

# Artificial Model Building

(searching for dispersed signals in the  
LHC search results)

# Disclaimer

What I wish to present here, is a proof of principle, no more.

(But hey, I will show running code, that mostly doesn't crash!)

The bigger philosophy behind this goes as follows:

We have all these hundreds of wonderful LHC results (simplified models results, to be more concrete). Not to mention non-LHC data.

**Let's maximally combine results and data-mine and machine-learn the sh\*t out of them!**

# This – I shall claim – is an interesting BSM model

1000 --

$\tilde{u}_L$   
ATLAS-SUSY-16-07  
CMS-SUS-13-012  
ATLAS-CONF-13-047  
ATLAS-CONF-13-054

Signal strength multipliers:  $\tilde{u}_L = 0.88, \tilde{b}_1 = 1.22, \tilde{t}_1 = 0.74, \tilde{\chi}_1^+ = 1.03$   
Contributions by particles:  $\tilde{u}_L = 0.76, \tilde{t}_1 = 0.72, \tilde{\chi}_1^+ = 0.08, \tilde{b}_1 = 0.15$

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$Z=3.25$

800 --

$\tilde{t}_1$   
ATLAS-CONF-13-047  
CMS-SUS-13-012  
ATLAS-CONF-13-037  
ATLAS-CONF-13-054  
ATLAS-SUSY-15-02

700 --

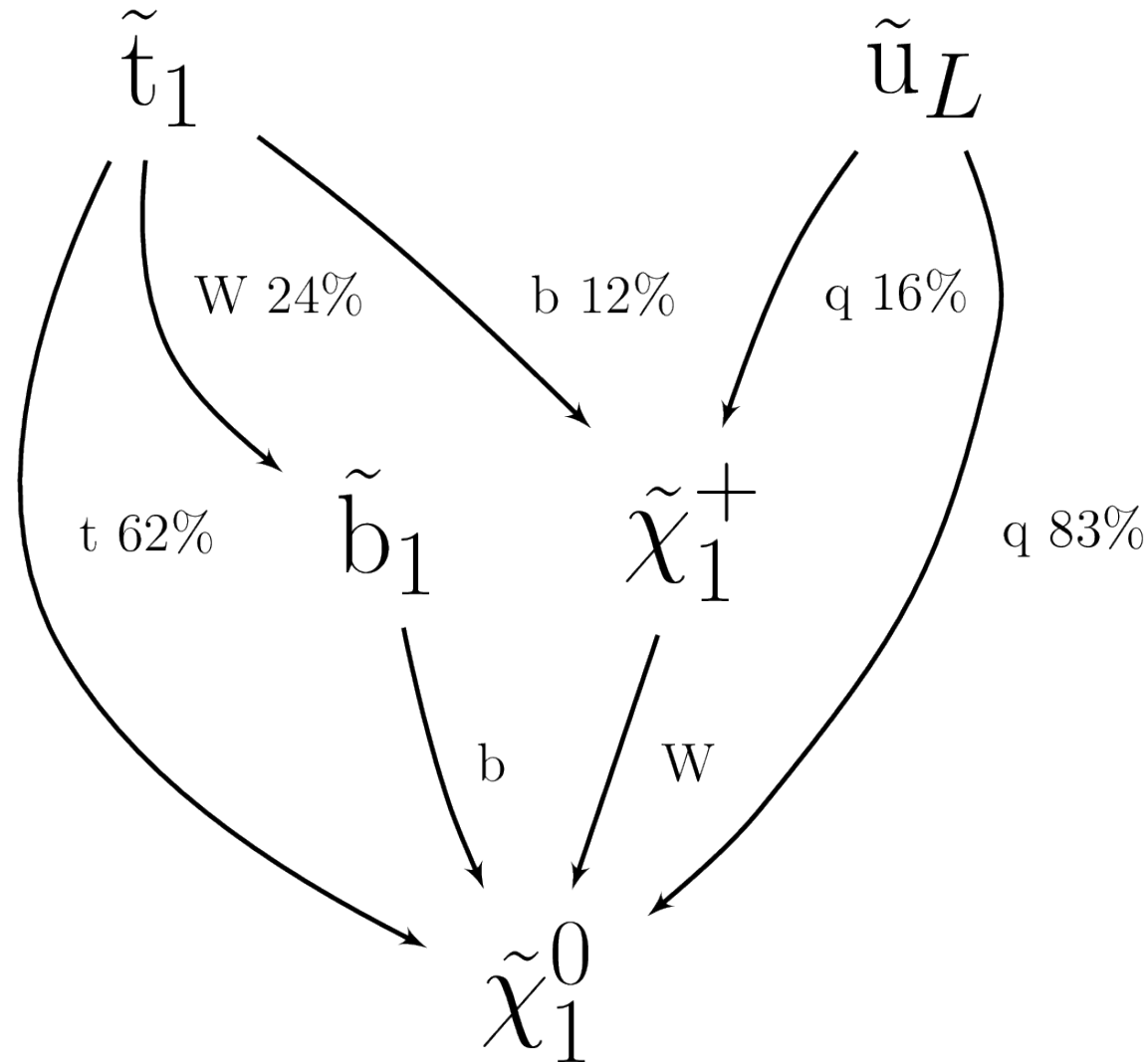
600 --

$\tilde{\chi}_1^+$   
ATLAS-SUSY-13-11  
CMS-SUS-13-012

500 --

$\tilde{b}_1$   
CMS-SUS-13-012  
ATLAS-CONF-13-047

$\tilde{\chi}_1^0$



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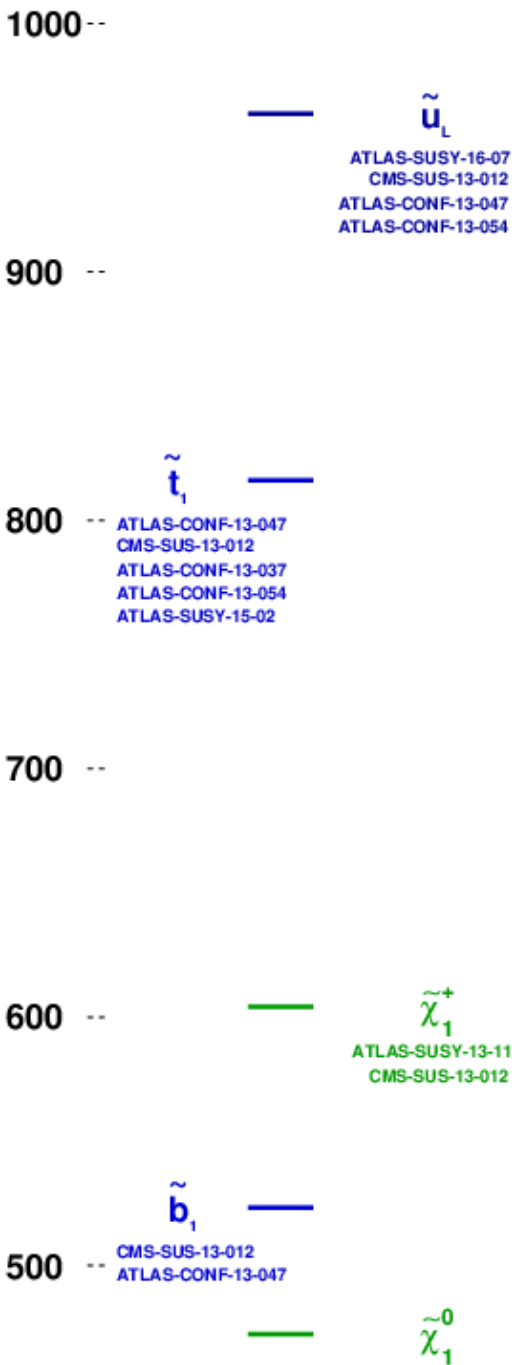
500 --

$\tilde{b}_1$   
CMS-SUS-13-012  
ATLAS-CONF-13-047

$\tilde{\chi}_1^0$

- Dark matter candidate +/- compatible with the WIMP miracle
- Spectrum +/- compatible with natural SUSY (stop < 1 TeV, can accommodate a gluino < 2.5 TeV)

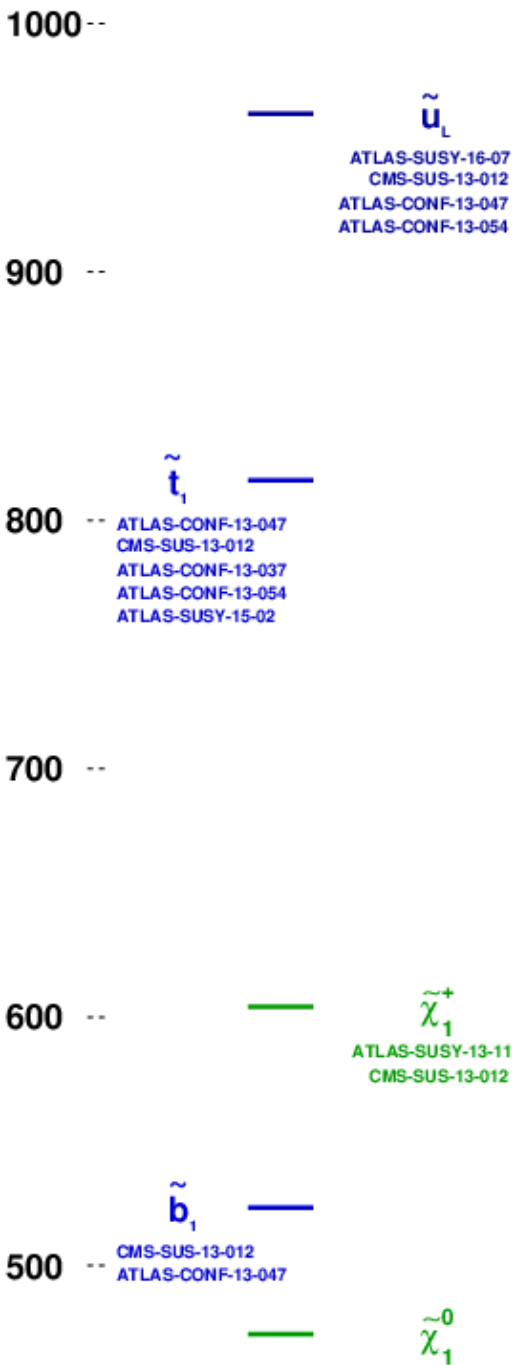
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- 42 SMS results of the SModelS database apply. None can exclude the model. With  $r := \sigma(\text{theory})/\sigma(\text{upper limit})$ , the highest  $r$  values are

CMS-SUS-16-032:T2bb  $r=0.56$ ,  $r_{\text{exp}}=\text{N/A}$   
 CMS-SUS-16-036:T2bb  $r=0.49$ ,  $r_{\text{exp}}=0.29$   
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- Consider that we combine the respective topologies and analyses listed on the left, and treat it as a single BSM model with an overall signal strength  $\mu$  as the only free parameter. Testing for compatibility with the Standard Model results in a test statistic  $Z$  (significance) of 3.25.

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Where does the significance Z come from?

- `- ATLAS-SUSY-2015-02:SR1 (EM, T2tt)  
nobs: 12, nbg: 5.5 +/- 0.72
- `- ATLAS-SUSY-2016-07:2j\_Meff\_1200 (EM, T2)  
nobs: 611.0, nbg: 526.0 +/- 31.0
- `- ATLAS-CONF-2013-037:SRtN3 (EM, T2tt)  
nobs: 7, nbg: 5.0 +/- 2.0
- `- ATLAS-CONF-2013-047:A Medium (EM, T2\*)  
nobs: 135, nbg: 122.0 +/- 18.0
- `- ATLAS-CONF-2013-054:8j50 flavor 0 b-jets (EM, T2\*)  
nobs: 40, nbg: 35.0 +/- 4.0
- `- ATLAS-SUSY-2013-11:WWc-DF (EM, TChiWW)  
nobs: 11, nbg: 9.0 +/- 2.2
- `- CMS-SUS-13-012:3NJet6\_1000HT1250\_600MHTinf (EM, many)  
nobs: 32, nbg: 22.8 +/- 5.2

(In that run we didn't produce "likelihoods from limits" → only efficiency-map based results)

How was this model constructed?

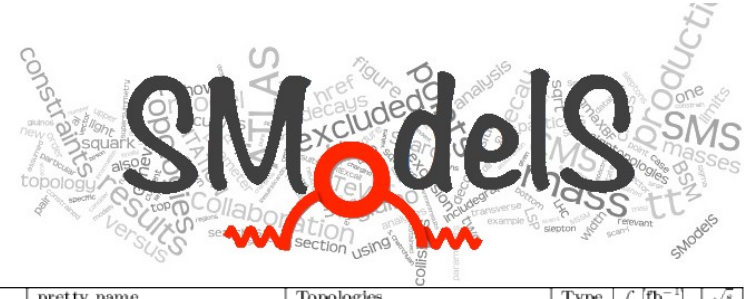


# How was this model constructed?

Two new components on top of SModelS:

- An analysis combiner algorithm that finds the optimal “legal” combination of analysis results.
- In this talk, “optimal” means “maximizing the significance  $Z$  while evading all exclusions”. Other criteria can however be employed (finding BSM models that are interesting in a different way).
- Different choices of what are “legal” combinations are possible. In this talk I am using “aggressive” combination: signal regions must be clearly distinct. Control regions are ignored.
- A “model builder” that randomly constructs BSM models in a Metropolis-Hastings-like fashion.
  - The walker starts from the Standard Model
  - It may randomly introduce and “kill” BSM particles.
  - It may randomly change masses of particles.
  - It may randomly change branching ratios.
  - The cross section is computed as if it were a SUSY model. However, the walker may randomly change particle-specific signal strength modifiers that are applied to the computed cross sections.
  - A neural network that learns to predict the “score” of the combiner, and then uses the gradient of the score instead of a random step may speed things up.

# SModels database



[illegible]

**green: uncorrelated, red: correlated, white: no likelihood**

many pairs of analyses  
can be treated as  
**approximately  
uncorrelated** in the  
“aggressive combination”  
scheme  
(the **green** blocks, think  
e.g. of a 8 TeV ATLAS  
result and a  
13 TeV CMS result)

<https://phystev.cnrs.fr/wiki/2019:groups:tools:correlations>

- finds optimal combinations of analyses, combinability given by matrix in slide before
- if a result can be added to a combination, it *has to be* added.
- will implement different criteria for what is considered “optimal”. In this talk, optimal means, it finds the combination that maximally falsifies the standard model hypothesis in a likelihood ratio test.

So we optimize for the test statistic of the hypothesis test, where the standard model is the null hypothesis and the BSM model is the alternative hypothesis with an overall signal strength multiplier as the only free parameter. That way Neyman-Pearson Lemma holds, at least in principle, as  $\mu=0$  gives the Standard Model. Since I search for models that maximize T, I do not compute a p value, as it would be misleading. **One should refrain from giving the test statistic a probabilistic meaning. In the next iteration I will want to replace it with a Bayes factor.**

- All models have to evade all exclusions of all results in the SModelS database (though I relaxed the requirement a bit since strictly speaking we are “allowed” to violate one out of twenty 95% exclusions).



# Houston, we have a problem!

CMS analyses with  
no digital SMS results

CMS-PAS-SUS-18-006  
CMS-PAS-SUS-19-005  
CMS-PAS-SUS-18-005  
CMS-PAS-SUS-18-005  
CMS-SUS-17-011  
CMS-SUS-17-006  
CMS-SUS-16-017  
CMS-SUS-16-048  
CMS-SUS-16-008  
CMS-SUS-16-003  
CMS-SUS-15-012  
CMS-SUS-15-004  
CMS-SUS-15-011  
CMS-SUS-15-005  
CMS-SUS-15-006  
CMS-SUS-15-003  
CMS-SUS-17-003  
CMS-SUS-17-012  
CMS-PAS-SUS-17-002

(The fix would be utterly simple. Just put the root files online, as was done in the past)

CMS analyses with  
no (simple) way to construct  
an approximate likelihood

CMS-PAS-SUS-17-004  
CMS-SUS-16-032  
CMS-SUS-16-034  
CMS-SUS-16-035  
CMS-SUS-16-037  
CMS-SUS-16-039  
CMS-SUS-16-041  
CMS-SUS-16-042  
CMS-SUS-16-043  
CMS-SUS-16-045  
CMS-SUS-16-046  
CMS-SUS-16-047  
CMS-SUS-17-001  
CMS-EXO-12-026  
CMS-PAS-SUS-13-018  
CMS-PAS-SUS-13-023  
CMS-SUS-13-004  
CMS-SUS-13-006  
CMS-SUS-13-019

(once we have expected upper limits, we are in the business. give us efficiency maps and we can go to the moon)

- Possible random steps:

- (we use the NLO SUSY cross sections for defaults)

- s)
- 
- The figure consists of three subplots illustrating the evolution of a trajectory in a parameter space defined by  $\theta_1$ ,  $\theta_2$ , and  $\theta_3$ .
- Top Plot:** A 1D line representing the  $\theta_1$  axis, ranging from -7 to -1. A red star marks the point at  $\theta_1 = -5$ .
  - Middle Plot:** A 2D plane representing the  $\theta_1$ - $\theta_2$  plane. The  $\theta_1$  axis ranges from -5 to -1, and the  $\theta_2$  axis ranges from 2 to 8. A red star marks the point at  $(\theta_1, \theta_2) = (-3, 3)$ .
  - Bottom Plot:** A 3D volume representing the  $\theta_1$ - $\theta_2$ - $\theta_3$  space. The  $\theta_1$  axis ranges from -7 to -1, the  $\theta_2$  axis ranges from 2 to 8, and the  $\theta_3$  axis ranges from 0 to 5. A red star marks the point at  $(\theta_1, \theta_2, \theta_3) = (-3, 3, 3)$ .

<http://www.hephy.at/user/wwaltenberger/models/mcmc.webm>

# Ach, come on – it's just a game!

Loosely speaking, we can think of it as a game, in the game-theoretical sense. Played between the algorithm that tries to exclude the model (“excluder”, “experimentalist”), and the algorithm that tries to build a model that maximally violates the Standard Model hypothesis (“builder”, “theorist”).

$$\hat{M} \equiv \operatorname{argmax}_{M:\text{models}} Z(M) \left| \max_{i:\text{results}} (r_i(M)) \lesssim 1.5 \right.$$

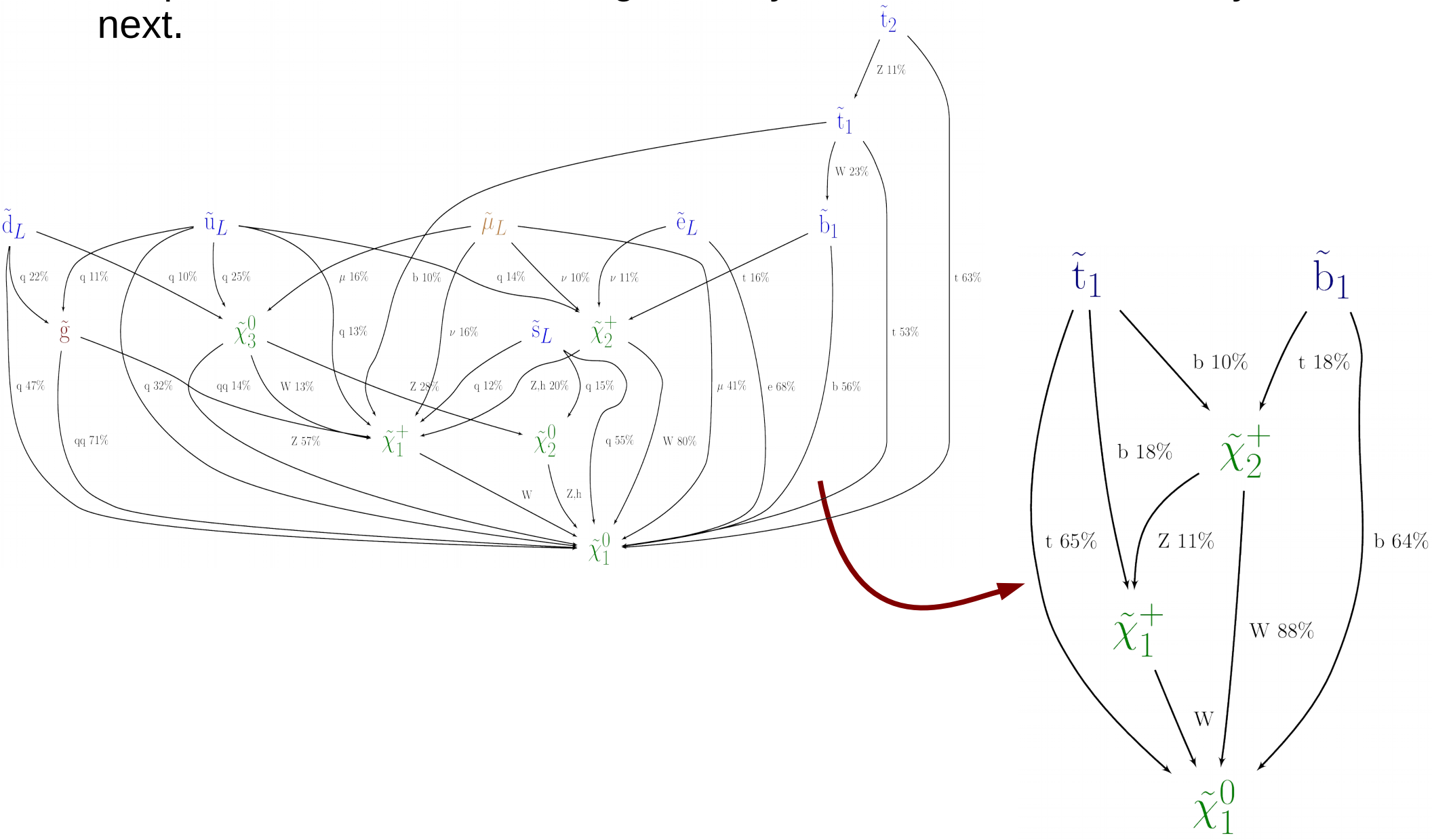
$r_i$ : predicted signal strength / experimental upper limit, for the result (combination) “i”

(Ok, ok, I guess one could also think of it as “optimization with constraints”.  
But that sounds so much less cool.)



# Trimming

After having found models of interest, we trim them. First we try to take out particles and see if that significantly reduces the score. Decays are next.





# To repeat: this is what the algorithm found after $O(100)$ steps

1000 --

$\tilde{u}_L$   
ATLAS-SUSY-16-07  
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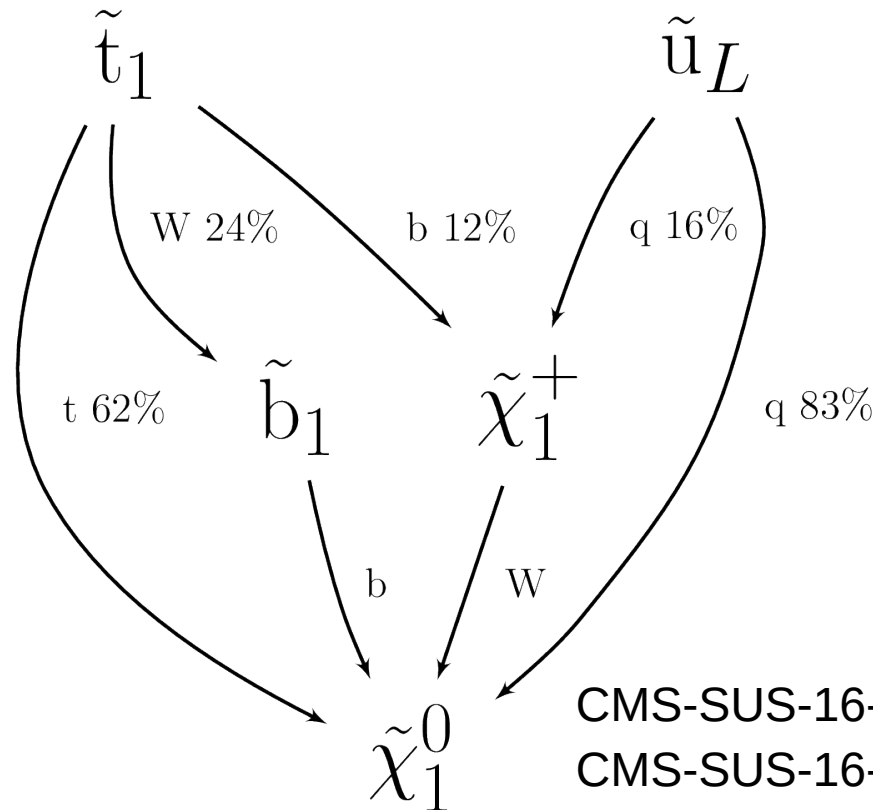
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500 --

$\tilde{b}_1$   
CMS-SUS-13-012  
ATLAS-CONF-13-047

$\tilde{\chi}_1^0$

(And no, I have no idea if the model was still interesting, were we to fully recast all analyses)

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**Proof-of-concept only**  
**Many aspects are still buggy /**  
**wrong / crude / ....**

700 --

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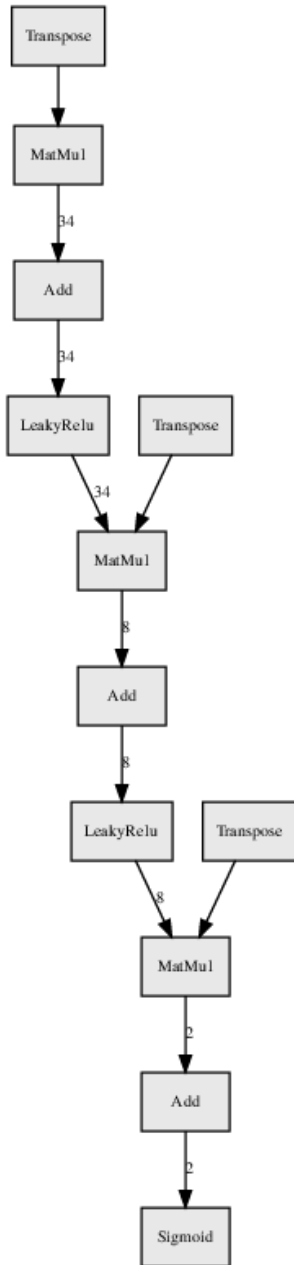
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# To Do



- Try learning different criteria, e.g. most “spectacular” signatures that miraculously evade all SMS constraints.
- Train a neural network that predicts the objective function (e.g. the significance  $Z$  for the builder,  $r_{\max}$  for the excluder) → differentiable function, should make for much faster convergence (as long as we only want central values)
- Add the most recent results (CMS, what shall we do?)
- Allow also for displaced signatures (widths as free parameters? computed widths?) [SModelS 2.0.0]
- Constraints from **measurements** may be added via **likelihoods on Wilson coefficients**.
- Compute the **distribution of** the test statistic **T** under the Standard Model assumption.
- SModelS actually gives much more detailed feedback than just a single test statistic. Make use of it.
- Long term vision: to have a full, real sample of a posterior in model space.
- Can we / should we move from SLHA files to **arbitrary Lagrangians** (described eg as UFO or Sarah files)?

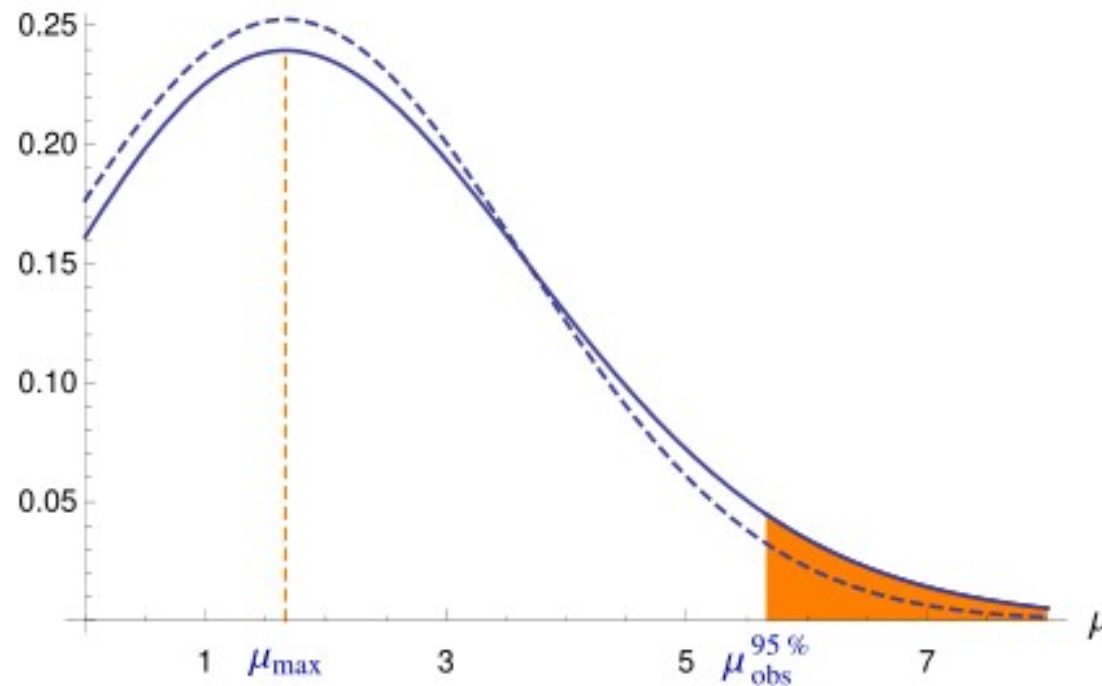
# Epilogue

The model shown was obtained before we had our experimental “likelihoods from limits” code in place. After adding these likelihoods, a few CMS results (CMS-SUS-16-051, CMS-SUS-16-033) pretty much ruined the Z score. Here is the best model obtained so far after having added these likelihoods:

Backup

# Likelihoods from limits

When we have observed **and** expected upper limits, we compute an approximate truncated Gaussian likelihood from it (procedure taken from arXiv:1202.3415)



# Communication of Likelihoods

CMS has introduced the simplified likelihoods (thanks a lot!),

[CMS-NOTE-2017-001](#)

The authors of that paper have addressed a conceptual problem when dealing with “deeply Poissonian regions (very small expected counts) in version 2 of the formalism,

[“The Simplified likelihood framework”](#)

ATLAS has only recently published their alternative to CMS’s simplified likelihoods,

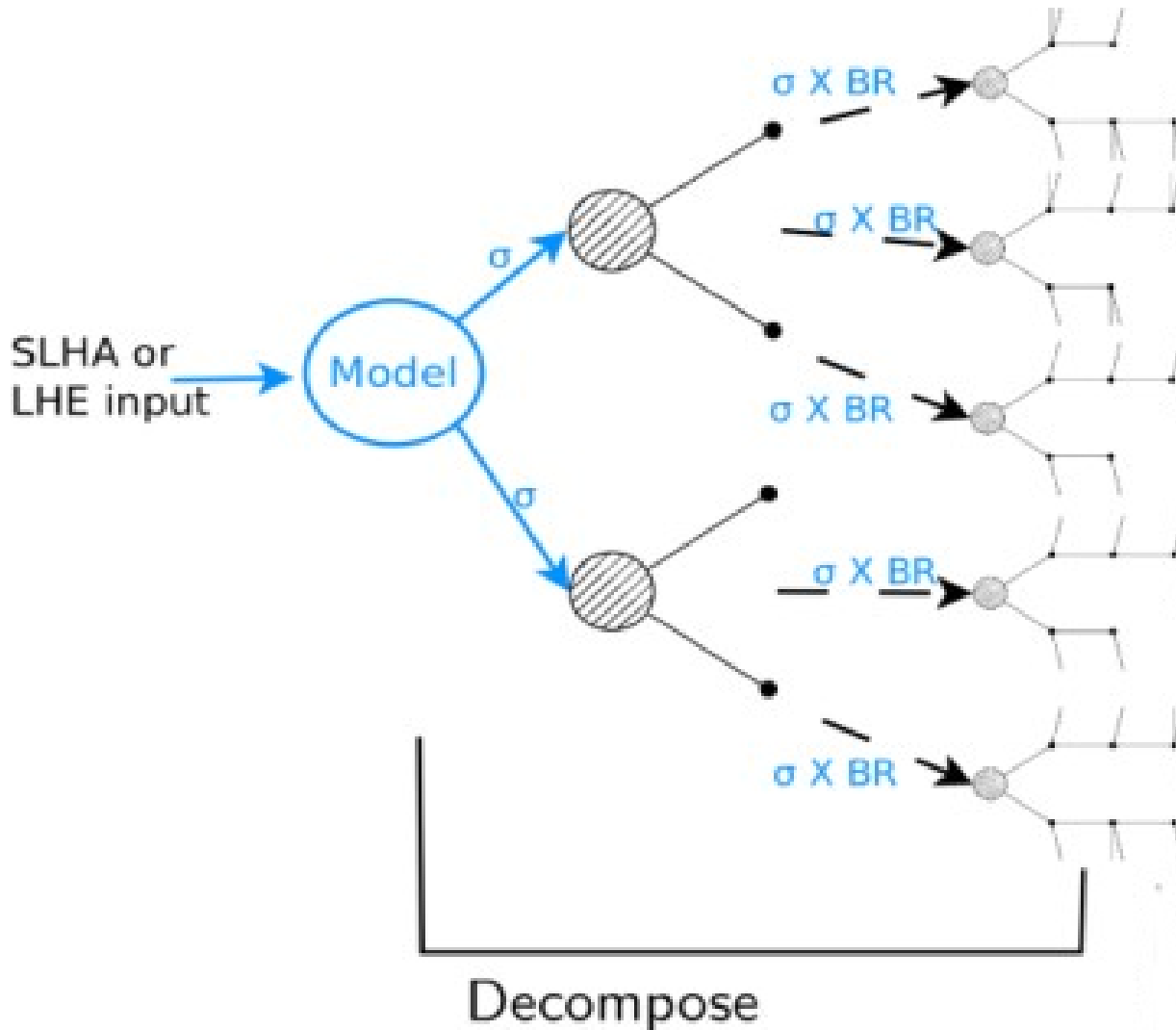
[ATL-PHYS-PUB-2019-029](#)

SModelS has implemented CMS’s simplified likelihoods, will implement ATLAS’s histogram-factory based approach in the future.





# 1) Decomposition of a fundamental model

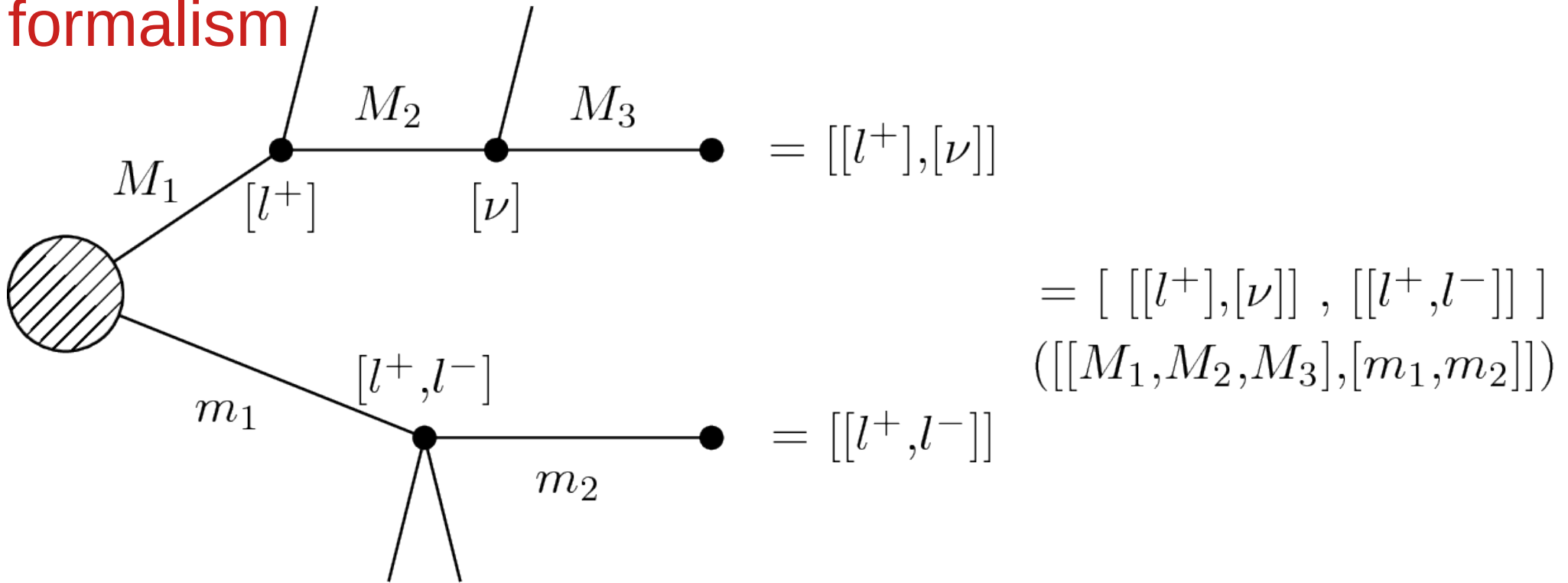


**Input:** SLHA file (mass spectrum, BRs) or LHE file (parton level)

Currently the model must have a  $\mathbf{Z}_2$  symmetry

The decomposition produces a set of simplified model topologies (dubbed “elements”)

## 2) Description of the topology in the SModelS formalism /



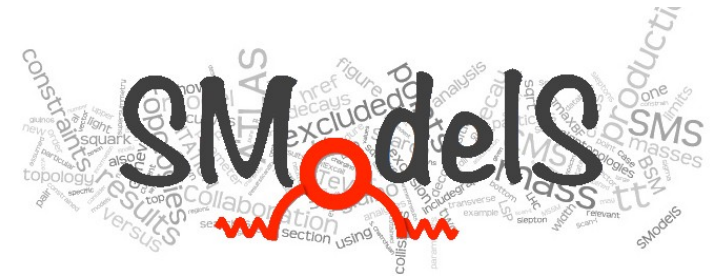
**Each topology is described by:**

- Topology shape + final states
- BSM masses
- $\sigma \times \text{BR}$

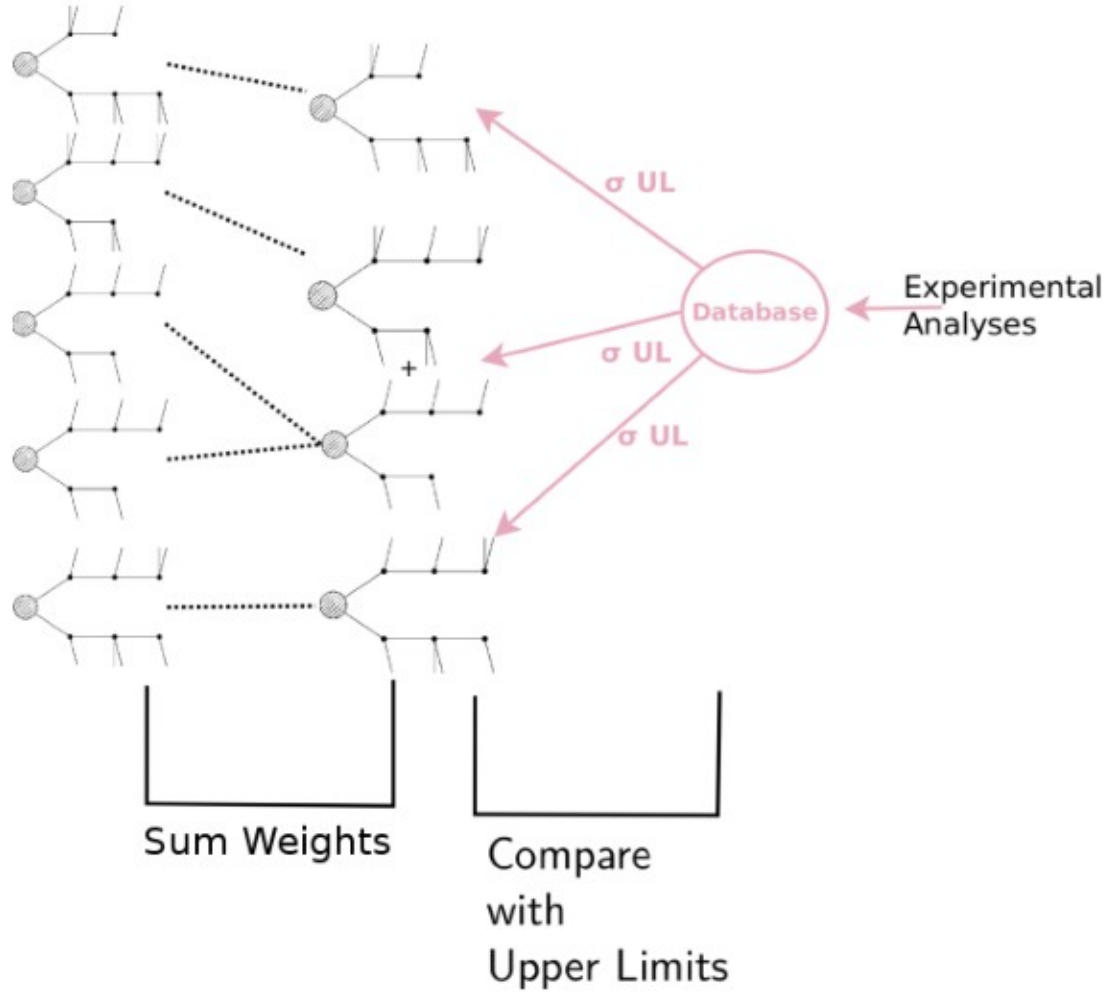
We (currently) ignore spin, color, etc of the BSM particles

It is model independent, there is no reference to the original model

# Recap: How SModels works



### 3) Comparison of predicted signal strengths with experimental result:



- **Upper Limit Results:**  
 Predicted signal strength =  $\sigma \times \text{BR}$   
 Experimental result:  $\sigma_{\text{UL}}$
- **Efficiency Map Results:**  
 Predicted signal strength =  $\sum \sigma \times \text{BR} \times \epsilon$   
 Experimental result:  $\sigma_{\text{UL}} = N_{\text{UL}} / L$  from  $N_{\text{observed}}$ ,  $\text{expected(BG)}$ ,  $\text{error(BG)}$
- $r = \text{predicted} / \sigma_{\text{UL}}$
- Model is excluded if most constraining analysis has  $r > 1$