An Abstract Model of Compartmentalization with Sharing

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1 Introduction

This document describes the desired behavior of a compartmentalized C system in terms of a correct-by-construction abstract machine. The model aims to fulfill a few key criteria:

- Compartments are obviously and intuitively isolated from one another by construction

- It is suitable for hardware enforcement without placing intensive constraints on the target

- Inter-compartment interactions via shared memory are possible

- Compartments can only access shared memory if they have first obtained a valid pointer to it, consistent with the C standard and "capability reasoning"

To this last case: we don't necessarily care that compartments' internal behavior conforms to the C standard. In fact the model explicitly gives compartments a concrete view of memory, giving definition to code that would be undefined behavior in the standard, such as described in Memarian et al. [1]. But when it comes to shared memory, the standard has a clear implication that the memory accessible to a piece of code is determined by the provenance of pointers that code can access. This model embraces that principle.

2 Abstract Semantics

We define a C semantics that separates the world into compartments, ranged over by A, B, C, etc., each with its own separate memory. The core memory model is shown in Figure 1. A concrete memory, m, partially maps machine integer (int) addresses to values with a basic axiomatization given in Figure 2.

One memory of this kind is assigned to each compartment, and additional memories will be allocated for shared objects. Memories are kept totally separate, fulfilling our first requirement: compartments' local memories are definitely never accessible to other compartments. A pointer value consists of a pair: a region ranged over by r drawn from the set $\mathcal{R}$ that determines which memory it accesses, and a machine integer address representing its concrete position. A region is either $\mathbf{L}(C)$, for local pointers into the compartment C, or $\mathbf{S}(id, base)$, where id is an abstract identifier and $base$ is a machine integer. Regions are identified in general by their compartment identifiers or abstract identifiers, collectively the set $\mathcal{C} + ident$. A "super-memory" M is a record

$$m \in mem$$
$$empty \in mem$$
$$read \in mem \to int \rightharpoonup val$$
$$write \in mem \to int \to val \rightharpoonup mem$$
$$M ::= \{ms \in \mathcal{C} + ident \rightharpoonup mem;$$
$$stk \in list(\mathcal{C} + ident \times int \times int);$$
$$heap \in list(\mathcal{C} + ident \times int \times int)\}$$
$$heap\_alloc \in \mathcal{M} \to \mathcal{C} + ident \to int \rightharpoonup (int \times \mathcal{M})$$
$$heap\_free \in \mathcal{M} \to \mathcal{C} + ident \to int \rightharpoonup \mathcal{M}$$
$$stk\_alloc \in \mathcal{M} \to \mathcal{C} + ident \to int \rightharpoonup (int \times \mathcal{M})$$
$$stk\_free \in \mathcal{M} \to \mathcal{C} + ident \rightharpoonup \mathcal{M}$$
$$perturb \in \mathcal{M} \rightharpoonup \mathcal{M}$$

$$C \in \mathcal{C} \quad id \in ident$$

$$\mathcal{R} ::= \mathbf{L}(C) \mid \mathbf{S}(id, base) \qquad base \in int$$
$$v \in val ::= \ldots \mid Vptr\ r\ a \qquad r \in \mathcal{R}, a \in int$$
$$e \in ident \rightharpoonup (\mathcal{R} \times int)$$

$$state ::= C, M, e, \ldots \mid \mathtt{expr}$$
$$\mid\ C, M, e, \ldots \mid \mathtt{stmt}$$
$$\mid\ CALL(f, M, \ldots)$$
$$\mid\ RET(M, v, \ldots)$$

$$(\longrightarrow) \in state \times state$$

Figure 1: Definitions

$\mathbf{WR1} : write\ m\ a\ v = m' \to$
$$read\ m\ a = v$$

$$\frac{M.ms\ C = m \qquad read\ m\ a = v}{C, M, e \mid *(Vptr\ \mathbf{L}(C)\ a) \longrightarrow C, M, e \mid v}\text{VALOFL}$$

$\mathbf{WR2} : read\ m\ a = v \to$

$$\frac{M.ms\ id = m \qquad read\ m\ a = v}{C, M, e \mid *(Vptr\ \mathbf{S}(id, base)\ a) \longrightarrow C, M, e \mid v}\text{VALOFS}$$

$write\ m\ a'\ v' = m' \to$
$a \neq a' \to read\ m'\ a = v$

$$\frac{M.ms\ C = m \quad write\ m\ a\ v = m' \quad M' = M[ms\ m \mapsto m']}{C, M, e \mid *(Vptr\ \mathbf{L}(C)\ a) := v \longrightarrow C, M', e \mid v}\text{ASSIGNL}$$

$$\frac{M.ms\ id = m \quad write\ m\ a\ v = m' \quad M' = M[ms\ id \mapsto m']}{C, M, e \mid *(Vptr\ \mathbf{S}(id, base)\ a) := v \longrightarrow C, M', e \mid v}\text{ASSIGNS}$$

Figure 2: Reads and Writes

$\textbf{HA} : heap\_alloc\ M\ r\ sz = (a, M') \rightarrow$
$M'.heap = (r, a, a + sz) :: M.heap$
$\wedge M'.stk = M.stk$

$\textbf{HF} : (r, a_1, a_2) \in M.heap \rightarrow$
$\exists M'.heap\_free\ M\ B\ a_1 = M' \wedge$
$M'.heap = M.heap - (r, a_1, a_2) \wedge$
$M'.stk = M.stk$

$\textbf{AM} : (r, a_1, a_2) \in M.heap \cup M.stk \rightarrow$
$\exists! m.M.ms\ r = m$

$\textbf{AR} : (r, a_1, a_2) \in M.heap \cup M.stk \rightarrow$
$m = M.ms\ r \rightarrow a_1 \le a < a_2 \rightarrow$
$\exists v.read\ m\ a = v$

$\textbf{AW} : (r, a_1, a_2) \in M.heap \cup M.stk \rightarrow$
$m = M.ms\ r \rightarrow a_1 \le a < a_2 \rightarrow$
$\exists m'.write\ m\ a\ v = m'$

$\textbf{DISJ} : (r, a_1, a_2) \in M.heap \cup M.stk \rightarrow$
$(r, a_1', a_2') \in M.heap \cup M.stk \rightarrow$
$a' + sz < a_1 \vee a_2 \le a'$

$\textbf{PERT1} : perturb\ M = M' \rightarrow$
$M'.heap = M.heap \wedge M'.stk = H.stk$

$$\frac{\begin{array}{c} expr = \texttt{malloc}(Vint\ sz) \\ heap\_alloc\ M\ C\ sz = (a, M') \end{array}}{C, M, e \mid expr \longrightarrow C, M', e \mid Vptr\ \mathbf{L}(C)\ a}\textsc{MallocL}$$

$$\frac{\begin{array}{c} fresh\ id \quad heap\_alloc\ M\ id\ sz = (a, M') \\ expr = \texttt{malloc\_share}(Vint\ sz) \end{array}}{C, M, e \mid expr \longrightarrow C, M', e \mid Vptr\ \mathbf{S}(id, a)\ a}\textsc{MallocS}$$

$$\frac{v = Vptr\ \mathbf{L}(C)\ a \quad heap\_free\ M\ C\ a = M'}{C, M, e \mid \texttt{free}(v) \longrightarrow C, M', e \mid Vundef}\textsc{FreeL}$$

$$\frac{\begin{array}{c} v = Vptr\ (\mathbf{S}(id, base))\ base \\ heap\_free\ M\ id\ a = M' \end{array}}{C, M, e \mid \texttt{free}(v) \longrightarrow C, M', e \mid Vundef}\textsc{FreeS}$$

$\textbf{SA} : stk\_alloc\ M\ r\ sz = (a, M') \rightarrow$
$M'.stk = (r, a, a + sz) :: M.stk$
$\wedge M'.heap = M.heap$

$\textbf{SF} : M.stk = (r, a_1, a_2) :: S' \rightarrow$
$\exists M'.stk\_free\ M\ r\ a_1 = M' \wedge$
$M'.stk = S' \wedge M'.heap = M.heap$

$\textbf{PERT2} : (r, a_1, a_2) \in M.heap \cup M.stk \rightarrow$
$perturb\ M = M' \rightarrow a_1 \le a < a_2 \rightarrow$
$read\ (M.ms\ r)\ a = v \rightarrow read\ (M'.ms\ r)\ a = v$

Figure 3: Heap Allocation and Integer-Pointer Cast

containing a map from region identities to memories, ms, and lists of allocated regions for both stack and heap, stk and $heap$.

The allocation and free operations for both stack and heap act on the super-memory as axiomatized in Figure 3. $M.heap$ and $M.stk$ are lists of triples (r, a_1, a_2) representing the allocated regions of the heap and stack, respectively. Once an object is allocated within a region, reads and writes are guaranteed to succeed within its bounds in that region's memory.

This axiomatization serves to abstract away concrete details about memory layout that may be specific to a given compiler-allocator-hardware combination. We can understand any particular instance of $\mathcal{M}$ as an oracle that divines where the target system will place each allocation and, with knowledge of the full layout of memory, determines what happens in the event of an out-of-bounds read or write. This oracle is constrained by the full set of axioms in Section **??**.

Allocation　The abstract operations $heap\_alloc$ and stk_alloc yield addresses at which they locate a new ident, either within a compartment's memory or in its own isolated region. In the latter case, the address provided becomes the new base of that region's pointers. Since the $*\_alloc$ operations are parameterized by the identity of the compartment or ident that they allocate, they are allowed to make decisions based on that information, such as clumping compartment-local allocations together in order to protect using a page-table-based enforcement mechanism. This is a nondeterministic semantics, but given any particular instantiation of the oracle, the semantics becomes deterministic.

Importantly, allocations are guaranteed to be disjoint from any prior allocations in the same region. (In fact, when targeting a system with a single address space, we further restrict them to be disjoint across all bases.) Addresses in allocated regions are guaranteed successful loads and stores, and once an unallocated address has been successfully accessed it will behave consistently until new memory is allocated anywhere in the system, at which point all unallocated memory again becomes unpredictable.

The $perturb$ operation similarly represents the possibility of compiler-generated code using unallocated memory and therefore changing its value or rendering it inaccessible. The only facts that are maintained over a call to perturb are those involving addresses in allocated regions. Perturb happens during every function call and return, because the compiler needs to be free to reallocate memory during those operations, but it may happen at other points in the semantics as well.

Arithmetic and Integer-Pointer Casts　Most arithmetic operations are typical of C. The interesting operations are those involving integers that have been cast from pointers. We give concrete definitions to all such operations based on their address. As shown in Figure 4, if they involve only a single former pointer, the result will also be a pointer into the same memory; otherwise the result is a plain integer. If the former pointer is cast back to a pointer type, it retains its value and is once again a valid pointer. Otherwise, if an integer value is cast to a pointer, the result is always a local pointer to the active compartment.

Calls and Returns　There are two interesting details of the call and return semantics: they allocate and deallocate memory, and they can cross compartment boundaries. In the first case, we need to pay attention to which stack-allocated objects are to be shared. This can again be done using escape analysis: objects whose references never escape, can be allocated locally. Objects whose references escape to another compartment must be allocated as shared. Those that escape to another function in the same compartment can be treated in either way; if they are allocated

$$\frac{}{C, M, e \mid \odot(\textit{Vptr I a}) \longrightarrow C, M, e \mid \textit{Vptr I } (\langle\odot\rangle a)}\text{U{\footnotesize NOP}}$$

$$\frac{}{C, M, e \mid (\textit{Vptr I a}) \oplus (\textit{Vint i}) \longrightarrow C, M, e \mid \textit{Vptr I } (a\langle\oplus\rangle i)}\text{B{\footnotesize INOP}P{\footnotesize OINTER}I{\footnotesize NTEGER}}$$

$$\frac{}{C, M, e \mid (\textit{Vint i}) \oplus (\textit{Vptr I a}) \longrightarrow C, M, e \mid \textit{Vptr I } (i\langle\oplus\rangle a)}\text{B{\footnotesize INOP}I{\footnotesize NTEGER}P{\footnotesize OINTER}}$$

$$\frac{}{C, M, e \mid (\textit{Vptr I } a_1) \oplus (\textit{Vptr I } a_2) \longrightarrow C, M, e \mid \textit{Vint } (a_1\langle\oplus\rangle a_2)}\text{B{\footnotesize INOP}P{\footnotesize OINTERS}}$$

Figure 4: Arithmetic Operations Involving Pointers

$alloc\_locals\ M\ C\ [\,] = (M, \lambda id.\bot)$

$alloc\_locals\ M\ C\ (id, \mathbf{L}, sz) :: ls = (M'', e[id \mapsto (\mathbf{L}(C), i)])$
  where $stk\_alloc\ M\ C\ sz = (i, M')$ and $alloc\_locals\ M'\ C\ ls = (M'', e)$

$alloc\_locals\ M\ C\ (id, \mathbf{S}, sz) :: ls = (M'', e[id \mapsto (\mathbf{S}(id, i), i)])$
  where $alloc\_locals\ M\ C\ ls = (M', e)$ and $stk\_alloc\ M'\ C\ sz = (i, M'')$

$$\frac{f = (C, locals, s) \quad alloc\_locals\ M\ C\ locals = (M', e)}{CALL(f, M) \longrightarrow C, perturb\ M', e \mid s}\text{F{\footnotesize ROM}C{\footnotesize ALLSTATE}}$$

Figure 5: Call Semantics and Local Variables

locally but are later passed outside the compartment, the system will failstop at that later point (see Section 3).

We assume that each local variable comes pre-annotated with how it should be allocated, with a simple flag $\mathbf{L}$ or $\mathbf{S}$, so that a function signature is a list of tuples $(id, \mathbf{L} \mid \mathbf{S}, sz)$. (Aside: there is a case to be made we should just allocate all stack objects locally barring some critical use case for share them. Doing so would simplify the model here.)

The allocation and deallocation of stack memory is shown in the step rules in Section 5. In the full semantics, calls and returns step through intermediate states, written $CALL$ and RET. During the step from the intermediate callstate into the function code proper, the semantics looks up the function being called and allocates its local variables before beginning to execute its statement. And during the step from the `return` statement into the intermediate returnstate, the semantics likewise deallocates every variable it had previously allocated.

3   Cross-compartment interfaces

In this system, each function is assigned to a compartment. A compartment interface is a subset of the functions in the compartment that are publicly accessible. At any given time, the compartment

that contains the currently active function is considered the active compartment. It is illegal to call a private function in an inactive compartment.

Public functions may not receive $L(\dots)$-based pointer arguments. Private functions may take either kind of pointer as argument. $L(\dots)$ pointers may also not be stored to shared memory. This guarantees that there can be no confusion between shared pointers and a compartment's own local pointer that escaped its control. Violations of a compartment interface exhibit failstop behavior.

As a consequence of these rules, a compartment can never obtain a $\mathbf{L}(\dots)$-based pointer from a compartment other than itself. It can recieve such a pointer if it is cast to an integer type. If the resulting integer is cast back into a pointer, it will have the same behavior as if it were cast from any other integer: accessing it may cause a failstop or else access the appropriate address in the active compartment's ident.

4   Machine Constraints

Now we consider the constraints that this system places on potential implementations. In particular, in a tag-based enforcemen mechanism with a limited quantity of tags, is this system realistic? In general it requires a unique tag per compartment, as well as one for each shared allocation. In the extreme, consider a system along the lines of ARM's MTE, which has four-bit tags. That could only enforce this semantics for a very small program, or one with very little shared memory (fewer than sixteen tags, so perhaps two-four compartments and around a dozen shared objects.)

On the other hand, this semantics is a reasonable goal under an enforcement mechanism with even eight-bit tags (512 compartments and shared objects.) If we go up to sixteen bits, we can support programs with thousands of shared objects.

That said, it only takes a minor adjustment for this model to be enforceable in even the smallest of tag-spaces. Instead of separate dynamic blocks for each shared object, we let the set of memory regions consist of the powerset of compartments, each region corresponding to the set of compartments that have permission to access it. We parameterize each instance of `malloc` with such a set, which will be the base of each pointer that it allocates. We write the identifiers for these `malloc` invocations $\texttt{malloc}_r$. Then we replace the relevant definitions and step rules with those in Figure 6, with call and return steps changed similarly.

This version can be enforced with a number of tags equal to the number of different sharing combinations present in the system—in the worst case this would be exponential in the number of compartments, but in practice it can be tuned to be arbitrarily small. (In extremis, all shared objects can be grouped together to run on a machine with only two tags.) Sadly it strays from the C standard in its temporal memory safety: under some circumstances a shared object can be accessed by a compartment that it has not (yet) been shared with.

References

[1] MEMARIAN, K., GOMES, V. B. F., DAVIS, B., KELL, S., RICHARDSON, A., WATSON, R. N. M., AND SEWELL, P. Exploring C semantics and pointer provenance. *Proc. ACM Program. Lang. 3*, POPL (Jan. 2019).

$$val ::= \ldots \mid Vptr\ r\ a \qquad r \in 2^{\mathcal{C}}$$

$$e \in ident \rightharpoonup (2^{\mathcal{C}} \times int)$$

$$M \in \mathcal{M} \subseteq 2^{\mathcal{C}} \to mem$$

$$heap\_alloc \in \mathcal{M} \to 2^{\mathcal{C}} \to int \rightharpoonup (int \times \mathcal{M})$$

$$heap\_free \in \mathcal{M} \to 2^{\mathcal{C}} \to int \rightharpoonup \mathcal{M}$$

$$stk\_alloc \in \mathcal{M} \to 2^{\mathcal{C}} \to int \rightharpoonup (int \times \mathcal{M})$$

$$stk\_free \in \mathcal{M} \to 2^{\mathcal{C}} \rightharpoonup \mathcal{M}$$

$$\frac{M\ r = m \qquad read\ m\ a = v}{C, M, e \mid *(Vptr\ r\ a) \longrightarrow C, M, e \mid v}$$

$$\frac{M\ r = m \quad write\ m\ a\ v = m' \quad M' = M[r \mapsto m']}{C, M, e \mid *(Vptr\ r\ a) := v \longrightarrow C, M', e \mid v}$$

$$\frac{heap\_alloc\ M\ r\ sz = (p, M')}{C, M, e \mid \mathtt{malloc}_r(Vint\ sz) \longrightarrow C, M', e \mid Vptr\ r\ p}$$

Figure 6: Selected Rules for Explicit Sharing