### **CS2030S Recitation Problem Set 8**

#### **Functor Laws**

A functor is a *structure* with at least 2 methods (of, map) obeying two laws:

- 1. Identity Morphism (basically mapping identity fn gives you the same functor)
  - $\circ \ orall ext{functor: functor.map}(x 
    ightarrow x) \ \equiv ext{functor}$
- 2. Composition morphism (any 2 maps is the same as 1 map with applying both function)
  - $egin{aligned} &\circ \; orall ext{functor}, f,g: ext{functor.map}(x 
    ightarrow f(x)). ext{map}(y 
    ightarrow g(y)) \ &\equiv ext{functor}, f,g: ext{functor.map}(x 
    ightarrow g(f(x))) \end{aligned}$

#### Monad Laws

A monad is a *structure* with at least two methods (of, flatMap) obeying three laws:

- 1. Left Identity Law
  - $x \circ \forall x, f : \mathrm{Monad.of}(x).\mathrm{flatMap}(y o \mathrm{f(y)}) \equiv f(x)$
- 2. Right Identity Law
  - $\circ \ \, orall \mathrm{monad.flatMap}(x 
    ightarrow \mathrm{Monad.of}(x)) \equiv \mathrm{monad}(x)$
- 3. Associative Law
  - $egin{aligned} &\circ \ orall \mathrm{monad}, f,g: \mathrm{monad}.\mathrm{flatMap}(x 
    ightarrow f(x)).\mathrm{flatMap}(y 
    ightarrow g(y)) \ &\equiv \mathrm{monad}.\mathrm{flatMap}(x 
    ightarrow f(x).\mathrm{flatMap}(y 
    ightarrow g(y))) \end{aligned}$

#### Question 1a

Complete the implementation of map using only flatMap so that the resulting Monad<T> satisfies the functor laws.

Need the identity and composition morphisms.

```
public <R> Monad<R> map(Transformer<? super T, ? extends R> f) {
   return this.flatMap(XXX); // Need to satisfy Functor laws
}
```

#### **Question 1a**

```
public <R> Monad<R> map(Transformer<? super T, ? extends R> f) {
   return this.flatMap(XXX); // Need to satisfy Functor laws
}
```

- ullet Notice that f:T o R
- What type should XXX be?
  - $\circ XXX: T \rightarrow Monad < R > 0$
  - $\circ$  How can I use f to produce XXX?
  - $\circ$  XXX = x -> Monad.of(f.transform(x))
  - $\circ$  Remember f.transform(x)  $\equiv$  f(x)

### **Question 1b**

Prove that composition is preserved.

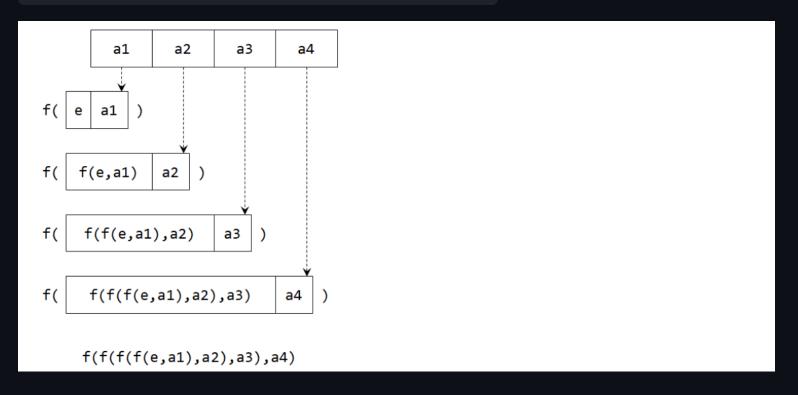
- A: m.map(x -> f(x)).map(x -> g(x)) = m.flatMap(x -> Monad.of(f(x))).flatMap(x -> Monad.of(g(x)))
   by implementation
- B:  $\equiv$  m.flatMap(x -> Monad.of(f(x)).flatMap(x -> Monad.of(g(x)))) by associative law.
- C: 
   = m.flatMap(x → Monad.of(g(f(x))))
   by left identity law.

## Sequential, Concurrent, and Parallel

- Sequential
  - Do things in order on one thread
- Concurrent
  - Do things in order one at a time but over different threads
- Parallel
  - Actually doing things at the same time

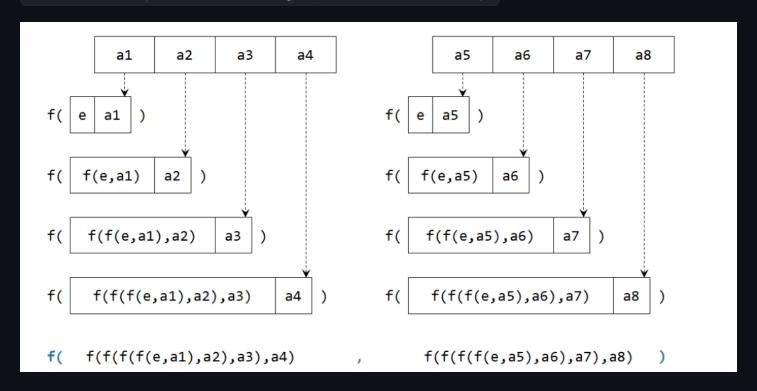
# **Reduce Sequential**

T reduce(T e, BinaryOperator<T> f)



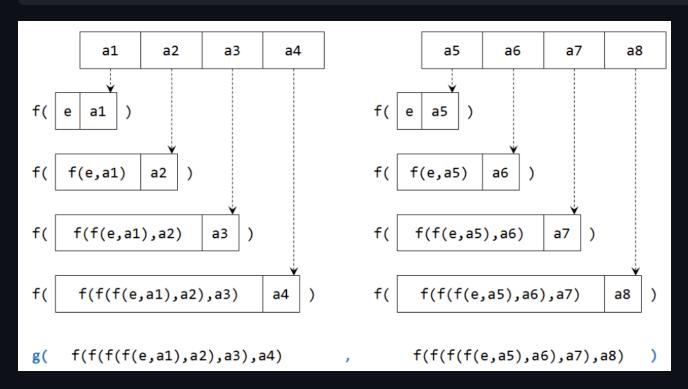
### Reduce Parallel

T reduce(T e, BinaryOperator<T> f)



### Reduce Parallel

<U> U reduce(U e, BiFunction<U,? super T,U> f, BinaryOperator<U> g)



#### Question 2a and 2b

What is the return value?

```
Stream.of(1, 2, 3, 4)
    .reduce(0, (a, x) -> (2 * a) + x, (a1, a2) -> a1 + a2);

Stream.of(1, 2, 3, 4)
    .parallel()
    .reduce(0, (a, x) -> (2 * a) + x, (a1, a2) -> a1 + a2);
```

Explain why there are differences

#### Reason

The accumulator is not associative

- ullet If associative, f(f(a,b),c)=f(a,f(b,c))
- Future Brian will show you on the white board why it's not.
- This causes combiner and accumulator to not be compatible
- Future Brian shows again

#### Side note

- It is **NOT** necessary for accumulator to be associative
- Parallel reduce will be split first into list of blocks.
- Each block will run in a sequential order, so the accumulator will be ran in a specific order
- So it is more of a sufficient condition rather than a necessary one

## Write estimatePi using Stream

- Whether a point is inside the circle or not is independent of each other
- Therefore can be parallelised
- Create a stream of random points
- Limit at numOfPoints
- Filter if they are in the circle
- Count

### **Evalutation**

- Does parallelisation speed it up?
  - Show code
  - Overhead of creating new threads

## Why is the number different each time

- Each thread has access to the random seed
- The order which the threads interleave is random
- when limit happens, the threads may have produced more than necessary elements and would be chopped off
- So what's left is a stream that can have different random points each run due to the randomness