

Code without memoization

```
import sys

def fib(x):
    if x < 2:
        return 1
    else:
        return fib(x-1) + fib(x-2)

def main():
    x = int(sys.argv[1])
    y = fib(x)
    print y

if __name__ == '__main__':
    main()
```

Code with memorization

```
import sys

memo = {0:1, 1:1}

def fib_memo(x):
    if x not in memo:
        memo[x] = fib_memo(x-1) + fib_memo(x-2)
    return memo[x]

def main():
    x = int(sys.argv[1])
    y = fib_memo(x)
    print y
    memo = {0:1, 1:1}

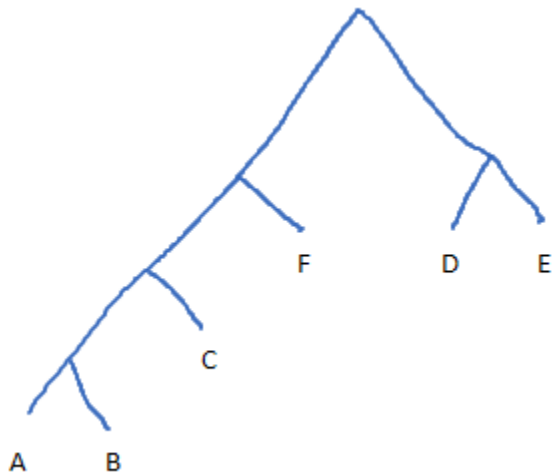
if __name__ == '__main__':
    main()
```

- 1) The code for the Fibonacci calculation is $O(2^n)$ since each calculation requires recursion with twice. The code with memorization will be $O(1)$ since it is accessing calculated results, but it will still need to run the Fibonacci calculation if the number had not been previously computed.
- 2) The running time would stay relatively the same for smaller array sizes, as the array size increases then there could be a point where the array is larger than the available memory.
- 3) Tree question
 - a. D, M, N, J, K, L
 - b. A
 - c. A
 - d. F, G, H
 - e. B, A
 - f. I, M, N
 - g. E is the right sibling of D, E does not have a right sibling
 - h. Left: C, A, B, D, E, I, M, N, F, J Right: K, H, L
 - i. 1
 - j. 1
- 4) 6: ABEI, ACGJ, ACGK, ACHL, BEIM, BEIN
- 5)

	Preorder(n) < Preorder(m)	Inorder(n) < Inorder(m)	Postorder(n) < Postorder(m)
N is to the left of M	Yes	Yes	Yes
N is to the right of M			
N is a proper ancestor of M	Yes	Yes	
N is a proper descendant of M			Yes

6) Huffman Code

Letter						Code	
A	.07					0000	
B	.09	.16				0001	
C	.12	.12	.28	.28		001	
D	.22	.22	.22			01	
E	.23	.23	.23	.45	.45	10	
F	.27	.27	.27	.27	.55	11	



$$(4 * .07) + (4 * .09) + (3 * .12) + (2 * .22) + (2 * .23) + (2 * .27) = 2.44 \text{ Avg. Code Length}$$

- 7) The depth of a node on a Huffman tree is directly correlated to the probability of that node compared to other nodes on the tree. On a Huffman tree if you are a sibling then your probability compared to your other sibling depends on your position. If you're on the left then you have a lower probability and vice versa. The nodes above you must have a higher probability than either you or your sibling or else they would have been chosen for either of your spots. This proves that if a node has a smaller depth than you then it must have a higher probability than you