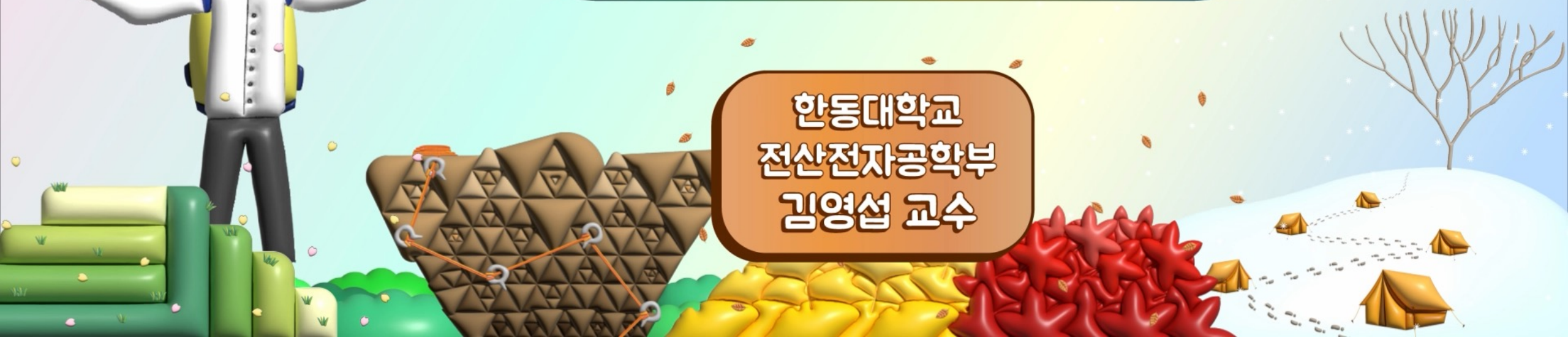


파이썬으로 배우는 데이터 구조



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학습 목표

퀵(Quick) 정렬의 알고리즘을
이해하고 구현할 수 있다

Data Structures in Python

Chapter 5 - 2

- Merge sort
- **Quick sort Algorithm**
- Quick sort Analysis
- Empirical Analysis

Agenda & Readings

- Agenda
 - Quick sort algorithm
 - $n \log(n)$ algorithm,
 - Divide and conquer algorithm
- Reference:
 - Problem Solving with Algorithms and Data Structures
 - Chapter 5 Search, Sorting and Hashing: [Quick sort](#)
 - Wikipedia [Quick sort](#)
 - [\[알고리즘\] 퀵정렬](#)

Quick sort

- Quick sort invented by British computer scientist C.A.R. Hoare in 1960
- Quick sort is another divide and conquer algorithm.
- Time complexity is $O(n \log n)$ average, $O(n^2)$ worst case, faster than merge sort in general.

Quick sort - Algorithm

- Choose a pivot element from the array. Although we can choose any element in the array as a pivot, it's easy to implement if we choose the rightmost element of the subarray.

index	0	1	2	3	4	5	6	7	8	9
value	32	23	81	43	92	39	57	16	75	65

pivot

- Partition or reorder the array so that all values smaller than the pivot are moved before it and all values larger (or equal) than the pivot are moved after it.

32	23	43	39	57	16	92	81	75	65
----	----	----	----	----	----	----	----	----	----

pivot

- When this is done, the pivot is in its final position.

32	23	43	39	57	16	65	81	75	92
----	----	----	----	----	----	----	----	----	----

sorted

- Conquer by repeating steps above for the left side and right side of the pivot recursively, except the pivot itself since it is sorted and positioned at the right place,

Quick sort - Partition

- Choose a pivot element and partition the array in place such that all elements to the left of the pivot element are smaller, while all elements to the right are greater than the pivot.

index	0	1	2	3	4	5	6	7	8	9
value	32	23	81	43	92	39	57	16	75	65
j=lo i=lo-1	j=0 i=0	j=1 i=1	j=2 i=1	j=3 i=2	j=4 i=2	j=5 i=3	j=6 i=4	j=7 i=5	j=8 i=5	pivot

while j traverses from **low** to **hi-1**
i increments only when **a[j] < pivot**

```
def partition(a, lo, hi):  
    pivot = a[hi]  
    i = lo - 1;  
    j = lo  
    while j <= hi - 1: scan  
        if a[j] < pivot:  
            i += 1  
            if i != j: swap  
                a[j], a[i] = a[i], a[j]  
            j += 1  
    a[hi], a[i+1] = a[i+1], a[hi] sorted  
    return i + 1
```

Quick sort - Partition

- Choose a pivot element and partition the array in place such that all elements to the left of the pivot element are smaller, while all elements to the right are greater than the pivot.

index	0	1	2	3	4	5	6	7	8	9
value	32	23	81	43	92	39	57	16	75	65
j=lo i=lo-1	j=0 i=0	j=1 i=1	j=2 i=1	j=3 i=2	j=4 i=2	j=5 i=3	j=6 i=4	j=7 i=5	j=8	pivot
				swap		swap	swap	swap		

Now, find elements to swap.

while j traverses from **low** to **hi-1**
i increments only when **a[j] < pivot**

```
def partition(a, lo, hi):  
    pivot = a[hi]  
    i = lo - 1;  
    j = lo  
    while j <= hi - 1: scan  
        if a[j] < pivot:  
            i += 1  
            if i != j: swap  
                a[j], a[i] = a[i], a[j]  
        j += 1  
    a[hi], a[i+1] = a[i+1], a[hi] sorted  
    return i + 1
```


Quick sort - Partition

- Choose a pivot element and partition the array in place such that all elements to the left of the pivot element are smaller, while all elements to the right are greater than the pivot.

index	0	1	2	3	4	5	6	7	8	9
value	32	23	81	43	92	39	57	16	75	65

j=lo	j=0	j=1	j=2	j=3	j=4	j=5	j=6	j=7	j=8	pivot
i=lo-1	i=0	i=1	i=1	i=2	i=2	i=3	i=4	i=5	i=5	
				swap		swap	swap	swap		

swap(2,3)

32	23	43	81	92	39	57	16	75	65
----	----	----	----	----	----	----	----	----	----

swap(3,5)

32	23	43	39	92	81	57	16	75	65
----	----	----	----	----	----	----	----	----	----

swap(4,6)

32	23	43	39	57	81	92	16	75	65
----	----	----	----	----	----	----	----	----	----

swap(5,7)

32	23	43	39	57	16	92	81	75	65
----	----	----	----	----	----	----	----	----	----

↑

not sorted

while j traverses from low to hi-1

i increments only when a[j] < pivot

```
def partition(a, lo, hi):
    pivot = a[hi]
    i = lo - 1;
    j = lo
    while j <= hi - 1:
        if a[j] < pivot:
            i += 1
            if i != j:
                a[j], a[i] = a[i], a[j]
            j += 1
    a[hi], a[i+1] = a[i+1], a[hi]
    return i + 1
```

Quick sort - Partition

- Choose a pivot element and partition the array in place such that all elements to the left of the pivot element are smaller, while all elements to the right are greater than the pivot.

index	0	1	2	3	4	5	6	7	8	9
value	32	23	81	43	92	39	57	16	75	65

j=lo	j=0	j=1	j=2	j=3	j=4	j=5	j=6	j=7	j=8	pivot
i=lo-1	i=0	i=1	i=1	i=2	i=2	i=3	i=4	i=5	i=5	
				swap		swap	swap	swap		

swap(2,3)	32	23	43	81	92	39	57	16	75	65
-----------	----	----	----	----	----	----	----	----	----	----

swap(3,5)	32	23	43	39	92	81	57	16	75	65
-----------	----	----	----	----	----	----	----	----	----	----

swap(4,6)	32	23	43	39	57	81	92	16	75	65
-----------	----	----	----	----	----	----	----	----	----	----

swap(5,7)	32	23	43	39	57	16	92	81	75	65
-----------	----	----	----	----	----	----	----	----	----	----

swap(6,9)	32	23	43	39	57	16	65	81	75	92
swap(i+1,hi)										

while j traverses from low to hi-1
i increments only when a[j] < pivot

```
def partition(a, lo, hi):  
    pivot = a[hi]  
    i = lo - 1;  
    j = lo  
    while j <= hi - 1: scan  
        if a[j] < pivot:  
            i += 1  
            if i != j: swap  
                a[j], a[i] = a[i], a[j]  
            j += 1  
    a[hi], a[i+1] = a[i+1], a[hi] sorted  
    return i + 1
```

recursively sort left a[] ≤ pivot sorted a[] ≥ pivot sort right

Quick sort - Partition

Repeat this process recursively:

index	0	1	2	3	4	5	6	7	8	9
value	32	23	43	39	57	16	65	81	75	92

sort left $a[] \leq \text{pivot}$ sorted $a[] \geq \text{pivot}$ sort right

partition

32	23	43	39	57	16
----	----	----	----	----	----

j=lo

i=lo-1

j=0	j=1	j=2	j=3	j=4	pivot
i=-1	i=-1	i=-1	i=-1	i=-1	

swap(0,5)

swap(i+1,hi)

16	23	43	39	57	32
----	----	----	----	----	----

sorted

sort right

partition

23	43	39	57	32
----	----	----	----	----

j=lo

i=lo-1

j=1	j=2	j=3	j=4	pivot
i=1	i=1	i=1	i=1	

swap(2,5)

swap(i+1,hi)

23	32	39	57	43
----	----	----	----	----

sorted

sort right

23

partition

39	57	43
----	----	----

j=lo

i=lo-1

j=3	j=4	pivot
i=3	i=3	

swap(4,5)

swap(i+1,hi)

39	43	57
----	----	----

sorted

39

57

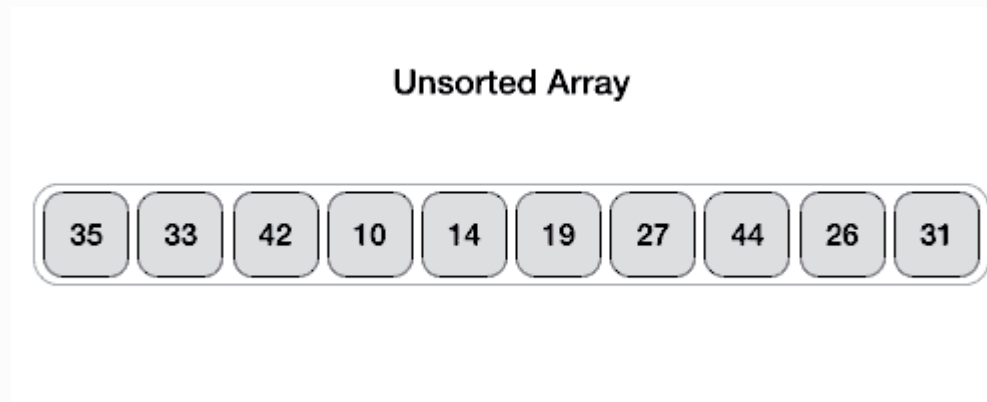
partition

81	75	92
----	----	----

The rest of this part is left as an exercise.

Summary

- Quick sort is one of the most efficient sorting algorithms.
- It is based on the splitting of an array (**partition**) into smaller ones and rearrange based on the comparison with '**pivot**' element selected.
- Like merge sort, quick sort also falls into the category of **divide and conquer** approach of problem-solving methodology.



학습 정리

- 1) 퀵 정렬은 가장 효과적인 정렬 알고리즘 중 하나이다
- 2) 퀵 정렬의 핵심은 피벗(pivot)으로 설정된 요소를 중심으로 배열을 구분(partition)하여 재귀함수를 적용한다
- 3) 병합 정렬과 퀵 정렬은 분할 정복법(divide and conquer)을 사용하는 알고리즘이다

파이썬으로 배우는 데이터 구조

수고했습니다
곧 다음 시간에
다시 뵙겠습니다

