

# Topics in Control: Control of Multiagent Systems

## Courseworks

Winter 2020

**Problem 1:** Consider a network of 5 agents described as

$$\dot{x}_i(t) = u_i(t), i = 1, 2, 3, 4, 5, \quad (1)$$

where the agents are randomly initialized between  $[-1 \ 1]$ .

- a) Design and simulate a control strategy for the control inputs  $u_i(t), i = 1, 2, 3, 4, 5$ , such that the agents states converge to a common value. First assume that the agents are in interaction under the leader-follower communication topology depicted in Fig. 1, and then they are in interaction under the leaderless communication topology depicted in Fig. 2.

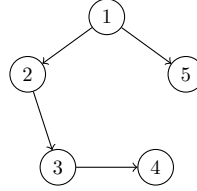


Figure 1: The leader-follower communication topology of the multiagent system in Question 1.

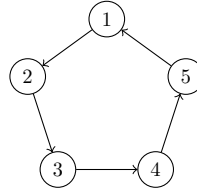


Figure 2: The leaderless communication topology of the multiagent system in Question 1.

- b) Assume that due to faults in the actuators of Agent 2,  $u_2 = 0$  for  $t > 1$ . Repeat the simulation scenario of Part (a) in this case, and discuss and conclude your observations.
- c) In the experiment of Part (b), analytically obtain the states of the agents when  $t \rightarrow \infty$ .

**Problem 2:** Consider a leaderless network of 9 agents when the network communication topology is depicted in Fig. 3.

- a) Show that the network communication topology has sufficient conditions to achieve consensus (no simulation is required).

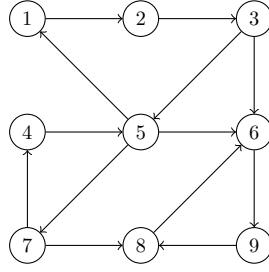


Figure 3: The network topology of the multiagent system in Question 2.

- b) According to the network communication topology and without computation of the network Laplacian matrix, discuss which agents can affect the final consensus value?

**Problem 3:** Consider a leader-follower network of 4 agents described as

$$\dot{x}_i(t) = u_i(t), i = 1, 2, 3, 4,$$

where the followers are randomly initialized between  $[-1, 1]$ , and the network topology is depicted in Fig. 4.

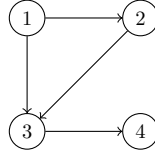


Figure 4: The network topology of the multiagent system in Question 3.

- a) For  $x_1(t) = 0$ , design a control strategy such that the followers follow the leader, and verify your answer by simulation test. Then, for the same control law, increase  $x_1(t)$  as  $0, 0.1, 0.1 \sin(2t), 0.5 \sin(2t), 0.5 \sin(0.2t)$  and discuss your observations.
- b) For your experiments in Part (a), analytically find the bound/maximum of  $|x_1(t) - x_i(t)|, i = 2, 3, 4$  when  $t \rightarrow \infty$ .

**Problem 4:** Consider a network of 4 agents described as

$$\begin{aligned} \dot{x}_i(t) &= u_{xi}(t), \\ \dot{y}_i(t) &= u_{yi}(t), i = 1, 2, 3, 4. \end{aligned}$$

- a) Design a communication topology along with a control strategy for the control input  $(u_{xi}(t), u_{yi}(t)), i = 1, 2, 3, 4$ , such that the agents reach a square formation with the side of 1 and with the center of the average of the initial positions of the agents.
- b) By assuming that the agents initial positions are  $[1, 0], [-1, 2], [3, 1]$ , and  $[1, 1]$ , verify the accuracy of your design in Part (a) by simulation test.
- c) Modify the designed control strategy of Part (a) such that the formation is moving with the desired velocity  $[1, 1]$ . Considering the initial conditions given in Part (b), verify the accuracy of your design by simulation test.

Note: In all the questions, assume that  $a_{ij} = 1$  if there is an edge from Node  $j$  to Node  $i$ .

In the case of questions or ambiguities, feel free to send email to [h.rezaee@imperial.ac.uk](mailto:h.rezaee@imperial.ac.uk).

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