

1) Give the value of each digit in the following decimal numbers :

(a) 6345

| Place | Thousands | Hundred | Tens | Ones |
|-------------|-----------|---------|------|------|
| Digit | 6 | 3 | 4 | 5 |
| Multipliers | 1,000 | 100 | 10 | 1 |
| Place Value | 6,000 | 300 | 40 | 5 |

Value of 6 = $6 \times 1000 = 6000$

Value of 3 = $3 \times 100 = 300$

Value of 4 = $4 \times 10 = 40$

Value of 5 = $5 \times 1 = 5$

(b) 278536

| Places | Hundred Thousands | Ten Thousands | Thousands | Hundred | Tens | Ones |
|-------------|-------------------|---------------|-----------|---------|------|------|
| Digits | 2 | 7 | 8 | 5 | 3 | 6 |
| Multipliers | 100,000 | 10,000 | 1,000 | 100 | 10 | 1 |
| Place Value | 200,000 | 70,000 | 8,000 | 500 | 30 | 6 |

Value of 2 = $2 \times 100,000 = 200,000$

Value of 7 = $7 \times 10,000 = 70,000$

Value of 8 = $8 \times 1,000 = 8,000$

Value of 5 = $5 \times 100 = 500$

Value of 3 = $3 \times 10 = 30$

Value of 6 = $6 \times 1 = 6$

2.) Convert the following binary numbers into decimal:

(a) 101110001

$$\Rightarrow 1 \times 2^8 + 0 \times 2^7 + 1 \times 2^6 + 1 \times 2^5 + 1 \times 2^4 + 0 \times 2^3 + 0 \times 2^2 + 0 \times 2^1 + 1 \times 2^0 \Leftarrow$$

$$\Rightarrow 256 + \cancel{128}^0 + 64 + 32 + 16 + 0 + 0 + 0 + 1$$

$$\Rightarrow \cancel{384} \boxed{369}$$

$$(101110001)_2 \rightarrow \cancel{(384)}_{10} (369)_{10}$$

(b) 10110011

$$\Rightarrow 1 \times 2^7 + 0 \times 2^6 + 1 \times 2^5 + 1 \times 2^4 + 0 \times 2^3 + 0 \times 2^2 + 1 \times 2^1 + 1 \times 2^0$$

$$\Rightarrow 128 + 0 + 32 + 16 + 0 + 0 + 2 + 1$$

$$\Rightarrow \boxed{179}$$

$$(10110011)_2 \rightarrow (179)_{10}$$

3.) Convert each binary number to decimal

(a) 1011110.1010

$$\Rightarrow 1 \times 2^6 + 0 \times 2^5 + 1 \times 2^4 + 1 \times 2^3 + 1 \times 2^2 + 1 \times 2^1 + 0 \times 2^0$$

$$+ (1 \times 2^{-1}) + (0 \times 2^{-2}) + (1 \times 2^{-3}) + (0 \times 2^{-4})$$

$$\Rightarrow 64 + 0 + 16 + 8 + 4 + 2 + 0 + \frac{1}{2} + 0 + \frac{1}{8} + 0$$

$$\Rightarrow \boxed{94.625}$$

$$(1011110.1010)_2 \rightarrow (94.625)_{10}$$

(b) 1111101.11011

$$\Rightarrow \cancel{1 \times 2^7} + \cancel{1 \times 2^6} + \cancel{1 \times 2^5} + \cancel{1 \times 2^4} + \cancel{1 \times 2^3} + \cancel{1 \times 2^2}$$

$$\Rightarrow 1 \times 2^6 + 1 \times 2^5 + 1 \times 2^4 + 1 \times 2^3 + 1 \times 2^2 + 1 \times 2^1 + 1 \times 2^0$$

$$+ (1 \times 2^{-1}) + (1 \times 2^{-2}) + (0 \times 2^{-3}) + (1 \times 2^{-4}) + (1 \times 2^{-5})$$

$$\Rightarrow 64 + 32 + 16 + 8 + 4 + 0 + 1 + \frac{1}{2} + \frac{1}{4} + 0 + \frac{1}{16} + \frac{1}{32}$$

$$\Rightarrow \boxed{125.84375}$$

$$(1111101.11011)_2 \rightarrow (125.84375)_{10}$$

4.) Convert each decimal fraction to binary using repeated multiplication by 2

(a) 0.3456

$$(0.3456)_{10} \rightarrow (0.0101)_2$$

$$0.3456 \times 2 = 0.6912$$

$$0.6912 \times 2 = 1.3824$$

$$0.3824 \times 2 = 0.7648$$

$$0.7648 \times 2 = 1.5296$$

(b) 0.9232

$$0.9232 \times 2 = 1.8464 \quad (0.9232)_{10} \rightarrow (0.1110)_2$$

$$0.8464 \times 2 = 1.6928$$

$$0.6928 \times 2 = 1.3856$$

$$0.3856 \times 2 = 0.7712$$

5.) Convert each decimal number to binary using repeated division by 2

(a) 47

$$\begin{array}{r|l} 2 & 47 \\ \hline 2 & 23 \rightarrow 1 \\ \hline 2 & 11 \rightarrow 1 \\ \hline 2 & 5 \rightarrow 1 \\ \hline 2 & 2 \rightarrow 1 \\ \hline & 1 \rightarrow 0 \end{array}$$

$$(47)_{10} \rightarrow (101111)_2$$

(b) 63

$$\begin{array}{r|l} 2 & 63 \\ \hline 2 & 31 \rightarrow 1 \\ \hline 2 & 15 \rightarrow 1 \\ \hline 2 & 7 \rightarrow 1 \\ \hline 2 & 3 \rightarrow 1 \\ \hline & 1 \rightarrow 1 \end{array}$$

$$(63)_{10} \rightarrow (111111)_2$$

6.) Determine the 1's complement of each binary number

a.) $(1001110)_2 \rightarrow (78)_{10}$

0100 1110 ; Original

10 1100 01 ; 1's Complement

b.) $(101110101)_2 \rightarrow (373)_{10}$

0000 0001 0111 0101 ; Original

1111 1110 1000 1010 ; 1's Complement

7.) Determine the 2's complement of each binary number using either method

a.) $(11001101)_2 \rightarrow (205)_{10}$

1100 1101

0011 0010 ; 1's Complement

0011 0011 ; 2's Complement

b.) $(11010111)_2 \rightarrow (215)_{10}$

1101 0111

0010 1000 ; 1's Complement

0010 1001 ; 2's Complement

8.) -121

01111001 ; Original (121)

a.) 11111001 ; (-121)

b.) 10000110 ; 1's complement

c.) 10000111 ; 2's complement

9.) $(10011001)_2 \rightarrow (153)_{10}$

00000000 10011001 ; Original (+153)

a.) 10000000 10011001 ; (-153)

b.) 01100110 ; 1's complement

c.) 01100111 ; 2's complement

10.) Convert each binary number to Gray Code:

a.) 11011

Gray Code = 10110

$$\begin{array}{c} \text{+ + + +} \\ 11011 \\ \downarrow \\ 10110 \end{array}$$

b.) 1001010

Gray Code: 1101111

$$\begin{array}{c} 1^+0^+0^+1^+0^+1^+0 \\ \downarrow \\ 1101111 \end{array}$$

c.) 1111011101110

Gray Code: 1000110011001

$$\begin{array}{c} 1^+1^+1^+1^+0^+1^+1^+1^+0^+1^+1^+1^+0 \\ \downarrow \\ 1000110011001 \end{array}$$

| | |
|---|--------|
| 2 | 121 |
| 2 | 60 → 1 |
| 2 | 30 → 0 |
| 2 | 15 → 0 |
| 2 | 7 → 1 |
| 2 | 3 → 1 |
| | 1 → 1 |

11.) Convert each Gray Code to binary :-

a.) $(1010)_{GC} \rightarrow (1100)_2$

$$\begin{array}{cccc} 1 & 0 & 1 & 0 \\ \downarrow & \nearrow & \nearrow & \nearrow \\ 1 & 1 & 0 & 0 \end{array}$$

Binary: 1100

b.) $(00010)_{GC} \rightarrow (00011)_2$

Binary: 00011

c.) $(11000010001)_{GC} \rightarrow (10000011110)_2$

$$11 \ 0000 \ 1000 \ 1$$

$$\downarrow \nearrow \nearrow \nearrow \nearrow \nearrow \nearrow$$

$$100000 \ 1111 \ 0$$

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