

**Homework 7**

1)

Def equivalent():

    A = set.init(1..n)

    For i in range(1,n):

        for j in range(i+1, len(A)):

            if A[j] == A[j-1]:

                set.Merge(A,j,j-1)

        Else:

            If( Find(A,j)%2 == 0 && Find(A, j-1)%2==0):

                Test1 = True

            Elif( Find(A,j)%2 != 0 && Find(A, j-1)%2 != 0):

                Test1 = True

            Else:

                Test1 = False

            If( Find(A,transitions[j,0])%2==0 && Find(A,transitions[j-1,0])%2==0):

                Test2 = True

            Elif( Find(A,transitions[j,0])%2!=0 && Find(A,transitions[j-1,0])%2!=0):

                Test2 = True

            Else:

                Test2 = False

            If( Find(A,transitions[j,1])%2==0 && Find(A,transitions[j-1,1])%2==0):

                Test3 = True

            Elif( Find(A,transitions[j,1])%2!=0 && Find(A,transitions[j-1,1])%2!=0):

                Test3 = True

            Else:

                Test3 = False

    If Test1 or (test2 and test 3):

        set.Merge(a,j,j-1)

return A

2)

If you take a graph with the base of  $m = 0$ , then you can take a single vertex and show that it has 0 edges with a degree of 0. This means that the  $\sum_{i=1..n}(d_i) = 2m$ , since  $2 * 0 = 0$

A similar assumption can be made when  $m = k$ . If we add one edge to the graph then we must connect it between two nodes. Each node will have their degree go up by one, increasing the total degree by 2. This would make the equation  $\sum_{i=1..n}(d_i) + 2 = 2(m+1)$ . By factoring and subtracting 2 on each side you get  $\sum_{i=1..n}(d_i) = 2k$ .

3)

The base case is a tree with a single vertex. This vertex has 0 in-degrees and 0 out-degrees. Which means the in-degrees and out-degrees are equal.

4)

	A	B	C	D	E	F
A		3		4		5
B			1			1
C				2		
D		3				
E				3		2
F				2		

