



What is a Language Model? · A model to assign a probability to a sentence o Machine Translation: OP(high winds tonight) > P(large winds tonight) Spell Correction • The office is about fifteen minuets from my house! • P(about fifteen minutes from) > P(about fifteen minuets from) Speech Recognition OP(I saw a van) >> P(eyes awe of an) o + Summarization, question, answering, etc., etc.!!

Probabilistic Language Modeling DEAKIN UNIVERSITY · Goal: compute the probability of a sentence or sequence of words: $P(W) = P(w_1, w_2, w_3, w_4, w_5...w_n)$ · Related task: probability of an upcoming word: $P(w_5 | w_1, w_2, w_3, w_4)$ • A model that computes either of these: P(W) or $P(w_n|w_1,w_2...w_{n-1})$ is called a language model. Better: the grammar But language model or LM is standard

How to compute P(W) DEAKIN UMAYERSITY · How to compute this joint probability: o P(its, water, is, so, transparent, that) · Intuition: let's rely on the Chain Rule of Probability

Reminder: The Chain Rule DEAKIN UNIVERSITY · Recall the definition of conditional probabilities p(B|A) = P(A,B)/P(A) Rewriting: P(A,B) = P(A)P(B|A) More variables: P(A,B,C,D) = P(A)P(B|A)P(C|A,B)P(D|A,B,C)• The Chain Rule in General $P(x_1,x_2,x_3,...,x_n) = P(x_1)P(x_2|x_1)P(x_3|x_1,x_2)...P(x_n|x_1,...,x_{n-1})$

The Chain Rule applied to compute joint probability of words in

DEAKIN UNIVERSITY

 $P(w_1 w_2 ... w_n) = \prod_i P(w_i | w_1 w_2 ... w_{i-1})$

P("its water is so transparent") =

 $P(its) \times P(water | its) \times P(is | its water)$

× P(so|its water is) × P(transparent|its water is so)

.

How to estimate these probabilities



• Could we just count and divide?

 $P(\text{the lits water is so transparent that}) = \frac{Count(\text{its water is so transparent that the})}{Count(\text{its water is so transparent that})}$

- No! Too many possible sentences!
- · We'll never see enough data for estimating these

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Markov Assumption



• Simplifying assumption:

 $P(\text{the }|\text{ its water is so transparent that}) \approx P(\text{the }|\text{that})$

Or maybe

 $P(\text{the }|\text{ its water is so transparent that}) \approx P(\text{the }|\text{transparent that})$

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Markov Assumption



$$P(w_1 w_2 \dots w_n) \approx \prod_i P(w_i \mid w_{i-k} \dots w_{i-1})$$

• In other words, we approximate each component in the product

$$P(w_i | w_1 w_2 \dots w_{i-1}) \approx P(w_i | w_{i-k} \dots w_{i-1})$$

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Simplest case: Unigram model



$$P(w_1 w_2 \dots w_n) \approx \prod_i P(w_i)$$

· Some automatically generated sentences from a unigram model

fifth, an, of, futures, the, an, incorporated, a, a, the, inflation, most, dollars, quarter, in, is, mass thrift, did, eighty, said, hard, 'm, july, bullish that, or, limited, the

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Bigram model



Condition on the previous word:

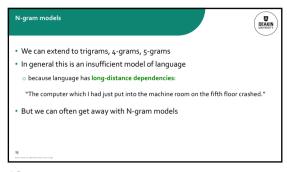
 $P(w_i | w_1 w_2 ... w_{i-1}) \approx P(w_i | w_{i-1})$

texaco, rose, one, in, this, issue, is, pursuing, growth, in, a, boiler, house, said, mr., gurria, mexico, 's, motion, control, proposal, without, permission, from, five, hundred, fifty, five, yen outside, new, car, parking, lot, of, the, agreement, reached this, would, be, a, record, november

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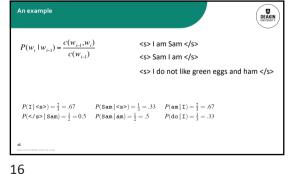
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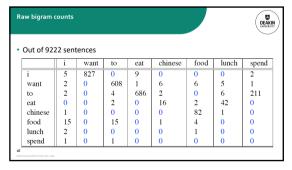


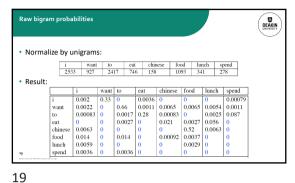
• The Maximum Likelihood Estimate $P(w_i \mid w_{i-1}) = \frac{count(w_{i-1}, w_i)}{count(w_{i-1})}$ $P(w_i \mid w_{i-1}) = \frac{c(w_{i-1}, w_i)}{c(w_{i-1})}$

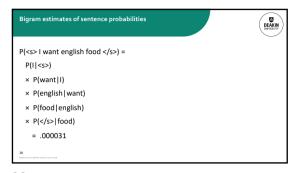
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What kinds of knowledge?

• P(english | want) = .0011

• P(chinese | want) = .0065

• P(to | want) = .66

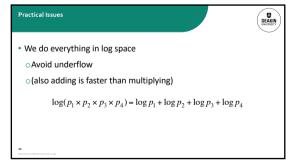
• P(eat | to) = .28

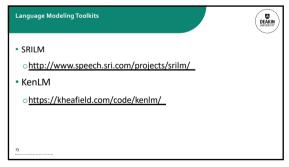
• P(food | to) = 0

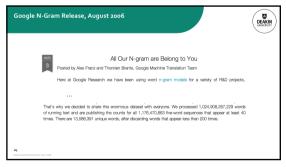
• P(want | spend) = 0

• P (i | <s>) = .25

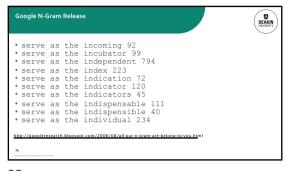
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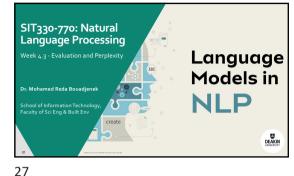




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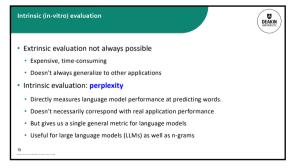
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"Extrinsic (in-vivo) Evaluation"

To compare models A and B

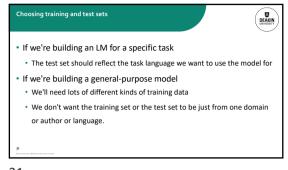
 Put each model in a real task
 Machine Translation, speech recognition, etc.

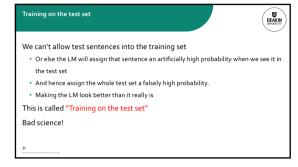
 Run the task, get a score for A and for B
 How many words translated correctly
 How many words transcribed correctly
 Compare accuracy for A and B



We train parameters of our model on a training set.
 We test the model's performance on data we haven't seen.
 A test set is an unseen dataset; different from training set.
 Intuition: we want to measure generalization to unseen data
 An evaluation metric (like perplexity) tells us how well our model does on the test set.

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If we test on the test set many times we might implicitly tune to its characteristics

Noticing which changes make the model better.

So we run on the test set only once, or a few times

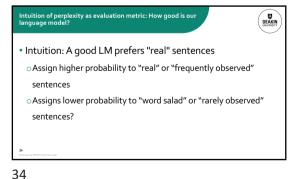
That means we need a third dataset:

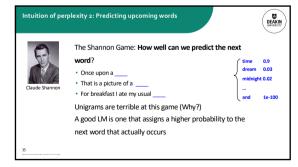
A development test set or, devset.

We test our LM on the devset until the very end
And then test our LM on the test set once

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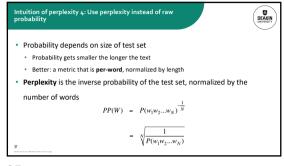
Ne said: a good LM is one that assigns a higher probability to the next word that actually occurs.

Let's generalize to all the words!
The best LM assigns high probability to the entire test set.

When comparing two LMs, A and B

We compute P_A(test set) and P_B(test set)
The better LM will give a higher probability to (=be less surprised by) the test set than the other LM.

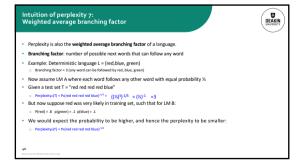
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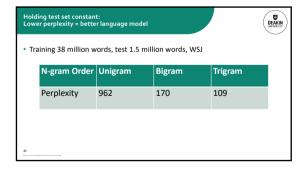


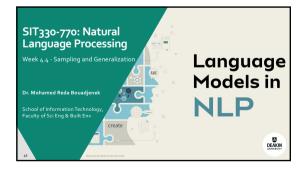
Intuition of perplexity 5: the inverse $PP(W) = P(w_1 w_2 ... w_N)^{\frac{1}{N}}$ $= \sqrt[N]{\frac{1}{P(w_1 w_2 ... w_N)}}$ (The inverse comes from the original definition of perplexity from cross-entropy rate in information theory)
Probability range is [0,1], perplexity range is $[1,\infty]$ Minimizing perplexity is the same as maximizing probability

Intuition of perplexity 6: N-grams $PP(W) = P(w_1w_2...w_N)^{\frac{1}{N}}$ $= \sqrt[N]{\frac{1}{P(w_1w_2...w_N)}}$ Chain rule: $PP(W) = \sqrt[N]{\prod_{i=1}^{N} \frac{1}{P(w_i|w_1...w_{i-1})}}$ Bigrams: $PP(W) = \sqrt[N]{\prod_{i=1}^{N} \frac{1}{P(w_i|W_{i-1})}}$

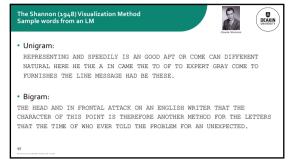
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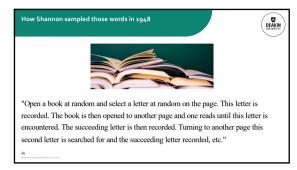


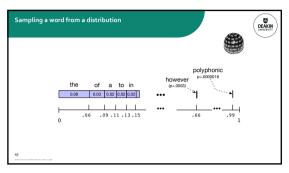




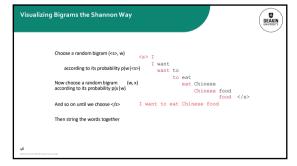
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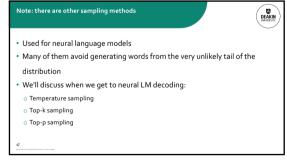


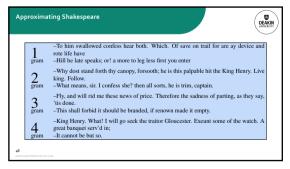


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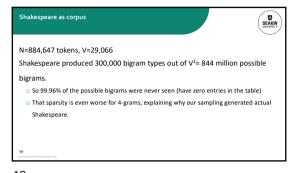


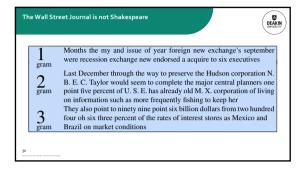
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47 48





Can you guess the author? These 3-gram sentences are sampled from an LM trained on who?

1) They also point to ninety nine point six billion dollars from two hundred four oh six three percent of the rates of interest stores as Mexico and gram Brazil on market conditions 2) This shall forbid it should be branded, if renown made it empty.

3) "You are uniformly charming!" cried he, with a smile of associating and now and then I bowed and they perceived a chaise and four to wish for.

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• If task-specific, use a training corpus that has a similar genre to your task.

· Make sure to cover different kinds of dialects and speaker/authors.

o If legal or medical, need lots of special-purpose documents

One of many varieties that can be used by African Americans and others

Can include the auxiliary verb finna that marks immediate future tense:

o Example: African-American Vernacular English (AAVE)

Choosing training data

• "My phone finna die"

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N-grams only work well for word prediction if the test corpus looks like the training corpus

But even when we try to pick a good training corpus, the test set will surprise us!

We need to train robust models that generalize!

One kind of generalization: Zeros

Things that don't ever occur in the training set

But occur in the test set

• Training set:

... ate lunch

... ate lunch

... ate lunch

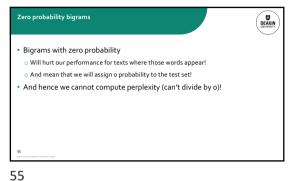
... ate breakfast

... ate the

P("breakfast" | ate) = 0

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The intuition of smoothing (from Dan Klein)

• When we have sparse statistics:

Five I denied the)
3 allegations
1 request
7 total

• Steal probability mass to generalize better

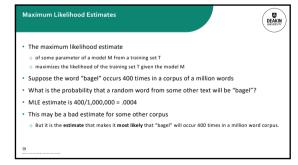
Five I denied the)
2.5 allegations
1.5 reports
0.5 claims
0.5 request
2.7 total

57

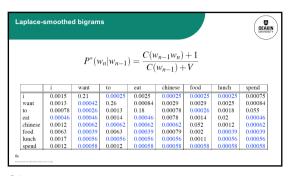
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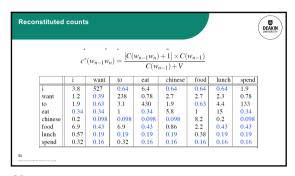
Add-one estimation $\begin{array}{c} \bullet \text{ Also called Laplace smoothing} \\ \bullet \text{ Pretend we saw each word one more time than we did} \\ \bullet \text{ Just add one to all the counts!} \\ \bullet \text{ MLE estimate: } P_{MLE}(w_i \mid w_{i-1}) = \frac{c(w_{i-1}, w_i)}{c(w_{i-1})} \\ \bullet \text{ Add-1 estimate: } P_{Add-1}(w_i \mid w_{i-1}) = \frac{c(w_{i-1}, w_i) + 1}{c(w_{i-1}) + V} \\ \end{array}$

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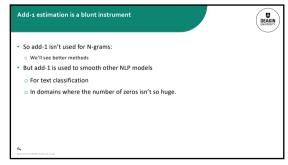
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ompan	e with raw	, bigit	aiii CC	unts						(
		i	want	to	eat	chinese	food	lunch	spend	
	i	5	827	0	9	0	0	0	2	
	want	2	0	608	1	6	6	5	1	
	to	2	0	4	686	2	0	6	211	
	eat	0	0	2	0	16	2	42	0	
	chines	e 1	0	0	0	0	82	1	0	
	food	15	0	15	0	1	4	0	0	
	lunch	2	0	0	0	0	1	0	0	
	spend	1	0	1	0	0	0	0	0	
		i	want	to	eat	chinese	food	lunch	spend	
	i	3.8	527	0.64	6.4	0.64	0.64	0.64	1.9	
	want	1.2	0.39	238	0.78	2.7	2.7	2.3	0.78	
	to	1.9	0.63	3.1	430	1.9	0.63	4.4	133	
	eat	0.34	0.34	1	0.34	5.8	1	15	0.34	
	chinese	0.2	0.098	0.098	0.098		8.2	0.2	0.098	
	food	6.9	0.43	6.9	0.43	0.86	2.2	0.43	0.43	
	lunch	0.57	0.19	0.19	0.19	0.19	0.38	0.19	0.19	
	spend	0.32	0.16	0.32	0.16	0.16	0.16	0.16	0.16	

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Sometimes it helps to use less context
Condition on less context for contexts you haven't learned much about

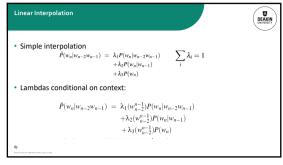
Backoff:
Use trigram if you have good evidence,
Otherwise bigram, otherwise unigram

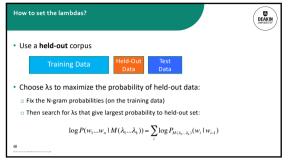
Interpolation:

mix unigram, bigram, trigram

Interpolation works better

64 65 66





Unknown words: Open versus closed vocabulary tasks

• If we know all the words in advanced
• Vocabulary Vis fixed
• Closed vocabulary task
• Often we don't know this
• Out of Vocabulary = OOV words
• Open vocabulary = OOV words
• Closer vocabulary = OOV words
• Create an unknown word token < UNK>
• Training of -UNKO protabilities
• Create a fixed lexicon (of like a fixed lexicon (of like a fixed lexicon) exist like a romal water of like a fixed lexicon (of like a romal water of l

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Huge web-scale n-grams

• How to deal with, e.g., Google N-gram corpus

• Pruning

• Only store N-grams with count > threshold.

• Remove singletons of higher ordern-grams

• Entropy-based pruning

• Efficiency

• Efficiency

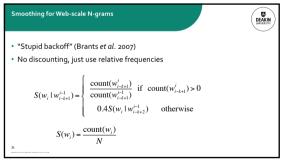
• Efficient data structures like tries

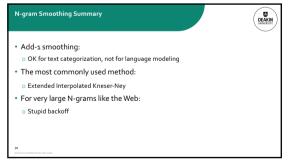
• Bloom filters: approximate language models

• Store words an idexes, not stripage

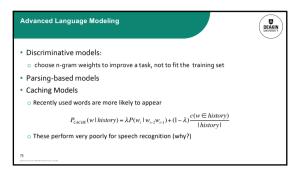
• Use Huffman coding to fit large numbers of words into two bytes

• Quantize probabilities (4-8 bits instead of 8-byte float)





70 71 72





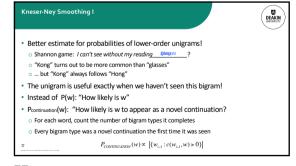
Absolute discounting: just subtract a little from each count DEAKIN UNIVERSITY Suppose we wanted to subtract a little from a count of 4 to save Bigram count in training Bigram count in heldout set probability mass for the zeros .0000270 How much to subtract ? 0.448 · Church and Gale (1991)'s clever idea 2.24 Divide up 22 million words of AP Newswire 3.23 o Training and held-out set 4.21 o for each bigram in the training set 5.23 o see the actual count in the held-out set! 6.21 It sure looks like c* = (c - .75) 7.21 8.26

75

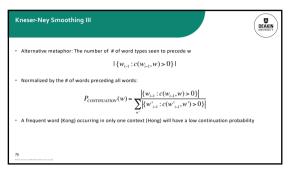
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• Save ourselves some time and just subtract 0.75 (or some d)! $P_{\text{Absolute Discounting}}(w_i \mid w_{i-1}) = \frac{c(w_{i-1}, w_i) - d}{c(w_{i-1})} + \lambda(w_{i-1})P(w)$ • (Maybe keeping a couple extra values of d for counts 1 and 2)
• But should we really just use the regular unigram P(w)?

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Kneser-Ney Smoothing II $P_{CONTINUATION}(w) \propto \left| \{w_{i-1}: c(w_{i-1}, w) > 0\} \right|$ • Normalized by the total number of word bigram types $\left| \{(w_{j-1}, w_j) : c(w_{j-1}, w_j) > 0\} \right|$ $P_{CONTINUATION}(w) = \frac{\left| \{w_{j-1}: c(w_{j-1}, w) > 0\} \right|}{\left| \{(w_{j-1}, w_j) : c(w_{j-1}, w_j) > 0\} \right|}$



Kneser-Ney Smoothing IV $P_{KN}(w_i \mid w_{i-1}) = \frac{\max(c(w_{i-1}, w_i) - d, 0)}{c(w_{i-1})} + \lambda(w_{i-1})P_{CONTINUATION}(w_i)$ λ is a normalizing constant; the probability mass we've discounted $\lambda(w_{i-1}) = \frac{d}{c(w_{i-1})} \Big| \{w : c(w_{i-1}, w) > 0\} \Big|$ The number of word types that can follow with the normalized discount = of times we applied normalized discount

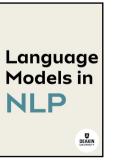
Kneser-Ney Smoothing: Recursive formulation $P_{KN}(w_i \mid w_{i-n+1}^{i-1}) = \frac{\max(c_{KN}(w_{i-n+1}^i) - d, 0)}{c_{KN}(w_{i-n+1}^{i-1})} + \lambda(w_{i-n+1}^{i-1})P_{KN}(w_i \mid w_{i-n+2}^{i-1})$ $c_{KN}(\bullet) = \begin{cases} count(\bullet) & \text{for the highest order} \\ continuation count(\bullet) & \text{for lower order} \end{cases}$ Continuation count = Number of unique single word contexts for \bullet

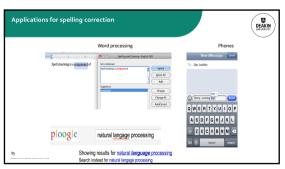
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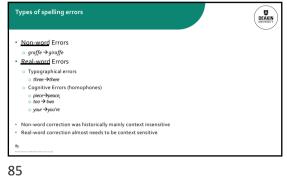
Spelling Tasks

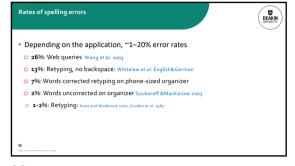
• Spelling Error Detection

• Spelling Error Correction:

○ Autocorrect
○ ohe → the
○ Suggest a correction
○ Suggestion lists

82 83 84





Non-word spelling error detection:

Any word not in a dictionary is an error

The larger the dictionary the better ... up to a point

(The Web is full of mis-spellings, so the Web isn't necessarily a great dictionary ...)

Non-word spelling error correction:

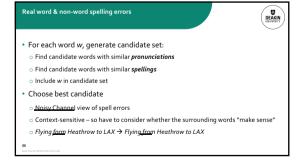
Generate candidates: real words that are similar to error

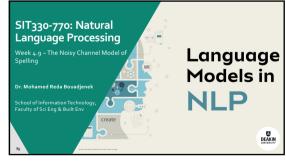
Choose the one which is best:

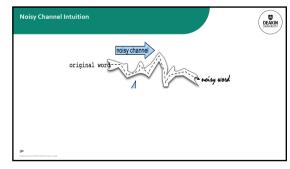
Shortest weighted edit distance

Highest noisy channel probability

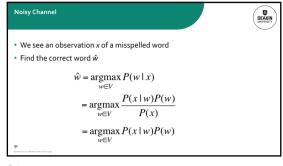
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88 89 90



• acress

Words with similar spelling
 Small edit distance to error
 Words with similar pronunciation
 Small distance of pronunciation to error

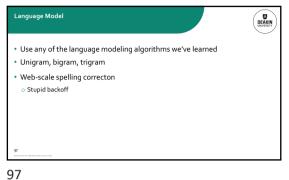
91 92 93

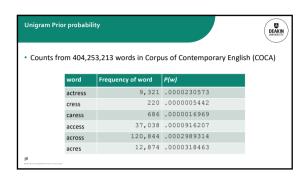
Candidate Testing: Damerau-Levenshtein edit distance	DEAKIN UNIVAESITY
Minimal edit distance between two strings, where edits are:	
o Insertion	
o Deletion	
o Substitution	
o Transposition of two adjacent letters	
94 southermore to 1800 to Francisco and pa	

Words within 1 of acress DEAKIN UMAYORSITY acress actress deletion acress cress insertion acress caress transposition substitution acress access acress across substitution insertion acress acres acress acres insertion

80% of errors are within edit distance 1
 Almost all errors within edit distance 2
 Also allow insertion of space or hyphen
 o thisidea → this idea
 o inlaw → in-law
 Can also allow merging words
 o data base → database
 For short texts like a query, can just regard whole string as one item from which to produce edits

94 95 96



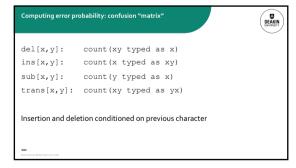


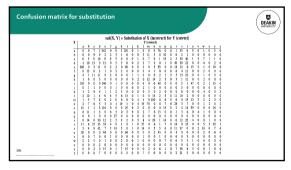
• Error model probability, Edit probability
• Kernighan, Church, Gale 1990

• Misspelled word x = xs, xs, xs,... xm
• Correct word w = ws, ws, ws,..., wn

• P(x|w) = probability of the edit
• (deletion/insertion/substitution/transposition)

7 98 99



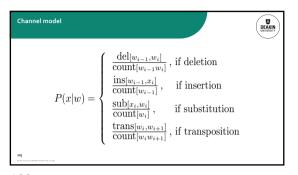


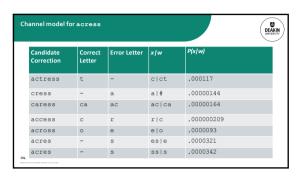
Peter Norvig's list of errors

Peter Norvig's list of counts of single-edit errors

All Peter Norvig's ngrams data links_http://norvig.com/ngrams/

100 101 102

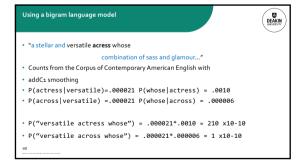


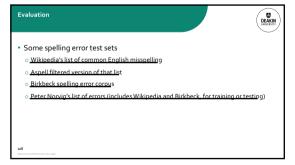


Candidate Correction	Correct Letter	Error Letter	x/w	P(x w)	P(w)	109+ P(x/w)* P(w)	
actress	t	-	c ct	.000117	.0000231	2.7	
cress	-	a	a #	.00000144	.000000544	.00078	
caress	ca	ac	ac ca	.00000164	.00000170	.0028	
access	С	r	r c	.000000209	.0000916	.019	
across	0	е	elo	.0000093	.000299	2.8	
acres	-	s	es e	.0000321	.0000318	1.0	
acres	-	s	ss s	.0000342	.0000318	1.0	

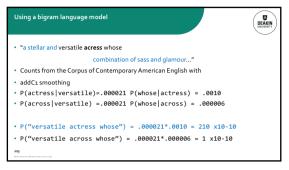
103 104 105

Candidate Correction	Correct Letter	Error Letter	x/w	P(x w)	P(w)	10∍ · P(x/w)* P(w)
actress	t	-	c ct	.000117	.0000231	2.7
cress	-	a	a #	.00000144	.000000544	.00078
caress	ca	ac	ac ca	.00000164	.00000170	.0028
access	С	r	r c	.000000209	.0000916	.019
across	0	е	elo	.0000093	.000299	2.8
acres	-	s	es e	.0000321	.0000318	1.0
acres	-	s	ss s	.0000342	.0000318	1.0





106 107 108





Real-word spelling errors DEAKIN UNIVERSITY ...leaving in about fifteen minuets to go to her • The design an construction of the system ... • Can they *lave* him my messages? • The study was conducted mainly be John Black. • 25-40% of spelling errors are real words Kukich 1992

111

109

Solving real-world spelling errors

o Generate candidate set

· Choose best candidates ONoisy channel model

owords that are homophones

o(all of this can be pre-computed!)

othe word itself

• For each word in sentence (phrase, query ...)

oall single-letter edits that are English words

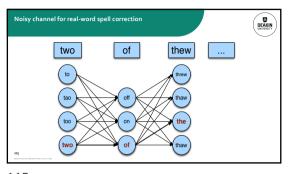
110

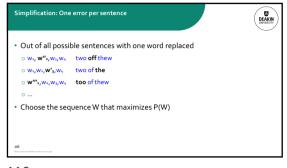
Noisy channel for real-word spell correction • Given a sentence w₁, w₂, w₃, ..., w_n · Generate a set of candidates for each word w o Candidate(w1) = {w1, w'1, w"1, w"1,...} o Candidate(w2) = {w2, w2, w2, w2, w2, ...} o Candidate(wn) = {wn, w'n, w''n, w'''n,...} · Choose the sequence W that maximizes P(W)

Noisy channel for real-word spell correction DEAKIN UNIVERSITY two of thew

112 113

DEAKIN UNIVERSITY





* Language model

Unigram

Bigram

etc.

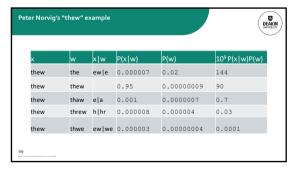
Channel model

Same as for non-word spelling correction

Plus need probability for no error. P(wlw)

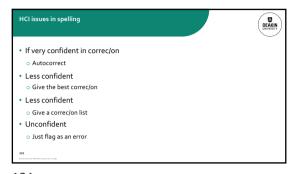
115 116 117

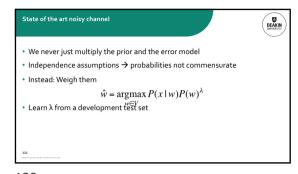
Probability of no error	DEAKIN UNIVERSITY
 What is the channel probability for a correctly typed word? P("the" "the") 	
\circ If you have a big corpus, you can estimate this percent correct	
But this value depends strongly on the application	
o .90 (1 error in 10 words)	
o .95 (1 error in 20 words)	
o .99 (1 error in 100 words)	





118 119 120





• Metaphone, used in GNU aspell

• Convert misspelling to metaphone pronunciation

• "brop duplicate adjacent letters, except for C."

• "If the word begins with "KN", 'GN", 'PN", 'AE", 'WR', drop the first letter."

• "brop "B' if aver 'M' and if it is at the end of the word"

• ...

• Find words whose pronunciation is 1C2 edit distance from misspelling's

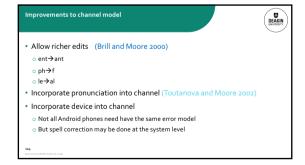
• Score result list

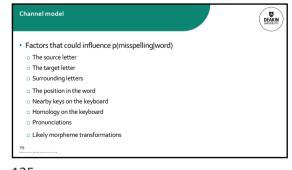
• Weighted edit distance of candidate to misspelling

• Edit distance of candidate pronunciation to misspelling pronunciation

123

121 122







124 125 126

Classifier-based methods for real-word spelling correction Instead of just channel model and language model Use many features in a classifier (next lecture). Build a classifier for a specific pair like: whether/weather "cloudy" within +C 10 words "to VERB "o or not