

duction of Order

$$e^{-\int p(x) dx}$$

$$y_1$$

$$x)y=0, C_1 e^x$$

Q₁₃ $X^2 y'' - X y' + 2y = 0, y_1 = X \sin(\ln X)$

$$y'' \left[\frac{1}{X} \right] y' + \frac{2}{X^2} y = 0$$

$$y_2 = X \sin(\ln X) \int \frac{e^{-\int (-\frac{1}{X}) dx}}{(X \sin(\ln X))^2} dx$$

$\ln X$
 $e^{\ln X}$
 $= X$

$$y_2 = X \sin(\ln X) \int \frac{X \cdot C_1}{X^2 \sin^2(\ln X)} dx$$

$$= C_1 X \sin(\ln X) \int \left[\frac{1}{X} \right] \csc^2(\ln X) dx$$

$$\text{Let } u = \ln X \Rightarrow du = \frac{1}{X} dx$$

$$= X \sin(\ln X) \int \csc^2 u \cdot du$$

$$= C_1 X \sin(\ln X) (-\cot u) + C_2$$

$$= -C_1 X \sin(\ln X) \cdot \cot(\ln X) + C_2$$