

# GMWM Package - Part II Automatic and Computationally Efficient Method For Model Selection In Inertial Sensor Calibration

#### Roberto Molinari

Research Center for Statistics University of Geneva, Switzerland

joint work with James Balamuta (UIUC) Stéphane Guerrier (UIUC) Jan Skaloud (EPFL) Xinyu Zhang (CAS)

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# The GMWM package in action

### Outline

- Visualizing the signal(s):
  - Is the signal disturbed (contaminated)?
  - Which models could best describe the visualized WV?
- ② Estimating the model(s)
  - The gmwm.imu() function for parameter estimation
  - The options for estimation
- Inference
  - Confidence intervals for the parameters
  - Goodness-of-fit of the model to the signal
- Model Selection
  - The efficient computation of the WVIC
  - Model selection from a set of user-specified models
  - Automatic model selection from a set of all sub-models of a single user-specified model

# The GMWM package in action

## Getting to know the package

The package comes with an example dataset called imu6

- The data comes from the calibration of an XSens MTi-G sensor
- To use the data within the R session:
  - Load the gmwmdata package (separate from the gmwm package)
  - Make the dataset available in the session by typing data(imu)
- Load external data (e.g. binary data) with read.imu()

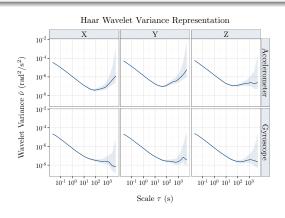
```
install.packages("gmwmdata")
library(gmwmdata)
data(imu6)
head(imu6)
```

```
Gyro. X Gyro. Y Gyro. Z Accel. X Accel. Y Accel. Z 1 -0.011138 -0.017646 -0.009531 1.083731 0.023897 9.638113 2 -0.006765 -0.013657 -0.021974 1.059858 0.042061 9.646901
```

# Visualizing the data

## The function wvar.imu()

Once the calibration data has been entered, it is possible to plot the observed WV vs au on a log-log scale



#### R code:

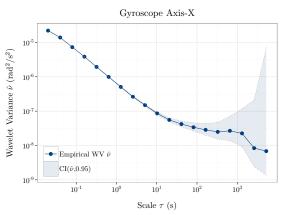
```
imu.obj = imu(imu6,
gyroscope = 1:3,
accelerometer = 4:6)
wv = wvar.imu(imu.obj)
plot(wv)
```

(Run time: 3.70 [sec])

## Visualizing the data

## The function wvar()

It is obviously possible to plot the WV from the axis of an accelerometer or gyroscope individually



#### R code:

```
WV.gx = wvar(imu6[,1])
plot(WV.gx)
```

(Run time: 0.65 [sec])

The Allan variance can also be computed through the function avar()

## The gmwm.imu() function

The function tailor-made for IMU error modeling is gmwm.imu()

## Main arguments of the gmwm.imu() function

- model: The structure of the model is specified through this argument
- data: The signal to be modelled
- ullet compute.v: The method for computing the weighting matrix  $\Omega$ 
  - fast: Estimated diagonal matrix
  - ullet diag: Use a diagonal matrix with the asymptotic variance of  $\hat{oldsymbol{
    u}}$
  - ullet bootstrap: Estimate  $\Omega$  through parametric bootsrap

## The model argument

The GMWM package can estimate each specific model or any latent model made by a combination of all or a subset of the following models

- AR1(): a first-order autoregressive process (reparametrization of Gauss-Markov process)
- WN(): white noise process
- QN(): quantization noise (rounding error)
- RW(): random walk process
- DR(): drift
- AR(): p-order autoregressive process
- MA(): q-order moving average process
- ARMA(): autoregressive-moving average processes

## Latent model syntax

To specify a latent model we use the sign "+" between the available models while the AR1() model can be included more than once (say k times) and is can be specified as k\*AR1(), for example

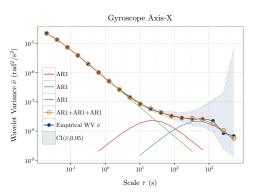
- ARMA()+WN()+RW()
- 3\*AR1()+DR()

## Convergence

If the gmwm.imu() function has problems of convergence, one can specify starting values for the parameters using the brackets in the syntax of each model (e.g. WN(sigma2=0.5))

## Visually assessing the fit

The function plot() applied to the object of a GMWM estimation allows to see how well the WV implied by the estimated model fits the observed WV



#### R code:

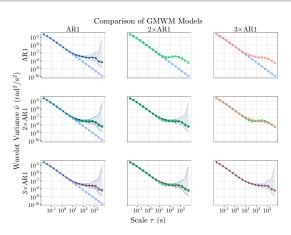
```
mod = gmwm.imu(3*AR1(),
imu6[,1]) plot(mod,
process.decomp = T)

(Run time: 0.56 [sec])
```

# Model Comparison

## Suppose we want to compare three models...

AR1(), 2\*AR1() and 3\*AR1()



#### R code:

```
Xt = imu[,1]
m1 = gmwm.imu(AR1(),Xt)
m2 = gmwm.imu(2*AR1(),Xt)
m3 = gmwm.imu(3*AR1(),Xt)
compare.models(m1, m2, m3)
```

10 / 16

(Run time: 5.20 [sec])

## Inference

## Output of estimation

Aside from the value of the estimated parameters, the output of the function gmwm.imu provides other information for inference which include confidence intervals and goodness of fit test (GoF)

```
mod = gmwm.imu(2*AR1(), imu6[,1])
summary(mod, inference = T)
Model Information:
          Estimates
                          CI Low
                                      CI High
AR1
       9.998700e-01 9.998336e-01 9.999064e-01 2.211547e-05
SIGMA2 5 223319e-11 4 343878e-11 6 102759e-11 5 346620e-12
AR1
       1.265324e-01 1.265324e-01 1.265324e-01 1.765050e-08
SIGMA2 = 5.031185e - 05 = 5.021566e - 05 = 5.040805e - 05 = 5.848209e - 08
* The initial values of the parameters used in the minimization
of the GMMM objective function were generated by the program
underneath seed: 1337
Objective Function: 20.9297
Asymptotic Goodness of Fit:
Test Statistic: 903.8 on 15 degrees of freedom
The resulting p-value is: 0
```

11 / 16

## WIC model selection

## Two options for model selection

- Manual: the function rank.models() allows the user to specify the set of models from which to select
- Automatic: the function auto.imu() allows to specify one single model from which all sub-models are generated to create a set from which to select

#### R code:

```
rank.models(3*AR1()+WN(),
2*AR1()+QN(), imu6[,1], nested =
F, bootstrap = F, model.type="imu",
robust = F)
```

```
mod.res = auto.imu(imu6, model
= 3*AR1()+WN()+RW()+QN()+DR(),
bootstrap = F, robust = F)
```

## WIC model selection

4. AR1 AR1 RW

5 AR1 AR1

19. RW

#### Automatic IMU model selection

Suppose we want to apply the auto.imu() function to the X-axis gyroscope in the imu dataset and consider all model combinations within the 4\*AR1() + WN() + RW() model

20.1044 0.4871 20.5915

0.2070

(Run time: 50.25 [sec]  $\approx 14x$  faster than the bootstrap option 685.4 [sec])

20 9864

28420.4972

0.0160 28420.5132

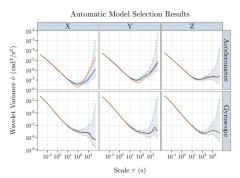
21 1933

0

## WIC Model Selection

## Visualizing the Automatic IMU Model Selection

We can observe the results of the auto.imu() function by requesting a plot. The plot will contain the empirical wavelet variance in addition to the best implied wavelet variance that we find. In this particular case, we used the defaults of the auto.imu() (63 models  $\times$  6 columns).



#### R code:

```
imu.obj = imu(imu6, gyroscope = 1:3,
accelerometer = 4:6, axis = c('X',
'Y', 'Z'))
auto.mod = auto.imu(imu.obj)
plot(auto.mod)
(Run time: 377.77 [sec])
```

# Upcoming features

Aside from **fine-tuning existing features** of the package (additional options, function optimization, support documentation, etc.), the GMWM package will be updated with the following features

Sensor calibration under dynamic conditions

$$Y_t = \rho_t Y_{t-1} + \epsilon_t$$

Multivariate latent models

$$Y_t^{(x)} = V_t + W_t^{(x)}$$
  
 $Y_t^{(y)} = V_t + W_t^{(y)}$   
 $Y_t^{(z)} = V_t + W_t^{(z)}$ 

• Others (e.g. additional moments for the GMWM (AGMWM), other wavelet filters, unit-root and independence testing)

# Thank you very much for your attention!

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# Any questions?

## More info...

http://publish.illinois.edu/SMAC-group stephane@illinois.edu

