Нейроинформатика. Лабораторная работа №3

Линейная нейронная сеть. Правило обучения Уидроу-Хоффа

Целью работы является исследование свойств многослойной нейронной сети прямого распространения и алгоритмов ее обучения, применение сети в задачах классификации и аппроксимации функции.

Выполнил Пивницкий Д.С. \ М8о-406Б-19

In [20]:
```
import matplotlib.pyplot as plt
import numpy as np
import keras
from keras import layers
import tensorflow as tf
import time
```

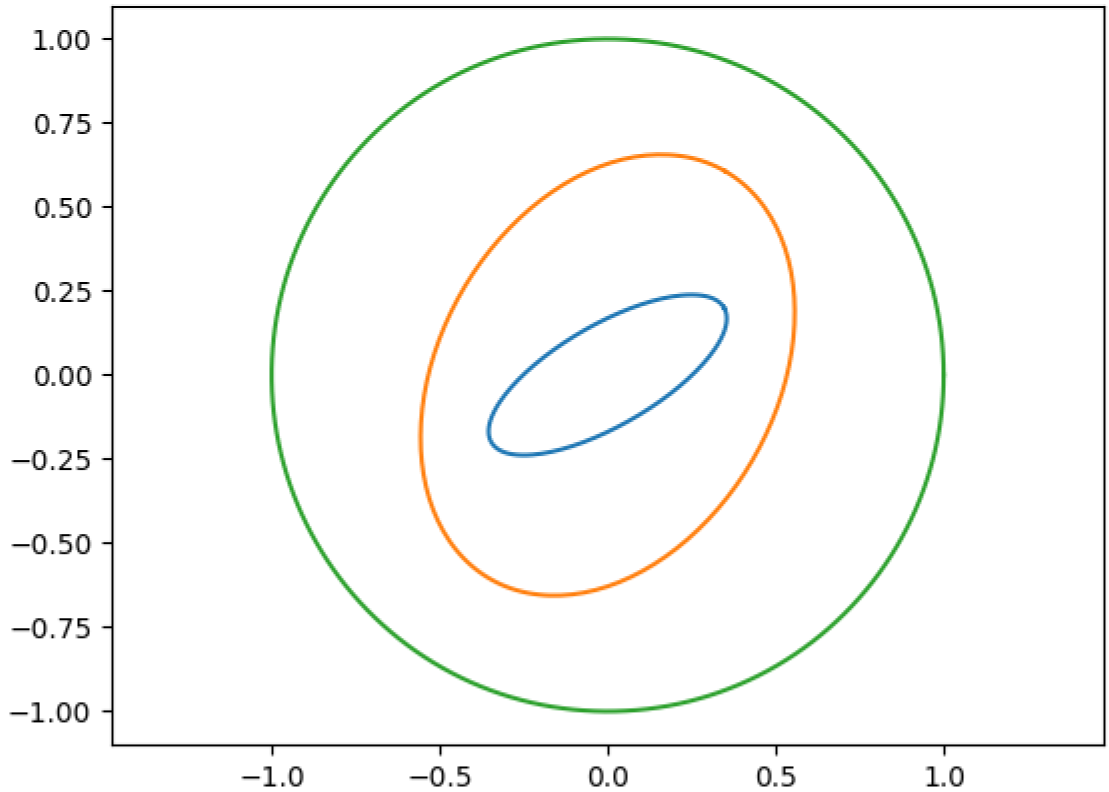
Классификация

In [5]:
```
def ellipse(t, a, b, x0, y0):
    x = x0 + a*np.cos(t)
    y = x0 + b*np.sin(t)
    return x, y


def rotate(x, y, alph):
    x_ans = x*np.cos(alph) - y*np.sin(alph)
    y_ans = x*np.sin(alph) + y*np.cos(alph)
    return x_ans, y_ans
```

In [6]:
```
t = np.linspace(0, 2*np.pi, 200)
x1, y1 = ellipse(t, 0.4, 0.15, 0, 0)
x1, y1 = rotate(x1, y1, np.pi / 6)

x2, y2 = ellipse(t, 0.7, 0.5, 0, 0)
x2, y2 = rotate(x2, y2, np.pi / 3)

x3, y3 = ellipse(t, 1, 1, 0, 0)
```

In [44]:
```
plt.plot(x1,y1)
plt.plot(x2,y2)
plt.plot(x3,y3)
plt.axis('equal')
```

Out[44]:
```
(-1.09986915899354, 1.0999937694758828, -1.099965731583572, 1.099965731583572)
```



Готовим датасет

In [12]:
```
data1 = [[cords, [1, 0, 0]] for cords in zip(x1, y1)]
data2 = [[cords, [0, 1, 0]] for cords in zip(x2, y2)]
data3 = [[cords, [0, 0, 1]] for cords in zip(x3, y3)]
dataset = data1 + data2 + data3
np.random.shuffle(dataset)
```

In [13]:
```
train_percent = 0.8
train_num = int(train_percent * len(dataset))
train_X = [x[0] for x in dataset[:train_num]]
train_y = [x[1] for x in dataset[:train_num]]
test_X = [x[0] for x in dataset[train_num:]]
test_y = [x[1] for x in dataset[train_num:]]
```

Создаем модель

In [23]:
```
predictor =  keras.Sequential([
        layers.Dense(100,input_dim=2, activation="tanh", name="tanh"),
        layers.Dense(3,activation='sigmoid', name="sigmoid")
    ]
)
predictor.summary()
```

```
Model: "sequential_3"
_________________________________________________________________
 Layer (type)                Output Shape              Param #
=================================================================
 tanh (Dense)                (None, 100)               300

 sigmoid (Dense)             (None, 3)                 303

=================================================================
Total params: 603
Trainable params: 603
Non-trainable params: 0
_________________________________________________________________
```

Компилируем модель

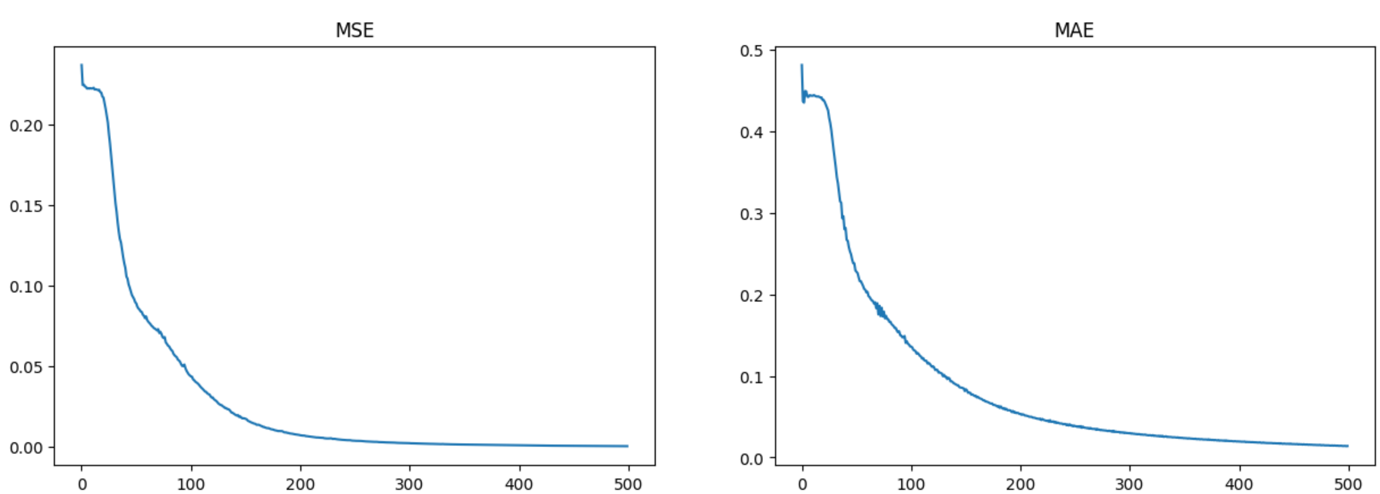
In [24]:
```
opt = keras.optimizers.Adam(learning_rate=0.01)
predictor.compile(loss='mse', optimizer=opt, metrics=['mae'])
```

Тренеруем модель

In [25]:
```
epochs = 500
time_start = time.time()
hist = predictor.fit(
    train_X,
    train_y,
    batch_size=len(dataset)//10,
    epochs=epochs,
    verbose=0,
    shuffle=True
    )
time_finish = time.time()
train_mse_loss, train_mae_loss = predictor.evaluate(train_X, train_y, verbose=0)
test_mse_loss, test_mae_loss = predictor.evaluate(test_X, test_y, verbose=0)

print(f'Fit time: {(time_finish - time_start):.{2}f}s')
print(f'Result train data MSE: {train_mse_loss}')
print(f'Result train data MAE: {train_mae_loss}')
print(f'Result test data MSE: {test_mse_loss}')
print(f'Result test data MAE: {test_mae_loss}')


fig, ax = plt.subplots(1, 2)
fig.set_figwidth(15)

ax[0].set_title('MSE')
ax[1].set_title('MAE')

ax[0].plot(range(epochs), hist.history['loss'])
ax[1].plot(range(epochs), hist.history['mae'])
```

```
Fit time: 11.24s
Result train data MSE: 0.0005530262715183198
Result train data MAE: 0.013956760987639427
Result test data MSE: 0.000679339689668268
Result test data MAE: 0.015304652974009514
```

Out[25]:
```
[<matplotlib.lines.Line2D at 0x7f61ac71c4f0>]
```



Создаем поле точек и скалярное поле

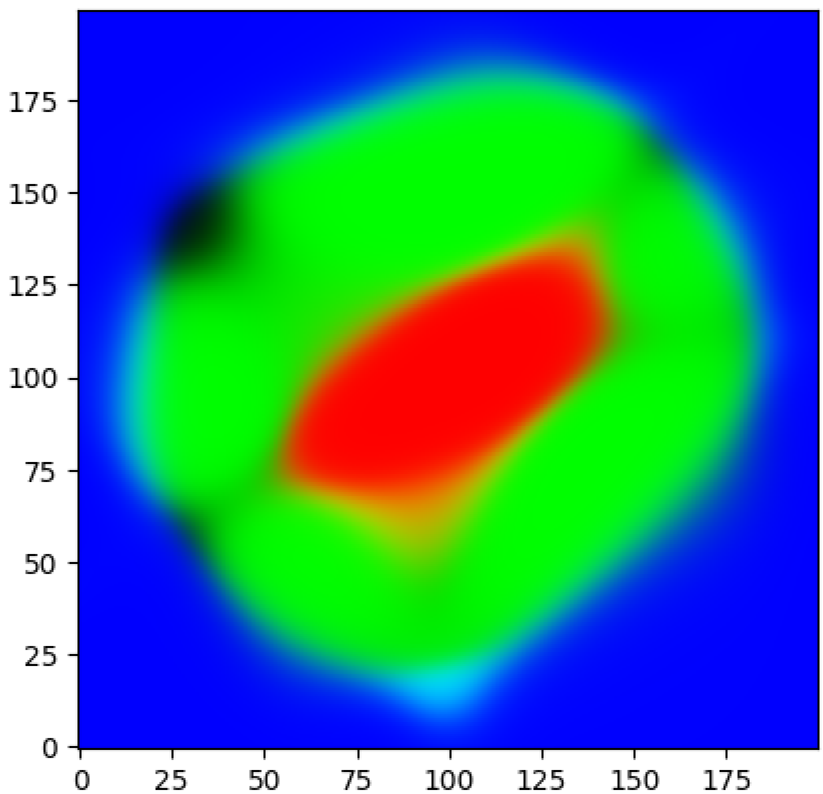
In [26]:
```
pole = []
```

```
for y in np.linspace(-1,1,200):
    for x in np.linspace(-1,1,200):
        pole.append((x,y))
```

In [27]:
```
pred = predictor.predict(pole)
z = []
for i in range(200):
    z.append(pred[i*200: (i+1)*200])
```

```
1250/1250 [==============================] - 1s 683us/step
```

In [33]:
```
fig, ax = plt.subplots()
ax.imshow(z)
ax.invert_yaxis()
```



Аппроксимация функции

In [38]:
```
def func(t):
    return np.cos(2.5*t**2 - 5*t)
```

In [39]:
```
h = 0.01
X = np.arange(0, 2.2+h,h)
y = func(X)
```

Создаем модель

In [35]:
```
predictor =  keras.Sequential([
        layers.Dense(100,input_dim=1, activation="tanh", name="tanh"),
        layers.Dense(30, activation="tanh", name="tanh2"),
        layers.Dense(1,activation='linear', name='linear')
    ]
)
predictor.summary()
```

```
Model: "sequential_4"
_________________________________________________________________
 Layer (type)                Output Shape              Param #
```

```
=================================================================
 tanh (Dense)                (None, 100)               200

 tanh2 (Dense)               (None, 30)                3030

 linear (Dense)              (None, 1)                 31

=================================================================
Total params: 3,261
Trainable params: 3,261
Non-trainable params: 0
_________________________________________________________________
```

Компилируем модель

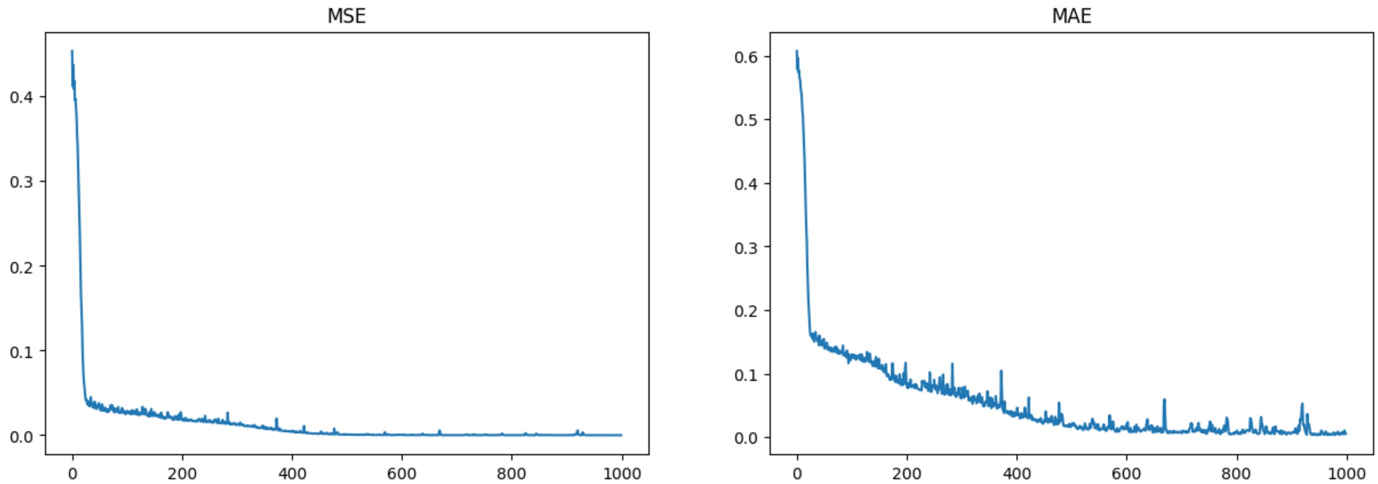
In [36]:
```
predictor.compile(loss='mse', optimizer='adam', metrics=['mae'])
```

Тренеруем модель

In [40]:
```
epochs = 1000
time_start = time.time()
hist = predictor.fit(
    X,
    y,
    batch_size=10,
    epochs=epochs,
    verbose=0,
    shuffle=True
    )
time_finish = time.time()
mse_loss, mae_loss = predictor.evaluate(X, y, verbose=0)

print(f'Fit time: {(time_finish - time_start):.{2}f}s')
print(f'Result MSE: {mse_loss}')
print(f'Result MAE: {mae_loss}')

fig, ax = plt.subplots(1, 2)
fig.set_figwidth(15)

ax[0].set_title('MSE')
ax[1].set_title('MAE')

ax[0].plot(range(epochs), hist.history['loss'])
ax[1].plot(range(epochs), hist.history['mae'])
```

```
Fit time: 22.84s
Result MSE: 5.414908810053021e-05
Result MAE: 0.005597070325165987
```

Out[40]:
```
[<matplotlib.lines.Line2D at 0x7f61cc29bc40>]
```

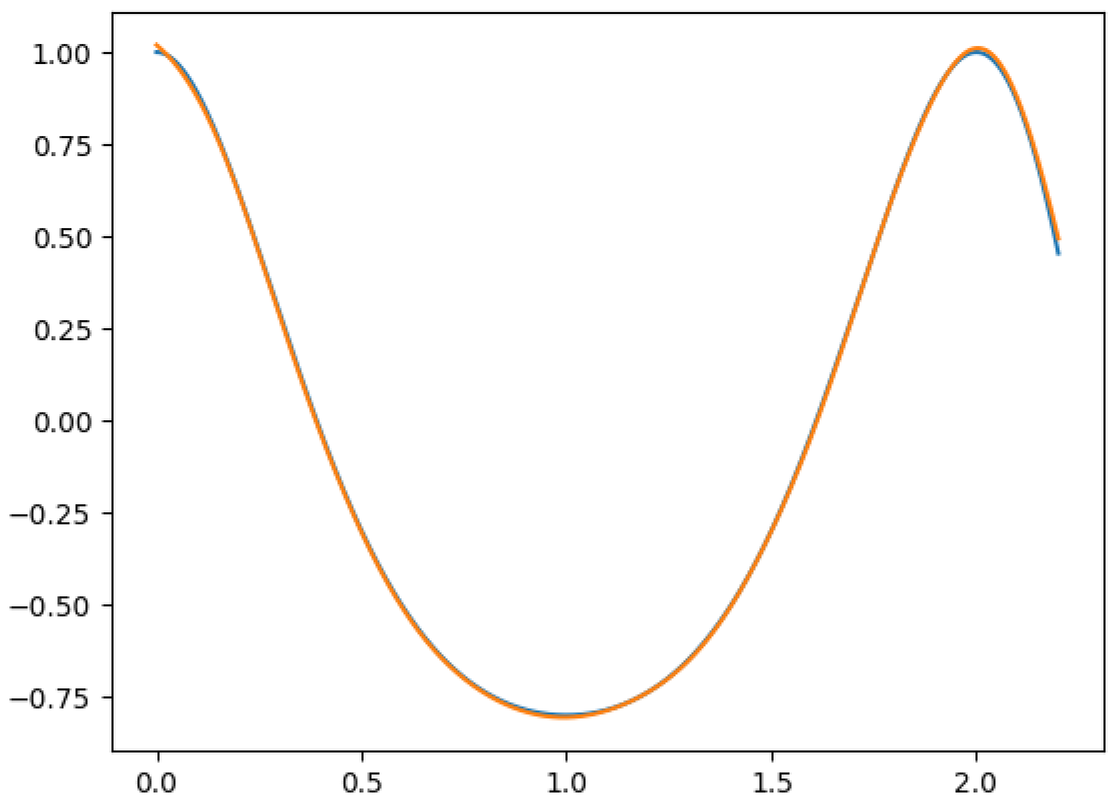


Аппроксимируем функцию

In [43]:
```
t = np.linspace(0, 2.2, 2000)
y_ans = func(t)
y_pred = predictor.predict(t)
plt.plot(t, y_ans)
plt.plot(t, y_pred)
```

```
63/63 [==============================] - 0s 735us/step
```

Out[43]:
```
[<matplotlib.lines.Line2D at 0x7f61cc0551f0>]
```



In [ ]: