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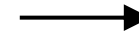
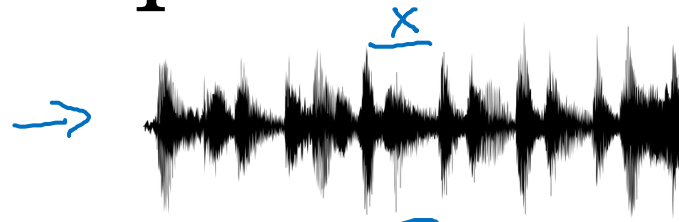
# Recurrent Neural Networks

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Why sequence  
models?

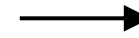
# Examples of sequence data

Speech recognition



y  
“The quick brown fox jumped  
over the lazy dog.”

Music generation

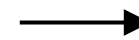


Sentiment classification

“There is nothing to like  
in this movie.”



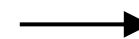
DNA sequence analysis → AGCCCCTGTGAGGAACTAG



AG**CCCCTGTGAGGAACTAG**

Machine translation

Voulez-vous chanter avec  
moi?



Do you want to sing with  
me?

Video activity recognition



Running

Name entity recognition → Yesterday, Harry Potter  
met Hermione Granger.



Yesterday, **Harry Potter**  
met **Hermione Granger**.

Andrew Ng



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# Recurrent Neural Networks

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## Notation

# Motivating example

NLP

x: Harry Potter and Hermione Granger invented a new spell.

$\rightarrow x^{(1)} \quad x^{(2)} \quad x^{(3)} \quad \dots \quad x^{(t)} \quad \dots \quad x^{(9)}$

$$T_x = 9$$

$\rightarrow y:$

$y^{(1)} \quad y^{(2)} \quad y^{(3)} \quad \dots \quad y^{(9)}$

$$T_y = 9$$

$x^{(i)(t)}$

$$T_x^{(i)} = 9$$

15

$y^{(i)(t)}$   
 $\uparrow$

$$T_y^{(i)}$$

# Representing words

$x^{(t)}$

$(x, y)$

$x \rightarrow y$

x: Harry Potter and Hermione Granger invented a new spell.

$x^{(1)}$

$x^{(2)}$

$x^{(3)}$

...

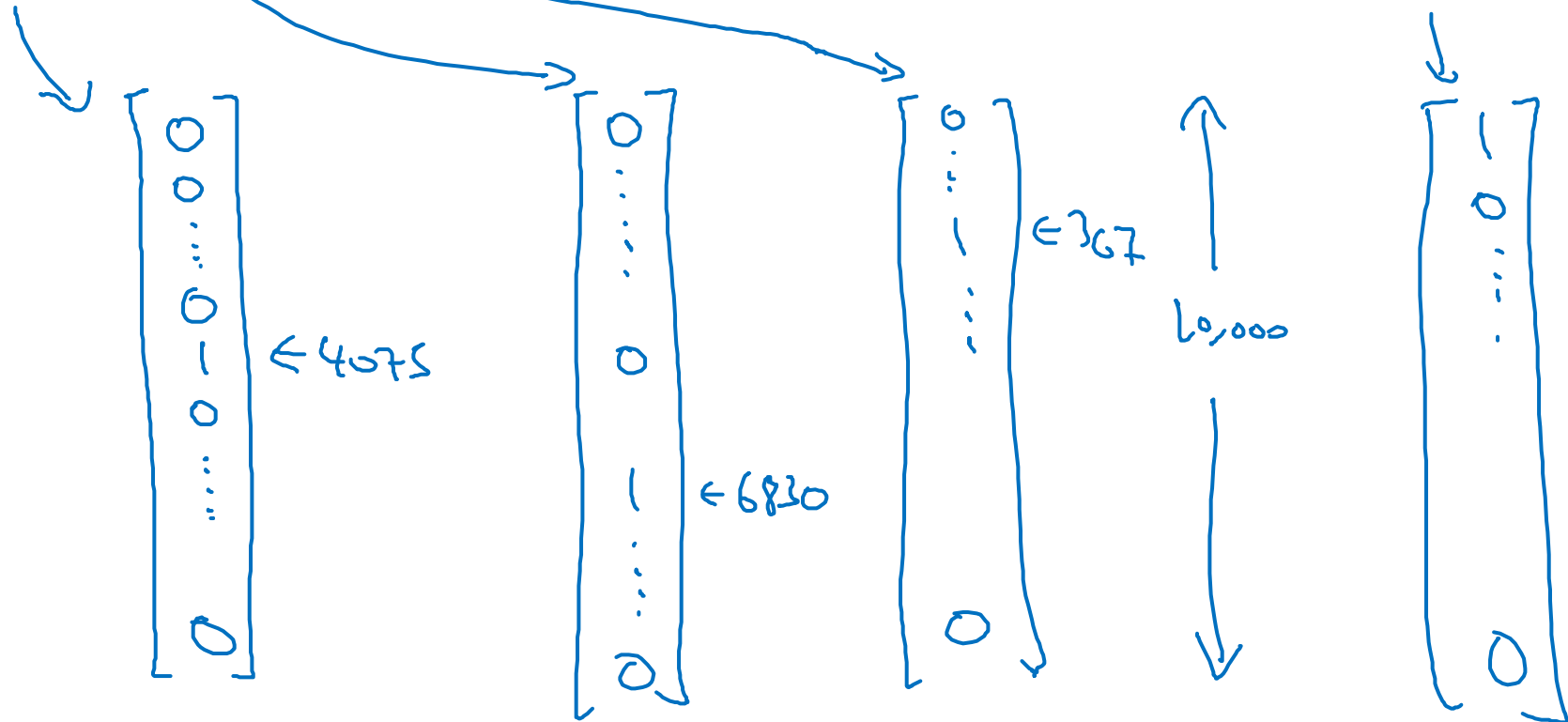
$x^{(7)}$

$x^{(9)}$

Vocabulary

a	1
aaron	2
...	...
and	367
...	...
harry	4075
...	...
potter	6830
...	...
zulu	10,000

<UNK> 10,000



One-hot

# Representing words

x: Harry Potter and Hermione Granger invented a new spell.

$$x^{<1>} \quad x^{<2>} \quad x^{<3>} \quad \dots \quad x^{<9>}$$

And = 367

Invented = 4700

$$A = 1$$

New = 5976

Spell = 8376

Harry = 4075

Potter = 6830

Hermione = 4200

Gran... = 4000



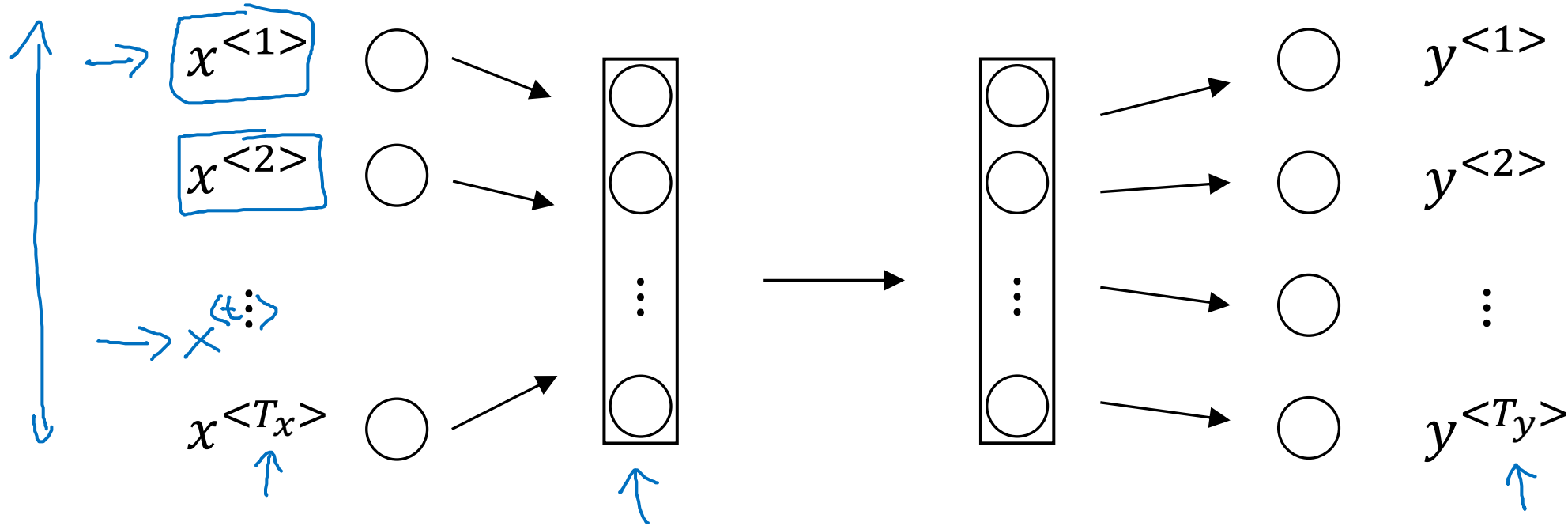
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# Recurrent Neural Networks

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## Recurrent Neural Network Model

# Why not a standard network?

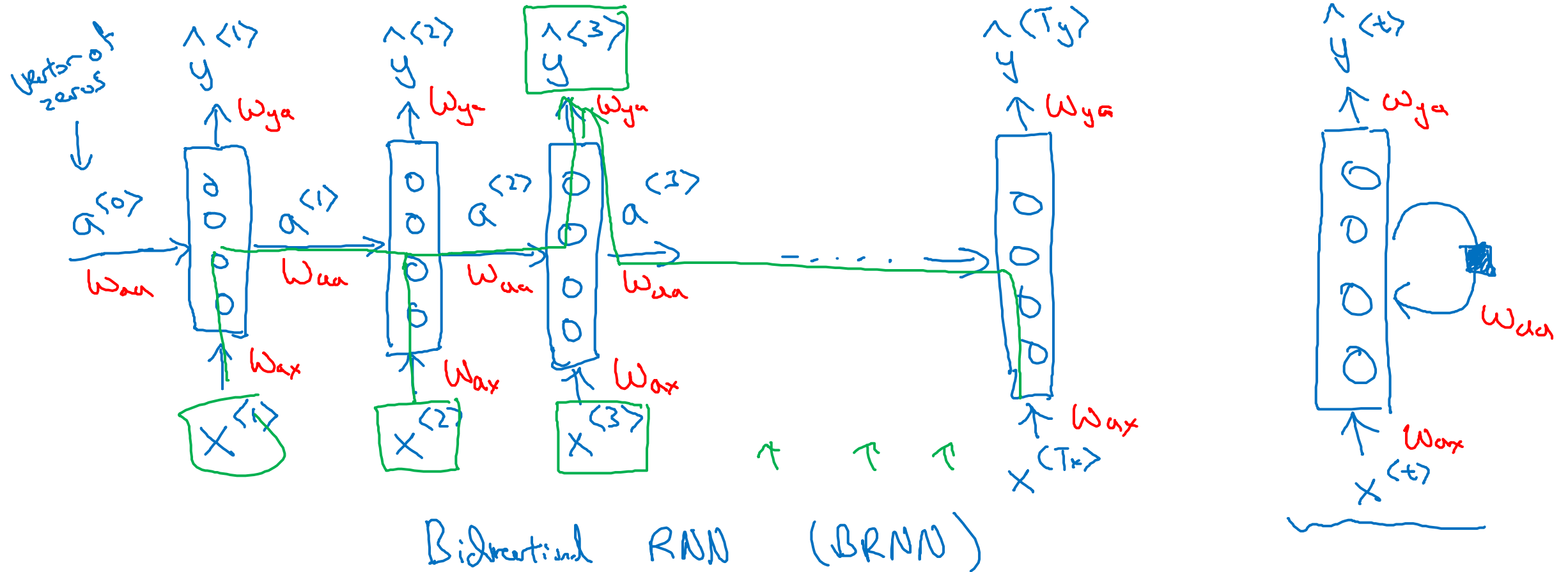


## Problems:

- - Inputs, outputs can be different lengths in different examples.
- - Doesn't share features learned across different positions of text.



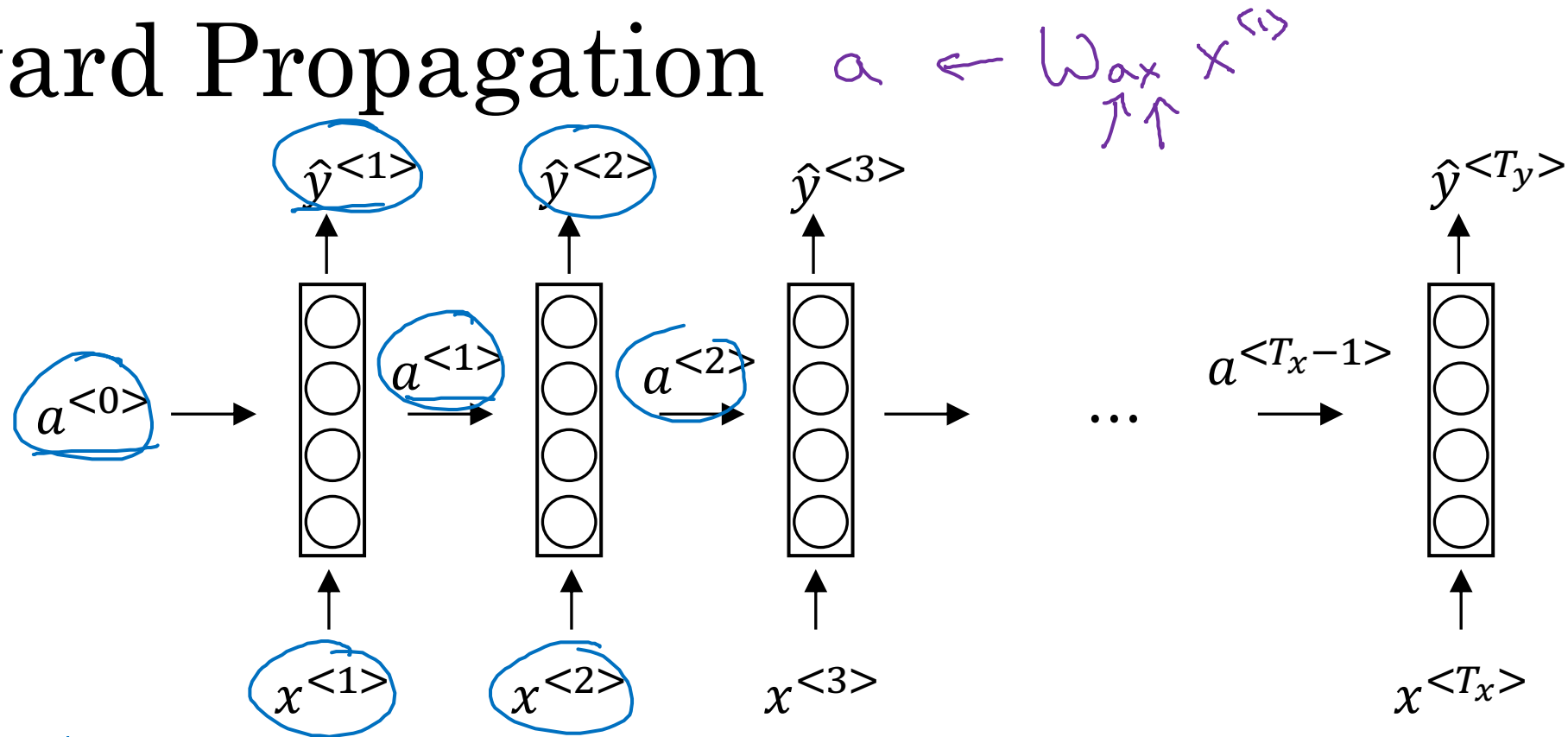
# Recurrent Neural Networks



He said, "Teddy Roosevelt was a great President."

He said, "Teddy bears are on sale!"

# Forward Propagation



$$a^{<0>} = \vec{0}.$$

$$\underline{a}^{<1>} = g_1(W_{aa} a^{<0>} + \underline{W_{ax}} x^{<1>} + b_a) \leftarrow \underline{\tanh / \text{Relu}}$$

$$\underline{\hat{y}}^{<1>} = g_2(\underline{W_{ya}} \underline{a}^{<1>} + b_y) \leftarrow \text{Sigmoid}$$

$$\boxed{\begin{aligned} a^{<t>} &= g(W_{aa} a^{<t-1>} + W_{ax} x^{<t>} + b_a) \\ \hat{y}^{<t>} &= g(W_{ya} a^{<t>} + b_y) \end{aligned}}$$

# Simplified RNN notation

$$a^{<t>} = g(\underbrace{W_{aa} a^{<t-1>}}_{\substack{\uparrow \\ (100, 100)}} + \underbrace{W_{ax} x^{<t>}}_{\substack{\uparrow \\ (100, 10,000)}} + b_a)$$

$$\hat{y}^{<t>} = g(W_{ya} a^{<t>} + b_y)$$

$$\hat{y}^{<t>} = g(W_y a^{<t>} + b_y)$$

$$a^{<t>} = g(W_a [a^{<t-1>}, x^{<t>}] + b_a)$$

$$\begin{matrix} \uparrow 100 \\ \left[ \begin{array}{c|c} W_{aa} & W_{ax} \end{array} \right] \\ \leftarrow 100 \quad \leftarrow 10,000 \end{matrix} = W_a \quad (100, 10,000)$$

$$[a^{<t-1>}, x^{<t>}] = \begin{bmatrix} a^{<t-1>} \\ x^{<t>} \end{bmatrix} \quad \begin{matrix} \updownarrow 100 \\ \updownarrow 10,000 \\ \updownarrow 10,100 \end{matrix}$$

$$\begin{bmatrix} W_{aa} & W_{ax} \end{bmatrix} \begin{bmatrix} a^{<t-1>} \\ x^{<t>} \end{bmatrix} = \underline{W_{aa} a^{<t-1>} + W_{ax} x^{<t>}}$$



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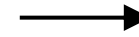
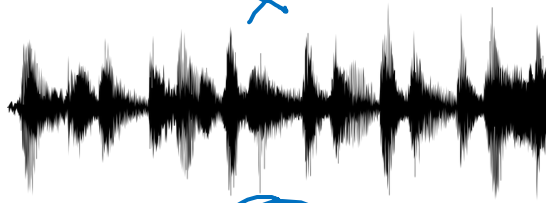
# Recurrent Neural Networks

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## Different types of RNNs

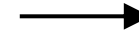
# Examples of sequence data

Speech recognition



$T_x$   $T_y$   $y$   
“The quick brown fox jumped over the lazy dog.”

Music generation



Sentiment classification

“There is nothing to like in this movie.”



DNA sequence analysis

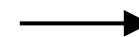
AGCCCCTGTGAGGAACTAG



AG**CCCCTGTGAGGAACTAG**

Machine translation

Voulez-vous chanter avec moi?



Do you want to sing with me?

Video activity recognition



Running

Name entity recognition

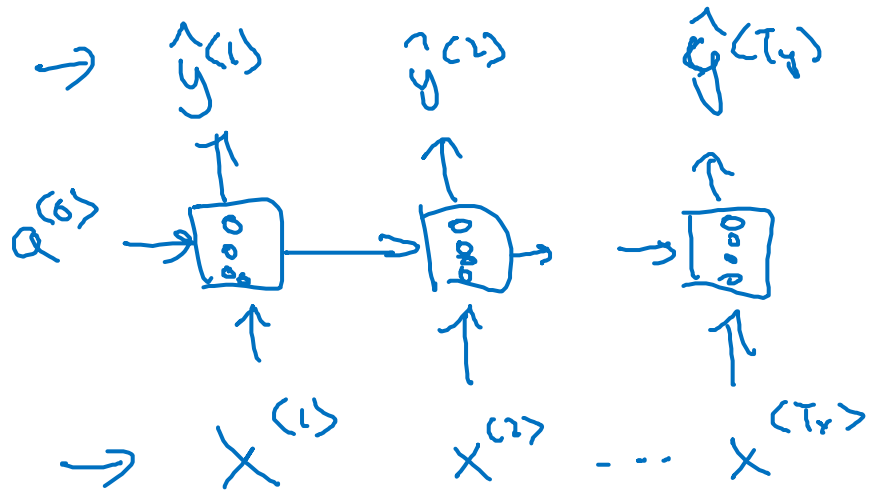
Yesterday, Harry Potter met Hermione Granger.



Yesterday, **Harry Potter** met **Hermione Granger**.

# Examples of RNN architectures

$$T_x = T_y$$

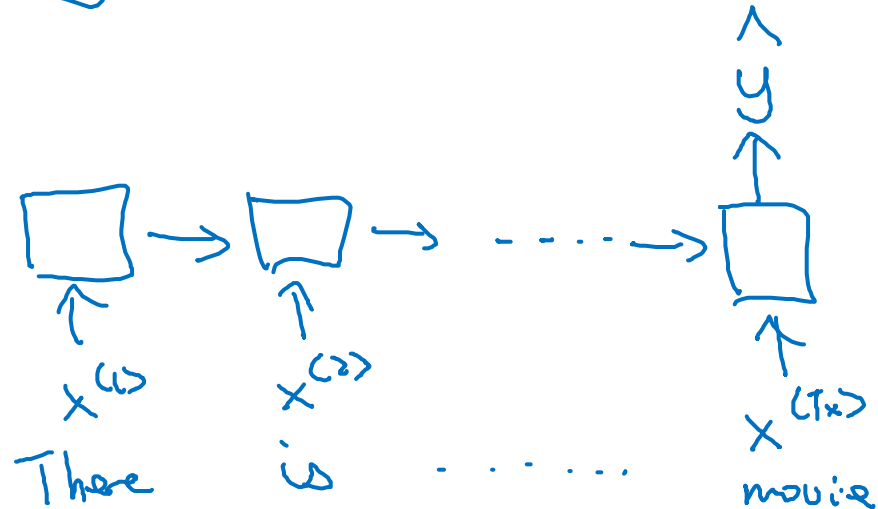


Many-to-many

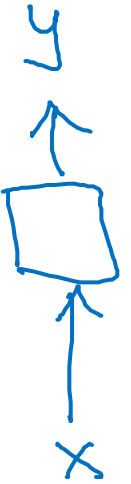
Sentiment classification-

$x = \text{text}$

$y = 0/1 \quad 1 \dots 5$

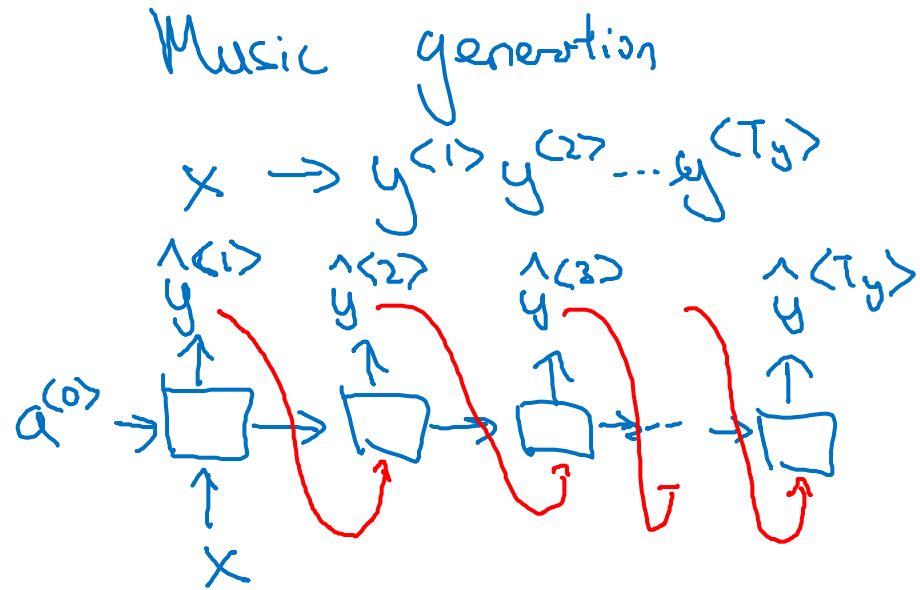


Many-to-one



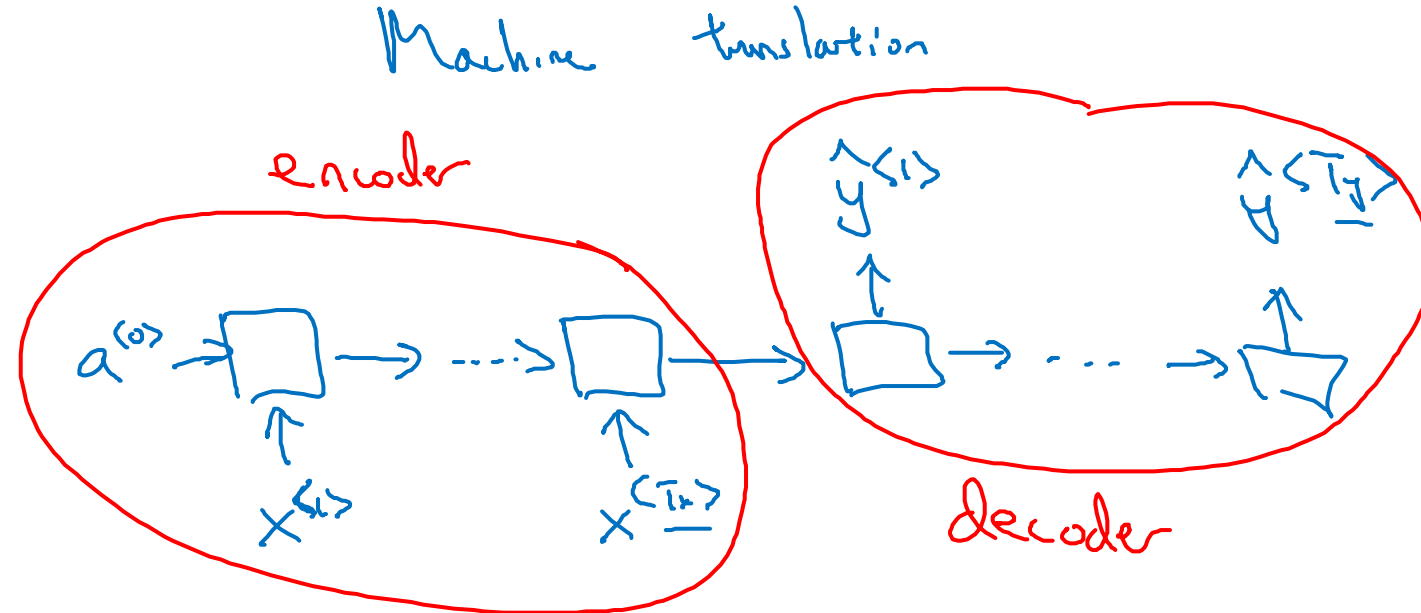
One-to-one

# Examples of RNN architectures



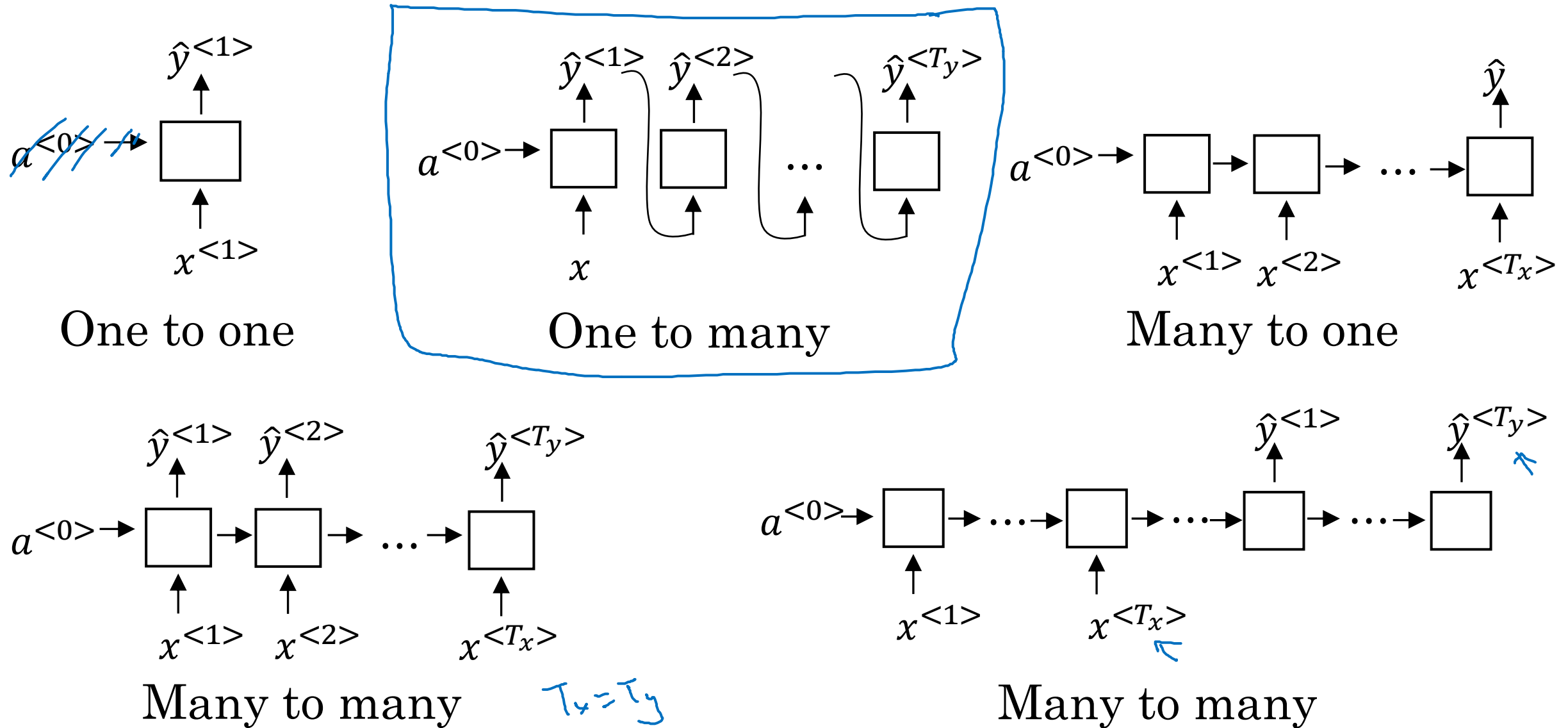
One-to-many

$$x = \phi$$



Many-to-many

# Summary of RNN types







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# Recurrent Neural Networks

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Language model and  
sequence generation

# What is language modelling?

## Speech recognition

The apple and pair salad.

→ The apple and pear salad.

$$P(\text{The apple and pair salad}) = 3.2 \times 10^{-13}$$

$$P(\text{The apple and pear salad}) = 5.7 \times 10^{-10}$$

$$P(\text{Sentence}) = ?$$

$$P(y^{(1)}, y^{(2)}, \dots, y^{(T)})$$

# Language modelling with an RNN

Training set: large corpus of english text.

Tokenize

Cats average 15 hours of sleep a day.  $\downarrow$   $\langle \text{EOS} \rangle$

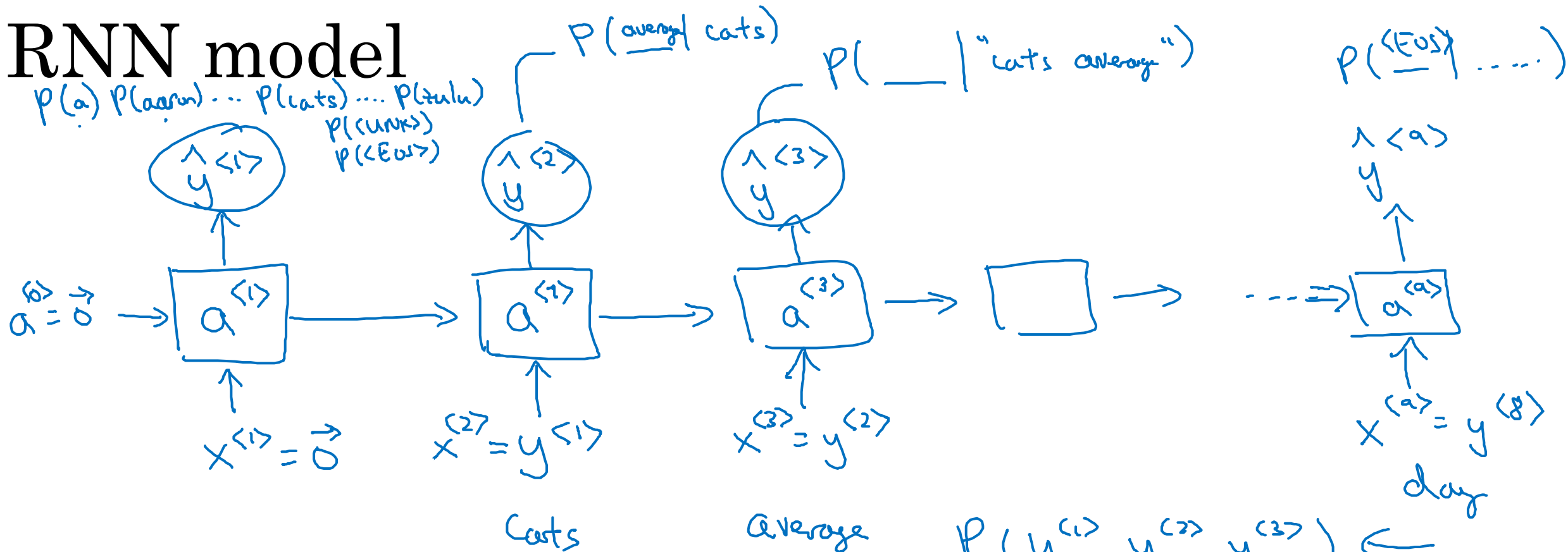
$y^{(1)}$     $y^{(2)}$     $y^{(3)}$    ...    $y^{(8)}$     $y^{(9)}$   
 $x^{(t)} = y^{(t-1)}$

The Egyptian ~~Mau~~ is a breed of cat.  $\langle \text{EOS} \rangle$

$\langle \text{UNK} \rangle$

10,000

# RNN model



→ Cats average 15 hours of sleep a day. <EOS>

$$\mathcal{L}(\hat{y}^{<t>}, y^{<t>}) = - \sum_i y_i^{<t>} \log \hat{y}_i^{<t>}$$

$$\mathcal{L} = \sum_t \mathcal{L}^{<t>}(\hat{y}^{<t>}, y^{<t>})$$

$$p(y^{(1)}, y^{(2)}, y^{(3)}) \leftarrow$$

$$= \frac{p(y^{(1)}) p(y^{(2)} | y^{(1)})}{p(y^{(3)} | y^{(1)}, y^{(2)})}$$



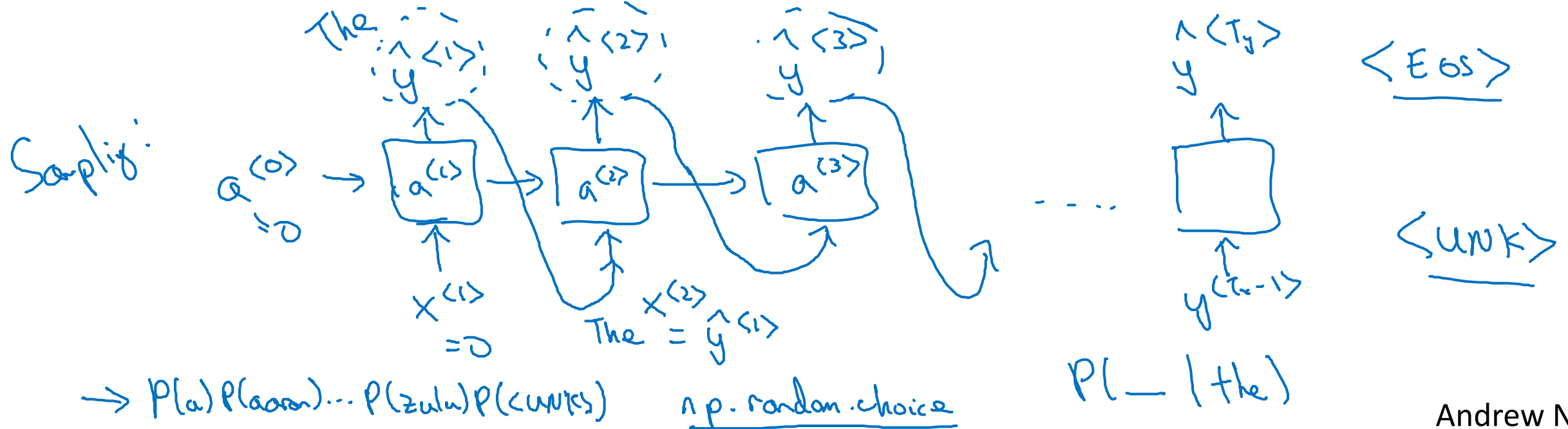
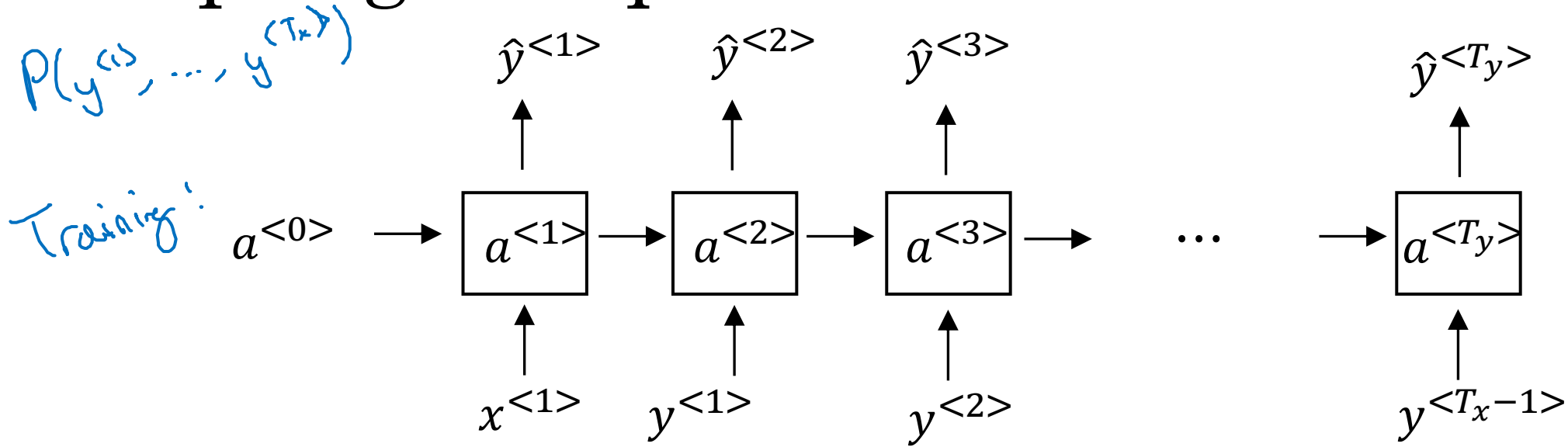
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# Recurrent Neural Networks

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Sampling novel  
sequences

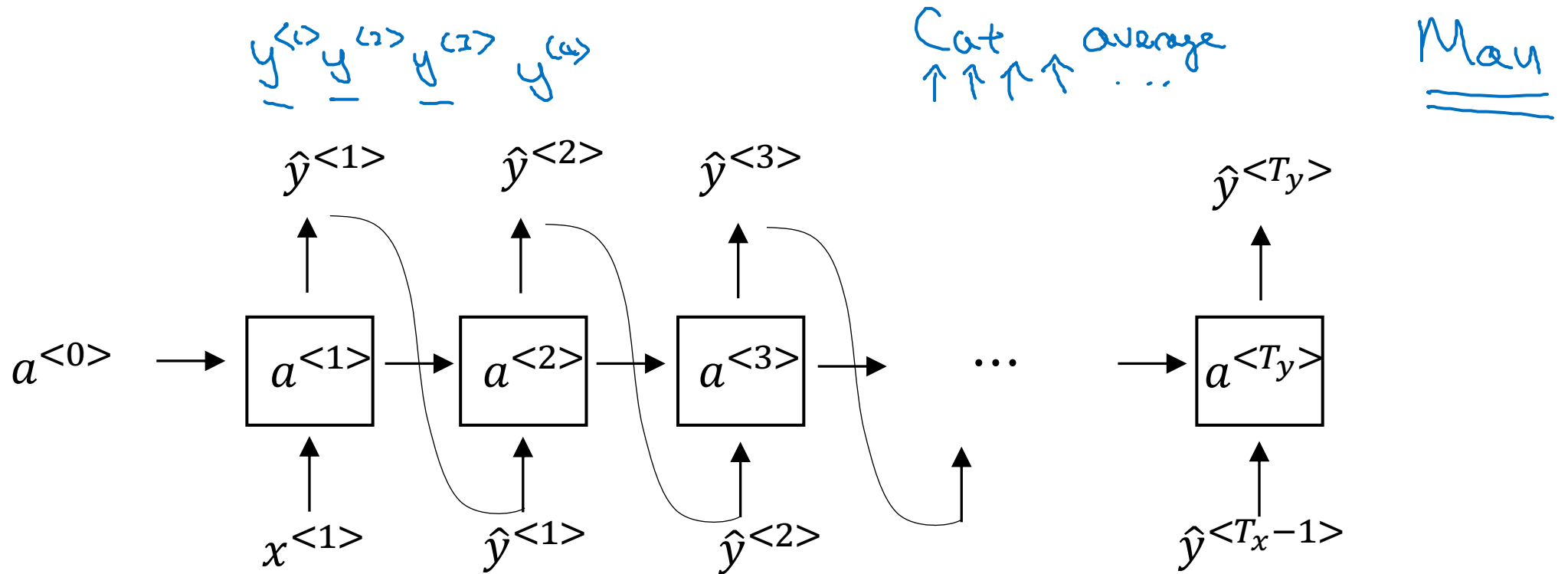
# Sampling a sequence from a trained RNN



# Character-level language model

→ Vocabulary = [a, aaron, ..., zulu, <UNK>] ←

→ Vocabulary = [a, b, c, ..., z,  $\backslash$ , ., , , ;, 0, ..., 9, A, ..., Z]




# Sequence generation

## News

President enrique peña nieto, announced  
sench's sulk former coming football langston  
paring.

"I was not at all surprised," said hich langston.

"Concussion epidemic", to be examined. 

The gray football the told some and this has on  
the uefa icon, should money as.

## Shakespeare

The mortal moon hath her eclipse in love.

And subject of this thou art another this fold.

When besser be my love to me see sabl's.

For whose are ruse of mine eyes heaves.





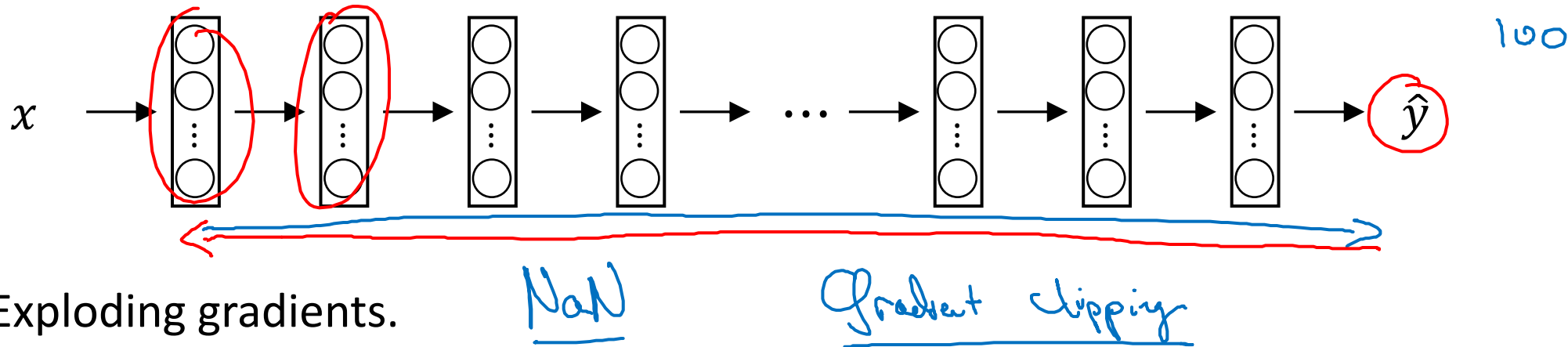
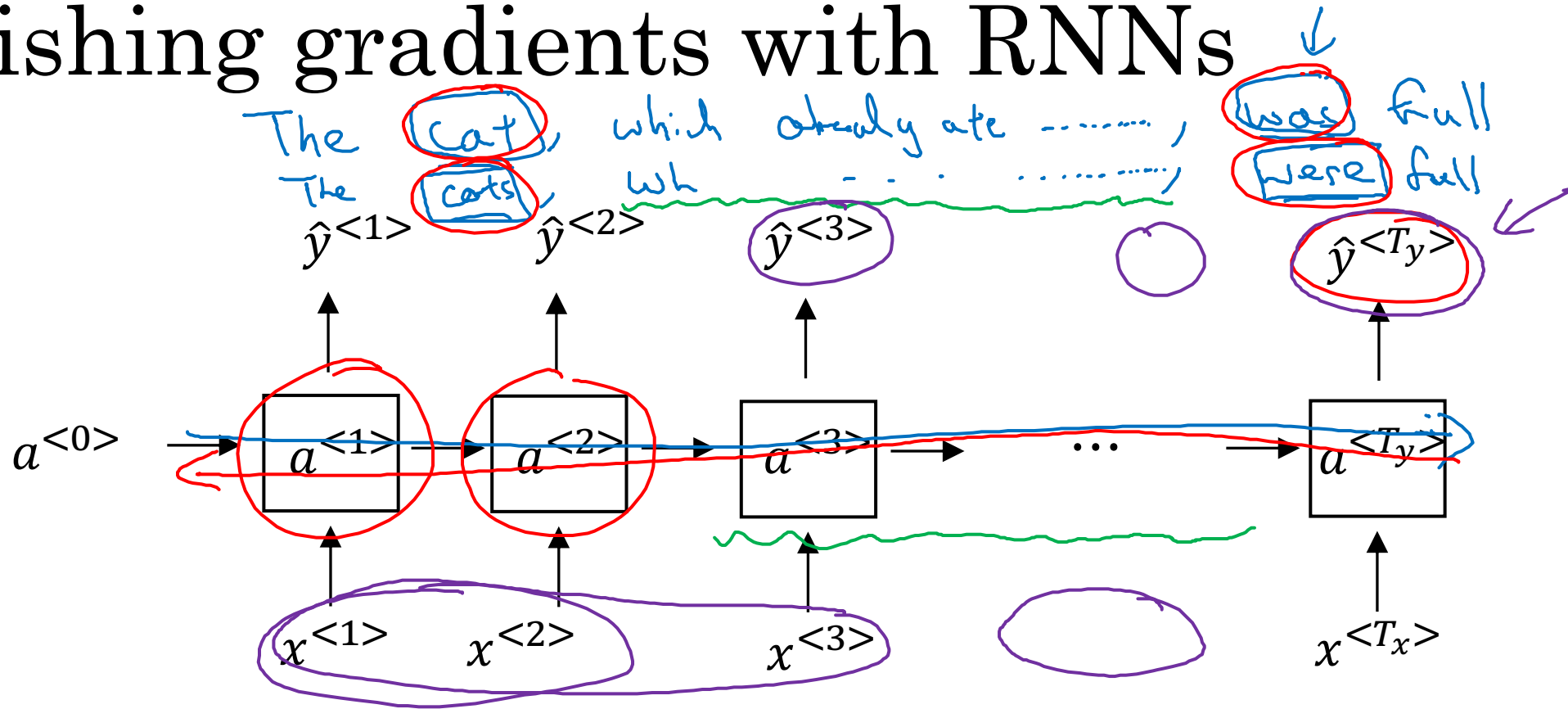
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# Recurrent Neural Networks

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## Vanishing gradients with RNNs

# Vanishing gradients with RNNs





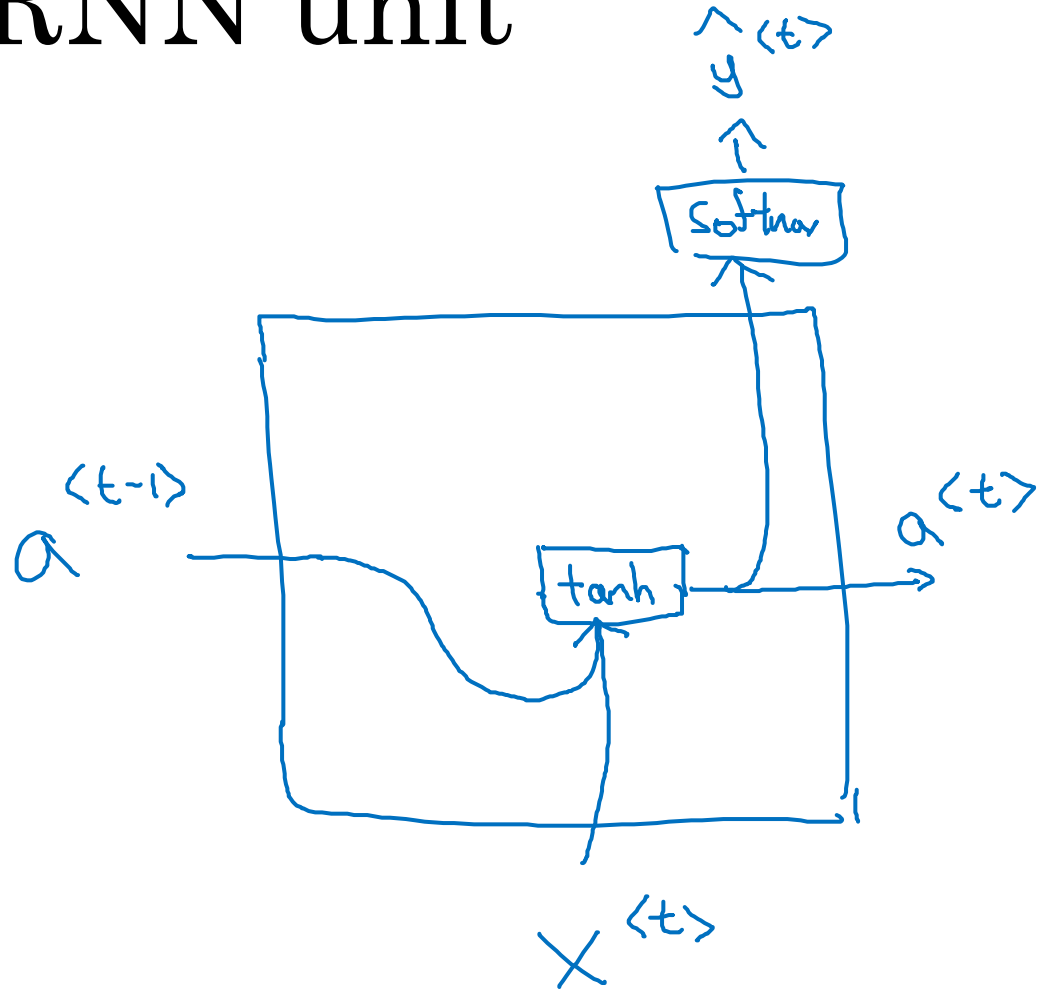
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# Recurrent Neural Networks

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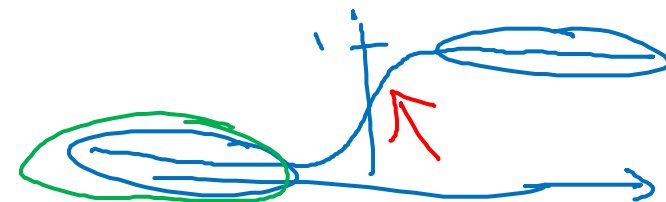
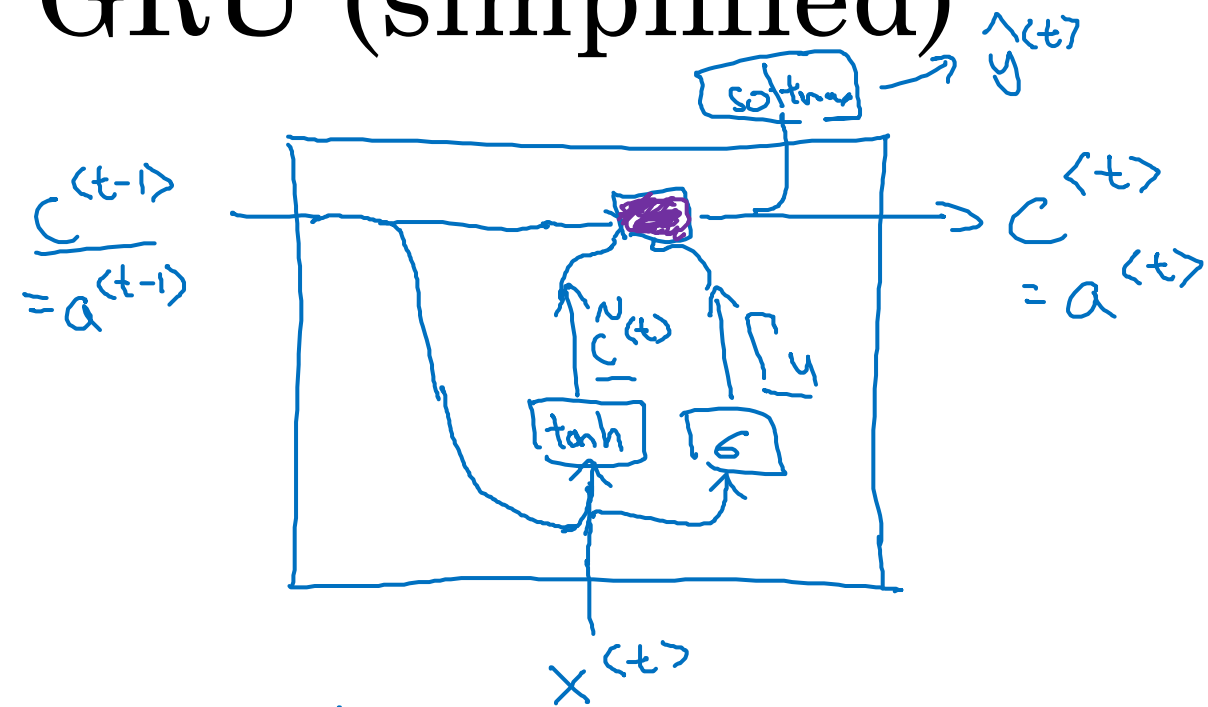
## Gated Recurrent Unit (GRU)

# RNN unit



$$\underline{a^{<t>}} = \overset{\substack{\text{tanh} \\ \downarrow}}{g}(\underbrace{W_a[a^{<t-1>}, x^{<t>}]}_{\uparrow} + b_a)$$

# GRU (simplified)



$C$  = memory cell

$$\rightarrow \underline{C}^{(t)} = \underline{a}^{(t)}$$

$$\rightarrow \tilde{C}^{(t)} = \tanh(W_c [c^{(t-1)}, x^{(t)}] + b_c)$$

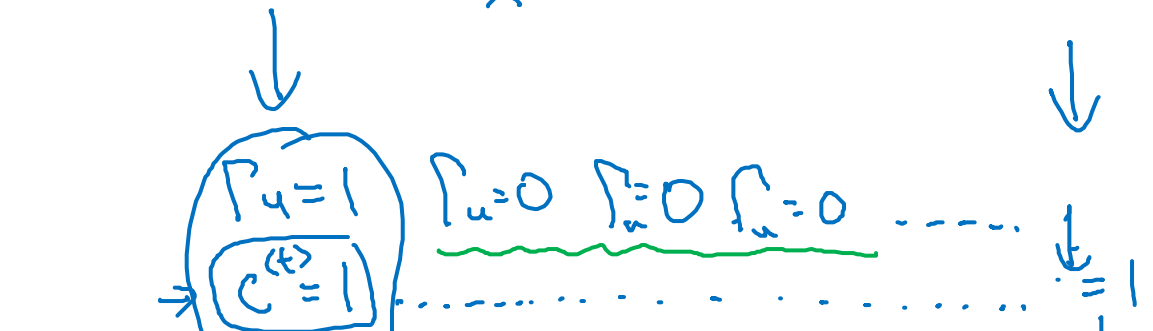
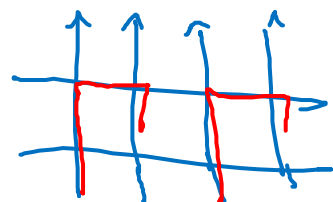
$$\rightarrow \Gamma_u = \sigma(W_u [c^{(t-1)}, x^{(t)}] + b_u)$$

$$\underline{C}^{(t)} = \Gamma_u * \tilde{C}^{(t)} + (1 - \Gamma_u) * \underline{C}^{(t-1)}$$

element-wise

$$\Gamma_u = 0.000001$$

Gate



The cat, which already ate ..., was full.

# Full GRU

$\tilde{h}$   $\tilde{c}^{<t>} = \tanh(W_c [ \tilde{c}^{<t-1>}, x^{<t>} ] + b_c)$

$u$   $\Gamma_u = \sigma(W_u [ c^{<t-1>}, x^{<t>} ] + b_u)$

$r$   $\Gamma_r = \sigma(W_r [ c^{<t-1>}, x^{<t>} ] + b_r)$

LSTM

$h$   $c^{<t>} = \Gamma_u * \tilde{c}^{<t>} + (1 - \Gamma_u) * c^{<t-1>}$

The cat, which ate already, was full.



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# Recurrent Neural Networks

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LSTM (long short  
term memory) unit

# GRU and LSTM

## GRU

$$\underline{\tilde{c}^{<t>}} = \tanh(W_c[\underline{\Gamma_r} * \underline{c^{<t-1>}}, x^{<t>}] + b_c)$$

$$\underline{\Gamma_u} = \sigma(W_u[\underline{c^{<t-1>}}, x^{<t>}] + b_u)$$

$$\underline{\Gamma_r} = \sigma(W_r[\underline{c^{<t-1>}}, x^{<t>}] + b_r)$$

$$\underline{c^{<t>}} = \underline{\Gamma_u} * \underline{\tilde{c}^{<t>}} + \underline{(1 - \Gamma_u)} * \underline{c^{<t-1>}}$$

$\underline{a^{<t>}} = \underline{c^{<t>}}$

$\uparrow$   
 $\Gamma_f$

## LSTM

$$\underline{\tilde{c}^{<t>}} = \tanh(W_c[a^{<t-1>}, x^{<t>}] + b_c)$$

(update)  $\Gamma_u = \sigma(W_u[a^{<t-1>}, x^{<t>}] + b_u)$

(forget)  $\Gamma_f = \sigma(W_f[a^{<t-1>}, x^{<t>}] + b_f)$

(output)  $\Gamma_o = \sigma(W_o[a^{<t-1>}, x^{<t>}] + b_o)$

$$\underline{c^{<t>}} = \underline{\Gamma_u} * \underline{\tilde{c}^{<t>}} + \underline{\Gamma_f} * \underline{c^{<t-1>}}$$

$$\underline{a^{<t>}} = \underline{\Gamma_o} * \underline{c^{<t>}}$$



# LSTM in pictures

$$\tilde{c}^{<t>} = \tanh(W_c[a^{<t-1>}, x^{<t>}] + b_c)$$

$$\Gamma_u = \sigma(W_u[a^{<t-1>}, x^{<t>}] + b_u)$$

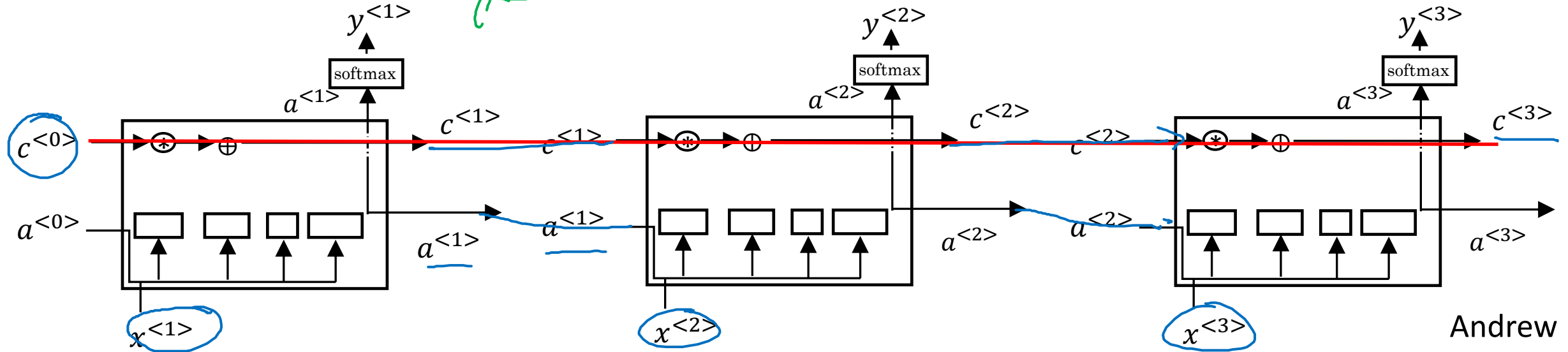
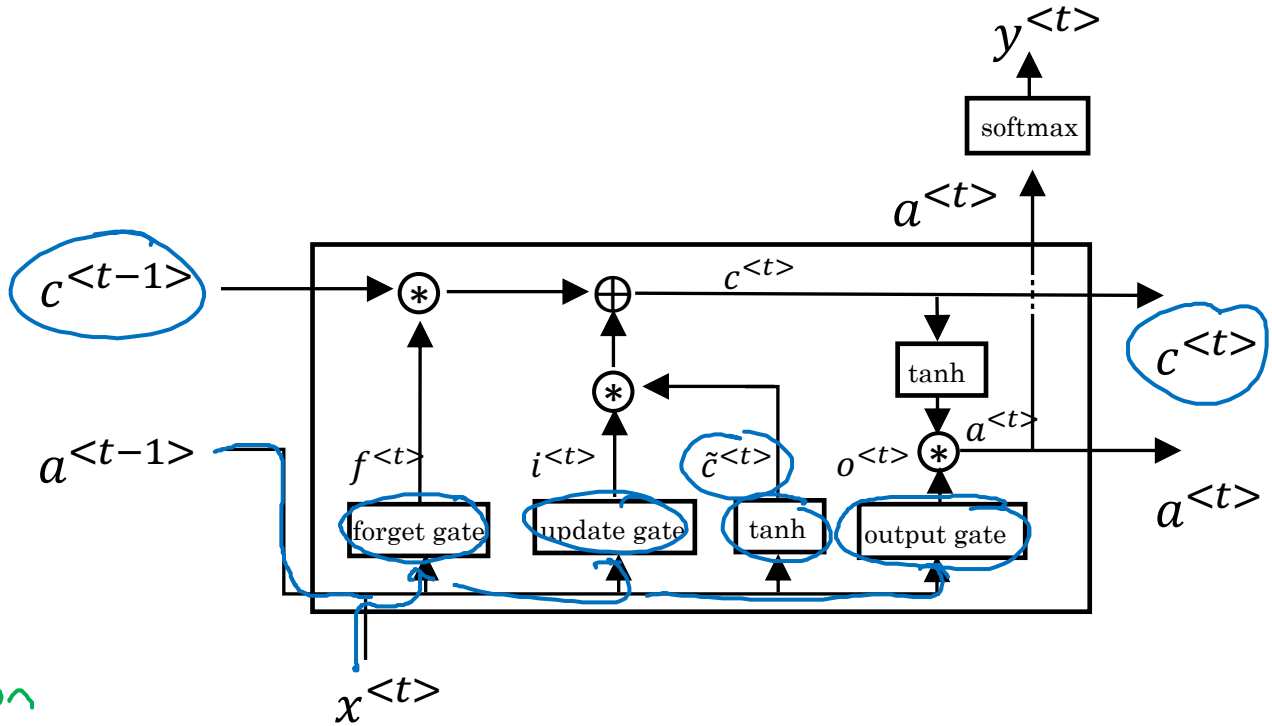
$$\Gamma_f = \sigma(W_f[a^{<t-1>}, x^{<t>}] + b_f)$$

$$\Gamma_o = \sigma(W_o[a^{<t-1>}, x^{<t>}] + b_o)$$

$$c^{<t>} = \Gamma_u * \tilde{c}^{<t>} + \Gamma_f * c^{<t-1>}$$

$$a^{<t>} = \Gamma_o * c^{<t>}$$

peephole  
connection





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# Recurrent Neural Networks

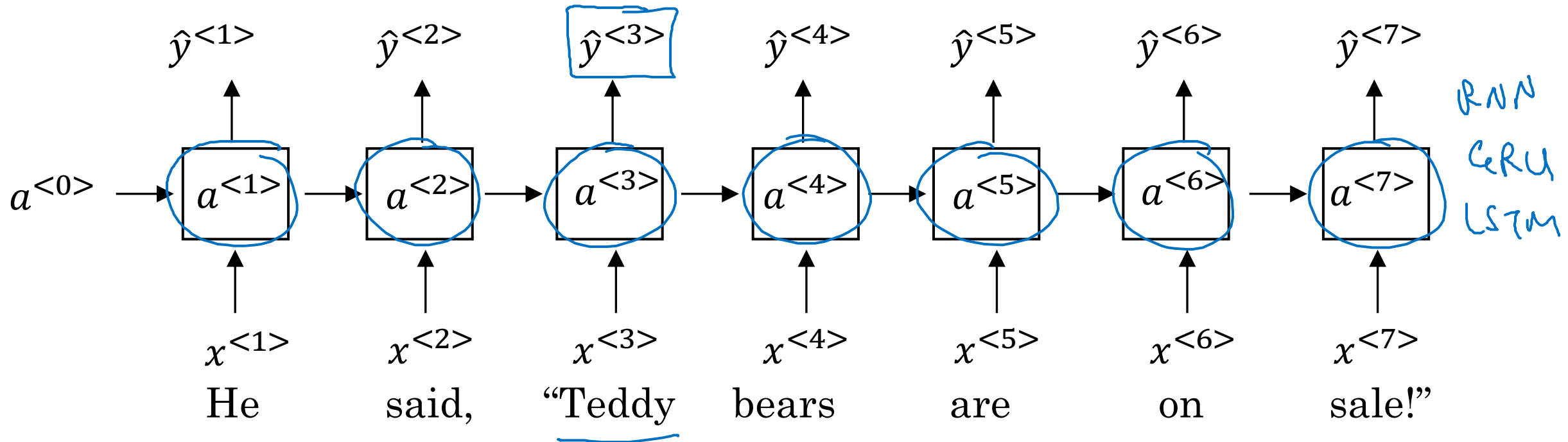
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## Bidirectional RNN

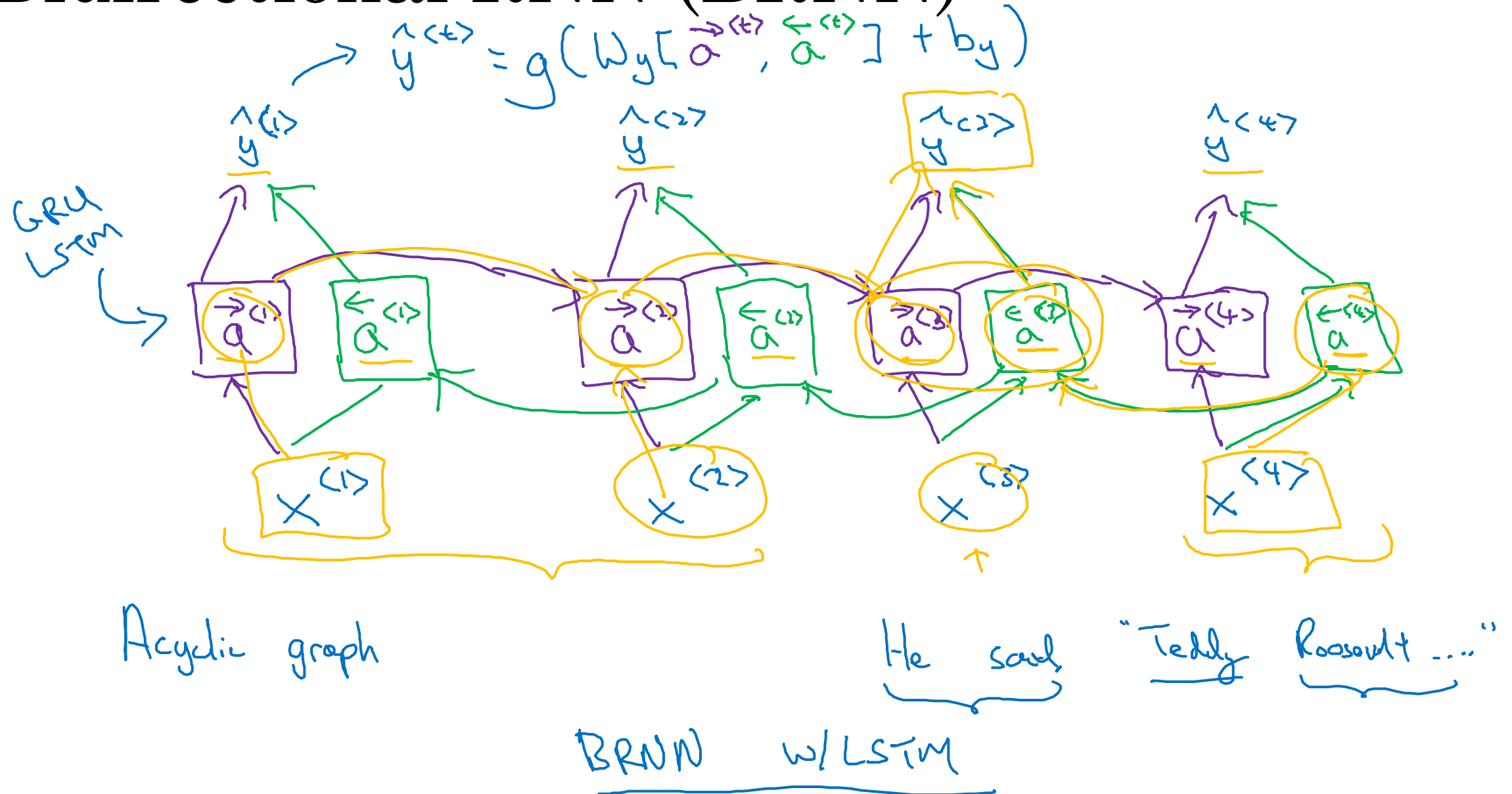
# Getting information from the future

He said, “Teddy bears are on sale!”

He said, “Teddy Roosevelt was a great President!”



# Bidirectional RNN (BRNN)





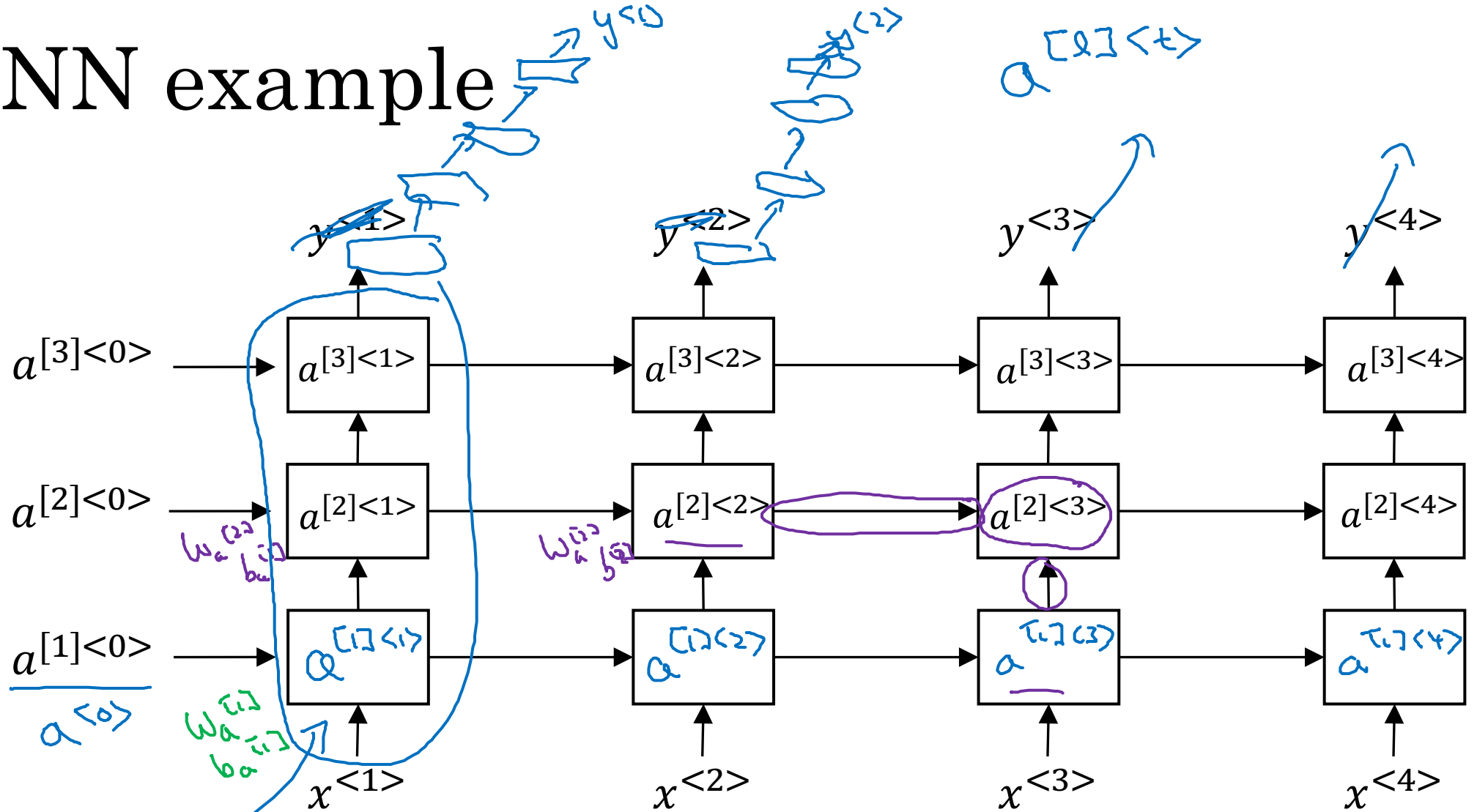
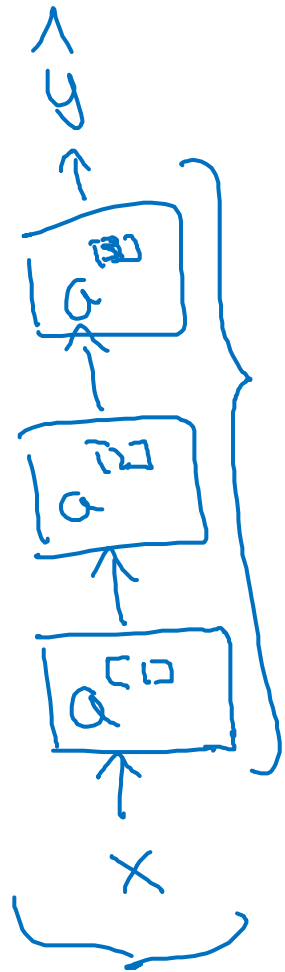
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# Recurrent Neural Networks

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## Deep RNNs

# Deep RNN example



RNN  
GRU  
LSTM

BRNN

$$a^{[2]<3>} = g(W_a^{[2]} [a^{[1]<3>}, a^{[2]<2>}] + b_a^{[2]})$$



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# Sequence to sequence models

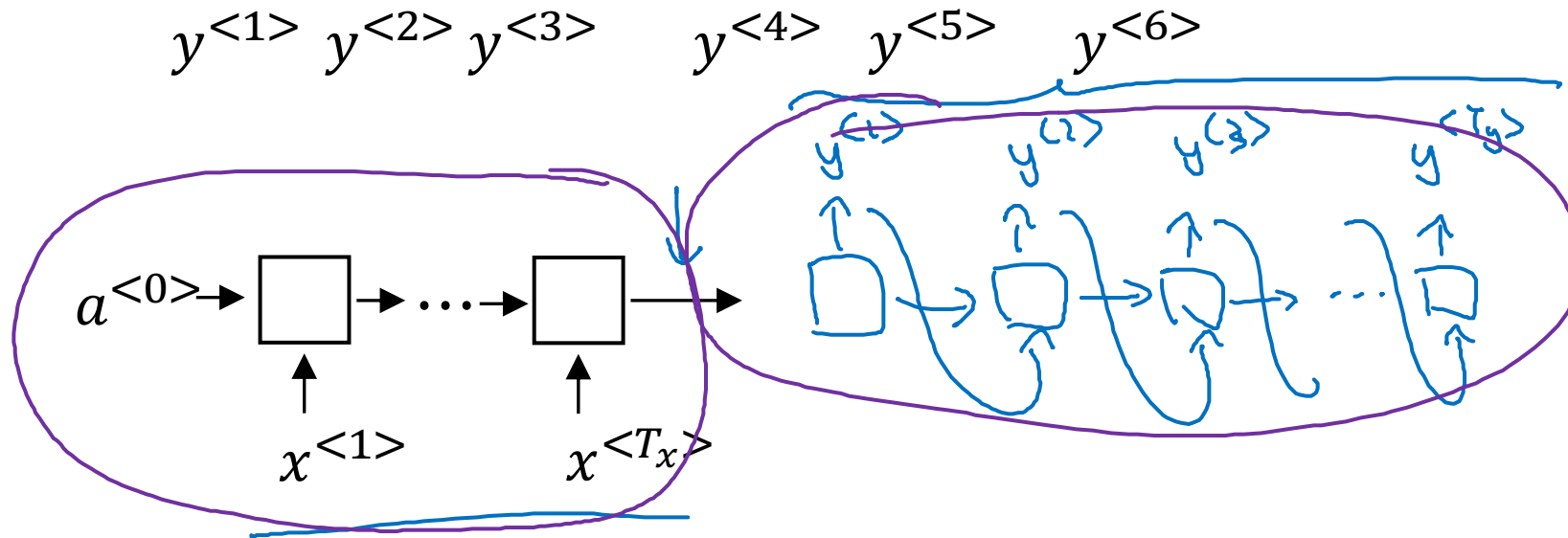
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## Basic models

# Sequence to sequence model

$x^{<1>} \quad x^{<2>} \quad x^{<3>} \quad x^{<4>} \quad x^{<5>}$   
Jane visite l'Afrique en septembre

→ Jane is visiting Africa in September.

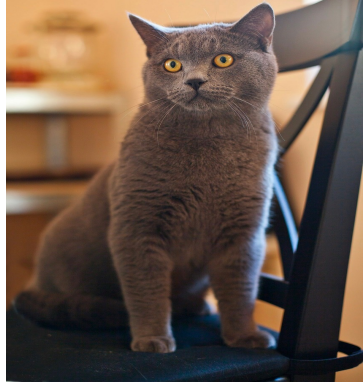


[Sutskever et al., 2014. Sequence to sequence learning with neural networks] ↩

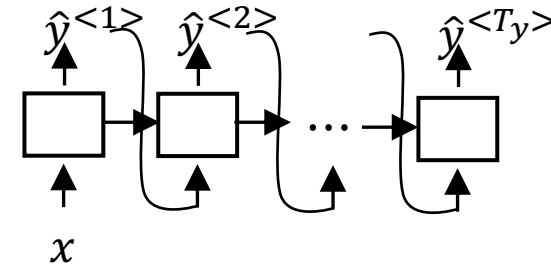
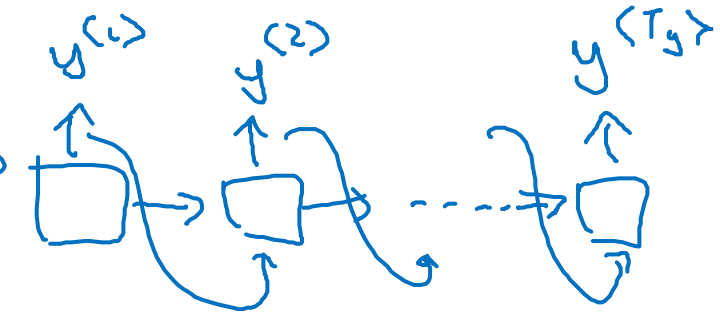
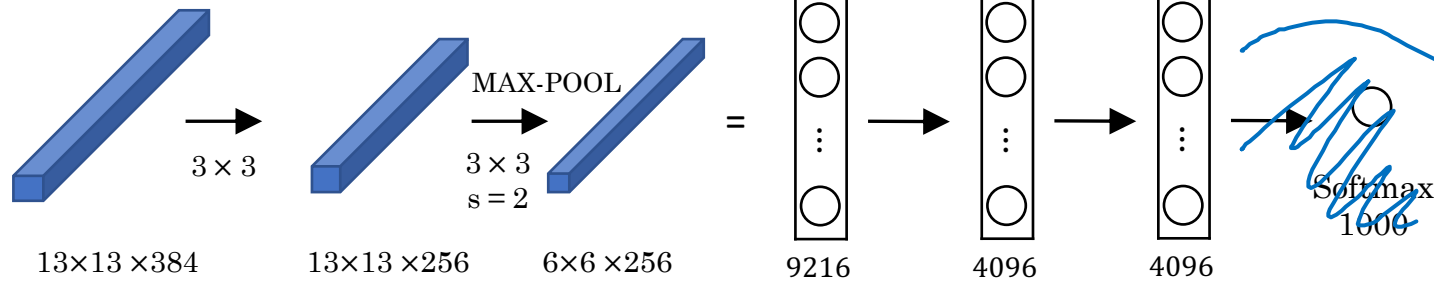
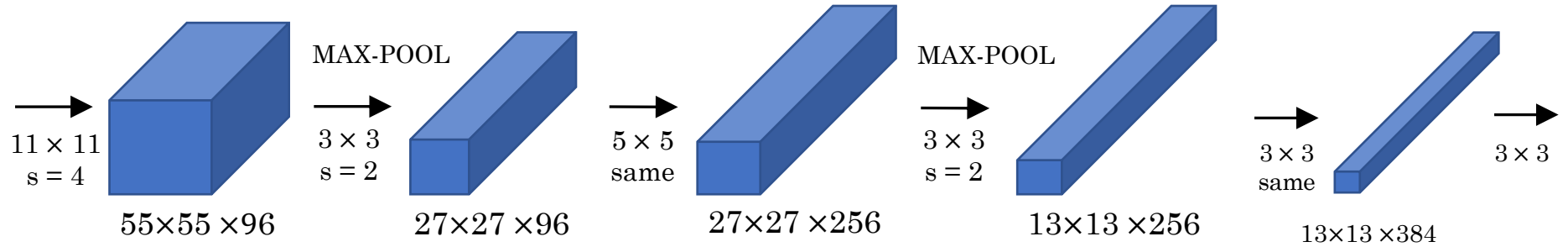
[Cho et al., 2014. Learning phrase representations using RNN encoder-decoder for statistical machine translation] ↩



# Image captioning



$y^{<1>}$   $y^{<2>}$   $y^{<3>}$   $y^{<4>}$   $y^{<5>}$   $y^{<6>}$  }  
 A cat sitting on a chair



[Mao et. al., 2014. Deep captioning with multimodal recurrent neural networks]

[Vinyals et. al., 2014. Show and tell: Neural image caption generator]

[Karpathy and Li, 2015. Deep visual-semantic alignments for generating image descriptions]



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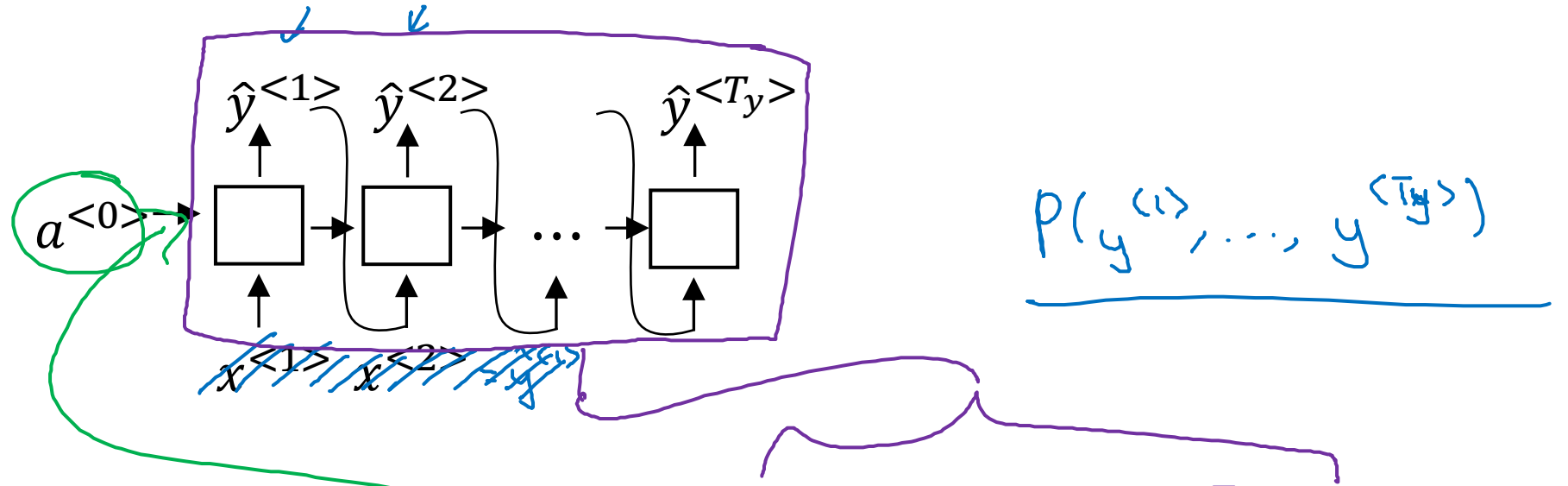
# Sequence to sequence models

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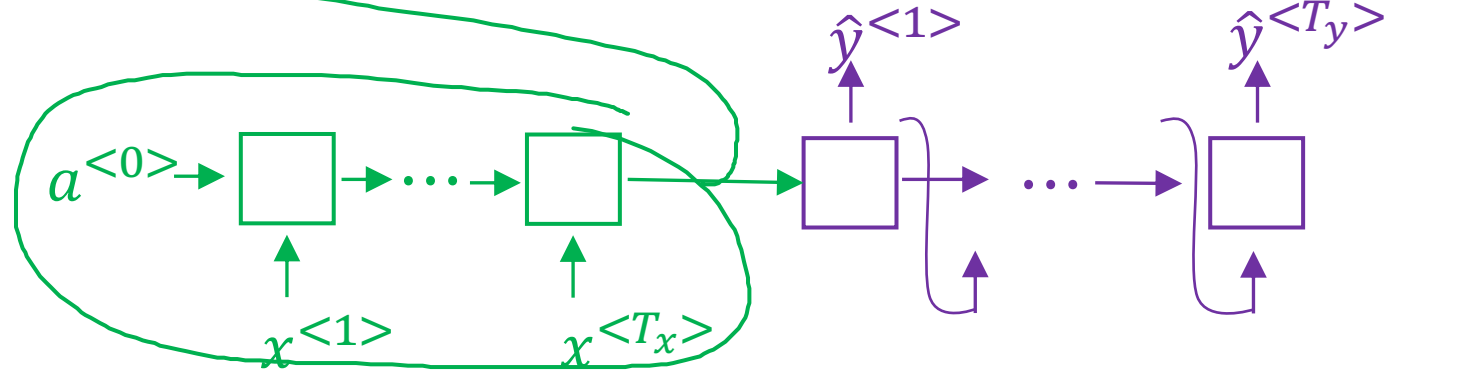
## Picking the most likely sentence

# Machine translation as building a conditional language model

Language model:



Machine translation:



"Conditional language model"

$$P(y^{<1>}, \dots, y^{<T_y>} | x^{<1>}, \dots, x^{<T_x>})$$

# Finding the most likely translation

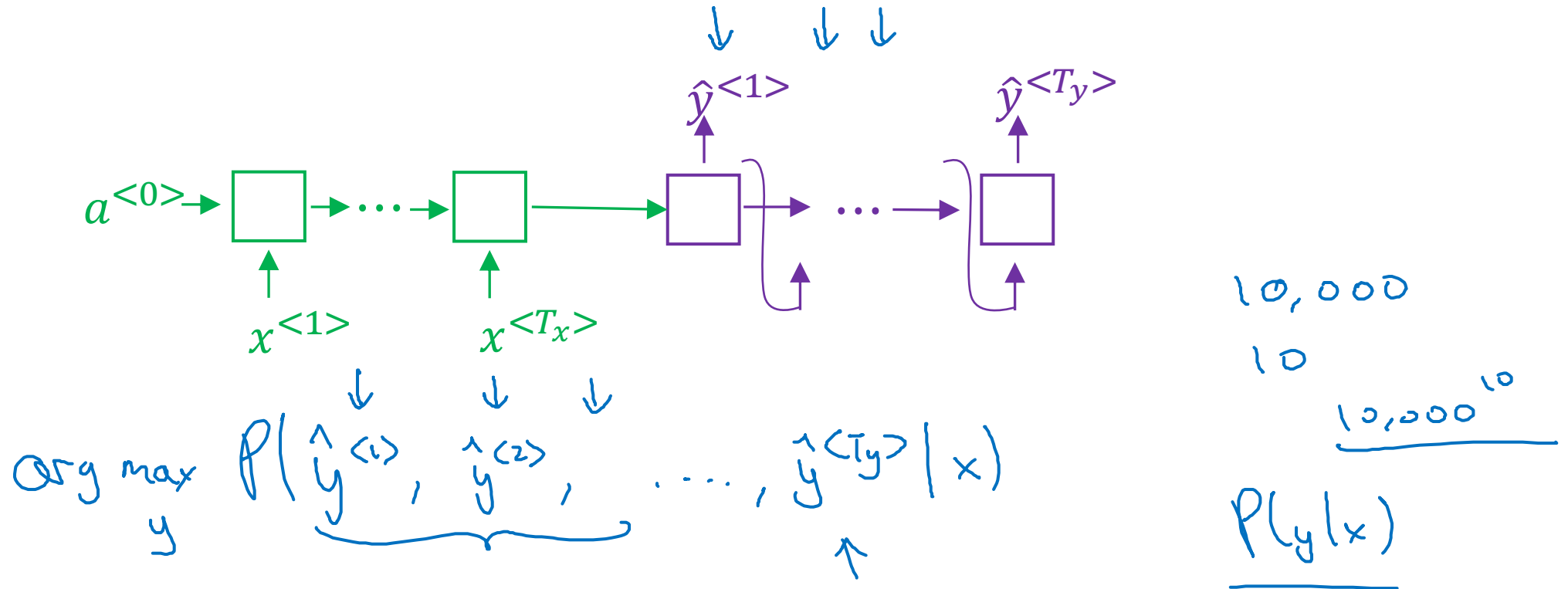
Jane visite l'Afrique en septembre.

$$P(y^{<1>}, \dots, y^{<T_y>} | x)$$

- Jane is visiting Africa in September.
- Jane is going to be visiting Africa in September.
- In September, Jane will visit Africa.
- Her African friend welcomed Jane in September.

$$\arg \max_{y^{<1>}, \dots, y^{<T_y>}} \underline{P(y^{<1>}, \dots, y^{<T_y>} | x)}$$

# Why not a greedy search?



→ Jane is visiting Africa in September.

→ Jane is going to be visiting Africa in September.

$$P(\text{Jane is going} | x) > P(\text{Jane is visiting} | x)$$



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# Sequence to sequence models

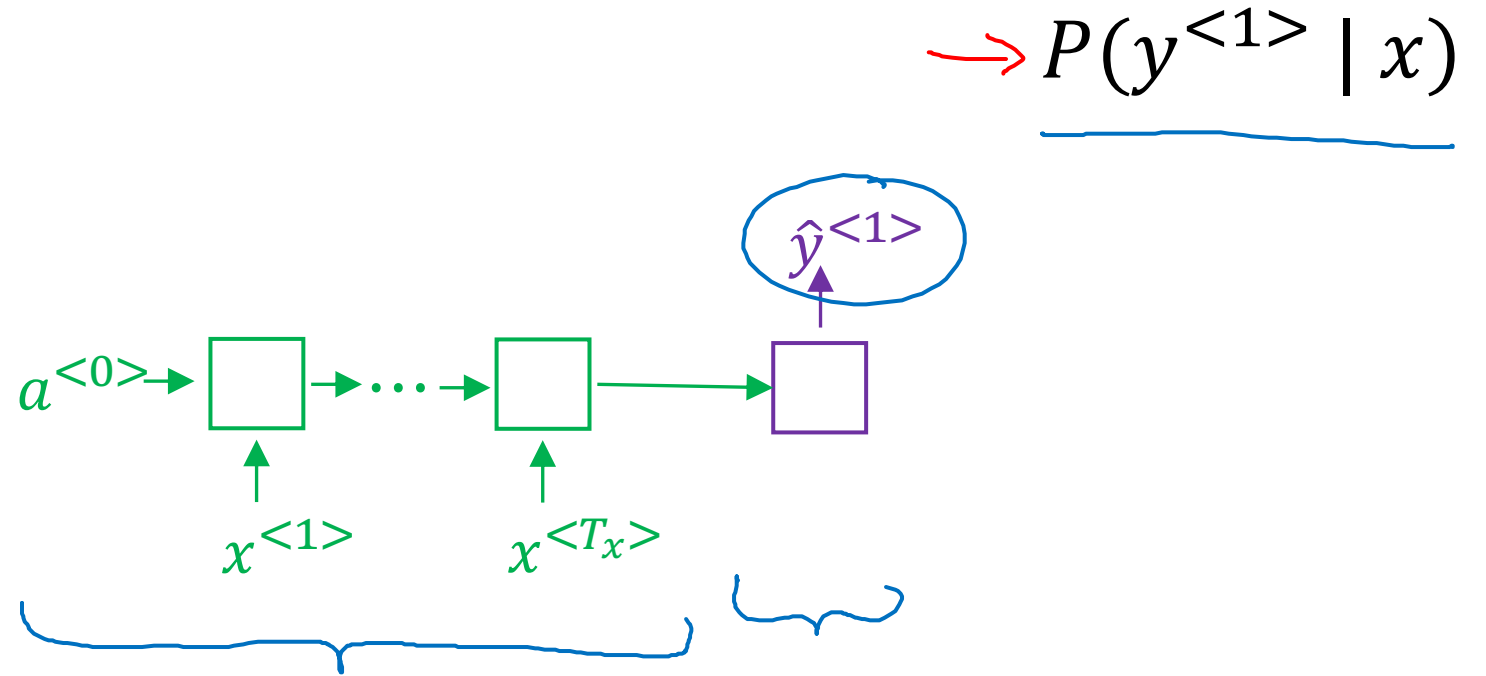
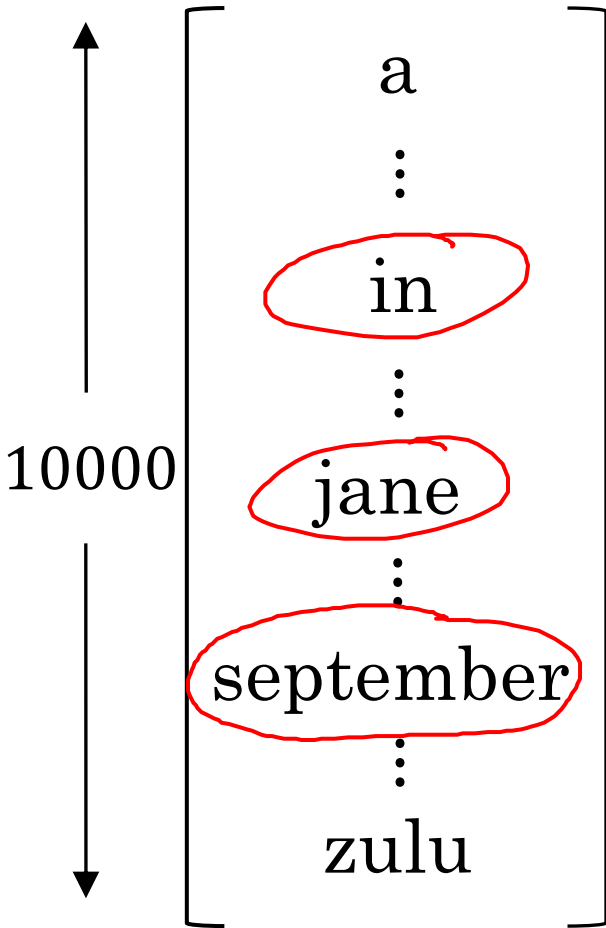
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## Beam search

# Beam search algorithm

$B = 3$  (beam width)

Step 1





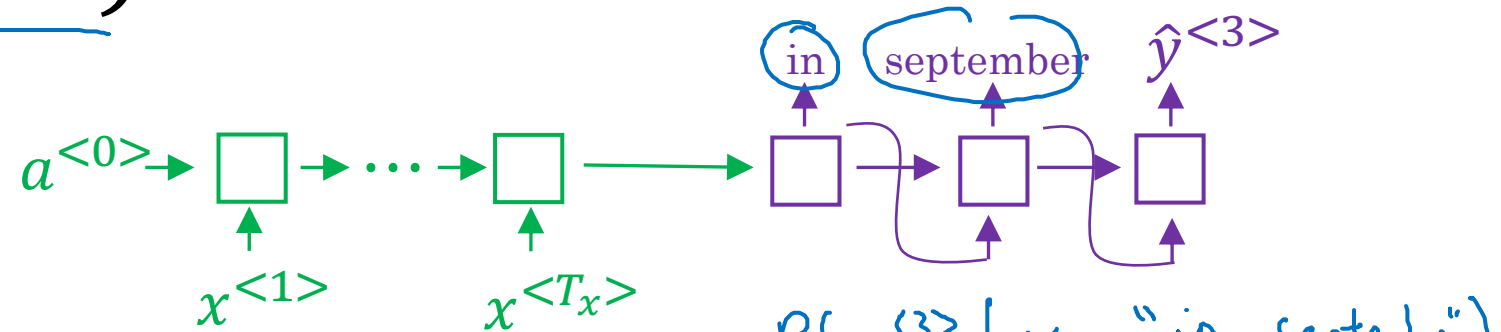


# Beam search ( $B = 3$ )

$B=1 \rightsquigarrow$  greedy search

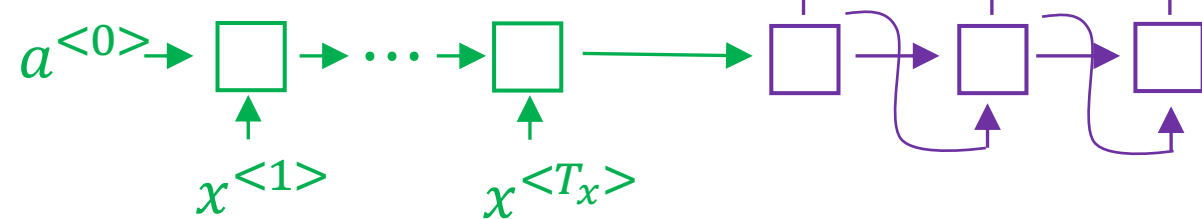
in september

*a*  
*aaron*  
*jane*  
*zulu*



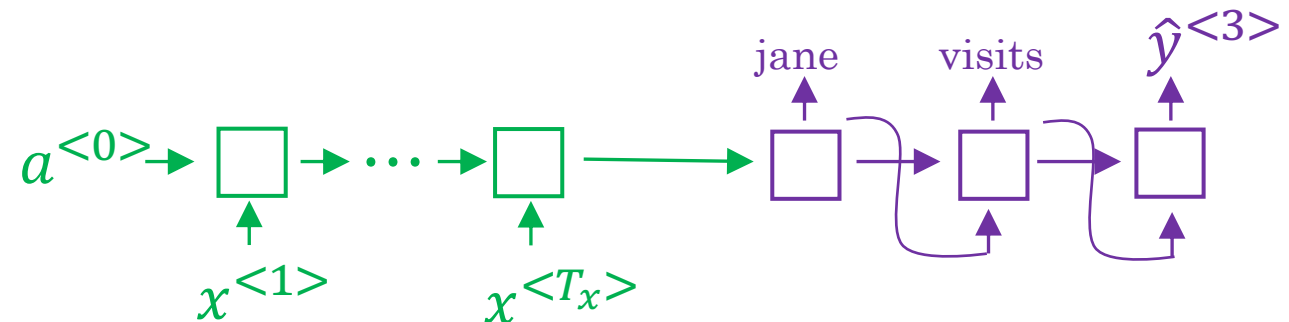
jane is

*a*  
*visiting*  
*zulu*



jane visits

*a*  
*africa*  
*zulu*



$$P(y^{<1>}, y^{<2>} | x)$$

jane visits africa in september. <EOS>



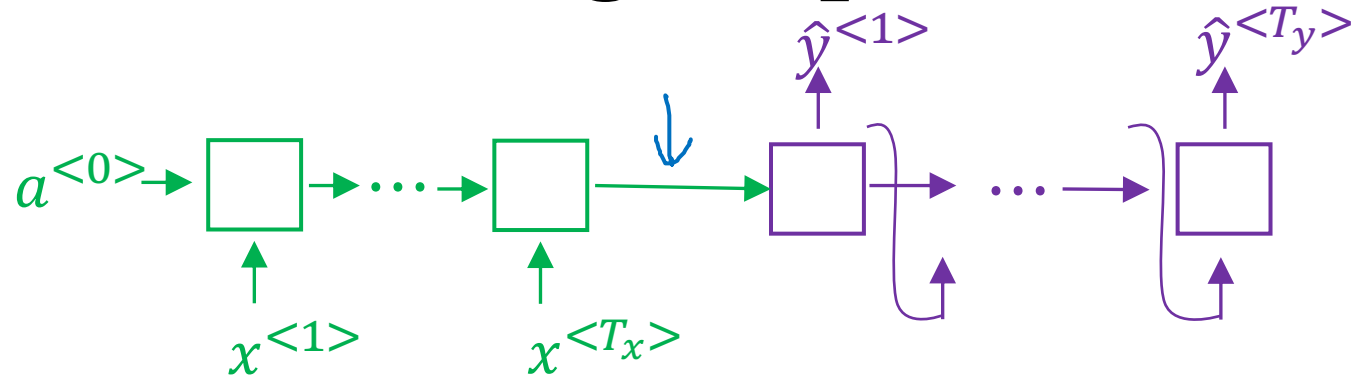
deeplearning.ai

# Sequence to sequence models

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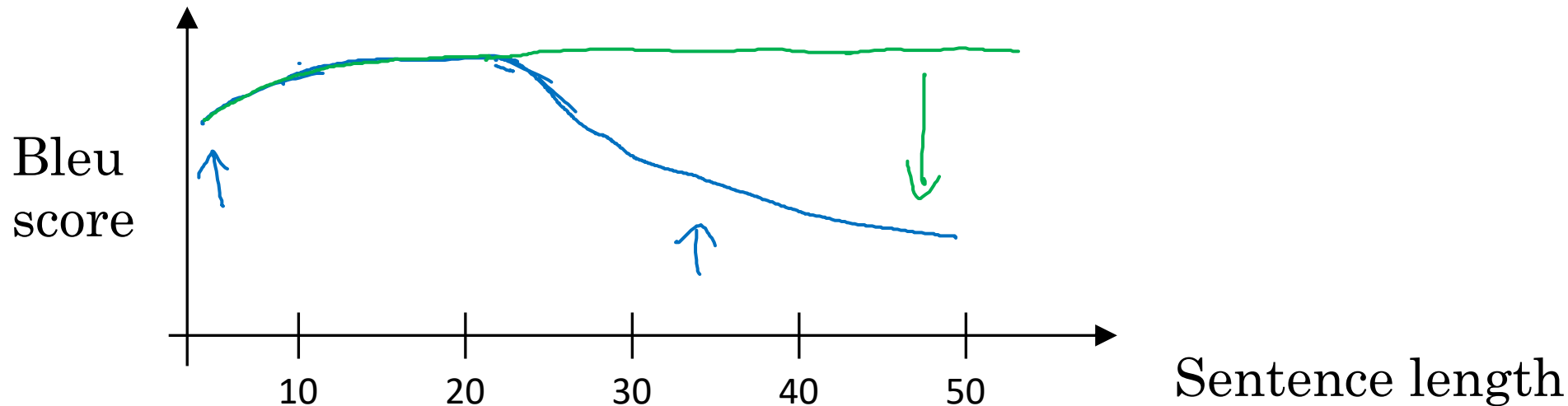
## Attention model intuition

# The problem of long sequences

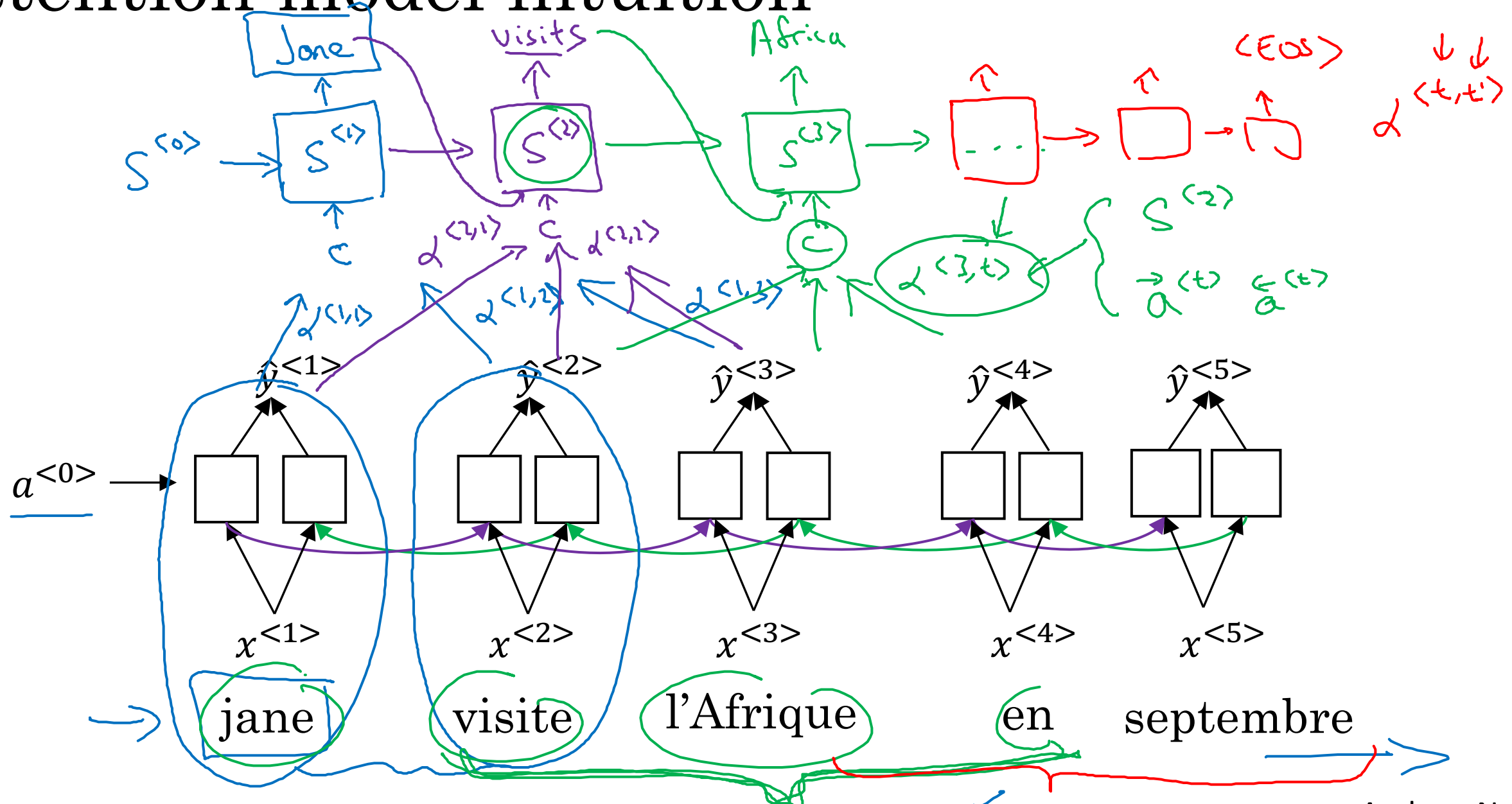


Jane s'est rendue en Afrique en septembre dernier, a apprécié la culture et a rencontré beaucoup de gens merveilleux; elle est revenue en parlant comment son voyage était merveilleux, et elle me tente d'y aller aussi.

Jane went to Africa last September, and enjoyed the culture and met many wonderful people; she came back raving about how wonderful her trip was, and is tempting me to go too.



# Attention model intuition





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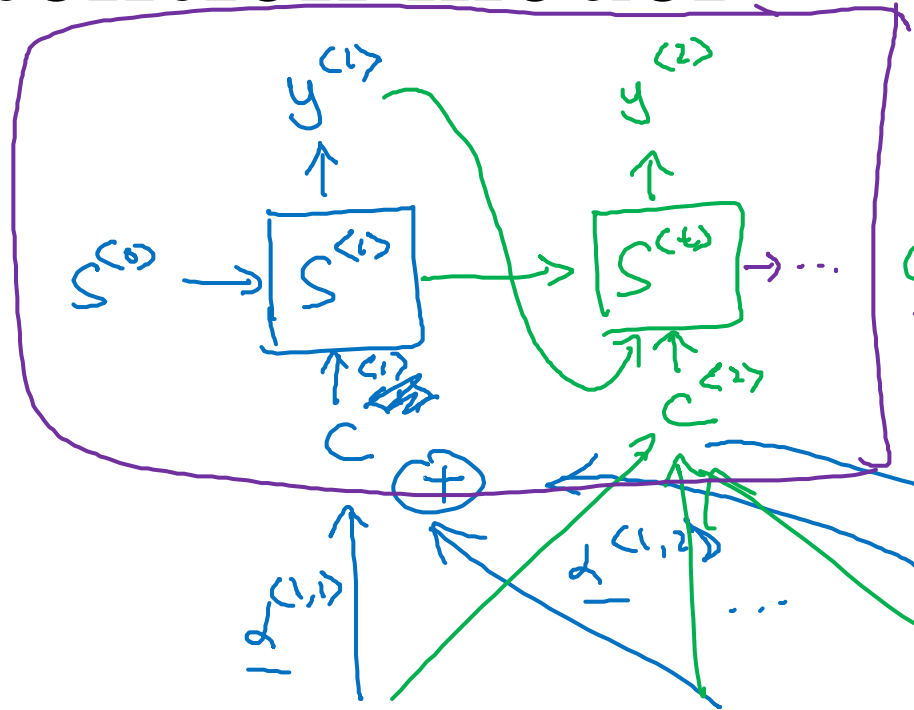
# Sequence to sequence models

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## Attention model

# Attention model

$\alpha^{(t,t')}$  = amount of 'attention'  $y^{(t)}$  should pay to  $a^{(t')}$ .

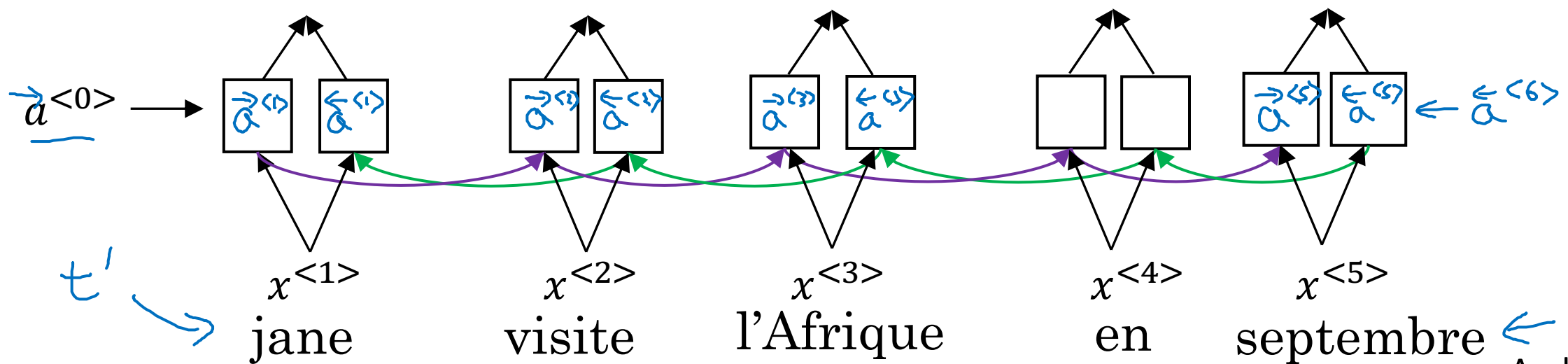


$$c^{(2)} = \sum_{t'} \alpha^{(2,t')} a^{(t')}$$

$$a^{(t')} = (\vec{a}^{(t')}, \leftarrow a^{(t')})$$

$$\sum_{t'} \alpha^{(1,t')} = 1$$

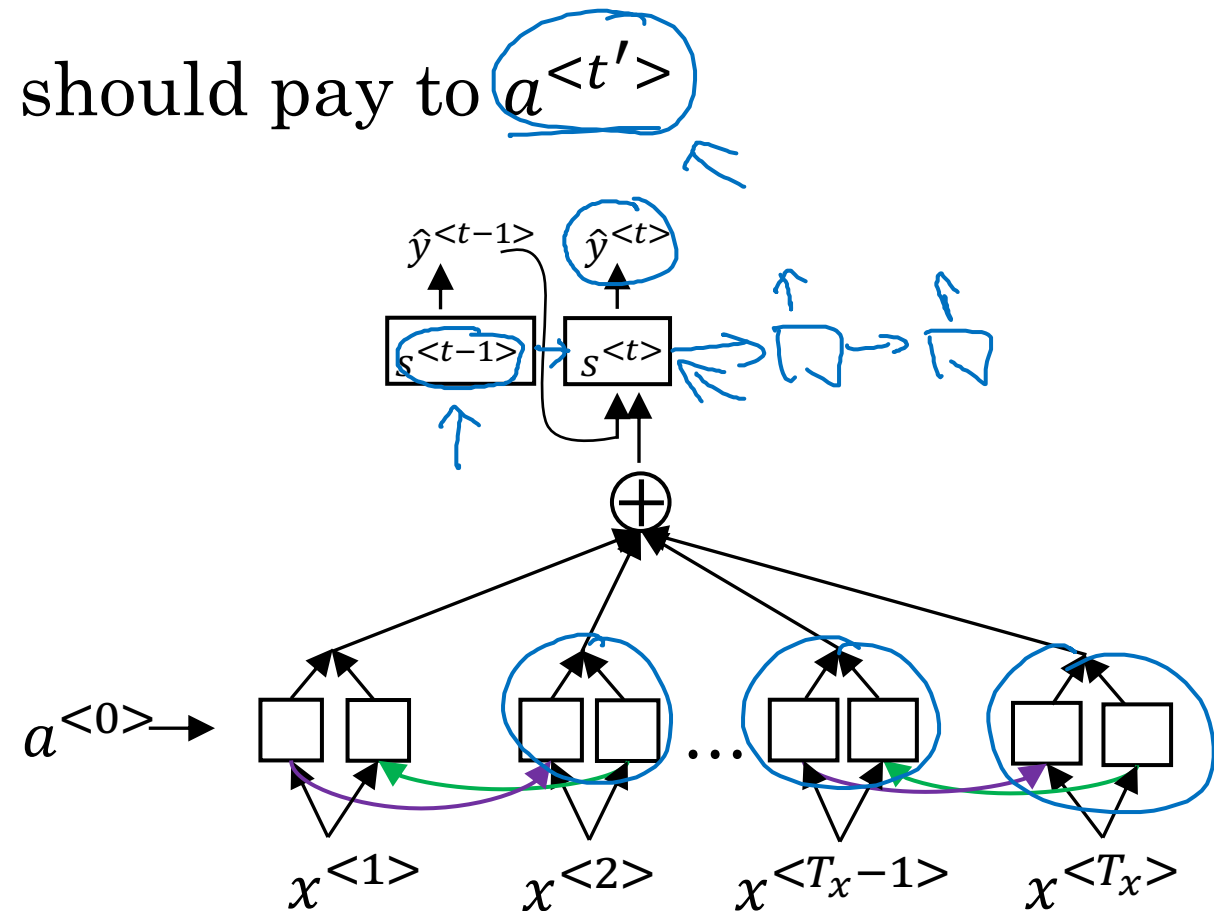
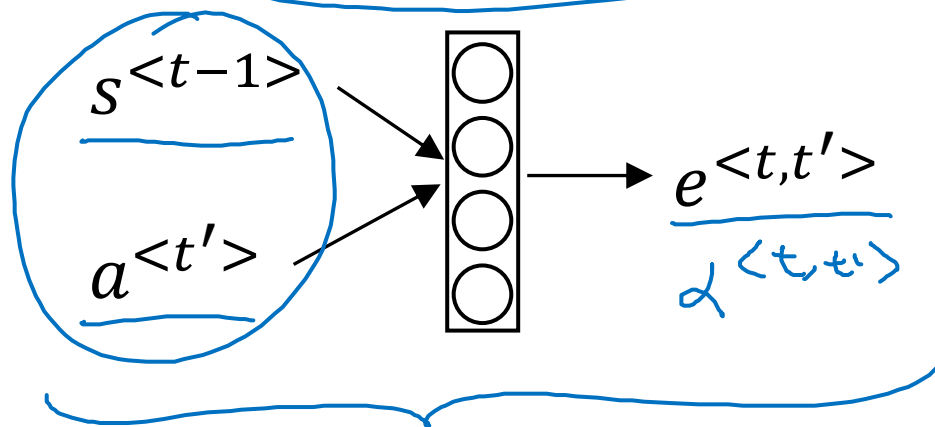
$$c^{(1)} = \sum_{t'} \alpha^{(1,t')} a^{(t')}$$



# Computing attention $\alpha^{<t,t'>}$

$\alpha^{<t,t'>}$  = amount of attention  $y^{<t>}$  should pay to  $a^{<t'>}$

$$\alpha^{<t,t'>} = \frac{\exp(e^{<t,t'>})}{\sum_{t'=1}^{T_x} \exp(e^{<t,t'>})}$$



[Bahdanau et. al., 2014. Neural machine translation by jointly learning to align and translate]

[Xu et. al., 2015. Show, attend and tell: Neural image caption generation with visual attention]

Andrew Ng

# Attention examples

July 20th 1969 → 1969 – 07 – 20

23 April, 1564 → 1564 – 04 – 23

Visualization of  $\alpha^{<t,t'>}$ :

