PROJECT ASSIGNMENT #1: COMBUSTION THERMODYNAMICS



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Submitted to: Professor. Jeffrey Bergthorson

Part I – Introduction to thermodynamics data:

Results from using the report of McBride et al.:

	C8H18	O2	N2	CO2	H2O	CO	H2
Enthalpy at 298.15K (KJ/mol)	-224.009	0.000	0.000	-393.508	-241.825	-110.535	0.000
Entropy at 298.15K (KJ/mol-K)	0.423	0.205	0.192	0.214	0.189	0.198	0.131
Enthalpy at 2000K (KJ/mol)	552.096	59.201	56.136	-302.071	-168.782	-53.799	52.950
Entropy at 2000K (KJ/mol-K)	1.171	0.269	0.252	0.309	0.265	0.259	0.188

Part II - Complete combustion

1. Global reaction equations

At stoichiometric($\Phi = 1$)

$$C_8H_{18} + 12.5(O_2 + N_2) \rightarrow CO_2 + H_2 + 47N_2$$

Fuel lean($\Phi < 1$):

$$\Phi C_8 H_{18} + 12.5 (O_2 + 3.76 N_2) \rightarrow 8 \Phi C O_2 + 9 \Phi H_2 O + 47 N_2 + (-12.5 \Phi + 12.5) O_2$$

Fuel rich($\Phi > 1$):

$$\begin{array}{c} \Phi C_8 H_{18} + 12.5 (O_2 + 3.76 N_2) \rightarrow 0.8 \\ \Phi CO + 7.2 \\ \Phi CO_2 + (-15.2 \\ \Phi + 25) \\ H_2O \\ + (24.2 \\ \Phi - 25) \\ H_2 + 47 \\ N_2 \end{array}$$

2. LHV and HHV comparison

The lower heating value at 300K can be calculated as follows:

$$\widetilde{q_{LHV}} = -h(C_8H_{18}) - 12.5h(O_2) + 8h(CO_2) + 9h(H_2O_{(g)}) = -5100392.819kJ/kmol$$

$$q_{LHV} = \widetilde{q_{LHV}}/114 = -44.7407MJ/kg$$

The higher heating value at 300K can be calculated as follow:

$$\widetilde{q_{\rm HHV}} = -h(C_8H_{18}) - 12.5h(O_2) + 8h(CO_2) + 9h\big(H_2O_{(l)}\big) = -5496911.204kJ/kmol$$

$$q_{HHV} = \widetilde{q_{HHV}}/114 = -48.219Mj/kg$$

Comparing with literature value:

	Computed value (MJ/kg)	Course slide value (MJ/kg)	Internet researched value (MJ/kg)
LHV	-44.741	-44.430	-44.651
HHV	-48.219	-47.890	-48.119

• HHV is always higher than LHV since water exist latent heat for vaporization

Although there exists small gap between the computed value and course slide value, the computed values are highly aligned with the internet researched value from the book (S. McAllister et al., Fundamentals of Combustion Processes). In conclusion I think the difference is small and negligible.

3. Adiabatic flame temperature estimation with constant C_p:

Phi	Phi Tad_estimation (K) Phi		Tad_estimation (K)
0.5	1717.342545	1.05	2957.496077
0.55	1853.594189	1.1	2897.512477
0.6	1988.86009	1.15	2839.06114
0.65	2123.150906	1.2	2782.084094
0.7	2256.477143	1.25	2726.526258
0.75	2388.849157	1.3	2672.335256
0.8	2520.277154	1.35	2619.461263
0.85	2650.771199	1.4	2567.856842
0.9	2780.341209	1.45	2517.476812
0.95	2908.996967	1.5	2468.278106
1	3019.072992		

T_ad_estimation_max (K)	@ Phi
3019.072992	1

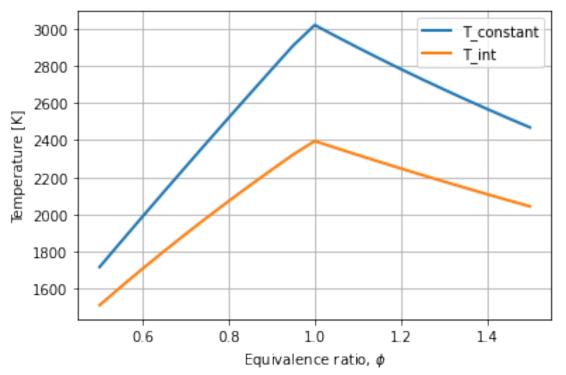
4. Adiabatic flame temperature estimation with integrated C_p:

Phi	Tad_integration (K)	Phi	Tad_integration (K)
0.5	1511.9443	1.05	2357.1678
0.55	1611.50358	1.1	2319.96217
0.6	1708.35635	1.15	2283.38067
0.65	1802.67053	1.2	2247.4029
0.7	1894.58947	1.25	2212.01499
0.75	1984.24193	1.3	2177.20214
0.8	2071.74254	1.35	2142.95009

0.85	2157.1948	1.4	2109.24511
0.9	2240.69285	1.45	2076.07393
0.95	2322.32287	1.5	2043.42374
1	2395.00973		

T_ad_integration_max (K)	@ Phi
2395.00973	1

5. Plot of T_ad against Φ :



The adiabatic flame temperature (y-axis) against Φ (x-axis)

Note that the T_constant in above figure stand for T_ad_estimation (constant Cp) and T_int stand for T ad integration.

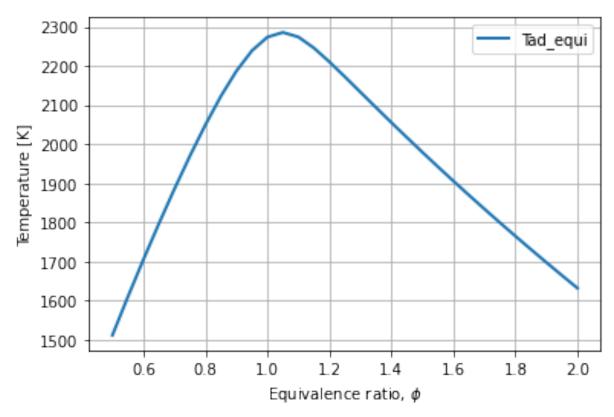
- Both plots have the same trend, peaked at $\Phi = 1$ since theoretically, fuel is fully oxidized to produce maximum heat output and no excessive product is formed to be heated by the heat released.
- The adiabatic flame temperature obtained from integrated Cp is much smaller than that from assuming the constant Cp, since Cp value is increasing as temperature increases. Therefore, the result is expected.

Part III – Calculation through Cantera:

1. The result and plot

The following result and plot are obtained at T=300K and 1 atm.

phi	T_ad_equi (K)	phi	T_ad_equi (K)
0.5	1511.33968	1.3	2132.87418
0.55	1609.68816	1.35	2093.79879
0.6	1704.82397	1.4	2055.06876
0.65	1796.71843	1.45	2016.83221
0.7	1885.16694	1.5	1979.14913
0.75	1969.67783	1.55	1942.03744
0.8	2049.3145	1.6	1905.49465
0.85	2122.50123	1.65	1869.50852
0.9	2186.81929	1.7	1834.06254
0.95	2238.78257	1.75	1799.1386
1	2273.55994	1.8	1764.71841
1.05	2285.63329	1.85	1730.78407
1.1	2273.84853	1.9	1697.31833
1.15	2245.77256	1.95	1664.30462
1.2	2210.23615	2	1631.72697
1.25	2171.95305		



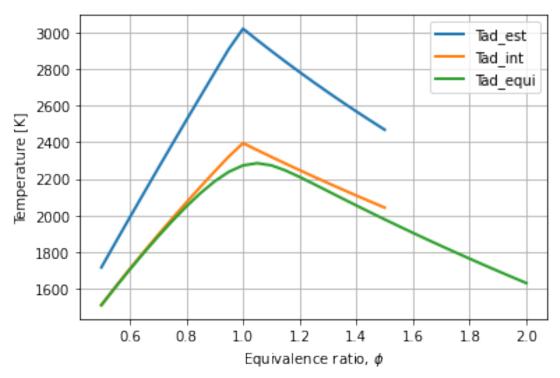
Adiabatic flame temperature vs Φ using cantera

2. Maximum flame temperature

T_ad_equilibrium_max (K)	@ Phi
2285.63329	1.05

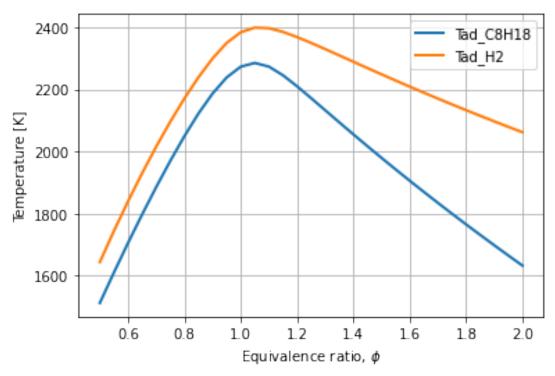
- The maximum adiabatic flame temperature occurred as slightly over stoichiometric equivalence ratio since the little added fuel in the reactant have promoted the combustion process
- The reaction could never make the isoocatane in the product to be zero, in the other word, there is always not-reacted isooctane left as product in the reaction, unless the pressure of the reaction approaches to infinite. Therefore, the C8H18 at stoichiometric ratio cannot have a complete combustion.
- CO2 formed in the product will dissociate into CO (H2O dissociate to H2 as well). Slightly more fuel in the reactant could also promote the reaction with CO formed in the reactant to contribute to full combustion.

3. Results comparison with Cantera and estimations



- The adiabatic flame temperature formed from using the integration Cp method is somewhat aligned with the result from Cantera.
- The plot from the integration method can be seen as the combustion result under 'optimal' and 'idealized' conditions
- The plot of the equilibrium condition in Cantera has the lowest adiabatic flame temperature, due to the fact that Cantera considers a lot non-idealized product and energy were taken up by those product to heat them up to the flame temperature. Hence, its temperatures are the lowest.

4. Bonus I – H2 compare with C8H18



Adiabatic flame temperature of two substances vs equivalence ratio

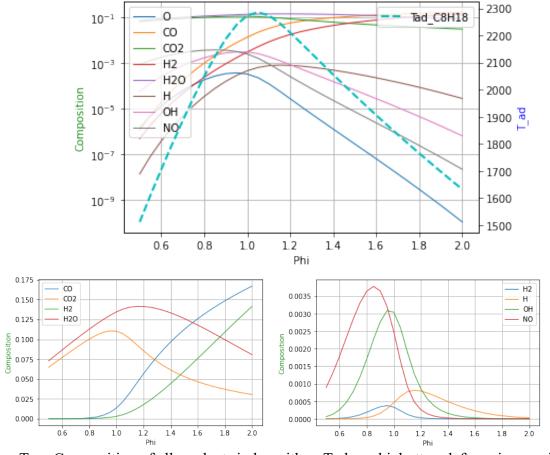
- The adiabatic flame temperature of hydrogen is higher than that of the isooctane since hydrogen contains more energy per mole of mass.
- H2 needs less energy per mole to dissociate it compare to C8H18, that could be one of the reasons why it has an increased adiabatic flame temperature compared to C8H18.

Part IV – Parameters affecting T_ad:

1. Species concentrations at different equivalence ratios:

phi	T (K)	О	Н	ОН	H2	Н2О	СО	CO2	NO
0.5	1511.34	1.53E-06	9.15E-04	9.15E-04	5.15E-07	7.50E-02	1.20E-06	6.67E-02	9.15E-04
0.55	1609.69	4.99E-06	1.35E-03	1.35E-03	2.02E-06	8.24E-02	5.44E-06	7.33E-02	1.35E-03
0.6	1704.82	1.36E-05	1.86E-03	1.86E-03	6.67E-06	8.97E-02	2.03E-05	7.98E-02	1.86E-03
0.65	1796.72	3.18E-05	2.41E-03	2.41E-03	1.92E-05	9.70E-02	6.45E-05	8.64E-02	2.41E-03
0.7	1885.17	6.54E-05	2.96E-03	2.96E-03	4.92E-05	1.04E-01	1.81E-04	9.28E-02	2.96E-03
0.75	1969.68	1.20E-04	3.45E-03	3.45E-03	1.15E-04	1.11E-01	4.56E-04	9.91E-02	3.45E-03
0.8	2049.31	1.96E-04	3.81E-03	3.81E-03	2.51E-04	1.18E-01	1.05E-03	1.05E-01	3.81E-03
0.85	2122.50	2.84E-04	3.97E-03	3.97E-03	5.11E-04	1.25E-01	2.24E-03	1.10E-01	3.97E-03
0.9	2186.82	3.63E-04	3.85E-03	3.85E-03	9.84E-04	1.32E-01	4.45E-03	1.15E-01	3.85E-03
0.95	2238.78	3.97E-04	3.40E-03	3.40E-03	1.81E-03	1.38E-01	8.27E-03	1.17E-01	3.40E-03
1	2273.56	3.55E-04	2.65E-03	2.65E-03	3.23E-03	1.44E-01	1.45E-02	1.18E-01	2.65E-03
1.05	2285.63	2.16E-04	1.53E-03	1.53E-03	4.86E-03	1.30E-01	2.07E-02	1.00E-01	1.53E-03
1.1	2273.85	1.16E-04	8.59E-04	8.59E-04	7.82E-03	1.31E-01	3.06E-02	9.36E-02	8.59E-04

1.15	2245.77	5.52E-05	4.51E-04	4.51E-04	1.17E-02	1.31E-01	4.15E-02	8.60E-02	4.51E-04
1.2	2210.24	2.52E-05	2.36E-04	2.36E-04	1.64E-02	1.30E-01	5.22E-02	7.86E-02	2.36E-04
1.25	2171.95	1.15E-05	1.25E-04	1.25E-04	2.16E-02	1.28E-01	6.19E-02	7.15E-02	1.25E-04
1.3	2132.87	6.66E-06	8.51E-05	8.51E-05	3.42E-02	1.58E-01	8.91E-02	8.20E-02	8.51E-05
1.35	2093.80	3.15E-06	4.77E-05	4.77E-05	4.25E-02	1.57E-01	1.01E-01	7.64E-02	4.77E-05
1.4	2055.07	1.50E-06	2.70E-05	2.70E-05	5.15E-02	1.55E-01	1.13E-01	7.14E-02	2.70E-05
1.45	2016.83	7.21E-07	1.54E-05	1.54E-05	6.11E-02	1.53E-01	1.23E-01	6.70E-02	1.54E-05
1.5	1979.15	3.46E-07	8.85E-06	8.85E-06	7.11E-02	1.50E-01	1.34E-01	6.31E-02	8.85E-06
1.55	1942.04	1.65E-07	5.10E-06	5.10E-06	8.16E-02	1.47E-01	1.44E-01	5.96E-02	5.10E-06
1.6	1905.49	7.89E-08	2.94E-06	2.94E-06	9.24E-02	1.43E-01	1.53E-01	5.65E-02	2.94E-06
1.65	1869.51	3.74E-08	1.69E-06	1.69E-06	1.03E-01	1.39E-01	1.62E-01	5.37E-02	1.69E-06
1.7	1834.06	1.76E-08	9.68E-07	9.68E-07	1.15E-01	1.35E-01	1.71E-01	5.12E-02	9.68E-07
1.75	1799.14	8.21E-09	5.53E-07	5.53E-07	1.26E-01	1.31E-01	1.80E-01	4.90E-02	5.53E-07
1.8	1764.72	3.78E-09	3.13E-07	3.13E-07	1.38E-01	1.26E-01	1.88E-01	4.69E-02	3.13E-07
1.85	1730.78	1.72E-09	1.77E-07	1.77E-07	1.50E-01	1.21E-01	1.96E-01	4.50E-02	1.77E-07
1.9	1697.32	7.72E-10	9.85E-08	9.85E-08	1.62E-01	1.16E-01	2.04E-01	4.33E-02	9.85E-08
1.95	1664.30	3.41E-10	5.45E-08	5.45E-08	1.74E-01	1.11E-01	2.12E-01	4.17E-02	5.45E-08
2	1631.73	1.48E-10	2.98E-08	2.98E-08	1.86E-01	1.06E-01	2.20E-01	4.02E-02	2.98E-08



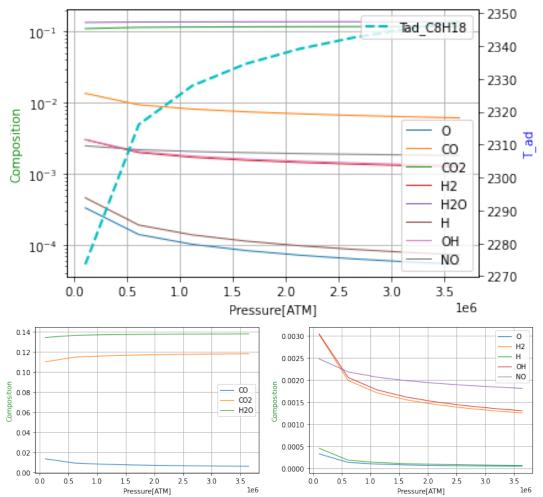
Top: Composition of all products in logarithm, Tad vs phi, bottom left: major species in linear vs phi, bottom right: minor species in linear vs phi

- Composition of CO and H2 have a significant increase as the equivalence ratio exceeds 1
- All other products have a favour of specific equivalence ratio to have a peak
- CO2 peaks at equivalence ratio = 1 since that's around the complete reaction, and no excess O2 are produced
- H2O peaks at equivalence ratio just passed 1, going onto the fuel rich side.
- The trend between CO2 and CO, H2O and H2 are very similar, CO2 and H2O both reach its peak right after the formation of CO and H2 starts.
- NO, O and OH peaks just before stoichiometric ratio, on fuel lean side.
- NO peaks since flame temperature at such equivalence ratio become high enough to oxidize the N2 in the product with O2 to form NO.
- The peak of O and OH are aligned since water will dissociate into O and OH together, hence they peaked at same ratio

2. Species concentrations at different pressures:

Pressure	T(K)	О	Н2	Н	ОН	H2O	NO	CO	CO2
101325	2273.559937	3.55E-04	3.23E-03	4.92E-04	3.25E-03	1.44E-01	2.85E-17	1.45E-02	1.18E-01
607950	2316.116999	1.49E-04	2.12E-03	2.03E-04	2.19E-03	1.45E-01	6.35E-17	9.95E-03	1.22E-01

1114575	2327.919851	1.09E-04	1.82E-03	1.47E-04	1.89E-03	1.46E-01	7.94E-17	8.66E-03	1.24E-01
1621200	2334.583337	8.87E-05	1.65E-03	1.20E-04	1.72E-03	1.46E-01	9.03E-17	7.93E-03	1.24E-01
2127825	2339.125652	7.64E-05	1.54E-03	1.04E-04	1.60E-03	1.46E-01	9.86E-17	7.43E-03	1.25E-01
2634450	2342.524247	6.78E-05	1.45E-03	9.22E-05	1.51E-03	1.47E-01	1.05E-16	7.05E-03	1.25E-01
3141075	2345.214007	6.14E-05	1.39E-03	8.36E-05	1.44E-03	1.47E-01	1.11E-16	6.75E-03	1.25E-01
3647700	2347.424599	5.64E-05	1.33E-03	7.69E-05	1.39E-03	1.47E-01	1.16E-16	6.50E-03	1.26E-01

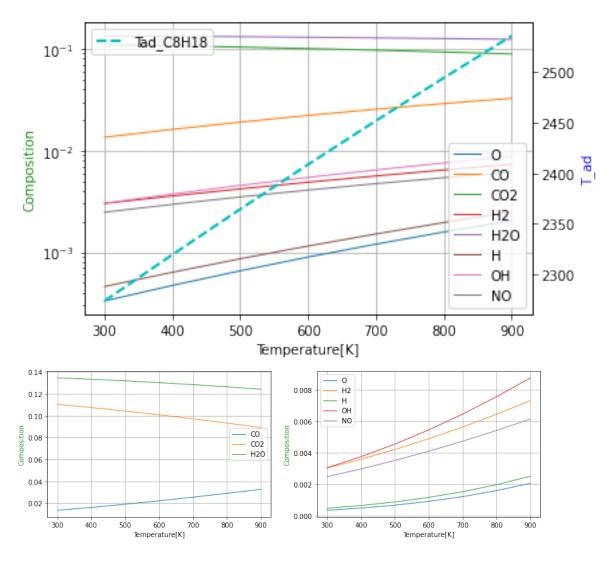


Top: Composition of all products in logarithm, Tad vs pressure, bottom left: major species in linear vs pressure, bottom right: minor species in linear vs pressure

- The molar fraction of CO2, H2O increases as pressure increases since they are the main product of the reaction.
- Molar fraction of all other minor species in the product decreases as the pressure increases.
- Both bullet points above have indicated a more complete combustion as pressure increases.
- A more complete combustion at higher pressure have made a higher adiabatic flame temperature. Therefore, the T_ad increases as pressure increases.

3	Species	concentration	at different	temperatures:
J.			at anicicit	terriberatures.

T_in	T (K)	О	H2	Н	ОН	H2O	СО	N	NO
300	2273.559937	3.55E-04	3.23E-03	4.92E-04	3.25E-03	1.44E-01	1.45E-02	1.18E-01	2.65E-03
400	2319.446165	5.06E-04	3.83E-03	6.82E-04	4.01E-03	1.43E-01	1.73E-02	1.15E-01	3.17E-03
500	2364.538248	7.06E-04	4.51E-03	9.27E-04	4.88E-03	1.41E-01	2.05E-02	1.12E-01	3.76E-03
600	2408.752787	9.67E-04	5.26E-03	1.24E-03	5.86E-03	1.40E-01	2.39E-02	1.08E-01	4.40E-03
700	2452.094131	1.30E-03	6.08E-03	1.63E-03	6.97E-03	1.38E-01	2.75E-02	1.05E-01	5.10E-03
800	2494.584992	1.71E-03	6.97E-03	2.12E-03	8.18E-03	1.37E-01	3.14E-02	1.01E-01	5.86E-03
900	2536.214896	2.22E-03	7.94E-03	2.72E-03	9.51E-03	1.35E-01	3.55E-02	9.68E-02	6.66E-03



Top: Composition of all products in logarithm, Tad vs T_in, bottom left: major species in linear vs T_in, bottom right: minor species in linear vs T_in

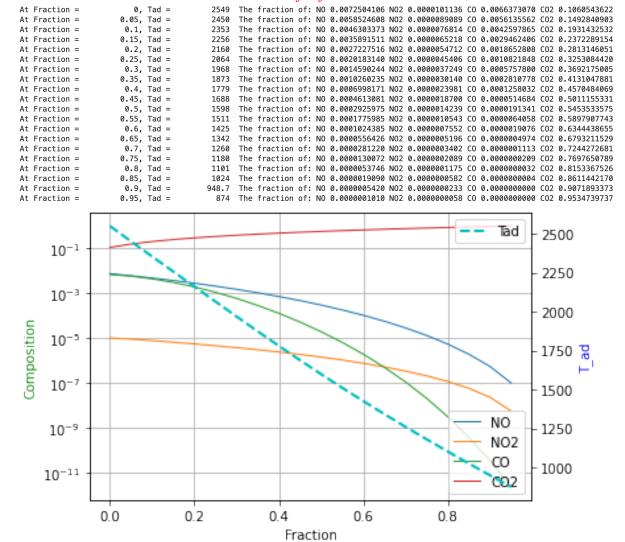
- As initial temperature increases, less major products (CO2 and H2O) are formed.
- As initial temperature increases, more minor species in the products are formed.

- Above two bullet points have indicated a less complete combustion process.
- Although adiabatic flame temperature increases as initial temperature increases. It has increased for less 400 K while T_in has increased for 600 K. Overall, the adiabatic flame temperature showed a decreasing trend, which is aligned with the theory that a less complete combustion should have a lower T_ad as a result, since not all chemical potentials of the reactants are released.

Part V - Effect of dilution on T ad:

1. Influence of CO2

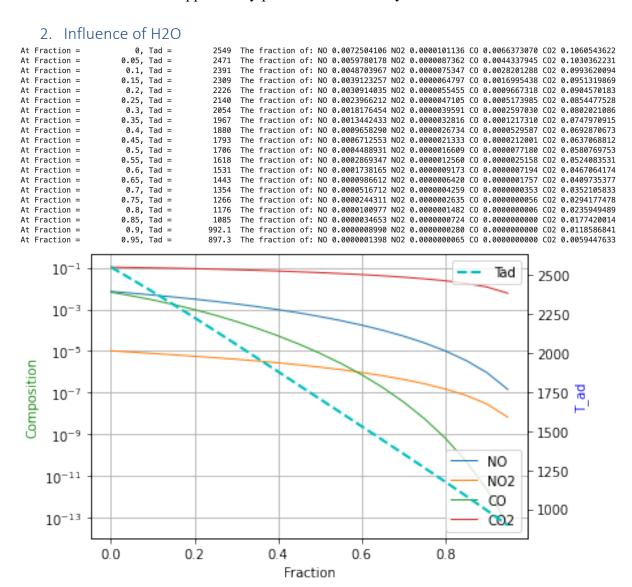
*Data was obtained using Cantera 2.6.0, csv files are not exportable in that version of Cantera for some reason, hence no table can be put out, please allow me to put a rough output result from jupyter, figures are exported using cached data. Instead of Gibbs solver, auto solver is selected to have a valid result for fraction over around 0,7.



Molar fraction of 4 products in log and adiabatic flame temperature vs fraction of CO2 diluted

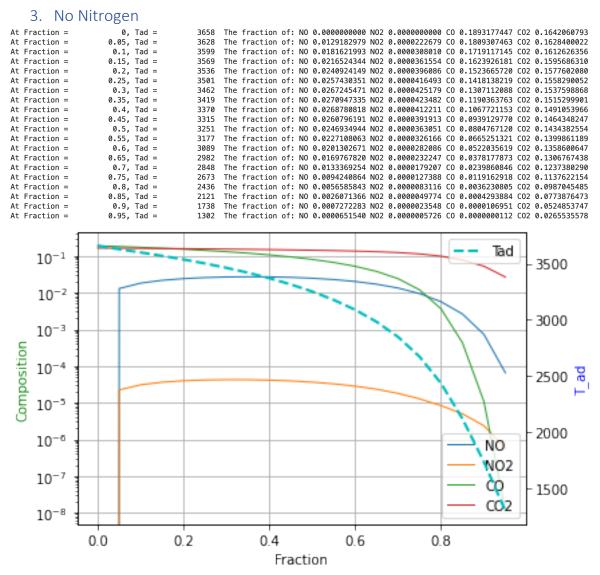
• As more fraction of CO2 gas is recirculated to dilute the reaction, less minor species, toxic gas, and pollutants are formed.

- Adiabatic flame temperature decreases as the fraction of CO2 increases since they do
 not participate in the reaction in theory and energy is required to heat up those
 molecules.
- The formation of NO decreases since the adiabatic flame temperature decreases.
- As the fraction increases, the reaction rate decreases. When fraction reaches 1, the reaction will be stopped in my prediction or at a very slow rate.



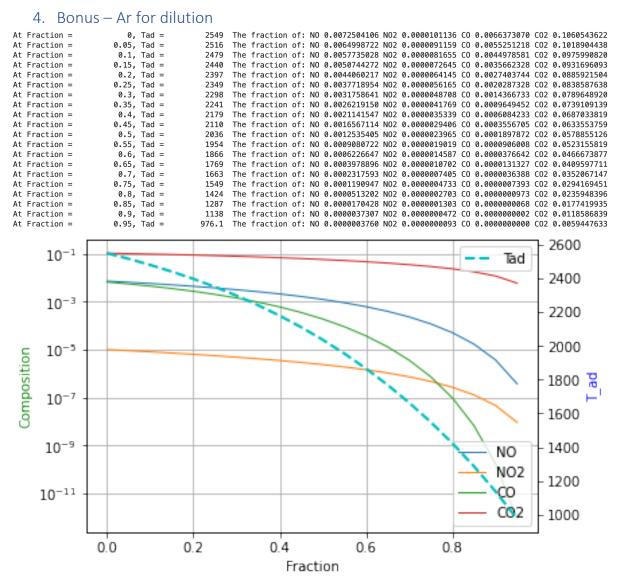
Molar fraction of 4 products in log and adiabatic flame temperature vs fraction of H2O diluted

- The general trend of H2O as dilutant is very similar to that of CO2.
- Amount of NO and NO2 pollutant produced is very similar to the result using CO2 as dilutant, with slightly more NO and NO2 produced at higher molar fractions.
- The reaction rate should be faster and at higher fractions, the reaction is more thorough compared to CO2 since more pollutant are formed.
- More CO is formed compared to CO2 at higher fraction.
- The adiabatic flame temperature is highly aligned with that of CO2 since the Cp value of H2O and CO2 are similar.



Molar fraction of 4 products in log and adiabatic flame temperature vs fraction of N2 in (diluted) the air

- It seems that when no nitrogen is added, Cantera cannot compute successfully using the auto solver, gibbs solver is used to obtain the above data and plots.
- The adiabatic flame temperature become much higher compare to N2 is included, it decreases as the fraction of N2 increases.
- Since no energy is needed to heat up the nitrogen gas.
- As N2 in the reaction increases, the pollutant first increases then decreases. And Nitrous pollutant are not formed when fraction is zero since no N atom can be reached.
- Pollutants concentration at high N2 concentration is lower than atmospheric air
- What I did not expect is that the pollutant concentration, especially nitrous (NO.NO2) pollutants are higher than the values obtained in the atmospheric conditions.



Molar fraction of 4 products in log and adiabatic flame temperature vs fraction of diluted Ar added

- Adiabatic flame temperature curve is no longer a straight line, but more curved, since the Cp value of Ar does not vary too much with temperature
- By looking very closely to the figure (since I did not plot them on one single figure, or they are too overlapped), I found that the pollutant fraction with Ar as dilutant is actually higher than using H2O, CO2. CO has a more significant impact.
- Since dissociation of CO2 to CO require participation of H2O, a theoretical guess would be that the concentration of CO is much higher compare to use CO2 and H2O as dilutant is due to the fact that lack of these two items have promoted the reaction equilibrium to the pollutant side, hence more CO is formed.

Part IV:

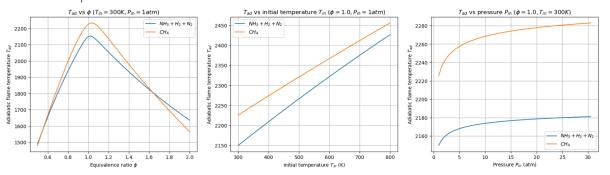
- 1. The chemical model you will need to use Cantera
- Chemical kinetics models describing nitrogen oxydation in combustion have been originally used to model thermal *NO* formation, such as the Konnov [1] mechanism.
- More recent models derived from older models are more suited to *NH*3 combustion modelling, such as the model from Xiao [2] wich will be used in our project.
- The Xiao combustion kinetics model contains 52 species and 272 reactions and was validated using experimental data in the 1-30 atm pressure range.
- The relatively high number of species and reactions for a *NH*3 oxydation mechanism should make it more accurate compared to the SanDiego [3] or the Jiang [4] mechanisms.

References:

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- 2. The global NH3+H2+N2 combustion reaction
 - For $X_{NH3} = X_{H2}$ which is a plausible case

$$(NH_3 + H_2 + 0.33N_2) + 1.25 (O_2 + 3.76 N_2) \rightarrow 0.5 N_2 + 2.5 H_2O + 5.03 N_2$$

3. The adiabatic temperature with varying equivalence ratio, initial temperature, and pressure.



4. The concentration of the main pollutants after equilibrium

