

SM-2302: Software for Mathematicians

Lecture 2: Visualization & Programming

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Semester I, 2025/26

Adapted from 6.057 IAP 2019 (MIT OCW)

Outline

Lecture 2: Visualization & Programming

- Functions

- Flow control

- Line plots

- Image and surface plots

- Efficient codes

- Debugging

User-defined Functions

- Functions look exactly like scripts, except they must start with a **function declaration**:

Must have the keyword: function

`function [x, y, z] = funcName (in1, in2)`

Function name should match m-file name

if more than one output,
use square brackets

inputs

- **No need for return:** MATLAB 'returns' the variables whose names match those in the function declaration.
- **Variable scope:** Any local variable created within the function but not returned disappears after the function stops running.

Overloading

- MATLAB functions are generally overloaded:
 - Can accept different numbers of input arguments
 - Can return different numbers of output arguments

- Example using `size()`:

<code>>> a = zeros(2, 4, 8)</code>	a 3D matrix (2×4×8)
<code>>> D = size(a)</code>	returns a vector: <code>[2 4 8]</code>
<code>>> [m, n] = size(a)</code>	returns first two dimensions: 2, 4
<code>>> [x, y, z] = size(a)</code>	returns all three dimensions
<code>>> m2 = size(a, 2)</code>	returns size along 2nd dimension: 4

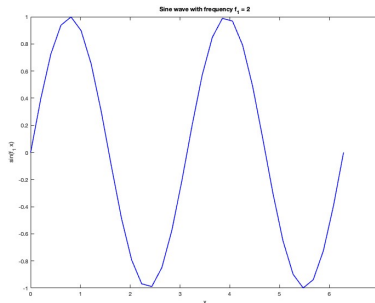
- You can overload your own functions:
 - Use special variables: `nargin`, `varargin` (for inputs)
 - And: `nargout`, `varargout` (for outputs)

Example 1 (Functions)

Goal: Write a function to plot a sine wave with a given frequency.

- Write a function with the following declaration: `>> function plotSin(f1)`
- Inside the function script, plot the sine wave $y = \sin(f_1 x)$ over the interval $x \in [0, 2\pi]$.
- Use 16 points per period for good sampling.

Expected output:



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Relational operators

The operation of many branching constructs is controlled by **boolean values** (0 is false, 1 is true).

- **Rational operators**

<code>==</code>	equal to	<code>~=</code>	not equal
<code>></code>	greater than	<code><</code>	less than
<code>>=</code>	greater or equal	<code><=</code>	less or equal

- **Logical operators**

<code>&</code>	and	<code>~</code>	logical not
<code> </code>	or	<code>xor</code>	logical exclusive or
<code>all</code>	all true	<code>any</code>	any true

if/else/elseif

- `if/else/elseif` are basic flow control, which is common to all languages
- MATLAB syntax is slightly unique:

`if`

```
if cond
    commands
end
```

`else`

```
if cond
    commands1
else
    commands2
end
```

`elseif`

```
if cond
    commands1
elseif cond2
    commands2
else
    commands3
end
```

- Conditional statements evaluate boolean (true or false)
- No parentheses required – common blocks are between reserved words
- Too many `elseif`s? Consider using `switch`

for

- `for` loops are used for a known number of iterations:

```
for n = 1:100 % loop variable
    commands % command block
    ...
end
```

- Loop variable:
 - defined as a vector
 - becomes a scalar within the command block
 - doesn't need consecutive values
- Command block is anything between the `for` line and the `end`

while

- `while` is a more general for loop, where the number of iterations is not required:

```
while cond % conditional expression
    % some loop that is executed when cond is true
    ...
end
```

- Beware of infinite loops (use CTRL+C)
- Add `break` line to exit a loop

Example 2 (Conditionals)

Goal: Make your function flexible by checking the number of input arguments.

- Modify your existing function `plotSin(f1)` to accept two inputs:
`function plotSin(f1,f2)`
- If the function is called with 1 input, plot the sine wave as before (using `f1` only).
Otherwise, display the line:
``Two inputs were given'`
- Use the built-in variable `nargin` to check how many inputs were passed.

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Plot options

- We can change the line colour, marker style and line style by adding a **string argument**:

```
>> plot(x, y, 'k . -');
```

color
(black)

marker
style

line
style



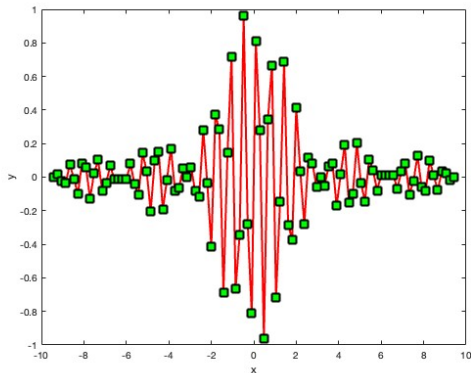
- Or we can plot without connecting the dots, by omitting the line style argument:

```
>> plot(x,y, '.')
```
- Refer to `help plot` for a full list of colours, markers and line styles

Line and marker options

Everything on a line can be customised:

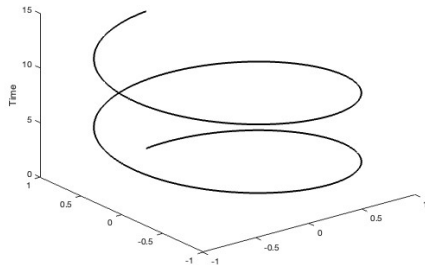
```
plot(x, y, 's-', 'LineWidth', 2, ...  
     'Color', [1 0 0], ... % RGB vector (red)  
     'MarkerEdgeColor', 'k', ... % black border  
     'MarkerFaceColor', 'g', ... % green fill  
     'MarkerSize', 10)
```



3D line plots

We can plot in three dimensions just as easily as in two dimensions

```
time = 0:0.001:4*pi;  
x = sin(time); y = cos(time); z = time;  
plot3(x, y, z, 'k', 'LineWidth', 2);  
zlabel('Time')  
xlim([-1 1]); ylim([-1 1]); zlim([0 15]); % set limits on all 3 axes
```



Axis modes

Built-in axis modes (see [doc axis](#) for more modes)

- `>> axis square` makes the current axis look like a square box
- `>> axis tight` fits axes to data
- `>> axis equal` makes x and y scales the same
- `>> axis xy` puts the origin in the lower left corner (default for plots)
- `>> axis ij` puts the origin in the upper left corner (default for matrices/images)

Multiple plots in one figure

- Use `subplot` to have multiple axes in one figure:
 - `>> subplot(2,3,1)` creates a figure with 2 rows and 3 columns of axes, and plots on the first axis
each axis can have labels, a legend, and a title
 - `>> subplot(2,3,4:6)` activates a range of axes and merges them into one.
- To close existing figures, use
 - `>> close([1 3])` closes figures 1 and 3
 - `>> close all` closes all figures (useful in scripts)

Saving figures

Figures can be saved in many formats. The common ones are

- **MATLAB figure (*.fig)** preserves all information
- **Bitmap file (*.bmp)** is an uncompressed image
- **EPS file (*.eps)** is a high-quality scaleable format
- **portable document format (*.pdf)** is a compressed image

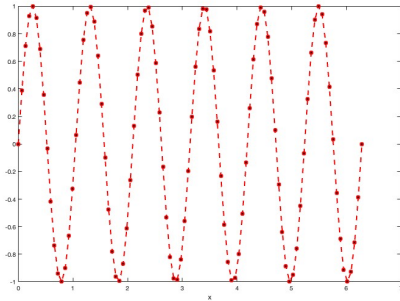
Example 3 (Advanced plotting)

Goal: Enhance your `plotSin` function with custom plotting features and subplot behaviour.

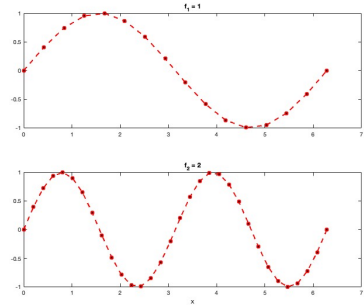
- Style the plot: using square markers connected by a dashed red line (`'r--s'`) with thickness of 2 as the line. Set the marker face colour to black, and use marker size 6.
- When called with 2 inputs: open a new figure and create a vertical layout with 2 plots. Plot each frequency in a separate subplot.
- MATLAB properties to use: `LineWidth`, `MarkerFaceColor`, `Marker`, `figure`, `subplot`

Expected outcome:

`plotSin(6)`



`plotSin(1,2)`



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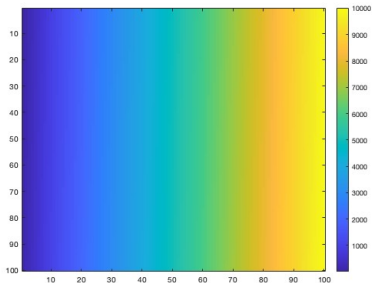
Efficient codes

Debugging

Visualising matrices

- Any matrix can be visualised as an image:

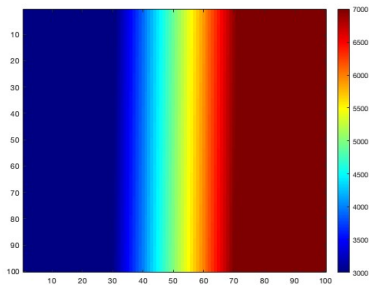
```
mat = reshape(1:10000, 100, 100);  
imagesc(mat); % Scales values to span the entire colormap  
colorbar
```



Visualising matrices

- Set limits for the color axis (analogous to `xlim`, `ylim`) and change the `colormap` (default is `parula`):

```
caxis([3000 7000])  
colormap(jet) % other options are cool, gray, hot ...
```



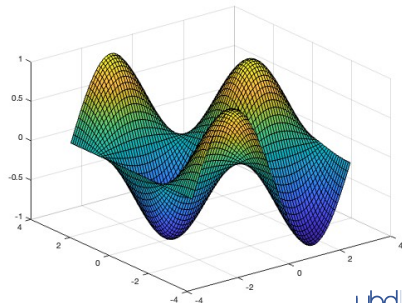
Surface plots

- It is more common to visualise surfaces in 3D. For example,

$$f(x, y) = \sin x \cos y, \quad x \in [-\pi, \pi], \quad y \in [\pi, \pi]$$

- `surf` creates a surface by connecting vertices at points in space (x, y, z) . See `help surf` for more options.
- The vertices can be denoted by matrices `X`, `Y`, `Z`, and created using `meshgrid`.

```
% make the x and y vectors  
x = -pi:0.1:pi; y = -pi:0.1:pi;  
[X,Y] = meshgrid(x,y); % create the matrices  
Z = sin(X).*cos(Y); % function to evaluate  
surf(X,Y,Z) % plot the surface
```



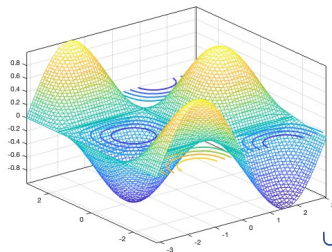
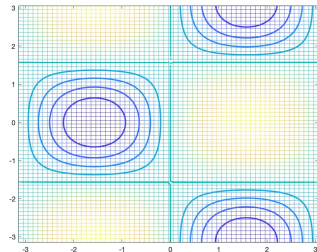
Contour

Make surfaces two-dimensional by using the `contour` command:

```
contour(X, Y, Z, 'LineWidth', 2)  
hold on  
mesh(X, Y, Z)
```

- `contour` takes the same arguments as `surf`
- the color indicates height
- linestyle and colormap properties can be modified

```
contour3(X, Y, Z, 50) % creates a 3D ...  
    contour plot with contour levels 50
```



Example 4 (3D plots)

Goal: Extend `plotSin(f1, f2)` to create 2D and 3D visualizations of a combined sine function.

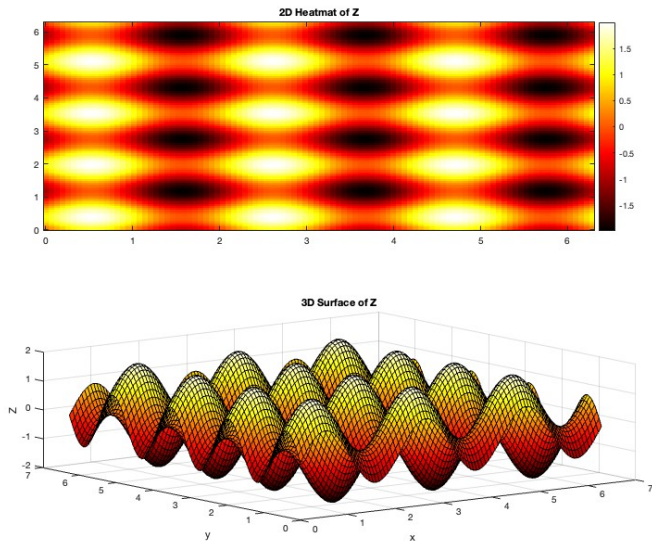
- If two inputs are passed, evaluate:

$$Z = \sin(f_1 X) + \sin(f_2 Y)$$

using a 2D grid of values (create matrices `X` and `Y` using `meshgrid`).

- Top subplot: 2D heatmap of `Z`. Use `imagesc(x,y,Z)`, apply `colormap hot`, add `colorbar`. Then set axis to `xy`.
- Bottom subplot: 3D surface plot of `Z` (Use `surf`)

Expected outcome: `plotSin(3,4)` generates this figure



Specialised plotting functions

Functions	Example
<code>polar</code> makes polar plots	<pre>>> theta = 0:0.01:2*pi; >> polar(theta, cos(theta*2));</pre>
<code>bar</code> makes bar graphs	<pre>>> bar(1:10, rand(1,10));</pre>
<code>quiver</code> adds velocity vectors to a plot	<pre>>> [X, Y] = meshgrid(1:10, 1:10); >> quiver(X, Y, rand(10), rand(10));</pre>
<code>stairs</code> plots piecewise constant functions	<pre>>> stairs(1:10, rand(1,10));</pre>
<code>fill</code> draws and fills a polygon with specified vertices	<pre>>> fill([0 1 0.5], [0 0 1], 'r');</pre>

see [help](#) on these functions for syntax.

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find

- `find` is a very important function that
 - returns indices of nonzero values
 - can simplify code and help avoid loops
- Basic syntax: `index = find(cond)` for example,

```
x = rand(1,100);  
inds = find(x<0.4 & x<0.6);
```

- Here, `inds` contain indices at which `x` has values between 0.4 and 0.6:

<code>x>0.4</code>	returns a vector with 1 for true, and 0 for false
<code>x<0.6</code>	returns a vector with 1 for true, and 0 for false
<code>&</code>	combines the two vectors using logical and operator
<code>find</code>	returns the indices of 1s

Avoiding loops

Consider the linear space: `x = sin(linspace(0, 10*pi, N));`
How many of the entries are positive?

Using a loop & conditional if/else:

```
count = 0;
for n = 1:length(x)
    if x(n)>0
        count = count + 1;
    end
end
```

Without loop:

```
count = length(find(x>0));
```

length(x)	loop time	find time
100	0.01	0
10,000	0.1	0
100,000	0.22	0
1,000,000	1.5	0.04

Avoid loops, and use built-in functions for more efficient codes.

Vectorization

- Another way to avoid loops is by using **vectorization**, which is more efficient for MATLAB
- Vectorized codes use indexing and matrix operations to avoid loops

For instance, to add every two consecutive terms:

```
% slow and complicated
```

```
a = rand(1,100);
```

```
b = zeros(1,100);
```

```
for n = 1:100
```

```
    if n==1
```

```
        b(n)=a(n);
```

```
    else
```

```
        b(n) = a(n-1)+a(n);
```

```
    end
```

```
end
```

```
% efficient and cleaner
```

```
a = rand(1,100);
```

```
b = [0 a(1:end-1)] + a;
```


Preallocation

- Avoid variables growing within a loop, as memory reallocation is a time-consuming process.
- Preallocate the required memory by initialising the array with its default value. For example,

```
a = zeros(1, 100);  
for n = 1:100  
    x = linspace(0, pi, 1000);  
    y = sin(n*x).*exp(-x);  
    res = trapz(x, y); % Numerical integration  
    a(n) = res;  
end
```

- Variable `a` is only assigned values, no memory is allocated here.

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Debugging

To use the debugger in MATLAB,

1. Set breakpoints - click the red dot next to a line number in the Editor
2. Run the script, then MATLAB pauses at the breakpoint
3. Step through the code using the debugging buttons:
 - **Step**: Execute current line and pause at the next
 - **Step In**: Dive into a called function
 - **Step Out**: Finish function and return to caller
 - **Continue**: Resume until next breakpoint
4. Use the command window or workspace to inspect variables
5. Stop debugging by clicking **Stop** button or type `dbquit` and `dbclear all`

Debugging measures

- When debugging functions, use the `disp` command to print messages instead of removing semicolons, which is easier. For example:
`>> disp(['loop iteration ' num2str(n)]);`
- It can be helpful to determine the execution time of your code by using the `tic/toc` function. For example,

```
A = zeros(1000); A(1,3)=10; A(21,5)=pi;  
B = sparse(A); % squeezes out any zero elements from full matrix A  
C = rand(1000,1);
```

```
tic; A\C; toc; % slow  
tic; B\C; toc; % much faster!
```