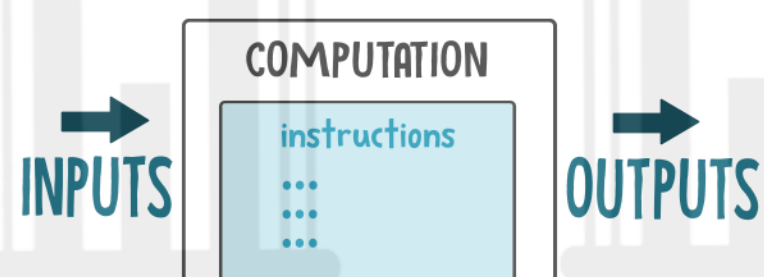


# QC CLASSICAL COMPUTING

## HISTORY OF CLASSICAL COMPUTING

### What is COMPUTATION

A mathematical calculation that maps inputs to an output based on a set of instructions

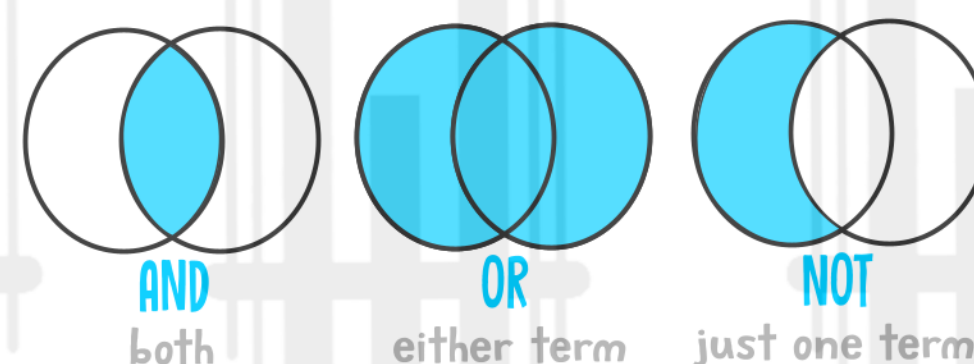


### BIT-SIZED history of computing

- ★ 1939 Turing machine
- ★ 1946 the Eniac
- ★ 1949 the Modem
- ★ 1957 Fortran, Hard-drive, Ramac
- ★ 1961 the Mouse
- ★ 1968 RAM
- ★ 1969 the Arpanet
- ★ 1970 Mp 944
- ★ 1971 Intel 4001, Floppy
- ★ 1972 Pong, {C}
- ★ 1973 Ethernet cable
- ★ 1975 8800 Altair
- ★ 1977 the Apple 2
- ★ 1979 C++

## BOOLEAN LOGIC

Boolean Logic: maps input bit(s) to output bit(s)



Logic gates + Truth tables

Logic: maps input bit(s) to output bit(s)

Tables: tells us the output of a logical operation

## GATES 1 BIT

GATES: NOT  
Flips the bit



INPUT	OUTPUT
0	1
1	0

GATES: FANOUT  
Copies the bit



a	OUTPUT
0	00
1	11

## GATES 2 BIT

GATES: AND  
Outputs 1 if both are 1, outputs 0 otherwise



a	b	OUTPUT
0	0	0
0	1	0
1	0	0
1	1	1

GATES: OR  
Outputs 1 if either of the inputs bits is 1  
outputs 0 if neither of the inputs bits is 1



a	b	OUTPUT
0	0	0
0	1	1
1	0	1
1	1	1

GATES: XOR  
Outputs 1 if either input bits are 1, but not both  
outputs 0 if neither or both bits are 1



a	b	OUTPUT
0	0	0
0	1	1
1	0	1
1	1	0

## BASE-REPRESENTATIONS

"Learning to think like a computer"

### DECIMALS

- ★ Decimal number system is based on numerical digits 0-9
- ★ Base determines how numbers get represented and how we perform arithmetic operations

Example:

$$6 = 6 \\ = (6 \cdot 10^0)$$

$$36 = 30 + 6 \\ = (3 \cdot 10^1) + (6 \cdot 10^0)$$

$$536 = 500 + 30 + 6 \\ = (5 \cdot 10^2) + (3 \cdot 10^1) + (6 \cdot 10^0)$$

### BINARY

- ★ We can describe any number with BITS

- ★ Base-2 is one of the most important bases for performing computation
- ★ It is binary, only 0 and 1
- ★ Also referred to as a BIT

- ★ We can still do operations; all of the operations in a classical computer happen by manipulating BITS

Converting:

$$1010 \rightarrow \text{decimal} \\ = (1 \cdot 10^3) + (0 \cdot 10^2) + (1 \cdot 10^1) + (0 \cdot 10^0)$$

$$1010 \rightarrow \text{binary} \\ = (1 \cdot 2^3) + (0 \cdot 2^2) + (1 \cdot 2^1) + (0 \cdot 2^0) = 8 + 2 = 10$$

## BITS: ARITHMETIC OPERATIONS

"How computers compute"

### BINARY ADDITION

- ★ Similar to the decimal we are used to
- ★ BITS carry over when the sum becomes larger than 2

$$\begin{array}{r} 0 + 0 = 0 \\ 0 + 1 = 1 \\ 1 + 0 = 1 \\ 1 + 1 = 10 \end{array}$$

### MULTIPLYING BITS

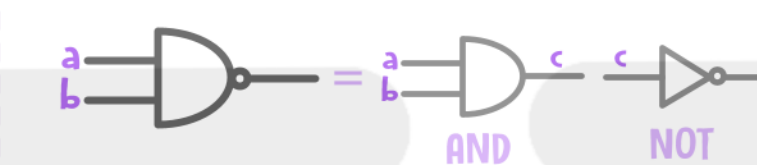
- ★ It is the same as binary multiplication
- ★ It's like "normal" (the decimal one)

$$\begin{array}{r} 0 \cdot 0 = 0 \\ 0 \cdot 1 = 0 \\ 1 \cdot 0 = 0 \\ 1 \cdot 1 = 1 \end{array}$$

## UNIVERSALITY

Any computation operation can be made by using a combination of {NOT, AND, OR, FANOUT}

GATES: NAND (NOT + AND)



a	b	c
0	0	0
0	1	0
1	0	0
1	1	1

c	OUT
0	1
1	0

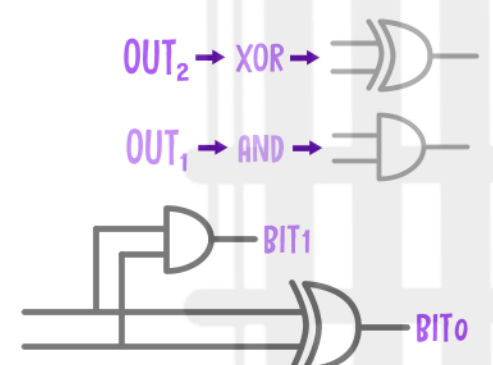
a	b	OUT
0	0	1
0	1	1
1	0	1
1	1	0

"Let's make a binary adder with the gates we have"  $a + b =$

a	b	OUT <sub>1</sub>	OUT <sub>2</sub>
0	0	0	0
0	1	0	1
1	0	0	1
1	1	1	0

a	b	BIT <sub>0</sub>
0	0	0
0	1	1
1	0	1
1	1	0

a	b	BIT <sub>1</sub>
0	0	0
0	1	0
1	0	0
1	1	1



## REVERSIBILITY

Given the output of a gate, we can determine what the inputs are

REVERSIBLE GATE preserves all the information

NON-REVERSIBLE GATE loses some information