

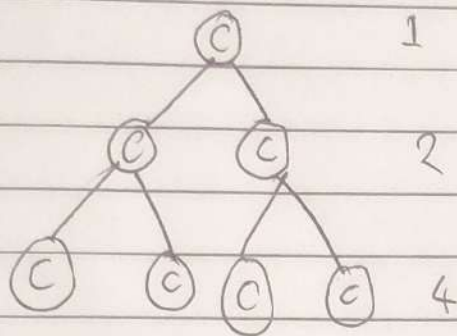
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Problem 2a:

Implementation 1 uses recursion to find the fibonacci number, and it calculates the same fibonacci number multiple times if required. *

$$T(n) = T(n-1) + T(n-2) + C$$



$$\begin{aligned} & 1 + 2 + 4 + \dots + 2^n \\ &= 2^{n+1} - 1 \\ &= O(2^n) \quad [\text{Time complexity of implementation 1}] \end{aligned}$$

Implementation 2 uses memoization technique to store fibonacci numbers that has also been calculated. So the repeated sub-trees don't have to be calculated using recursion again, thus saving time.

Time complexity of implementation = $O(n)$ (linear)

∴ Implementation 2 is far better than implementation 1.

The graph in problem 2b also highlights this time complexity.