



What is a Language Model? · A model to assign a probability to a sentence o Machine Translation: OP(high winds tonight) > P(large winds tonight) Spell Correction • The office is about fifteen minuets from my house! • P(about fifteen minutes from) > P(about fifteen minuets from) Speech Recognition OP(I saw a van) >> P(eyes awe of an) o + Summarization, question, answering, etc., etc.!!

Probabilistic Language Modeling DEAKIN UNIVERSITY · Goal: compute the probability of a sentence or sequence of words: $P(W) = P(w_1, w_2, w_3, w_4, w_5...w_n)$ · Related task: probability of an upcoming word: $P(w_5 | w_1, w_2, w_3, w_4)$ • A model that computes either of these: P(W) or $P(w_n|w_1,w_2...w_{n-1})$ is called a language model. Better: the grammar But language model or LM is standard

How to compute P(W) DEAKIN UMAYERSITY · How to compute this joint probability: o P(its, water, is, so, transparent, that) · Intuition: let's rely on the Chain Rule of Probability

Reminder: The Chain Rule DEAKIN UNIVERSITY · Recall the definition of conditional probabilities p(B|A) = P(A,B)/P(A) Rewriting: P(A,B) = P(A)P(B|A) More variables: P(A,B,C,D) = P(A)P(B|A)P(C|A,B)P(D|A,B,C)• The Chain Rule in General $P(x_1,x_2,x_3,...,x_n) = P(x_1)P(x_2|x_1)P(x_3|x_1,x_2)...P(x_n|x_1,...,x_{n-1})$

The Chain Rule applied to compute joint probability of words in

DEAKIN UNIVERSITY

 $P(w_1 w_2 ... w_n) = \prod_i P(w_i | w_1 w_2 ... w_{i-1})$

P("its water is so transparent") =

P(its) × P(water|its) × P(is|its water)

× P(so|its water is) × P(transparent|its water is so)

How to estimate these probabilitiesCould we just count and divide?



P(the lits water is so transparent that) = Count(its water is so transparent that the)

Count(its water is so transparent that)

- No! Too many possible sentences!
- · We'll never see enough data for estimating these

8

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Markov Assumption



• Simplifying assumption:

 $P(\text{the }|\text{ its water is so transparent that}) \approx P(\text{the }|\text{that})$

Or maybe

 $P(\text{the }|\text{ its water is so transparent that}) \approx P(\text{the }|\text{transparent that})$

na sina niy (Willia Familia Indo-114)

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Markov Assumption



$$P(w_1 w_2 \dots w_n) \approx \prod_i P(w_i \mid w_{i-k} \dots w_{i-1})$$

• In other words, we approximate each component in the product

$$P(w_i | w_1 w_2 ... w_{i-1}) \approx P(w_i | w_{i-k} ... w_{i-1})$$

20

Simplest case: Unigram model



$$P(w_1 w_2 \dots w_n) \approx \prod_i P(w_i)$$

· Some automatically generated sentences from a unigram model

fifth, an, of, futures, the, an, incorporated, a, a, the, inflation, most, dollars, quarter, in, is, mass thrift, did, eighty, said, hard, 'm, july, bullish that, or, limited, the

11

Bigram model



Condition on the previous word:

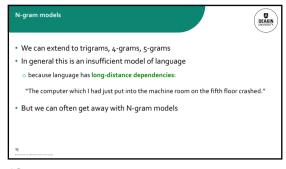
 $P(w_i | w_1 w_2 ... w_{i-1}) \approx P(w_i | w_{i-1})$

texaco, rose, one, in, this, issue, is, pursuing, growth, in, a, boiler, house, said, mr., gurria, mexico, 's, motion, control, proposal, without, permission, from, five, hundred, fifty, five, yen outside, new, car, parking, lot, of, the, agreement, reached this, would, be, a, record, november

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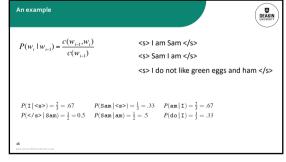
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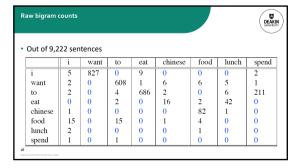


• The Maximum Likelihood Estimate $P(w_i \mid w_{i-1}) = \frac{count(w_{i-1}, w_i)}{count(w_{i-1})}$ $P(w_i \mid w_{i-1}) = \frac{c(w_{i-1}, w_i)}{c(w_{i-1})}$

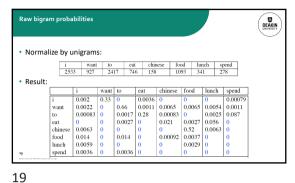
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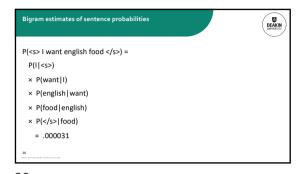






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What kinds of knowledge?

• P(english | want) = .0011

• P(chinese | want) = .0065

• P(to | want) = .66

• P(eat | to) = .28

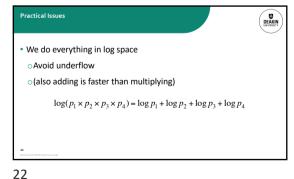
• P(food | to) = 0

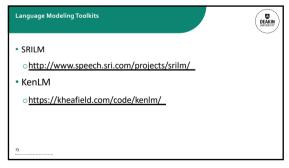
• P(want | spend) = 0

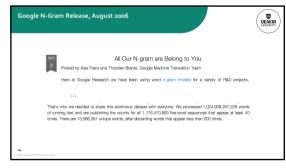
• P(i | <s>) = .25

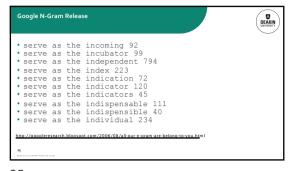
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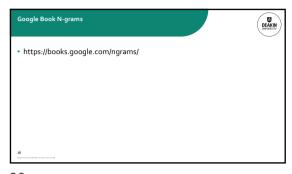
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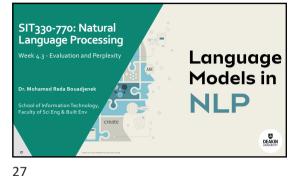












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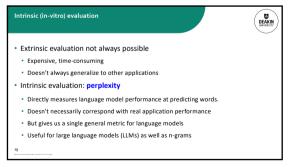
"Extrinsic (in-vivo) Evaluation"

To compare models A and B

 Put each model in a real task
 Machine Translation, speech recognition, etc.

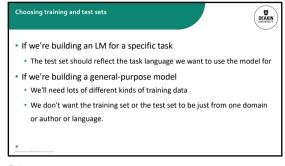
Run the task, get a score for A and for B
 How many words translated correctly
 How many words transcribed correctly

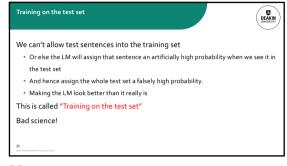
Compare accuracy for A and B



We train parameters of our model on a training set.
 We test the model's performance on data we haven't seen.
 A test set is an unseen dataset; different from training set.
 Intuition: we want to measure generalization to unseen data
 An evaluation metric (like perplexity) tells us how well our model does on the test set.

28 29 30





If we test on the test set many times we might implicitly tune to its characteristics

Noticing which changes make the model better.

So we run on the test set only once, or a few times

That means we need a third dataset:

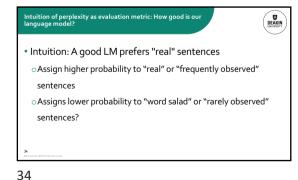
A development test set or, devset.

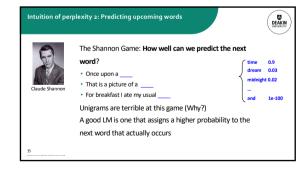
We test our LM on the devset until the very end

And then test our LM on the test set once

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31 32





Intuition of perplexity 3: The best language model is one that best predicts the entire unseen test set

• We said: a good LM is one that assigns a higher probability to the next word that actually occurs.

• Let's generalize to all the words!

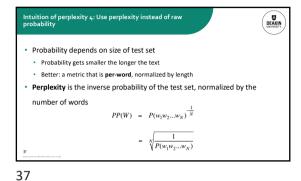
• The best LM assigns high probability to the entire test set.

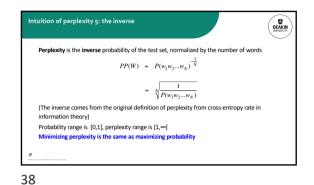
• When comparing two LMs, A and B

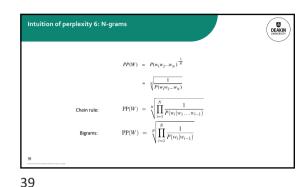
• We compute Px(test set) and Px(test set)

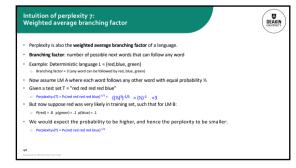
• The better LM will give a higher probability to (=be less surprised by) the test set than the other LM.

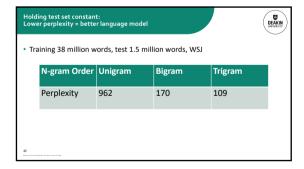
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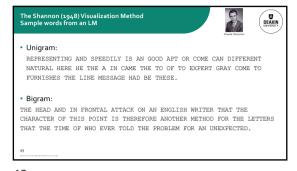


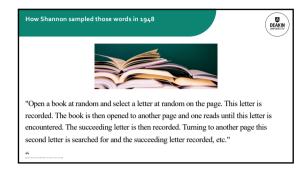


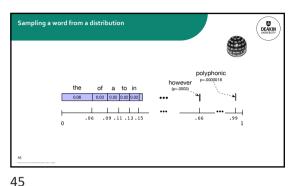


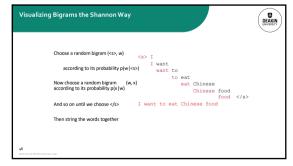


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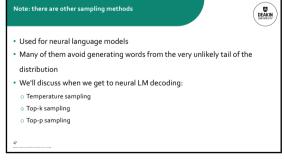


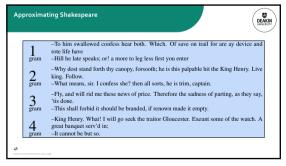




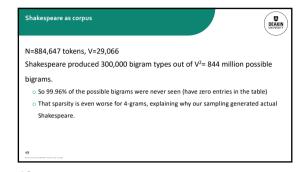


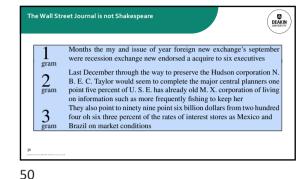
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47 48





Can you guess the author? These 3-gram sentences are sampled from an LM trained on who?

1) They also point to ninety nine point six billion dollars from two hundred four oh six three percent of the rates of interest stores as Mexico and gram Brazil on market conditions
2) This shall forbid it should be branded, if renown made it empty.

3) "You are uniformly charming!" cried he, with a smile of associating and now and then I bowed and they perceived a chaise and four to wish for.

51

49

If task-specific, use a training corpus that has a similar genre to your task.
 If legal or medical, need lots of special-purpose documents
 Make sure to cover different kinds of dialects and speaker/authors.
 Example: African-American Vernacular English (AAVE)
 One of many varieties that can be used by African Americans and others
 Can include the auxiliary verb finna that marks immediate future tense:
 "My phone finna die"

N-grams only work well for word prediction if the test corpus looks like the training corpus

But even when we try to pick a good training corpus, the test set will surprise us!

We need to train robust models that generalize!

One kind of generalization: Zeros

Things that don't ever occur in the training set

But occur in the test set

• Training set:

... ate lunch

... ate lunch

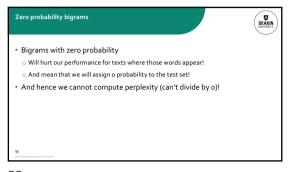
... ate dinner

... ate a

... ate the

P("breakfast" | ate) = 0

53 54





The intuition of smoothing (from Dan Klein)

• When we have sparse statistics:

Fig. | denied the)
3 allegations
2 reports
1 claims
1 request
7 total

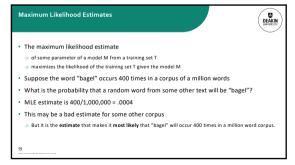
• Steal probability mass to generalize better

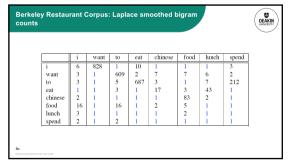
Fig. | denied the)
2.5 allegations
1.5 reports
0.5 claims
0.5 request
2.7 total

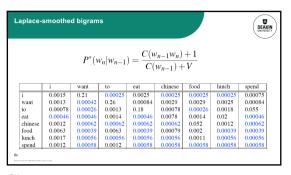
55 56 57

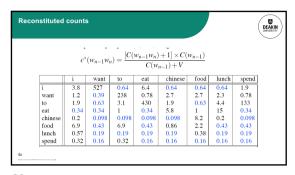
Add-one estimation $\begin{array}{c} \bullet \text{ Also called Laplace smoothing} \\ \bullet \text{ Pretend we saw each word one more time than we did} \\ \bullet \text{ Just add one to all the counts!} \\ \bullet \text{ MLE estimate: } P_{MLE}(w_i \mid w_{i-1}) = \frac{c(w_{i-1}, w_i)}{c(w_{i-1})} \\ \bullet \text{ Add-1 estimate: } P_{Add-1}(w_i \mid w_{i-1}) = \frac{c(w_{i-1}, w_i) + 1}{c(w_{i-1}) + V} \\ \end{array}$

58

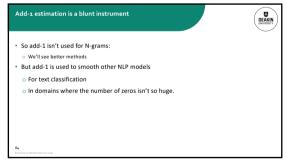








61 62 63





Sometimes it helps to use less context
Condition on less context for contexts you haven't learned much about

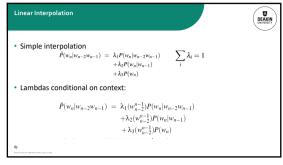
Backoff:
Use trigram if you have good evidence,
Otherwise bigram, otherwise unigram

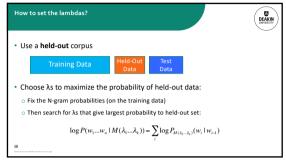
Interpolation:

mix unigram, bigram, trigram

Interpolation works better

64 65 66





Unknown words: Open versus closed vocabulary tasks

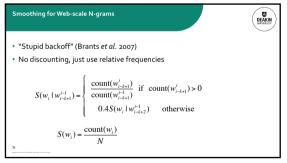
• If we know all the words in advanced
• Vocabulary Vis fixed
• Closed vocabulary task
• Often we don't know this
• Out of Vocabulary = OOV words
• Open vocabulary = OOV words
• Copen vocabulary = OOV words
• Copen vocabulary = OOV words
• Training of -UNIXO protabilities
• Create an unknown word token < UNIXO
• Training of -UNIXO protabilities
• Create a fixed lexicos (of eight less around word
• At text normalization phase, any training word not in Lichanged to -UNIXO
• Now we train as probabilities is around word
• At decoding time
• If text input: Use UNIX probabilities for any word not in training

67 68 69

Huge web-scale n-grams

How to deal with, e.g., Google N-gram corpus

Pruning
Only store N-grams with count > threshold.
Remove singletors of higher-order n-grams
Entropy-based pruning
Efficiency
Efficiency
Efficient data structures like tries
Bloom filters: approximate language models
Store words as indexes, not strings
Use Het/filman coding to filtage numbers of words into two bytes
Quantize probabilities (4-8 bits instead of 8-byte float)

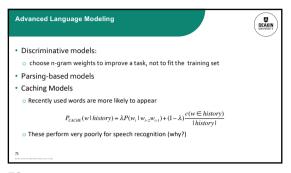


N-gram Smoothing Summary

 Add-1 smoothing:
 OK for text categorization, not for language modeling

 The most commonly used method:
 Extended Interpolated Kneser-Ney
 For very large N-grams like the Web:
 Stupid backoff

70 71 72



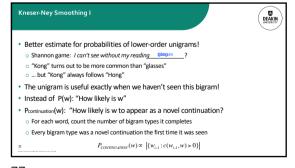


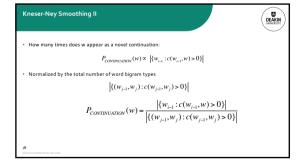
Absolute discounting: just subtract a little from each count DEAKIN UNIVERSITY Suppose we wanted to subtract a little from a count of 4 to save
 Bigram count in training Bigram count in heldout set probability mass for the zeros .0000270 How much to subtract? 0.448 · Church and Gale (1991)'s clever idea 2.24 Divide up 22 million words of AP Newswire 3.23 o Training and held-out set 4.21 o for each bigram in the training set 5.23 o see the actual count in the held-out set! 6.21 It sure looks like c* = (c - .75) 7.21 8.26

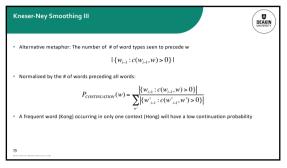
73 74 75

• Save ourselves some time and just subtract 0.75 (or some d)! $P_{\text{Absolute Discounting}}(w_i \mid w_{i-1}) = \frac{c(w_{i-1}, w_i) - d}{c(w_{i-1})} + \lambda(w_{i-1})P(w) \text{ unigram}$ • (Maybe keeping a couple extra values of d for counts 1 and 2)
• But should we really just use the regular unigram P(w)?

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Kneser-Ney Smoothing IV $P_{KN}(w_i \mid w_{i-1}) = \frac{\max(c(w_{i-1}, w_i) - d, 0)}{c(w_{i-1})} + \lambda(w_{i-1})P_{CONTINUATION}(w_i)$ λ is a normalizing constant; the probability mass we've discounted $\lambda(w_{i-1}) = \frac{d}{c(w_{i-1})} \Big| \{w : c(w_{i-1}, w) > 0\} \Big|$ The number of word types that can follow with the normalized discount = of times we applied normalized discount

 $R_{KN}(w_i \mid w_{i-n+1}^{i-1}) = \frac{\max(c_{KN}(w_{i-n+1}^i) - d, 0)}{c_{KN}(w_{i-n+1}^i)} + \lambda(w_{i-n+1}^{i-1})P_{KN}(w_i \mid w_{i-n+2}^{i-1})$ $c_{KN}(\bullet) = \begin{cases} count(\bullet) & \text{for the highest order} \\ continuation count(\bullet) & \text{for lower order} \end{cases}$ Continuation count = Number of unique single word contexts for \bullet

81

79 80





Spelling Tasks

• Spelling Error Detection

• Spelling Error Correction:

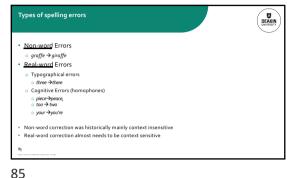
○ Autocorrect

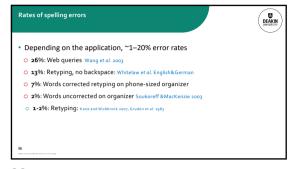
○ hte → the

○ Suggest a correction

○ Suggestion lists

82 83 84





Non-word spelling error detection:

Any word not in a dictionary is an error

The larger the dictionary the better ... up to a point

(The Web is full of mis-spellings, so the Web isn't necessarily a great dictionary ...)

Non-word spelling error correction:

Generate candidates: real words that are similar to error

Choose the one which is best:

Shortest weighted edit distance

Highest noisy channel probability

5 86 87

* For each word w, generate candidate set:

• Find candidate words with similar pronunciations

• Find candidate words with similar spellings

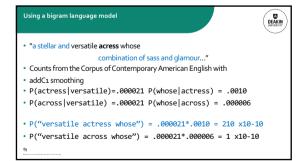
• Include w in candidate set

• Choose best candidate

• Noisy Channel view of spell errors

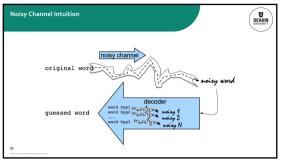
• Context-sensitive – so have to consider whether the surrounding words "make sense"

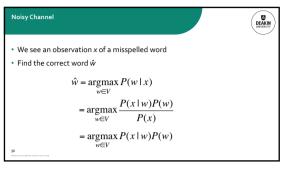
• Flying form Heathrow to LAX → Flying from Heathrow to LAX





88 89 90

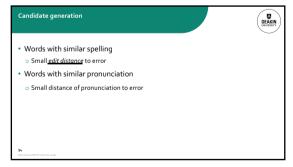


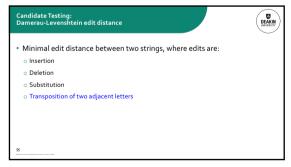


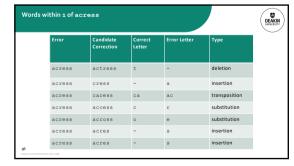
Non-word spelling error example

acress

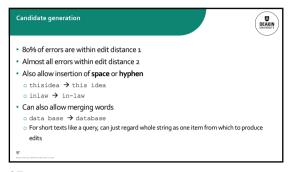
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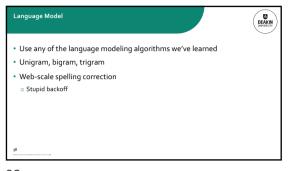


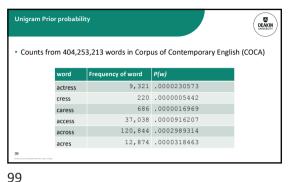




94 95 96







* Error model probability, Edit probability

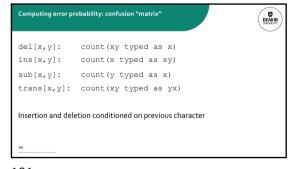
* Kernighan, Church, Gale 1990

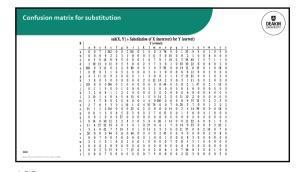
* Misspelled word x = x₁, x₂, x₃... x_m

* Correct word w = w₁, w₂, w₃,..., w_n

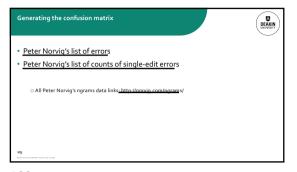
* P(x|w) = probability of the edit

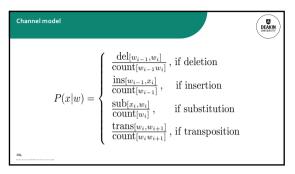
o (deletion/insertion/substitution/transposition)





100 101 102





Candidate Correction	Correct Letter	Error Letter	x/w	P(x w)		
actress	t	-	c ct	.000117		
cress	-	a	a #	.00000144		
caress	ca	ac	ac ca	.00000164		
access	С	r	r c	.000000209		
across	0	е	elo	.0000093		
acres	-	s	es e	.0000321		
acres	-	s	ss s	.0000342		

103 104 105

	1				1	-
Candidate Correction	Correct Letter	Error Letter	x/w	P(x w)	P(w)	10∍ · P(x w)* P(w)
actress	t	-	c ct	.000117	.0000231	2.7
cress	-	a	a #	.00000144	.000000544	.00078
caress	ca	ac	ac ca	.00000164	.00000170	.0028
access	С	r	r c	.000000209	.0000916	.019
across	0	е	elo	.0000093	.000299	2.8
acres	-	s	es e	.0000321	.0000318	1.0
acres	-	s	ss s	.0000342	.0000318	1.0

					DI	
Candidate Correction	Correct Letter	Error Letter	x/w	P(x w)	P(w)	10∍ • P(x/w)* P(w)
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* "a stellar and versatile acress whose combination of sass and glamour..."

* Counts from the Corpus of Contemporary American English with add-1 smoothing

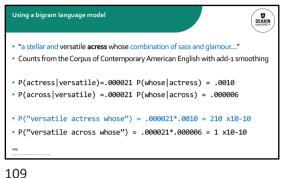
* P(actress|versatile)=.000021 P(whose|actress) = .0010

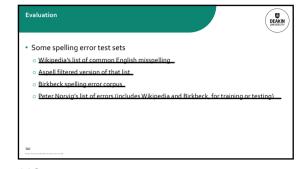
* P(across|versatile) = .000021 P(whose|across) = .000006

* P("versatile actress whose") = .000021*.0010 = 210 x10-10

* P("versatile across whose") = .000021*.000006 = 1 x10-10

106 107 108







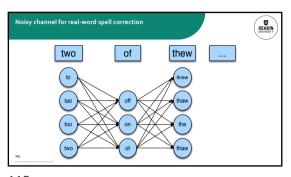
Real-word spelling errors DEAKIN UNIVERSITY • ...leaving in about fifteen **minuets** to go to her • The design an construction of the system ... • Can they *lave* him my messages? • The study was conducted mainly **be** John Black. • 25-40% of spelling errors are real words Kukich 1992

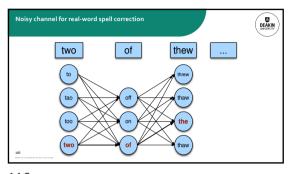
112

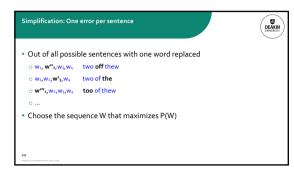
Solving real-world spelling errors DEAKIN UMAYERSITY • For each word in sentence (phrase, query ...) o Generate candidate set othe word itself oall single-letter edits that are English words owords that are homophones o(all of this can be pre-computed!) · Choose best candidates ONoisy channel model

Noisy channel for real-word spell correction DEAKIN UNIVERSITY • Given a sentence w₁, w₂, w₃, ..., w_n Generate a set of candidates for each word w_i o Candidate(w1) = {w1, w1, w1, w1, w1,...} o Candidate(w2) = {w2, w2, w2, w2, w2, ...} o Candidate(wn) = {wn, w'n, w''n, w'''n,...} Choose the sequence W that maximizes P(W)

113 114

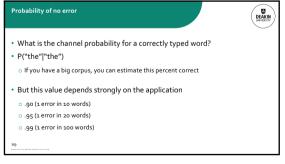


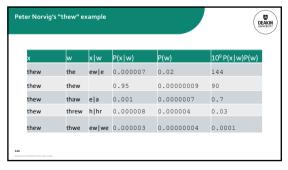




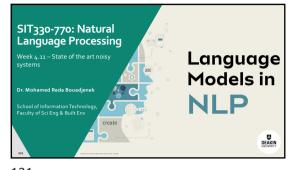
115 116 117

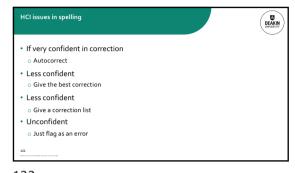
Language model	
Language model	
o Unigram	
o Bigram	
o etc.	
Channel model	
o Same as for non-word spelling correction	
 Plus need probability for no error, P(w w) 	

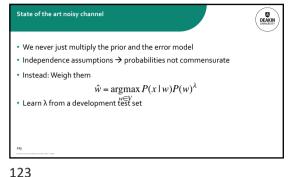




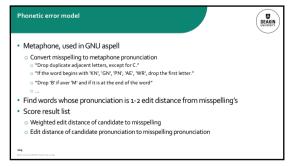
118 119 120

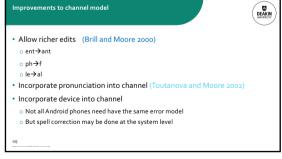






121 122 12





Factors that could influence p(misspelling|word)

The source letter

The target letter

Surrounding letters

The position in the word

Nearby keys on the keyboard

Homology on the keyboard

Pronunciations

Likely morpheme transformations

124 125 126



