

INFO 6205-PROGRAM STRUCTURE AND ALGORITHMS ASSIGNMENT-1

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Task:

The programmer is expected to solve the 3-sum problem using the Quadratic, Quadarithmic and Quadtratic with Calipers approaches. Testing the code by running unit tests and benchmark the time taken for each algorithm to execute successfully, using the double benchmark approach. Analyzing the behaviour and performance of different time-complexity approaches is required.

Test Case Runs:

The screenshot shows an IDE with a Java project named 'INFO6205'. The main code file is 'ThreeSumTest.java', which contains a class 'ThreeSum' with methods 'getTriples()' and 'getTriplesC0()'. The 'getTriples()' method uses a quadratic approach, and 'getTriplesC0()' uses a cubic approach. The test results pane shows that 11 tests passed in 5 seconds and 221 milliseconds. The test results are as follows:

Test Case	Time (ms)	Output
testGetTriples0	37	ints: [-40, -20, -10, 0, 5, 10, 30, 40]
testGetTriples1	10	triples: [Triple{x=-40, y=0, z=40}, Triple{x=-40, y=10, z=30}, Triple{x=-40, y=5, z=45}, Triple{x=-20, y=0, z=40}, Triple{x=-20, y=10, z=30}, Triple{x=-20, y=5, z=45}, Triple{x=-10, y=0, z=40}, Triple{x=-10, y=10, z=30}, Triple{x=-10, y=5, z=45}, Triple{x=0, y=0, z=40}, Triple{x=0, y=10, z=30}, Triple{x=0, y=5, z=45}, Triple{x=5, y=0, z=40}, Triple{x=5, y=10, z=30}, Triple{x=5, y=5, z=45}, Triple{x=10, y=0, z=40}, Triple{x=10, y=10, z=30}, Triple{x=10, y=5, z=45}, Triple{x=30, y=0, z=40}, Triple{x=30, y=10, z=30}, Triple{x=30, y=5, z=45}]
testGetTriples2	1	triples: [Triple{x=-51, y=2, z=49}, Triple{x=-51, y=9, z=42}, Triple{x=-44, y=2, z=49}, Triple{x=-44, y=9, z=42}, Triple{x=-44, y=5, z=45}, Triple{x=-44, y=12, z=39}, Triple{x=-44, y=24, z=24}]
testGetTriplesC0	1	ints: [-40, -20, -10, 0, 5, 10, 30, 40]
testGetTriplesC1	3	triples: [Triple{x=-40, y=0, z=40}, Triple{x=-40, y=10, z=30}, Triple{x=-40, y=5, z=45}, Triple{x=-20, y=0, z=40}, Triple{x=-20, y=10, z=30}, Triple{x=-20, y=5, z=45}, Triple{x=-10, y=0, z=40}, Triple{x=-10, y=10, z=30}, Triple{x=-10, y=5, z=45}, Triple{x=0, y=0, z=40}, Triple{x=0, y=10, z=30}, Triple{x=0, y=5, z=45}, Triple{x=5, y=0, z=40}, Triple{x=5, y=10, z=30}, Triple{x=5, y=5, z=45}, Triple{x=10, y=0, z=40}, Triple{x=10, y=10, z=30}, Triple{x=10, y=5, z=45}, Triple{x=30, y=0, z=40}, Triple{x=30, y=10, z=30}, Triple{x=30, y=5, z=45}]
testGetTriplesC2	1	triples: [Triple{x=-51, y=2, z=49}, Triple{x=-51, y=9, z=42}, Triple{x=-44, y=2, z=49}, Triple{x=-44, y=9, z=42}, Triple{x=-44, y=5, z=45}, Triple{x=-44, y=12, z=39}, Triple{x=-44, y=24, z=24}]
testGetTriplesC3	1	ints: [-40, -20, -10, 0, 5, 10, 30, 40]
testGetTriplesC4	3	triples: [Triple{x=-40, y=0, z=40}, Triple{x=-40, y=10, z=30}, Triple{x=-40, y=5, z=45}, Triple{x=-20, y=0, z=40}, Triple{x=-20, y=10, z=30}, Triple{x=-20, y=5, z=45}, Triple{x=-10, y=0, z=40}, Triple{x=-10, y=10, z=30}, Triple{x=-10, y=5, z=45}, Triple{x=0, y=0, z=40}, Triple{x=0, y=10, z=30}, Triple{x=0, y=5, z=45}, Triple{x=5, y=0, z=40}, Triple{x=5, y=10, z=30}, Triple{x=5, y=5, z=45}, Triple{x=10, y=0, z=40}, Triple{x=10, y=10, z=30}, Triple{x=10, y=5, z=45}, Triple{x=30, y=0, z=40}, Triple{x=30, y=10, z=30}, Triple{x=30, y=5, z=45}]
testGetTriplesI0	0	ints: [-40, -20, -10, 0, 5, 10, 30, 40]
testGetTriplesI1	1	triples: [Triple{x=-51, y=2, z=49}, Triple{x=-51, y=9, z=42}, Triple{x=-44, y=2, z=49}, Triple{x=-44, y=9, z=42}, Triple{x=-44, y=5, z=45}, Triple{x=-44, y=12, z=39}, Triple{x=-44, y=24, z=24}]
testGetTriplesI2	0	ints: [-40, -20, -10, 0, 5, 10, 30, 40]

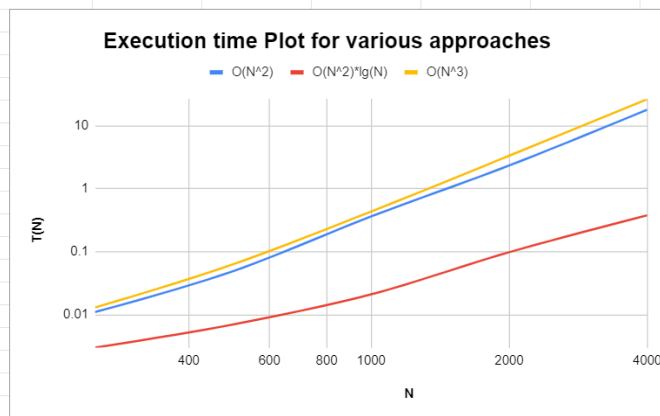
Benchmarking Results:

Tests for obtaining the execution time have been carried out for the three approaches. The input array size has been doubled for every successive three-algorithm test run. In case of the cubic complexity algorithm, a limit on the permissible input size is set to avoid long execution times.

The timing is performed by using the Stopwatch class present in the repository.

Execution times of Quadratic, Quadrithmic and Cubic approaches to 3-sum, for different inputs

N	$O(N^2)$	$O(N^2) \cdot \lg(N)$	$O(N^3)$
250	0.011	0.003	0.013
500	0.049	0.007	0.063
1000	0.362	0.021	0.433
2000	2.329	0.098	3.326
4000	17.874	0.378	26.267



Note: Execution time calculated in seconds.

More on the Quadratic Approach:

In the quadratic approaches, solutions are arrived at by sequentially deriving the solution spaces pertaining to an input array. The sequence followed is by fixing an index in the triplet and finding the other two indices which satisfy the zero sum condition. As the arrays are sorted, depending on which index is fixed, searching can begin outwards in both directions from the fixed index. The middle element is fixed before the search operation in quadratic approach, whereas the first element is fixed in the quadratic with calipers approach. Both the approaches exhibit a time complexity of $O(N^2)$.