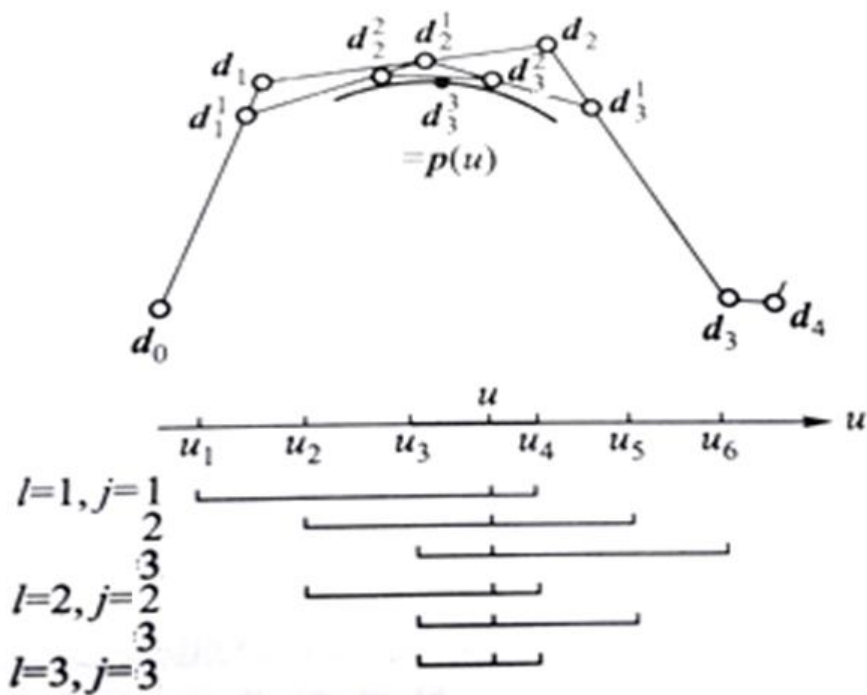


de Boor 算法示例：求三次 B 样条曲线上点  $p(u), u \in (u_3, u_4)$ 。

解：不妨假设  $u_i = i, u = 3.5$ 。利用 DeBoor 算法，求出各层顶点。



一、 $l=1$

$$1) \quad j=1: d_0^1 = \frac{u_4 - u}{u_4 - u_1} d_0 + \frac{u - u_1}{u_4 - u_1} d_1 = \frac{4 - 3.5}{3} d_0 + \frac{3.5 - 1}{3} d_1 = \frac{1}{6} d_0 + \frac{5}{6} d_1$$

$$2) \quad j=2: d_1^1 = \frac{u_5 - u}{u_5 - u_2} d_1 + \frac{u - u_2}{u_5 - u_2} d_2 = \frac{5 - 3.5}{3} d_1 + \frac{3.5 - 2}{3} d_2 = \frac{1}{2} d_1 + \frac{1}{2} d_2$$

$$2) \quad j=3: d_2^1 = \frac{u_6 - u}{u_6 - u_3} d_2 + \frac{u - u_3}{u_6 - u_3} d_3 = \frac{6 - 3.5}{3} d_2 + \frac{3.5 - 3}{3} d_3 = \frac{5}{6} d_2 + \frac{1}{6} d_3$$

二、 $l=2$

$$1) \quad j=2: d_2^2 = \frac{u_4 - u}{u_4 - u_2} d_1^1 + \frac{u - u_2}{u_4 - u_2} d_2^1 = \frac{4 - 3.5}{2} d_1^1 + \frac{3.5 - 2}{2} d_2^1 = \frac{1}{4} d_1^1 + \frac{3}{4} d_2^1$$

$$2) \quad j=3: d_3^2 = \frac{u_5 - u}{u_5 - u_3} d_2^1 + \frac{u - u_3}{u_5 - u_3} d_3^1 = \frac{5 - 3.5}{2} d_2^1 + \frac{3.5 - 3}{2} d_3^1 = \frac{3}{4} d_2^1 + \frac{1}{4} d_3^1$$

三、 $l=3$

$$1) \quad j=3: d_3^3 = \frac{u_4 - u}{u_4 - u_3} d_2^2 + \frac{u - u_3}{u_4 - u_3} d_3^2 = \frac{4 - 3.5}{1} d_2^2 + \frac{3.5 - 3}{1} d_3^2 = \frac{1}{2} d_2^2 + \frac{1}{2} d_3^2$$