**Important Concepts**

Central Limit Theorem (CLT)

* The mean for a sample taken from any data has an approximate normal distribution regardless of the distribution of the original data if the sample size is large enough (n30).
* Applies to nominal, ordinal, and interval data.

Distribution

* A table, graph, or function that describes all possible outcomes of a random variable.

Population proportion (*p*)

* The proportion of observations in the population that have a certain characteristic.

Random Variable

* A characteristic whose value for any given sample cannot be predicted.

Sample proportion ()

* The proportion of observations in the sample that have a certain characteristic.

Standard Error

* The difference between a population parameter and a sample result.
* Standard error decreases as sample size increases.
* Standard error increases as population standard deviation increases (i.e., diversity increases).

**Summary Table**

| Objective | Constraints and Assumptions | Concept or Tool | Equations and Algorithms |
| --- | --- | --- | --- |
| Analyze individual values within a population:  Find the probability of a value. | * The outcome is a discrete random variable. * There are a fixed number of trials (n). * Each trial has only two possible outcomes. * The probability of success (p) is the same for each trial. * The outcome of one trial does NOT influence the outcome of any other trial. | Binomial distribution  Use the normal distribution to approximate the binomial distribution if both of the following are true:   * (n)(p) 10 * (n)(1-p) 10 | 1. Locate the binomial table associated with the value of n. 2. Find the column that represents p. 3. Find the row that represents the number of successes. 4. The intersection of the row and column provides the probability of x successes, p(x). |
| Analyze individual values within a population:  Find the probably for an outcome greater than some specific value.  Find the probably for an outcome less than some specific values.  Find the probably for an outcome between two specific values. | * The outcome is a discrete random variable. * There are a fixed number of trials (n). * Each trial has only two possible outcomes. * The probability of success (p) is the same for each trial. * The outcome of one trial does NOT influence the outcome of any other trial. | Binomial distribution  Use the normal distribution to approximate the binomial distribution if both of the following are true:   * (n)(p) 10 * (n)(1-p) 10 | Add the probabilities of the individual values.  For n=3  p(1≤x≤3)=p(1)+p(2)+p(3)  p(x>1)=p(2)+p(3) |
| Analyze individual values within a population:  Find the mean, variance, and standard deviation for a specific outcome. | * The outcome is a discrete random variable. * There are a fixed number of trials (n). * Each trial has only two possible outcomes. * The probability of success (p) is the same for each trial. * The outcome of one trial does NOT influence the outcome of any other trial. | Binomial distribution  Use the normal distribution to approximate the binomial distribution if both of the following are true:   * (n)(p) 10 * (n)(1-p) 10 | Mean of X is μ=np  Variance of X is  σ2=np(1-p)  Standard deviation of X is σ = |
| Analyze individual values within a population:  Find the probability of a value.  Compare values from different distributions. | * The probability of a random outcome has a normal distribution. * The outcome is a continuous random variable. * The mean and standard deviation are known. | Normal distribution  Standard normal distribution (Z) | Normal distribution depends on its mean and standard deviation.  Any normal distribution can be converted to the Z-distribution.  Z-value represents the number of standard deviations above or below the mean.  z =  x = μ + zσ  Probabilities on Z-table represent the area under the curve to the left of the value. |
| Analyze individual values within a population:  Find the value of X given the percentage or probability of X   * Find the pth percentile for X {Find a where p(X<a)=p} * Find the (1-p)th percentile for X {Find b where p(X>b)=p which is rewritten as p(X<b)=1-p. | * The probability of a random outcome has a normal distribution. * The outcome is a continuous random variable. | Normal distribution  Standard normal distribution (Z) | Normal distribution depends on its mean and standard deviation.  Any normal distribution can be converted to the Z-distribution.  Z-value represents the number of standard deviations above or below the mean.  z =  x = μ + zσ  Probabilities on Z-table represent the area under the curve to the left of the value. |
| Analyze individual values within a population:  Approximate the binomial distribution when the number of trials (n) is large. | * (*n*)(*p*) 10 * (*n*)(1-*p*) 10 | Normal distribution  Standard normal distribution (Z) | μ = np  σ = |
| Analyze a population parameter:  Find the probability of a population parameter given a specific sample size | * The population is fairly close to normal distribution. * Data set is small * The standard deviation of the population is unknown | t-distribution  t-table  Columns=prob  Rows=degr of free | t-distribution has a mean of zero like the z-distribution.  t-distribution with sample size of 30 approximately equal to z-distribution  t-distribution depends on sample size.  Each t-distribution is characterized by its degrees of freedom.  t-table classified by degrees of freedom and probabilities.  t-table values represent greater-than probabilities (right-side tail of the t-distribution). |
| Analyze a population parameter:  Find the percentile of a population parameter given a specific sample size (i.e., the number on a distribution whose less-than probability [left-side tail] is the given percentage) | * The population is fairly close to normal distribution. * Data set is small * The standard deviation of the population is unknown | t-distribution  t-table  Columns=prob  Rows=degr of free  Bottom=confid inter | 1. Calculate degrees of freedom. 2. Determine the greater-than probability of interest (right-side tail). |
| Analyze a population parameter:  Find the confidence interval for population parameter | * The population is fairly close to normal distribution. * Data set is small * The standard deviation of the population is unknown | t-distribution  t-table  Columns=prob  Rows=degr of free  Bottom=confid inter  n30, use Z-distribution  n<30, use t-distribution | statisticmargin of error  margin of error defined by the critical value  critical value = std errors  To find critical value:   1. Find confidence interval on bottom row of table 2. Move up to the degrees of freedom for sample size |
| Analyze a population parameter when the distribution is non-normal or unknown | * The sample size is large (n30) * (*n*)(*p*) 10 * (*n*)(1-*p*) 10 | Central Limit Theorem  Approximate with the Normal distribution and the Z-distribution  Confidence interval  Standard error | Mean of the sampling distribution equals the population proportion:  = *p*  Standard error equals:  = |
| Analyze a population parameter when the distribution is non-normal or unknown:  Find the probability for a sample proportion given a population proportion | * The sample size is large (n30) * (*n*)(*p*) 10 * (*n*)(1-*p*) 10 | Central Limit Theorem  Approximate with the Normal distribution and the Z-distribution  Confidence interval  Standard error | 1. Confirm constraints 2. Convert sample proportion to z-value 3. Find probability of z |