then, the equation for ranking computation in the probabilistic model could be rewritten $Sim(q,d) \approx \sum_{t_i = q_i = 1} \log \left(\frac{r_i}{R - r_i} \times \frac{N - n_i - R + r_i}{n_i - r_i} \right)$

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DEAKIN UNIVERSITY • In the previous formula, we are still dependent on an estimation of the relevant • For handling small values of r_{ij} we add 0.5 to each of the terms in the formula above, which changes Sim(q,d) into $Sim(q,d) \approx \sum_{t_i = q_i = 1} \log \left(\frac{r_i + 0.5}{R - r_i + 0.5} \times \frac{N - n_i - R + r_i + 0.5}{n_i - r_i + 0.5} \right)$ • This formula is considered as the classic ranking equation for the probabilistic model and is known as the Robertson-Sparck Jones Equation

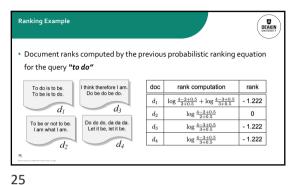
Ranking Formula

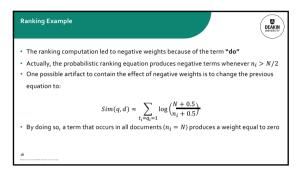
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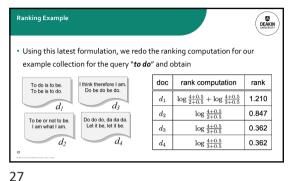
Ranking Formula DEAKIN UMVERSITY • The previous equation cannot be computed without estimates of r_i and R• One possibility is to assume $R = r_i = 0$, as a way to boostrap the ranking equation, which leads to $Sim(q, d) \approx \sum_{t_i = q_i = 1} \log \left(\frac{N - n_i + 0.5}{n_i + 0.5} \right)$ This equation provides an idf-like ranking computation • In the absence of relevance information, this is the equation for ranking in the probabilistic model

network office structure document search digital technology security **BIM Ranking Example** order software retrieve connection metadata record tracking record tracking service control enterprise analysis documentation DEAKIN online access consulting

23 24

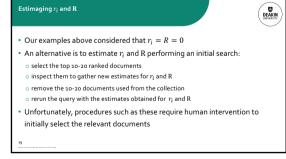


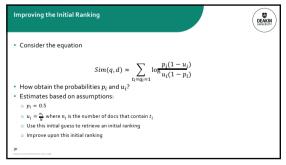




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29 30

Improving the Initial Ranking

DEAKIN UNIVERSITY

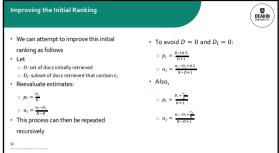
ullet Substituting p_i and u_i into the previous Equation, we obtain:

$$Sim(q,d) \approx \sum_{t_i = q_i = 1} \log \frac{\left(N - n_i\right)}{n_i}$$

- That is the equation used when no relevance information is provided, without the 0.5 correction factor
- Given this initial guess, we can provide an initial probabilistic ranking
- After that, we can attempt to improve this initial ranking as follows

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Pluses and Minuses

Advantages:
Docs ranked in decreasing order of probability of relevance

Disadvantages:
need to guess initial estimates for p_l method does not take into account tf factors
the lack of document length normalization

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Comparison of Classic Models



- Boolean model does not provide for partial matches and is considered to be the weakest classic model
- There is some controversy as to whether the probabilistic model outperforms the vector model
- Croft suggested that the probabilistic model provides a better retrieval performance
- However, Salton et al showed that the vector model outperforms it with general collections
- This also seems to be the dominant thought among researchers and practitioners of $\ensuremath{\mathsf{IR}}$

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The BM (Best Match) Models data technology security

The BM (Best Match) Models data

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BM25 (Best Match 25)



- BM25 was created as the result of a series of experiments on variations of the probabilistic model
- · A good term weighting is based on three principles
- o inverse document frequency
- term frequency
- o document length normalization
- $\bullet\,$ The classic probabilistic model covers only the first of these principles
- This reasoning led to a series of experiments with the Okapi system, which led to the BM25 ranking formula

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BM1, BM11 and BM15 Formulas

DEAKIN UNIVERSITY

• At first, the Okapi system used the Equation below as ranking formula

$$Sim(q,d) \approx \sum_{t_i=q_i=1} \log \left(\frac{N-n_i+0.5}{n_i+0.5} \right)$$

which is the equation used in the probabilistic model, when no relevance information is

• It was referred to as the BM1 formula (Best Match 1)

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BM1, BM11 and BM15 Formulas



- The first idea for improving the ranking was to introduce a term-frequency factor $\mathcal{F}_{t,d}$ in the BM1 formula
- · This factor, after some changes, evolved to become

$$\mathcal{F}_{t,d} = S_1 \times \frac{tf_{t,d}}{K_1 + tf_{t,d}}$$

- o $tf_{t,d}$ is the frequency of term t within document d
- K₁ is a constant setup experimentally for each collection S₁ is a scaling constant, normally set to S₂ = (K₂₊₁)
- If $K_1 = 0$ this whole factor becomes equal to and bears no effect in the ranking

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BM1, BM11 and BM15 Formulas



DEAKIN UNIVERSITY

• The next step was to modify the $\mathcal{F}_{t,d}$ factor by adding document length normalization to it, as follows:

$$\mathcal{F}_{t,d}^{\cdot} = S_1 \times \frac{tf_{t,d}}{\frac{K_1 \times len(d)}{avg_doclen} + tf_{t,d}}$$

- \circ len(d) is the length of document d (computed, for instance, as the number of terms in the
- o avg_doclen is the average document length for the collection

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BM1, BM11 and BM15 Formulas



- Next, a correction factor \mathcal{G}_q dependent on the document and query lengths was added

$$G_q = K_2 \times len(q) \times \frac{avg_doclen - len(d)}{ave_doclen + len(d)}$$

Where

- \circ len(q) is the query length (number of terms in the query)
- K₂ is a constant

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BM1, BM11 and BM15 Formulas



• A third additional factor, aimed at taking into account term frequencies within queries, was defined as

$$\mathcal{F}_{t,d} = S_3 \times \frac{t f_{t,q}}{K_2 + t f_{t,q}}$$

- o $tf_{t,d}$ is the frequency of term t within query q
- K₃ is a constant
- o S_3 is a scaling constant related to K_3 , normally set to $S_3 = (K_3 + 1)$

 $Sim_{BM15}(q,d) \approx \mathcal{G}_q + \sum_{t_i = q_i = 1} \mathcal{F}_{t,d} \times \mathcal{F}_{t,q} \times \log \frac{\left(N - n_i + 0.5\right)}{n_i + 0.5}$

 $Sim_{BM1}(q,d) \approx \sum_{t_i=q_i=1} \log \frac{\left(N-n_i+0.5\right)}{n_i+0.5}$

Introduction of these three factors led to various BM (Best Matching) formulas, as follows:

 $Sim_{BM11}(q,d) \approx \mathcal{G}_q + \sum_{t_i = q_i = 1} \mathcal{F}_{t,d} \times \mathcal{F}_{t,q} \times \log \frac{\left(N - n_i + 0.5\right)}{n_i + 0.5}$

BM1, BM11 and BM15 Formulas

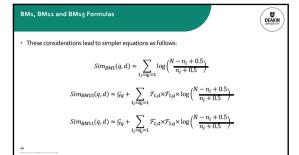
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BM1, BM11 and BM15 Formulas



- Experiments using TREC data have shown that BM11 outperforms BM15
- · Further, empirical considerations can be used to simplify the previous equations, as follows:
- \circ Empirical evidence suggests that a best value of K_2 is 0, which eliminates the \mathcal{G}_q factor from these equations
- \circ Further, good estimates for the scaling constants S_1 and S_3 are K_1+1 and K_3+1 , respectively
- \circ Empirical evidence also suggests that making K_3 very large is better. As a result, the $\mathcal{F}_{t,q}$ factor is reduced simply to $f_{t,d}$
- \circ For short queries, we can assume that $f_{t,d}$ is 1 for all terms

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network office structure document search digital technology security The BM25 Model record tracking record tracking service control enterprise analysis documentation consulting

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BM25 Ranking Formula



- BM25: combination of the BM11 and BM15
- The motivation was to combine the BM11 and BM25 term frequency factors as follows:

$$B_{t,d} = \frac{(K_1 + 1)tf_{t,q}}{K_1\left[(1-b) + b\frac{len(d)}{avg_doclen}\right] + tf_{t,q}}$$

Where b is a is a constant with values in the interval [0,1]

- If b = 0, it reduces to the BM15 term frequency factor
- $_{\odot}\,$ If b=1 , it reduces to the BM11 term frequency factor
- o For values of b between 0 and 1, the equation provides a combination of BM11 with BM15

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• The ranking equation for the BM25 model can then be written as:

$$Sim_{BM25}(q,d) \approx \sum_{t_i=q_i=1} \mathcal{B}_{t,d} \times \log\left(\frac{N-n_i+0.5}{n_i+0.5}\right)$$

where K_1 and b are empirical constants

- K₁ = 1 works well with real collections
- o b should be kept closer to 1 to emphasize the document length normalization effect present in the BM11
- \circ For instance, $b=0.75\,$ is a reasonable assumption
- Constants values can be fine tunned for particular collections through proper experimentation

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BM25 Ranking Formula



- Unlike the probabilistic model, the BM25 formula can be computed without relevance information
- There is consensus that BM25 outperforms the classic vector model for general collections
- · Thus, it has been used as a baseline for evaluating new ranking functions, in substitution to the classic vector model



Measures for a search engine DEAKIN · How fast does it index Number of documents/hour (Average document size) How fast does it search o Latency as a function of index size Expressiveness of query language o Ability to express complex information needs Speed on complex queries Uncluttered UI Is it free?

Measures for a search engine DEAKIN UNIVERSITY • All of the preceding criteria are measurable: we can quantify speed/size o we can make expressiveness precise • The key measure: user happiness O What is this? Speed of response/size of index are factors o But blindingly fast, useless answers won't make a user happy · Need a way of quantifying user happiness

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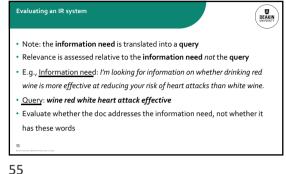
Measuring user happiness DEAKIN UNIVERSITY · Issue: who is the user we are trying to make happy? Depends on the setting Web engine: User finds what s/he wants and returns to the engine o Can measure rate of return users o User completes task – search as a means, not end o See Russell http://dmrussell.googlepages.com/JCDL-talk-June-2007-short.pdf · eCommerce site: user finds what s/he wants and buys o Is it the end-user, or the eCommerce site, whose happiness we measure? o Measure time to purchase, or fraction of searchers who become buyers?

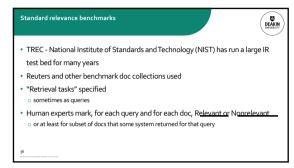
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Measuring user happiness DEAKIN UMVERSITY • Enterprise (company/govt/academic): Care about "user productivity" o How much time do my users save when looking for information? o Many other criteria having to do with breadth of access, secure access, etc.

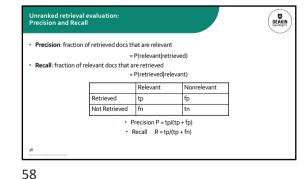
Happiness: elusive to measure DEAKIN UNIVERSITY · Most common proxy: relevance of search results But how do you measure relevance? • We will detail a methodology here, then examine its issues Relevance measurement requires 3 elements: 1. A benchmark document collection 2. A benchmark suite of queries 3. A usually binary assessment of either Relevant or Nonrelevant for each query and each document o Some work on more-than-binary, but not the standard

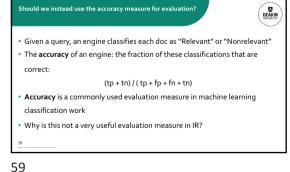
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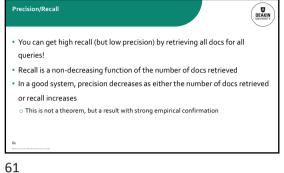












Difficulties in using precision/recall DEAKIN UNIVERSITY • Should average over large document collection/query ensembles • Need human relevance assessments o People aren't reliable assessors · Assessments have to be binary o Nuanced assessments? · Heavily skewed by collection/authorship o Results may not translate from one domain to another

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A combined measure: F DEAKIN UNIVERSITY Combined measure that assesses precision/recall tradeoff is F measure (weighted harmonic mean): People usually use balanced F₂ measure o i.e., with $\beta = 1$ or $\alpha = \frac{1}{2}$ Harmonic mean is a conservative average o See CJ van Rijsbergen, Information Retrieval

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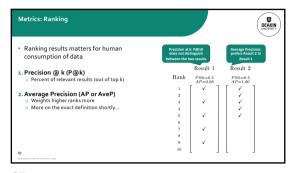
F₂ and other averages DEAKIN UNIVERSITY Combined Measures Maximum 20 40 60 80

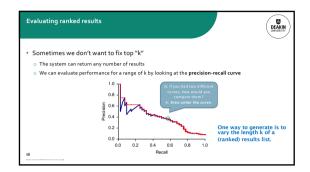
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Ranked evaluation metrics order software retrieve connection metadata record tracking record tracking service control enterprise analysis documentation online access consulting

Evaluating ranked results DEAKIN UNIVERSITY • Up until now we've been considering metrics for boolean (set-based) retrieval o Precision, Recall, F1 But users don't really care about all results · Users care about getting results near top of ranking...

65 66





For a good, but people want summary measures!

P@k good for most of web search... why? what k?

But P@k averages badly

if only so relevant docs, max P@soo is 0.1

Also has an arbitrary parameter of k

Sometimes R-Prec is better

R-Prec definition P@k with k-#irrelevant docs (for query)

max R-Prec is 10, wh?

But P@k and R-Prec still use a fixed k. Does any ranking metric approximate area under precision-recall curve?

Well yes, average precision does just that...

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• Average Precision (AveP or AP) and Mean AP (MAP)

 • Average Precision (AveP or AP) and Mean AP (MAP)

 • MAP = \(\frac{\subseteq_{q-1}^{Q} \text{ AveP}(q)}{Q} \)

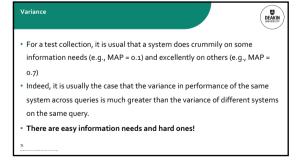
 • AveP = \(\frac{\subseteq_{q-1}^{N-1}(P(k) \times \text{rel}(k))}{\subseteq_{q-1}^{N-1}(P(k) \times \text{rel}(k))} \)

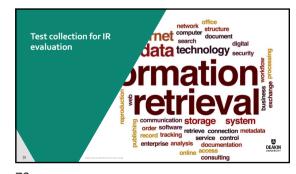
 • AP = higher ranked docs are counted more often

 • Unlike P@k, ordering natters!

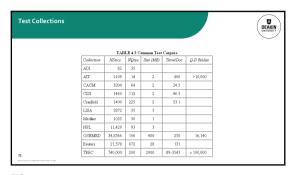
 • AP = area under precision-recall curve when n→#all docs!

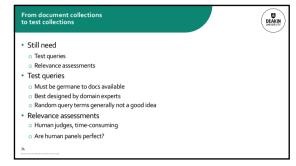
 • Good discussions in R book and on Wilsipeds treasing unloads are inhabit frameton introdiffictures and constructions are in the construction of the construction





70 71 72





* TREC Ad Hoc task from first 8 TRECs is standard IR task

• so detailed information needs a year

• Human evaluation of pooled results returned

• More recently other related things: Web track, HARD

• A TREC query (TREC s)

*ctops

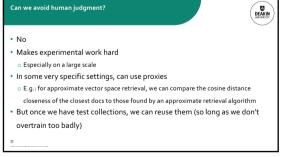
roum> Number: 225

<desc- Description:
What is the main function of the Federal Emergency Management Agency (FEMA) and the funding level provided to meet emergencies? Also, what resources are available to FEMA such as people, equipment, facilities?

*c/top?

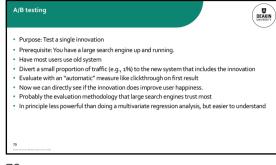
73 74 75

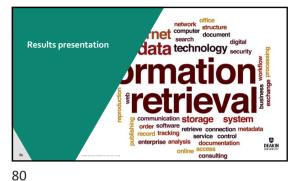




Search engines have test collections of queries and hand-ranked results
Recall is difficult to measure on the web
Search engines often use precision at top k, e.g., k = 10
... or measures that reward you more for getting rank 1 right than for getting rank 10 right.
NDCC (Normalized Cumulative Discounted Gain)
Search engines also use non-relevance-based measures.
Clickthrough on first result
No two reyrelable if you look at a single clickthrough ... but pretty reliable in the aggregate.
Studies of user behavior in the lab
All testing

76 77 78





Result Summaries DEAKIN UNIVERSITY · Having ranked the documents matching a guery, we wish to present a results Most commonly, a list of the document titles plus a short summary, aka "10 blue links"

81

79

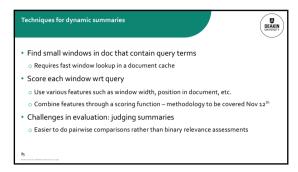
Summaries DEAKIN UNIVERSITY • The title is often automatically extracted from document metadata. What about the summaries? User can identify good/relevant hits based on description. · Two basic kinds: Static Dynamic A static summary of a document is always the same, regardless of the guery that hit the doc • A dynamic summary is a query-dependent attempt to explain why the document was retrieved for the query at hand

82

Static summaries DEAKIN UMAYERSITY · In typical systems, the static summary is a subset of the document • Simplest heuristic: the first 50 (or so – this can be varied) words of the document Summary cached at indexing time · More sophisticated: extract from each document a set of "key" sentences Simple NLP heuristics to score each sentence Summary is made up of top-scoring sentences. · Most sophisticated: NLP used to synthesize a summary o Seldom used in IR; cf. text summarization work

Dynamic summaries DEAKIN UNIVERSITY · Present one or more "windows" within the document that contain several of the query terms o "KWIC" snippets: Keyword in Context presentation

83 84







85 86 87

