

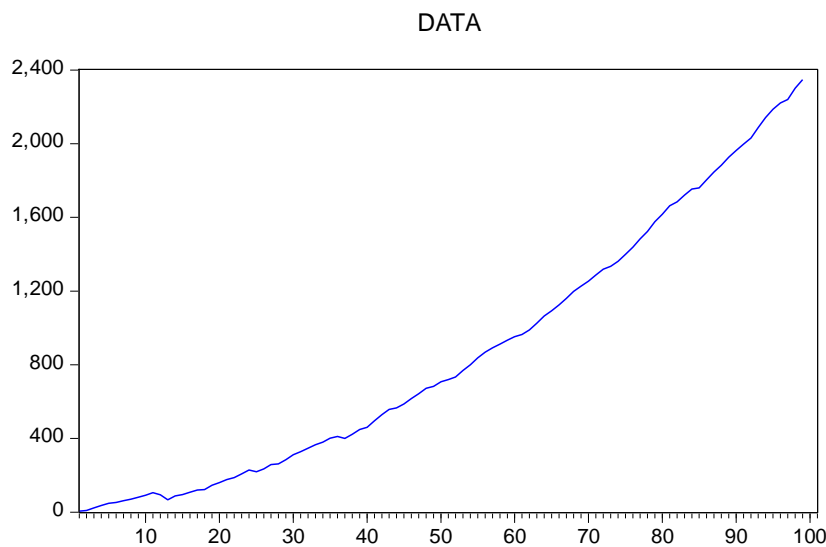
TSAF Project – Dataset 4

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Exploratory analysis

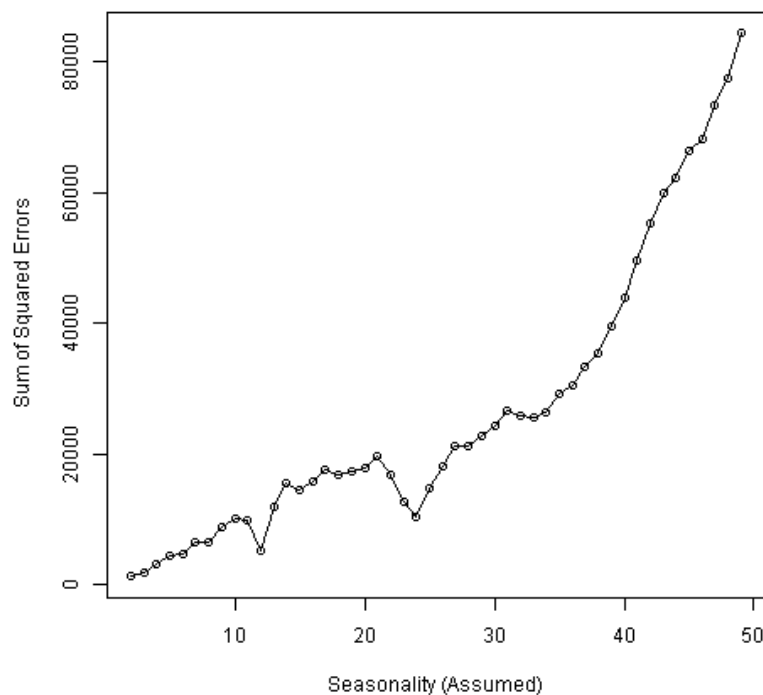
Trend



This graph shows that the trend is likely to be non-linear. Regressing the data against t and t^2 suggests that the trend is quadratic (higher order terms are insignificant)

Seasonality

Without assuming the period of seasonality, we used decompose function of R and generated a graph showing the trend, seasonality and residual series for different assumed seasonalities varying from 2 to $\text{floor}(99/2)=49$. In the absence of seasonality, the sum of squared residuals is expected to increase with seasonality.



This shows that the seasonality of the data is either 12 or 24. Period of seasonality will be confirmed in the steps that follow.

Modelling strategy

Estimation/Forecast 1: ARIMA (2,2,0) (12,0,0)

1. As suggested in the exploratory analysis, the trend is quadratic. This can be verified by finding order of integration (ADF test on level, 1st difference and 2nd difference). The series is I(2) in nature, which confirms the presence of quadratic trend

Table 1: ADF test on first differenced series

Null Hypothesis: D(DATA) has a unit root

Exogenous: Constant

Lag Length: 11 (Automatic - based on SIC, maxlag=11)

	t-Statistic	Prob.*
Augmented Dickey-Fuller test statistic	-0.756046	0.8260
Test critical values:		
1% level	-3.508326	
5% level	-2.895512	
10% level	-2.584952	

*MacKinnon (1996) one-sided p-values.

Table 2: ADF test on second differenced series

Null Hypothesis: D(DATA,2) has a unit root

Exogenous: Constant

Lag Length: 10 (Automatic - based on SIC, maxlag=11)

	t-Statistic	Prob.*
Augmented Dickey-Fuller test statistic	-7.894673	0.0000
Test critical values:		
1% level	-3.508326	
5% level	-2.895512	
10% level	-2.584952	







































































*MacKinnon (1996) one-sided p-values.

2. Correlogram of residue from regression (quadratic in t) shows presence of autoregressive effect in lags 1, 2 and seasonal (AR or MA) effect at lag 12


















































































































































































Date: 02/20/15 Time: 13:07

Sample: 1 101

Included observations: 99

Autocorrelation	Partial Correlation		AC	PAC	Q-Stat	Prob
		1	0.702	0.702	50.252	0.000
		2	0.364	-0.254	63.883	0.000
		3	0.115	-0.057	65.249	0.000
		4	-0.140	-0.264	67.309	0.000
		5	-0.287	-0.036	76.092	0.000
		6	-0.395	-0.220	92.849	0.000
		7	-0.372	0.073	107.89	0.000
		8	-0.327	-0.200	119.64	0.000
		9	-0.220	0.103	125.04	0.000
		10	-0.100	-0.147	126.17	0.000
		11	0.073	0.276	126.78	0.000
		12	0.244	-0.076	133.61	0.000
		13	0.165	-0.242	136.79	0.000
		14	0.085	-0.022	137.64	0.000
		15	0.013	-0.056	137.66	0.000
		16	-0.150	-0.243	140.36	0.000
		17	-0.279	-0.117	149.88	0.000
		18	-0.326	-0.044	162.99	0.000
		19	-0.264	-0.024	171.71	0.000
		20	-0.173	-0.046	175.52	0.000
		21	-0.003	0.138	175.52	0.000
		22	0.173	0.006	179.38	0.000
		23	0.318	0.052	192.69	0.000
		24	0.411	-0.035	215.17	0.000
		25	0.299	-0.130	227.24	0.000
		26	0.145	-0.183	230.12	0.000
		27	-0.011	-0.119	230.14	0.000
		28	-0.183	-0.062	234.84	0.000
		29	-0.262	0.049	244.62	0.000
		30	-0.265	-0.025	254.77	0.000
		31	-0.189	0.118	260.01	0.000
		32	-0.121	-0.070	262.19	0.000
		33	-0.024	-0.024	262.27	0.000
		34	0.065	-0.195	262.93	0.000
		35	0.136	-0.037	265.81	0.000

3. After regressing residual with AR(1), AR(2) and SAR(12), we observed that all the coefficients are significant and less than 1 and the residue has reached white noise (p-value(Q-stat)>.05). Correlogram of squared residue suggests that the errors are iid (p-value(Q-stat)>.05)

Date: 02/20/15 Time: 13:10 Sample: 1 101 Included observations: 85 Q-statistic probabilities adjusted for 3 ARMA terms						Date: 02/20/15 Time: 13:10 Sample: 1 101 Included observations: 85									
Autocorrelation		Partial Correlation	AC	PAC	Q-Stat	Prob*	Autocorrelation		Partial Correlation	AC	PAC	Q-Stat	Prob		
				1	0.013	0.013	0.0149			1	-0.077	-0.077	0.5251	0.469	
				2	-0.026	-0.026	0.0746			2	-0.041	-0.047	0.6722	0.715	
				3	0.118	0.118	1.3224			3	-0.129	-0.137	2.1826	0.535	
				4	-0.137	-0.144	3.0406	0.081			4	0.081	0.058	2.7794	0.595
				5	0.012	0.026	3.0542	0.217			5	-0.051	-0.054	3.0205	0.697
				6	-0.115	-0.143	4.2861	0.232			6	0.192	0.179	6.4631	0.373
				7	0.042	0.092	4.4549	0.348			7	0.086	0.134	7.1713	0.411
				8	0.041	-0.001	4.6198	0.464			8	-0.113	-0.099	8.4024	0.395
				9	-0.085	-0.044	5.3282	0.502			9	-0.075	-0.030	8.9498	0.442
				10	-0.143	-0.203	7.3392	0.394			10	-0.116	-0.154	10.270	0.417
				11	-0.033	-0.005	7.4504	0.489			11	-0.094	-0.165	11.150	0.431
				12	-0.093	-0.114	8.3218	0.502			12	0.127	0.083	12.789	0.385
				13	-0.150	-0.110	10.634	0.387			13	0.184	0.143	16.262	0.235
				14	0.019	-0.033	10.672	0.471			14	-0.118	-0.058	17.722	0.220
				15	0.086	0.088	11.458	0.490			15	-0.106	-0.030	18.910	0.218
				16	-0.001	-0.047	11.458	0.573			16	-0.071	-0.054	19.450	0.246
				17	-0.030	-0.045	11.558	0.642			17	0.084	0.085	20.224	0.263
				18	-0.040	-0.094	11.738	0.699			18	-0.012	-0.035	20.240	0.319
				19	-0.041	-0.062	11.926	0.749			19	0.150	0.039	22.774	0.247
				20	-0.139	-0.185	14.129	0.658			20	-0.019	0.020	22.814	0.298
				21	-0.018	-0.011	14.165	0.718			21	0.048	0.101	23.083	0.340
				22	0.129	0.038	16.109	0.650			22	-0.131	-0.057	25.082	0.293
				23	0.116	0.093	17.719	0.606			23	-0.046	-0.073	25.337	0.333
				24	0.071	0.009	18.329	0.628			24	0.070	0.057	25.931	0.357
				25	0.033	0.019	18.465	0.678			25	0.089	-0.026	26.898	0.361
				26	0.062	-0.000	18.946	0.704			26	-0.070	-0.116	27.509	0.383
				27	-0.068	-0.058	19.544	0.722			27	-0.121	-0.087	29.362	0.344
				28	-0.146	-0.157	22.320	0.617			28	-0.084	-0.062	30.275	0.350
				29	0.057	0.020	22.755	0.647			29	-0.018	0.005	30.318	0.398
				30	0.038	-0.039	22.953	0.688			30	0.010	-0.027	30.332	0.449
				31	0.065	0.089	23.524	0.706			31	0.011	-0.023	30.349	0.499
				32	-0.035	-0.096	23.700	0.744			32	-0.051	-0.047	30.712	0.532
				33	-0.023	0.009	23.778	0.782			33	0.075	0.111	31.520	0.541
				34	0.049	0.017	24.128	0.805			34	-0.086	-0.065	32.588	0.537
											35	-0.021	0.036	32.655	0.582

4. ARCH LM test suggests that there is no ARCH effect (null hypothesis cannot be rejected)

Table 3: ARCH test (12 lags)
Heteroskedasticity Test: ARCH

F-statistic	1.007144	Prob. F(12,60)	0.4539
Obs*R-squared	12.23901	Prob. Chi-Square(12)	0.4267

5. Dynamic forecast on the last 12 observations shows MAPE of 0.4732%
Static forecast on the last 12 observations shows MAPE of 0.3376%

Estimation/Forecast 2: ARIMA (2,1,0) (12,1,0)

1. New series was generated by performing one difference and one seasonal difference simultaneously. The new series was found to be stationary

Table 4: ADF test on detrended, deseasonalized series

Null Hypothesis: DTDS has a unit root

Exogenous: Constant

Lag Length: 0 (Automatic - based on SIC, maxlag=11)

	t-Statistic	Prob.*
Augmented Dickey-Fuller test statistic	-8.045251	0.0000
Test critical values: 1% level	-3.509281	
5% level	-2.895924	
10% level	-2.585172	

*MacKinnon (1996) one-sided p-values.

2. Correlogram of this series does not show clear AR, MA signs, but it shows presence of SAR at lag 12. After including SAR(12), AR(2) was also found to be significant, leading to increase in adj R². Residual correlogram showed white noise & squared residual correlogram showed iid

Date: 02/20/15 Time: 13:31 Sample: 1 101 Included observations: 72 Q-statistic probabilities adjusted for 2 ARMA terms						Date: 02/20/15 Time: 13:32 Sample: 1 101 Included observations: 72					
Autocorrelation	Partial Correlation	AC	PAC	Q-Stat	Prob	Autocorrelation	Partial Correlation	AC	PAC	Q-Stat	Prob
		1 0.035 0.035 0.0930						1 0.037 0.037 0.1018 0.750			
		2 -0.054 -0.055 0.3151						2 0.080 0.078 0.5850 0.746			
		3 -0.056 -0.052 0.5591 0.455						3 -0.021 -0.026 0.6177 0.892			
		4 -0.150 -0.150 2.3108 0.315						4 0.130 0.127 1.9484 0.745			
		5 -0.020 -0.018 2.3439 0.504						5 -0.095 -0.103 2.6601 0.752			
		6 -0.097 -0.119 3.0957 0.542						6 0.002 -0.009 2.6604 0.850			
		7 0.168 0.162 5.4182 0.367						7 0.018 0.040 2.6870 0.912			
		8 0.017 -0.035 5.4424 0.488						8 -0.098 -0.127 3.4917 0.900			
		9 -0.059 -0.053 5.7338 0.571						9 -0.034 -0.001 3.5903 0.936			
		10 -0.234 -0.268 10.433 0.236						10 -0.049 -0.041 3.7973 0.956			
		11 -0.133 -0.089 11.968 0.215						11 -0.055 -0.066 4.0593 0.968			
		12 -0.048 -0.111 12.175 0.273						12 -0.082 -0.036 4.6587 0.968			
		13 -0.065 -0.085 12.554 0.323						13 0.186 0.190 7.7790 0.858			
		14 0.006 -0.146 12.557 0.402						14 -0.068 -0.085 8.2080 0.878			
		15 0.132 0.065 14.194 0.360						15 -0.074 -0.088 8.7131 0.892			
		16 0.006 -0.113 14.198 0.435						16 0.001 0.037 8.7133 0.925			
		17 0.008 0.045 14.204 0.510						17 0.082 0.021 9.3578 0.928			
		18 0.052 0.017 14.469 0.564						18 -0.092 -0.065 10.193 0.925			
		19 -0.020 -0.017 14.507 0.631						19 -0.049 -0.049 10.437 0.941			
		20 0.054 -0.033 14.805 0.675						20 -0.115 -0.158 11.784 0.923			
		21 -0.149 -0.203 17.122 0.582						21 0.064 0.119 12.217 0.934			
		22 0.093 0.006 18.053 0.584						22 -0.071 -0.045 12.753 0.940			
		23 0.125 0.053 19.755 0.537						23 0.128 0.110 14.522 0.911			
		24 -0.195 -0.292 23.981 0.348						24 -0.079 -0.059 15.216 0.914			
		25 0.112 0.112 25.411 0.329						25 -0.126 -0.186 17.002 0.882			
		26 0.031 -0.004 25.526 0.378						26 0.018 0.035 17.041 0.908			
		27 -0.038 -0.065 25.699 0.424						27 0.055 0.066 17.400 0.921			
		28 -0.173 -0.188 29.316 0.297						28 -0.002 0.006 17.401 0.940			
		29 -0.006 0.040 29.320 0.346						29 -0.109 -0.131 18.868 0.925			
		30 0.078 -0.079 30.094 0.359						30 0.112 0.038 20.465 0.904			
		31 0.121 0.184 32.007 0.320						31 -0.031 0.021 20.593 0.922			
		32 0.092 -0.058 33.138 0.317						32 -0.032 -0.030 20.729 0.937			

3. ARCH LM test suggests that there is no ARCH effect (null hypothesis cannot be rejected)

Table 5: ARCH test

Heteroskedasticity Test: ARCH

F-statistic	0.373076	Prob. F(12,47)	0.9668
Obs*R-squared	5.218160	Prob. Chi-Square(12)	0.9503

4. Dynamic forecast on the last 12 observations shows MAPE of 0.7352%
Static forecast on the last 12 observations shows MAPE of 0.4243%

Estimation/Forecast 2: ARIMA (1,0,1) (12,2,0)

1. Deseasonalizing twice: Series is stationary, verified using ADF test
2. Correlogram suggests AR(1), MA(1), SAR(12). Correlogram of residual after estimation shows white noise and iid. ARCH tests showed that ARCH effect is absent

Date: 02/20/15 Time: 19:18 Sample: 1 101 Included observations: 62 Q-statistic probabilities adjusted for 3 ARMA terms						Date: 02/20/15 Time: 19:18 Sample: 1 101 Included observations: 62					
Autocorrelation	Partial Correlation	AC	PAC	Q-Stat	Prob	Autocorrelation	Partial Correlation	AC	PAC	Q-Stat	Prob
		1 -0.015	-0.015	0.0149				1 -0.129	-0.129	1.0854	0.297
		2 -0.017	-0.018	0.0349				2 0.170	0.156	3.0045	0.223
		3 0.082	0.082	0.4916				3 -0.050	-0.012	3.1758	0.365
		4 0.025	0.028	0.5353	0.464			4 -0.087	-0.125	3.6893	0.450
		5 -0.065	-0.062	0.8261	0.662			5 0.269	0.272	8.7223	0.121
		6 -0.105	-0.114	1.6035	0.659			6 -0.165	-0.093	10.653	0.100
		7 0.192	0.187	4.2739	0.370			7 -0.062	-0.212	10.928	0.142
		8 0.043	0.058	4.4091	0.492			8 -0.164	-0.129	12.895	0.116
		9 -0.026	-0.003	4.4606	0.615			9 0.001	0.075	12.895	0.167
		10 -0.275	-0.329	10.252	0.175			10 0.076	0.027	13.339	0.205
		11 -0.029	-0.077	10.317	0.243			11 -0.068	-0.059	13.697	0.250
		12 -0.212	-0.226	13.878	0.127			12 -0.068	-0.073	14.068	0.296
		13 -0.076	0.036	14.342	0.158			13 -0.058	0.011	14.339	0.350
		14 -0.026	-0.056	14.399	0.212			14 0.153	0.145	16.263	0.298
		15 0.133	0.159	15.892	0.196			15 -0.052	-0.127	16.489	0.350
		16 0.032	-0.041	15.978	0.250			16 -0.035	-0.135	16.596	0.412
		17 -0.130	-0.031	17.464	0.232			17 -0.100	-0.007	17.478	0.422
		18 0.013	-0.054	17.480	0.291			18 -0.092	-0.059	18.235	0.440
		19 -0.180	-0.135	20.461	0.200			19 0.045	-0.116	18.422	0.494
		20 -0.005	-0.068	20.463	0.251			20 -0.244	-0.273	24.044	0.240
		21 -0.116	-0.141	21.763	0.243			21 0.054	0.086	24.331	0.277
		22 0.102	-0.062	22.795	0.247			22 -0.232	-0.110	29.686	0.126
		23 0.119	0.057	24.224	0.233			23 0.097	-0.048	30.633	0.132
		24 -0.205	-0.292	28.610	0.124			24 -0.027	-0.121	30.710	0.162
		25 0.004	0.025	28.612	0.156			25 0.020	0.117	30.751	0.197
		26 -0.007	-0.041	28.618	0.193			26 0.021	-0.058	30.799	0.236
		27 -0.076	-0.011	29.272	0.210			27 0.088	0.088	31.680	0.244
		28 -0.092	-0.099	30.253	0.215			28 0.188	0.068	35.785	0.148

3. Dynamic forecast on the last 12 observations shows MAPE of 0.7963%
Static forecast on the last 12 observations shows MAPE of 0.4755%

Choice of model and results

Since the first model showed lesser in-sample error, we proceed with the forecast results of first model. Point estimates and interval estimates (95% confidence) for 100 and 101 are:

Time period #	Lower limit 95% CI	Point estimate	Upper limit 95% CI
100	2370.076	2386.697	2403.318
101	2404	2429.459	2455