

# Python Recursion Practice

1. Write a function `f1(list)` that returns the sum of the elements in the list.

```
>>> f1([1,2,3,4])
10
>>> f1([])
0
```

2.

Consider the following function:

$$f(n) = \begin{cases} n//2 & \text{if } n \text{ is even} \\ 3n+1 & \text{if } n \text{ is odd} \end{cases}$$

Write a function `f2(n)` that returns the number of steps of the function `f(n)` until it reaches 1 (this is also known as the Collatz Conjecture).

For example, consider `f(6):6→3→10→5→16→8→4→2→1`, since there are a total of 9 steps, `f2(6)` evaluates to 9.

```
>>> f2(1)
1
>>> f2(6)
9
>>> f2(11)
15
>>> f2(637228127)
276
```

3. Write a function `f3(list)` that prints out the elements in the list in reverse order.

```
>>> f3([1,2,3])
3
2
1
>>> f3([])
>>> f3([3,2,1])
1
2
3
```

4. Write a function `f4(list)` that multiplies all of the odd elements in the list by 3 and prints out each tripled element.

```
>>> f4([1,2,3,4])
3
9
>>> f4([2,4])
>>> f4([11,42,63,15])
33
189
45
```

5. Write a function `f5(list)` that multiplies all of the odd elements in the list by 3 and prints out each element of the modified list in reverse order.

```
>>> f5([1,2,3,4])
4
9
2
3
>>> f5([2,4])
4
2
>>> f5([11,42,64,15])
45
64
42
33
```

6. Write a function `f6(lst)` that takes any multidimensional list and returns a one dimensional list with the same values. This is also known as flattening a list. Remember that you can use `type([1,2,3]) == list` to determine if something is a list. There should be one base case and two recursive cases.

```
>>> f6(['baa'])
['baa']
>>> f6(['baa', [4, True, [10, 5], [1, 2, ['moo']]], ["chirp"]])
['baa', 4, True, 10, 5, 1, 2, 'moo', "chirp"]
>>> f6([])
[]
>>> f6([[[[[[[[[[[[[[[[[[23]]]]]]]]]]]]]]]]))
[23]
```

7.

Consider a function  $L_n$ :

```
Ln = 2      if n=0;  
     1      if n=1;  
     Ln-1+Ln-2 if n>1;
```

Write a function  $f_7(n)$  that calculates  $L_n$

```
>>> f7(3)  
4  
>>> f7(14)  
843  
>>> f7(0)  
2  
>>> f7(22)  
39603
```

8. Write a function  $f_8(s)$  that returns True if  $s$  is a palindrome, and False otherwise.

```
>>> f8("")  
True  
>>> f8("kayak")  
True  
>>> f8("penguin")  
False  
>>> f8("a")  
True
```

;

9. Write a function `f9(n)` that returns  $n!$

```
>>> f9(0)
1
>>> f9(1)
1
>>> f9(2)
2
>>> f9(3)
6
```

10. Write a function `f10(list)` that returns `len(list)`.

```
>>> f10([1,2,3])
3
>>> f10([])
0
>>> f10([2])
1
```

11. Write a function `f11(list)` that returns the last element in the list.

```
>>> f11([1,2,3])
```

```
3
```

```
>>> f11([])
```

```
>>> f11([1])
```

```
1
```

12. Write a function `f12(n)` that prints the numbers `n` through 1 in descending order.

```
>>> f12(3)
```

```
3
```

```
2
```

```
1
```

```
>>> f12(0)
```

```
>>> f12(1)
```

```
1
```

13. Write a function `f13(n)` that returns the number of digits in `n`. You may assume `n` is a positive integer.

```
>>> f13(9175)
```

```
4
```

```
>>> f13(34)
```

```
2
```

```
>>> f13(268)
```

```
3
```

```
>>> f13(0)
```

```
1
```

14. Write a function `f14(list)` that returns the first odd number in the list, and `None` if there are no odd numbers in the list.

```
>>> f14([1,2,3])
```

```
1
```

```
>>> f14([2,4])
```

```
>>> f14([2,4,6,8,10,3])
```

```
3
```



15. Write a function `f15(list)` that returns the sum of all the odd numbers in the list.

```
>>> f15([1,2,3])
4
>>> f15([2,4])
0
>>> f15([1,3,6,9])
13|
```

16. Write a function `f16(list)` that returns a list of all the odd numbers in the list.

```
>>> f16([1,3,5,7])
[1, 3, 5, 7]
>>> f16([2,4])
[]
>>> f16([1,2,3,4,5])
[1, 3, 5]
```

17. Write a function `f17(list)` that returns the second to last element in the list. Assume `len(list) > 1`.

```
>>> f17([1,2])
1
>>> f17([1,2,3,4])
3
>>> f17([1,2,3])
2
```

18. Write a function `f18(a,b)` that returns the greatest common divisor of `a` and `b`.

```
>>> f18(5,4)
1
>>> f18(40,60)
20
>>> f18(9,3)
3
```

19. Write a function `f19(list1, list2)` that merges `list1` and `list2` in ascending order. Assume `|list1|` and `|list2|` are already sorted.

```
>>> f19([1,2,3],[4,5])
[1, 2, 3, 4, 5]
>>> f19([4,5],[1,2,3])
[1, 2, 3, 4, 5]
>>> f19([], [1,2,3])
[1, 2, 3]
>>> f19([1,2,3], [])
[1, 2, 3]
>>> f19([], [])
[]
```

20. Write a function `f20(list)` that mergesorts the `list`. Consider using `f19(list1, list2)` for the merging step.

```
>>> f20([3,2,1])
[1, 2, 3]
>>> f20([])
[]
>>> f20([5,3,1,2,4,6])
[1, 2, 3, 4, 5, 6]
```

21. Write a function `f21(tree)` that returns the height of the tree. The tree has the structure `[value, left subtree, right subtree]`.

```
>>> f21([])
0
>>> f21([1,[],[]])
1
>>> f21([1,[1,[],[]],[]])
2
```

22. Write a function `f22(tree)` that returns the number of nodes in the tree. The tree has the structure `[[value, left subtree, right subtree]]`.

```
>>> f22([])
0
>>> f22([1,[],[]])
1
>>> f22([1,[1,[],[]],[1,[],[]]])
3
```

23. Write a function `f23(tree)` that returns the sum of the nodes in the tree. The tree has the structure `[[value, left subtree, right subtree]]`.

```
>>> f23([])
0
>>> f23([1, [], []])
1
>>> f23([1, [2, [], []], [3, [], []]])
6
```

24. Write a function `f24(tree)` that prints out the values of the tree in ascending order. The tree has the structure `[[value, left subtree, right subtree]]` and is a binary search tree.

```
>>> f24([])
>>> f24([1, [], []])
1
>>> f24([2, [1, [], []], [3, [], [4, [], []]])
1
2
3
4
```

25. Write a function `f25(tree)` that returns the smallest element in the tree. The tree has the structure `[value, left subtree, right subtree]` and is a binary search tree. Return `-1` if the tree is empty.

```
>>> f25([])
```

```
-1
```

```
>>> f25([1,[],[]])
```

```
1
```

```
>>> f25([2,[1,[],[]],[3,[],[4,[],[]]])
```

```
1
```