

$g(x)$

Ex 3 Solve $y'' + 3y' + 2y = 4x^2$

$$\downarrow m^2 + 3m + 2 = 0$$
$$m = -1, -2$$

$$y_c = c_1 e^{-x} + c_2 e^{-2x}$$

For y_p $D^3(D^2 + 3D + 2)y = 0$

$$0, 0, 0 \quad \downarrow -1, -2$$

$$y = A + Bx + Cx^2 + \boxed{Ee^{-x} + Fe^{-2x}}$$

$$\textcircled{1} \quad D^3 X^2 = 0$$

Unboxed part of y is candidate X^{n-1}

y_p

$$y_p = A + Bx + Cx^2 \quad \text{---} \textcircled{2}$$

x

$$\left[D^2 - 2\alpha D + (\alpha^2 + \beta^2) \right]^n X^n$$