

(ME 543)
COMPUTATIONAL FLUID DYNAMICS

Assignment - 2

Submitted by :

SIVA NAVEEN GURRAM

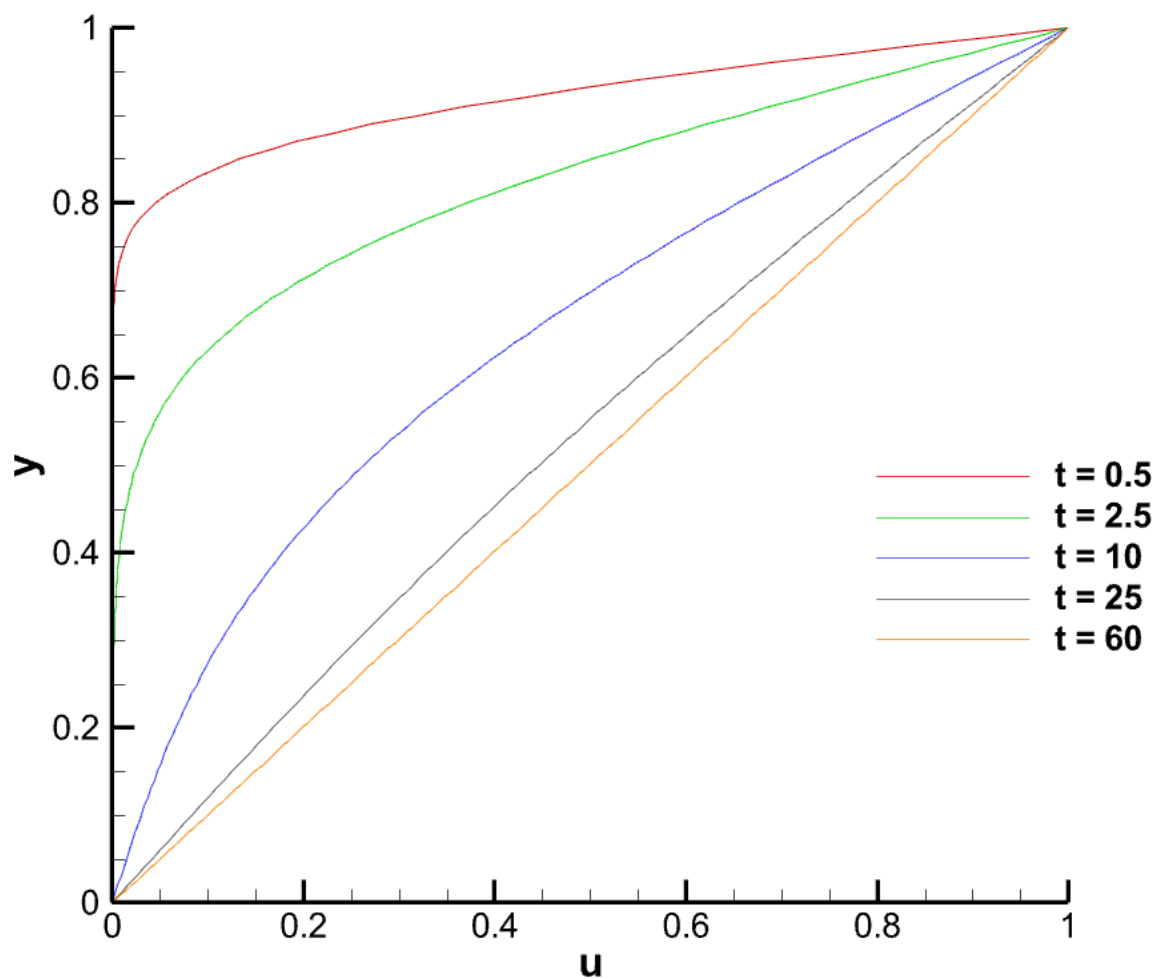
(Roll No: **224103108**)

COMPUTATIONAL MECHANICS

Problem - 1

1. Explicit method : FTCS

$$\phi_i^{n+1} = \gamma_x \phi_{i+1}^n + (1 - 2\gamma_x) \phi_i^n + \gamma_x \phi_{i-1}^n$$



- Number of time iterations to converge up to $\epsilon < 10^{-6}$ = **11641**
- Physical time taken to converge up to $\epsilon < 10^{-6}$ = **58.205**

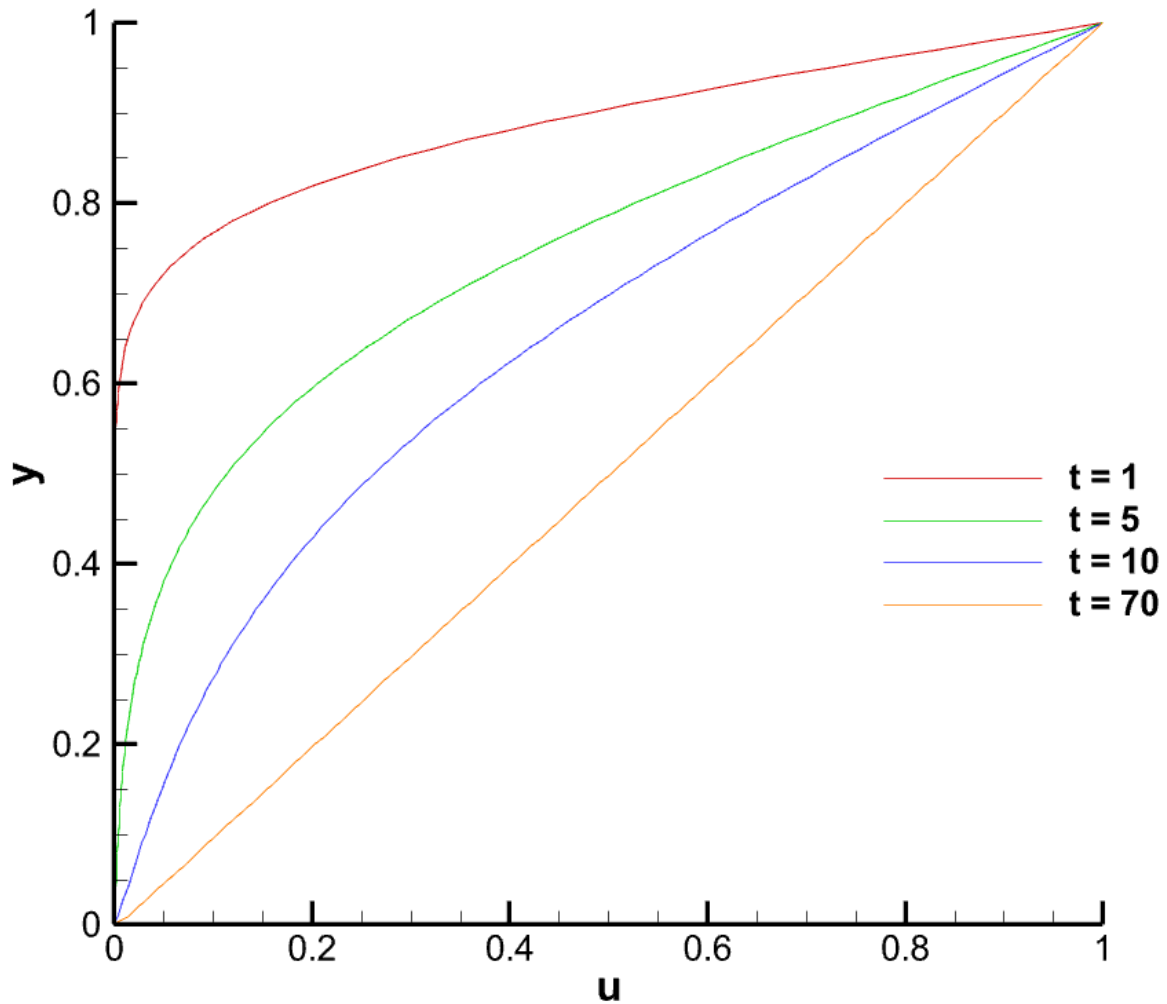
Time (t)	No. of iterations
0.5	100
2.5	500
10	2000
25	5000
60	12000

Problem - 2

2. Implicit method : **BTCS**

Line Gauss-Seidel iterative method (*TriDiagonal Matrix Algorithm*)

$$\gamma_x \phi_{i-1}^{n+1} - (1 + 2\gamma_x) \phi_i^{n+1} + \gamma_x \phi_{i+1}^{n+1} = -\phi_i^n$$



- Number of time iterations to converge up to $\epsilon < 10^{-6} = 6230$
- Physical time taken to converge up to $\epsilon < 10^{-6} = 62.29$

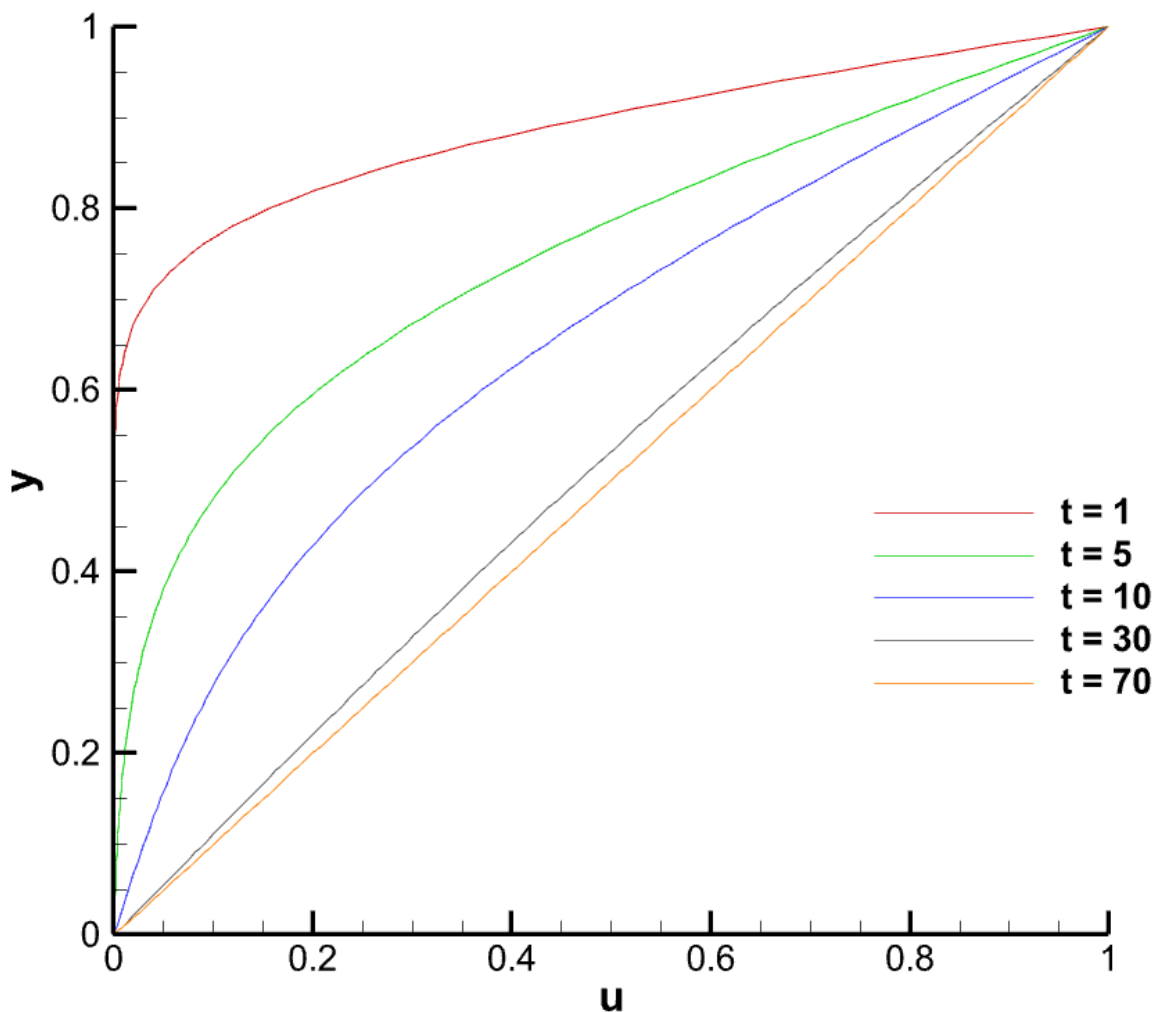
Time (t)	No. of iterations
1	100
5	500
10	1000
70	7000

Problem - 2

2. Implicit method : **Crank-Nicolson**

Line Gauss-Seidel iterative method (***TriDiagonal Matrix Algorithm***)

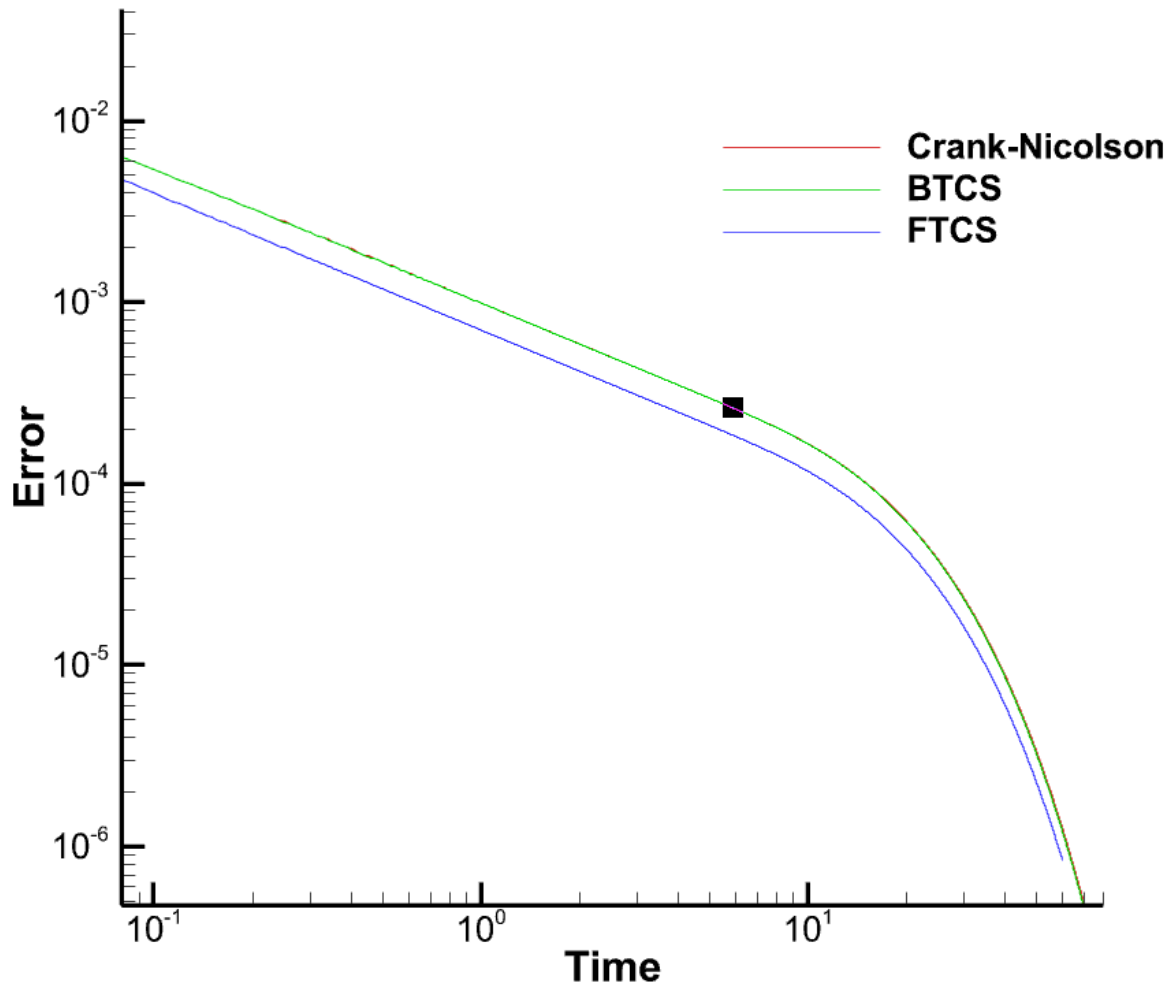
$$\frac{\phi_i^{n+1} - \phi_i^n}{\Delta t} = \frac{\Gamma}{2} \left[\frac{\phi_{i+1}^{n+1} - 2\phi_i^{n+1} + \phi_{i-1}^{n+1}}{(\Delta x)^2} + \frac{\phi_{i+1}^n - 2\phi_i^n + \phi_{i-1}^n}{(\Delta x)^2} \right]$$



- Number of time iterations to converge up to $\epsilon < 10^{-6}$ = **6189**
- Physical time taken to converge up to $\epsilon < 10^{-6}$ = **61.88**

Time (t)	No. of iterations
1	100
5	500
10	1000
70	7000

Error Vs Time



Error vs Time plot on log-log scale