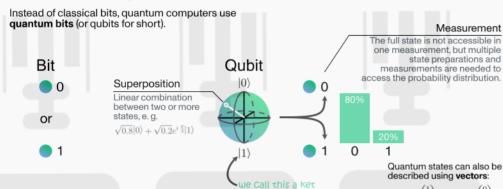
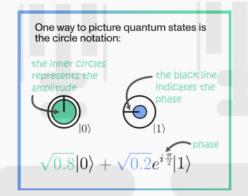
# Quantum Computing CHEATSHEET MARGICIAN For circuit Margicians

## Bits and Qubits

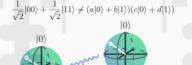




Multiple qubits form a register. The number of computational states doubles with each new qubit. A state with multiple qubits involved is often denoted like  $|00\rangle = |0\rangle \otimes |0\rangle$  (where  $\otimes$  is the tensor product)

1	2	$\bigcirc\!\!\!\bigcirc_{_{[0]}}\bigcirc\!\!\!\!\bigcirc_{_{[1]}} \frac{1}{\sqrt{2}} 0\rangle - \frac{1}{\sqrt{2}} 1\rangle$
2	4	$ \textcircled{$ \textcircled{$ \textcircled{$ \textcircled{$ \textcircled{$ \textcircled{$ \textcircled{$ \textcircled{$ \textcircled{$ \textcircled$
3	8	$ \bigoplus_{i\in \Phi_{   }} \frac{\frac{1}{2\sqrt{2}} 000\rangle - \frac{1}{2\sqrt{2}} 001\rangle - \frac{1}{2\sqrt{2}} 010\rangle + \frac{1}{2\sqrt{2}} 011\rangle}{\frac{1}{2\sqrt{2}} 011\rangle + \frac{1}{2\sqrt{2}} 01$

Two or more qubits can be entangled meaning that the state cannot be factorized as a product of states:



Entanglement Entanglement between two qubits can be created, for example,

|1)

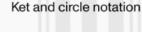


#### **One-Qubit Gates**

Gate

Pauli-X is a 180° rotation around the x-axis; also known as the quantum NOT gate

Matrix













 $|0\rangle = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$   $|1\rangle = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$ 



Y	Pauli-Y is a 180° rotation around the y-axis
	yanis





 $(1 \quad 0)$ 

 $\begin{pmatrix} 0 & -1 \end{pmatrix}$ 















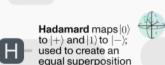












S is a 90° rotation around the z-axis:

The inverse S rotates

in the opposite direction

S S = Z

rotation around





























T is a 45° rotation around the z-axis; The inverse notates in the opposite direction

 $(1 \ 0)$ 

 $a|0\rangle + b|1\rangle$ 

(S)

Quantum circuits are a model to visualize operations on qubits.

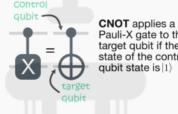


Binary and decimal: You will find both the use of the binary representation of qubit states as well as the

Decimal	Binary	Decimal	Binary
0>	000 angle means that the first	$ 4\rangle$	$ 100\rangle$
$ 1\rangle$	$ 001\rangle$ and second qubit are $ 1\rangle$ and the third	$ 5\rangle$	$ 101\rangle$
$ 2\rangle$	$ 010\rangle$ qubit is $ 0\rangle$	$ 6\rangle$	$ 110\rangle$
$ 3\rangle$	$ 011\rangle^{r}$	$ 7\rangle$	$ 111\rangle$

Matrix

## Multi-Qubit Gates



the	1 1	U	U	U
ne	0	1	0	0
ntrol	0	0	0	1
)	0	0	1	0
	`			,



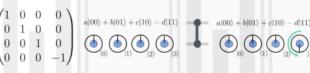




# gubits # basis states



Ket and circle notation





SWAP swaps the state of 2 qubits; can be implemented using 3 alternating

Toffoli applies a

Pauli-X gate to the target gubit if both

control gubits are in

state |1); can be used to construct a

reversible version of

the classical AND-gate

qubit if the state of the control qubit is  $|1\rangle$ 



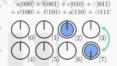












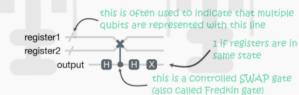
# **Building Blocks for** Quantum Algorithms

There are many clever ways to arrange quantum circuits. A couple of them are depicted below.

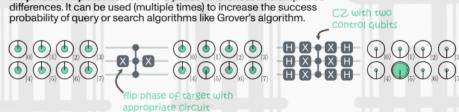
Increment & decrement are used to add or subtract one from a register and are an example of how to do arithmetic with quantum gates.



Swap test allows for checking how similar the states in two registers are.



Amplitude Amplification converts phase differences into amplitude



Quantum Fourier Transform can reveal the signal frequency in a register. Among other algorithms, it is used in Shor's algorithm for factoring numbers and computing the discrete logarithm.

