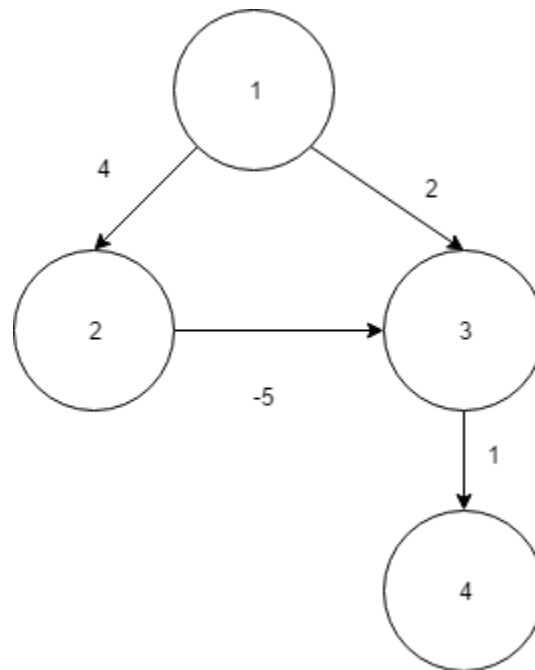


Homework 8

1)



Dijkstra's algorithm can start on Node 1, popping it off the priority queue. There are two places it can go which are $1 \rightarrow 2$ and $1 \rightarrow 3$, but it will go to 3 because it has a lower cost. So it will pop 3 off the priority queue and see $3 \rightarrow 4$, so it will pop 4 off the priority queue. Now it will go back to 2 since it will go back to the lowest remaining node, popping 2 off the priority queue. The distance to Node 3 will be updated -1. The algorithm will say that the shortest path from 1 to 4 is $1 \rightarrow 3 \rightarrow 4$ because Dijkstra's algorithm does not handle negative edge weights well.

2)

To insert the edge(i, j) into the adjacency list the algorithm will go to i and scan the adjacency list to see if j already exists there. If j exists then nothing will happen, if it does not then it will be appended to the list. The algorithm will then go to j and look for i , appending it if it doesn't exist. To delete edge(i, j) it's the same as inserting but with deleting.

3)

Delete(i, j, S)

For j in $\text{adj}[i]$

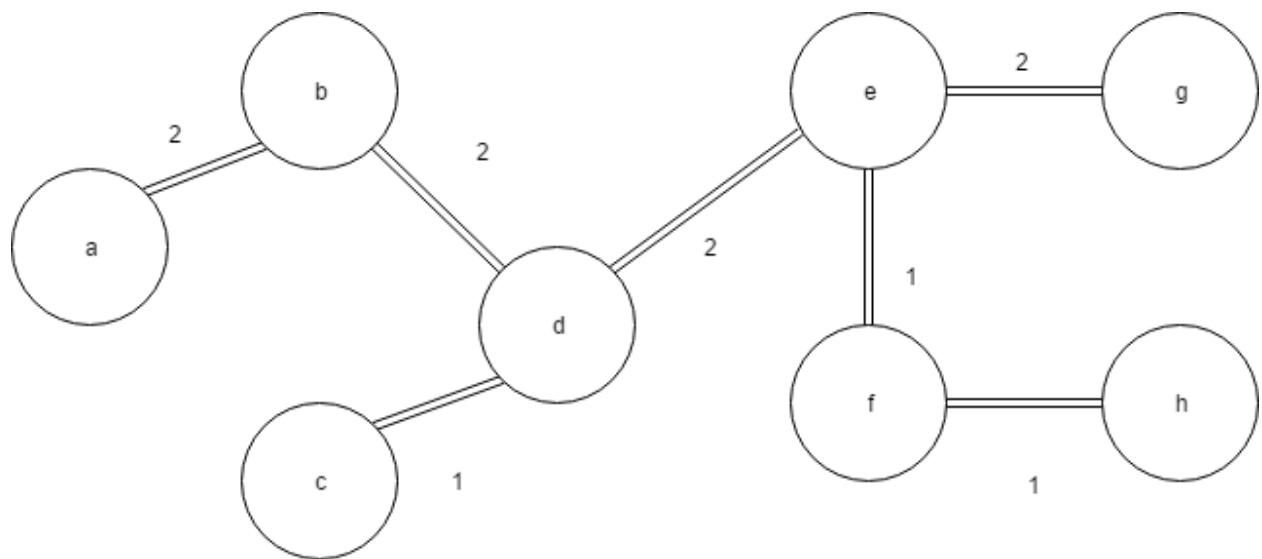
 Delete $j.\text{SharingEdge}$

 Delete j

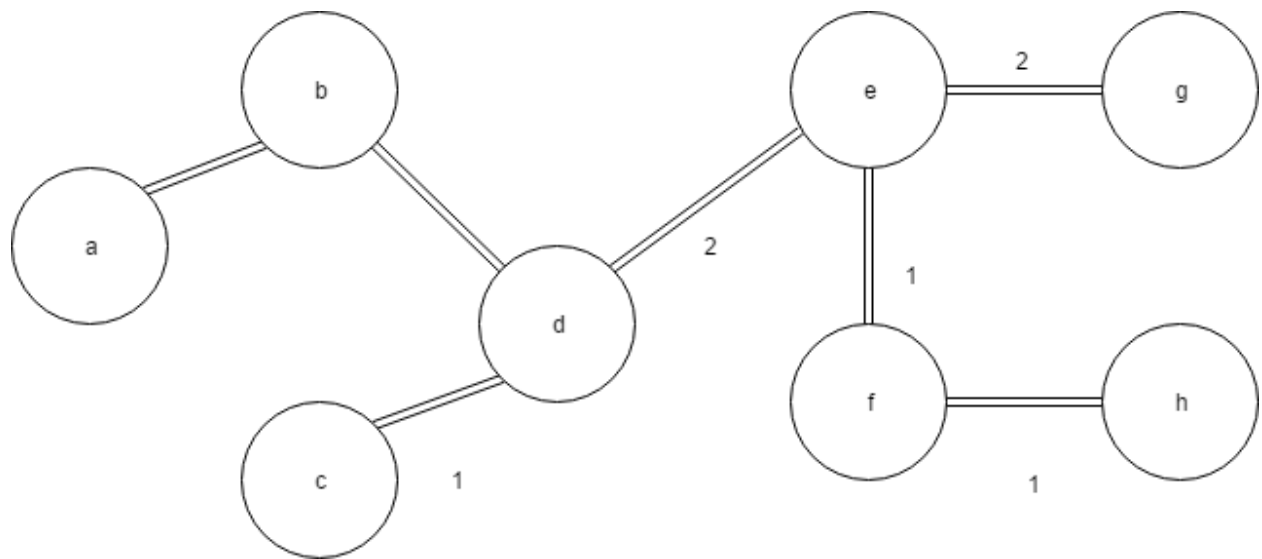
This will have a linear run time with the number of items in the adjacency matrix since we have to loop through it.

4)

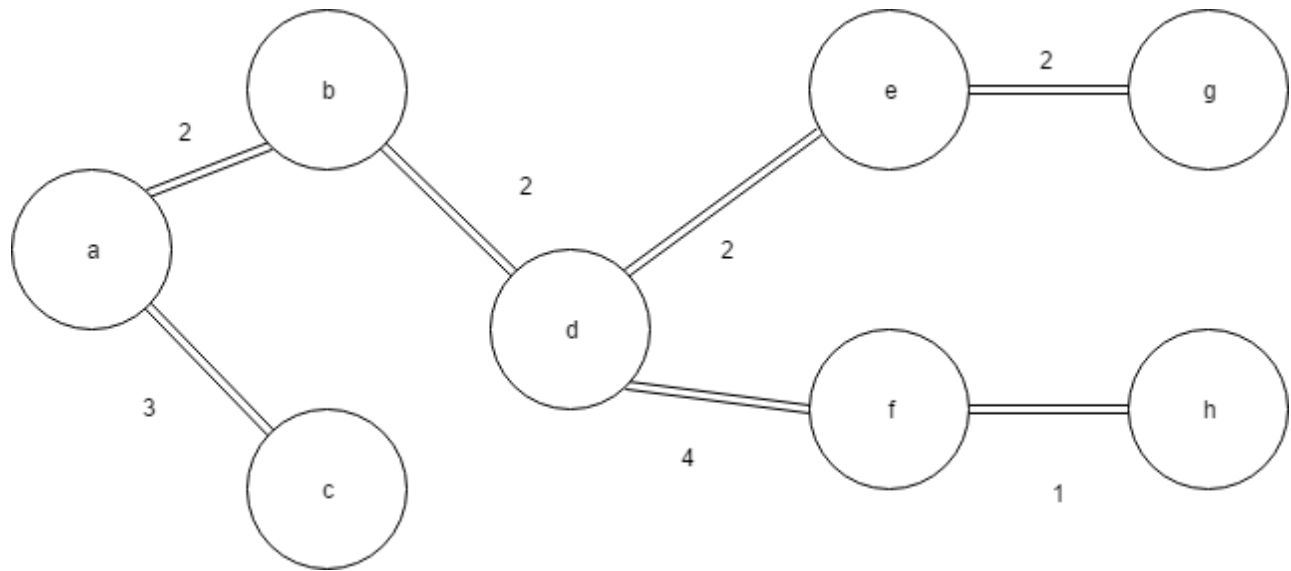
a)



b)



d) i)



ii)

