

# Influence Maximization Problem Report

Using IMM to solve the problem

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**Abstract**—This is a report for the third project in AI class, the influence maximization problem (IMP). The problem IMP is a popular question which has been researched by lots of people. The challenge is how to find the optimal seeds with maximum influence in the shortest possible time. For solving this problem, I researched the method IMM. I learned a lot from this method and implemented part of it.

**Index Terms**—IMP, ISE, IMM, LT, IC

## I. PRELIMINARY

### A. Problem Description

The influence maximization problem(CARP) can be described as follows: a social network  $G = (V, E)$ , with a set of vertices denoted by  $V$ , a set of directed edges denoted by  $E$ . Each directed edge has a weight which represent the probability of influence. There are two diffusion models, IC and LT used in this project which decide a activated node how to influence others. A solution to the problem is a seed set which has biggest influence in social network when activated them at first.

### B. Problem Applications

Nowadays, social network is becoming more valuable. How to influence or transmate some information to maximum numbers of people in lowest cost has got a lot attention. This project can be used in lots of scenes, for exemple:

- Advertising Stats
- Shops Recommended

## II. METHODOLOGY

### A. Notation

- **G**: a social network  $G$  with a node set  $V$  and an edge set  $E$ ;
- **n**: number of nodes;
- **m**: number of edges;
- **k**: the size of the seed set for influence maximization;
- **RR**: research reachable set;
- **MAX**: 9999, a constraint factor used in programing;
- **process**: number of multiprocess
- **I(S)**: the influence of a node set  $S$  in a diffusion process on  $G$ ;
- **Rtimes**: the times of ISE;

### B. Data Structure

- **NETWORK**: In ISE, a two-dimensional list which stores all edges with their out-neighbors and weight;
- **NETWORK**: In IMP, a two-dimensional dictionary which stores all edges with their in-neighbors and weight;
- **Rset**: a list which stores *RR* sets;

### C. ISE and diffusion modle design

Task one in this project is to find the maximum size of influenced nodes of a given seed set. This is also a function helps us to estimate the effect of the seed. There are two kinds of diffusion modles, IC and LT, which decide the way to spread influence, I will introduce them in detail soon.

**IC**, the independent cascade model, The IC model originates from the marketing literature [22,23], and it assumes that each edge  $e \in E$  is associated with a probability  $p(e) \in [0, 1]$ . For any node  $u$  and any of its outgoing neighbors  $v$ , if  $u$  is first activated at timestamp  $i$ , then it has  $p(u, v_i)$  probability to activate  $v$  at timestamp  $i + 1$ . In other words, whether or not  $u$  can activate  $v$  is independent of the history of diffusion before  $u$  is activated, and hence, the order of node activations does not affect the diffusion results.

**LT**, the linear threshold model. The LT model is another diffusion modle. For any node  $u$  and any of its in-neighbors  $v$ ,  $u$  has a probability  $P(u)$ , only when the sum of  $p(v, u_i)$  of all activated in-neighbor  $v$  of  $u$  bigger than  $P(u)$ ,  $u$  will be activated.

In ISE task, I apply Monte Carlo Method to simulate diffusion process. After *Rtimes* times, find the mean value as the influence size.

### D. IMP Model design

The first thing I need to do is to load the data in properly data structure. In IMM algorithm, for each node, we only need to consider about its in-neighbor nodes, so we need to store these messages. I use *NETWORKT*, a two-dimension dictionary. The keys are every nodes, and values are list of their in-neighbor nodes and weights.

And then apply the IMM algorithm which can split to two parts, *sampling()* and *nodeselection()*.

*sampling()*: This phase iteratively generates random *RR* sets and puts them into a set *Rset*, until a certain stopping condition is met.

For generating *RR* for node  $u$ , we need to use iteration method. Firstly, in all in-neighbor nodes  $v$  of  $u$ , choose them

in probability  $p(v, u_i)$  to be activated and add them to  $RR$ . Then do the same thing on the new activated nodes until no nodes to be activated. Finally return  $RR$ .

*nodeselectin()*: This phase applies the standard greedy algorithm for maximum coverage to derive a size- $k$  node set  $Sk$  that covers a large number of  $RR$  sets in  $Rset$ . It then returns  $Sk$  as the final result.

It worth to noting that, *nodeselectin()* need to be optimized, because it will be really slow if we use the simple algorithm. The details will be showed in pseudocode.

And in *sampling()*, I use multiprocessing to generate  $Rset$  as fast as possible.

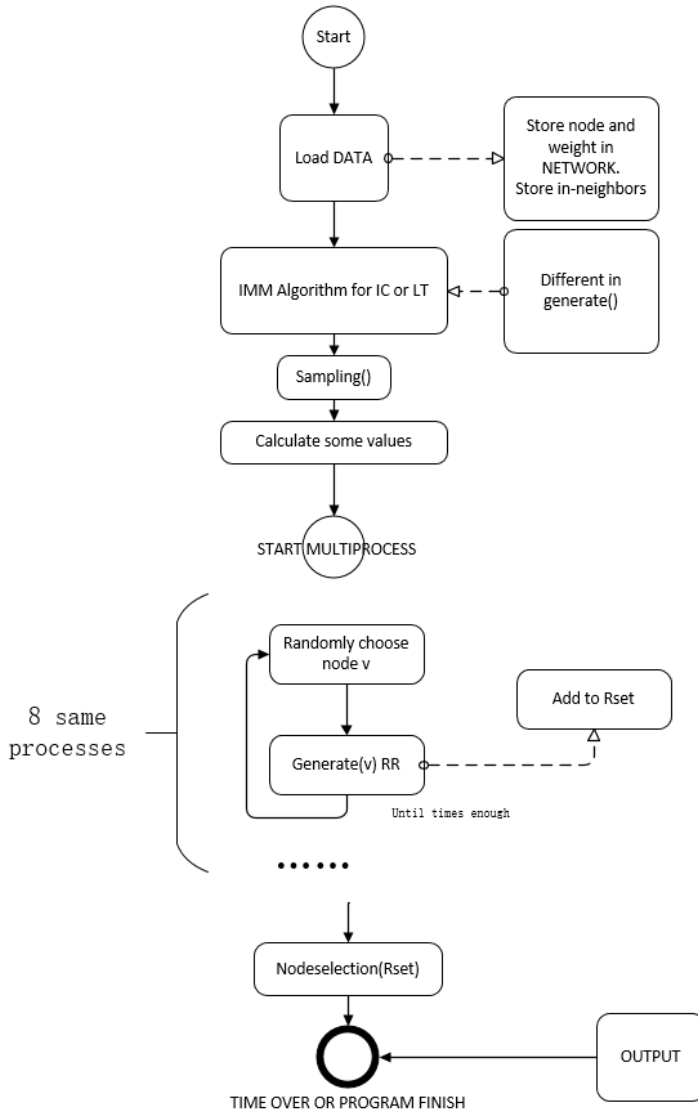


Fig. 1. Model Achitecture

#### E. Detail of algorithms

1-6 pseudocodes have showed the details of IMM algorithms. There are some necessary formulas used in IMM:

$$\alpha = \sqrt{l * \log n + \log 2}$$

$$\beta = \sqrt{(1 - 1/e) * (\log C(n, k) + l * \log n + \log 2)}$$

$$\lambda_a = 2n * ((1 - 1/e) * \alpha + \beta)^2 * \text{Epsilon}^{-2}$$

$$\lambda_b = \frac{(2 + \frac{2}{3}\text{Epsilon})(\log C(n, k) + l \log n + \log \log_2 n)n}{\text{Epsilon}^2}$$

For different diffusion models, IC and LT, there are a little different in *generate()* function. For IC, I use iteration method to add node to  $Rr$  under the probability given by weight  $p(< u_j, u >)$ . But for LT, I suppose that there must be a node and only a node would be activated of an activated node's in-neighbors. So i just need to do iteration and randomly select one of the in-neighbors to add in  $RR$ .

I find that when the *NETWORK* is a big network,  $Rset$  will be a huge set. That makes program runing time too long, So I apply multiprocessing to help program to find the  $Rset$ .

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#### Algorithm 1 ICsearch

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**Input:** *SEED*

**Output:** *count*

```

1: active ← SEED
2: actived ← SEED
3: count += len(actived)
4: while active is not empty do
5:   newactive = []
6:   for node u ∈ active do
7:     for node v ∈ in-neighbor of u do
8:       if v ∈ actived then
9:         continue
10:      end if
11:      p = random(0,1)
12:      if p >  $p(< v, u >)$  then
13:        newactive.append(v)
14:        actived.append(v)
15:      end if
16:    end for
17:  end for
18:  active = newactive
19:  count += len(newactive)
20: end while
21: return count
    =0
  
```

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#### Algorithm 2 LT search

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**Input:** *SEED*

**Output:** *count*

```

1: active ← SEED =0
  
```

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**Algorithm 3** LT search (continued))

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**Input:** *SEED***Output:** *count*

```

1: active  $\leftarrow$  SEED
2: actived  $\leftarrow$  SEED
3: count += len(actived)
4: for node in network do
5:   pnow(node) = 0
6:   threshold(node) = random(0,1)
7: end for
8: while active is not empty do
9:   newactive = []
10:  for node u  $\in$  active do
11:    for node v  $\in$  in-neighbor of u do
12:      if v  $\in$  actived then
13:        continue
14:      end if
15:      pnow(u) = random(0,1) + pnow(u)
16:      if pnow(u) > threshold(u) then
17:        newactive.append(v)
18:        actived.append(v)
19:      end if
20:    end for
21:  end for
22:  active = newactive
23:  count += len(newactive)
24: end while
25: return count
    =0

```

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**Algorithm 4** sampling

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**Input:** *NETWORK*, *K*, *Epsilon*, *l***Output:** *Rset*

```

1: Rset = []
2: LB = 1
3: Epsilonnew =  $2^{1/2} * \text{Epsilon}$ 
4: for i = 1 to log2(n)-1 do
5:   x =  $b/2^i$ 
6:   theta =  $\lambda_a/x$ 
7:   while len(Rset)  $\leq$  theta do
8:     v  $\leftarrow$  randomlyfromNETWORK
9:     Rset += generate(v)
10:  end while
11:  Si, Fractioni = nodeselection(Rset)
12:  if  $n * \text{Fractioni} \geq (1 + \text{Epsilon}_{\text{new}}) * x$  then
13:    LB =  $n * \text{Fractioni} / (1 + \text{Epsilon}_{\text{new}})$ 
14:    break
15:  end if
16: end for
17: theta =  $\lambda_b/LB$  =0

```

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**Algorithm 5** sampling (continued)

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```

1: while len(Rset)  $\leq$  theta do
2:   v  $\leftarrow$  randomlyfromNETWORK
3:   Rset += generate(v)
4: end while
5: return Rset
    =0

```

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**Algorithm 6** nodeselection

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**Input:** *Rset*, *k***Output:** *Sk*, *fraction*

```

1: Sk = []
2: Rdict = []
3: num = []
4: total = len(Rset), active = 0
5: for i = 0 to total do
6:   for node j in Rset[i] do
7:     num[j] += 1
8:     Rdict[j].append(i)
9:   end for
10: end for
11: while len(Sk)  $\geq k$  do
12:   maxnumber = max(num)
13:   seed = num.index(maxnumber)
14:   active += maxnumber
15:   Sk.append(s)
16:   for each node in Rdict(seed), remove them from other
     Rdict and num changed
17: end while
18: fraction = active/total
19: return Sk, fraction
    =0

```

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### III. EMPIRICAL VERIFICATION

#### A. Dataset

All datasets from the platform: *network-5-IC*, *network-5-LT*, *NetHEOT-5-IC*, *NetHEPT-5-LT*, *NetHEPT-50-LT-bonus*, *NetHEPT-50-LT-bonus*

#### B. Performance measure

Given a time, look at the difference between the solution given at the end of the program and the optimal solution.

Test envirmint is given by CARP-Oj-Platform.

#### C. Hyperparameters

*Epsilon* = 0.07  
*l* = 1  
*process* = 8

#### D. Experimental results

See table 1.

Among these six datasets, the solution is not very well but also far from worst. It performs well in little size network.

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**Algorithm 7** generate

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**Input:**  $v, NETWORK$ **Output:**  $RR$ 

```
1:  $Rnew = []$ 
2: for node  $u$  in  $NETWORK[v]$  do
3:    $Rnew.append(u)$ 
4:    $RR = Rnew$ 
5: end for
6: while  $Rnew \neq []$  do
7:    $NEW = []$ 
8:   for node  $u$  in  $Rnew$  do
9:     for node  $uj$  in  $NETWORK[u]$  do
10:       $p = \text{random}(0,1)$ 
11:      if  $p \leq p(<uj, u>)$  then
12:        if  $uj$  not in  $RR$  then
13:           $NEW.append(uj)$ 
14:           $RR.append(uj)$ 
15:        end if
16:      end if
17:    end for
18:  end for
19:   $Rnew = NEW$ 
20: end while
21: return  $RR$ 
    =0
```

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**Algorithm 8** IMM

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**Input:**  $k, NETWORK, Epsilon, l$ **Output:**  $S$ 

```
1:  $Rset = \text{sampling}(NETWORK, k, Epsilon, l)$ 
2:  $S = \text{nodeselection}(Rset, k)$ 
3: return  $S$ 
    =0
```

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## REFERENCES

- [1] Youze Tang, Yanchen Shi, Xiaokui Xiao, "Influence Maximization in Near-Linear Time: A Martingale Approach," Proceedings of the 2015 ACM SIGMOD International Conference on Management of Data. ACM, 2015, 1539-1554.

The disadvantages of my program is that it doesn't perform well on big data sets. For big datasets, it will be really slow and have a relative bigger bias.

## ACKNOWLEDGMENT

I would like to thanks my classmates who discussed algorithms with me which help me finish this project. And I also want to thanks for TA Yao Zhao who taught algorithms and guided me to research. Last I would like to thank forward to all the student assistances who will assess my codes and reports.

TABLE I  
EXPERIMENTAL RESULTS

Dataset	time(s)	optimal	MySeed
$network - 5 - IC$	1.6	30.73	30.68
$network - 5 - LT$	1.4	37.54	36.2
$NetHEOT - 5 - IC$	20.6	324.16	317.09
$NetHEPT - 5 - LT$	17.0	392.98	392.96
$NetHEPT - 50 - LT - bonus$	40.6	1294.55	1298.10
$NetHEPT - 50 - LT - bonus$	32.87	1652.49	1702.00