

Expand  $A = [(x + 1) - y][(x + 1) + y]$ .

Verify that  $3! + 2! < (3 + 2)!$  and  $3! - 2! > (3 - 2)!$ .

The fraction  $5/10$  is of ratio  $1 : 2$ .

If  $f(x) = x^2$  then show that  $f'(x) = 2x$  and  $f''(x) = 2$

16 is divisible by 2 so we write  $2|16$ .

The sum of the inner angles of a triangle is 180 degree.

If the  $\alpha, \beta$  and  $\gamma$  are the inner angles then

$$\alpha + \beta + \gamma = \pi$$

The set of positive integer is denoted by  $\mathbb{N}$ .

The set of integer is denoted by  $\mathbb{Z}$ .

The set of rational, real and complex numbers are denoted by  $\mathbb{Q}, \mathbb{R}$  and  $\mathbb{C}$  respectively.

The numbers of permutation of  $k$  elements taken from distinct  $n$  elements is given by  $P(n, k) = \frac{n!}{(n-k)!}$

The number of combination of  $k$  elements taken from distinct  $n$  elements is given by  $C(n, k) = \frac{n!}{k!(n-k)!}$

The relation between combination and permutation is

$$C(n, k) = \frac{P(n, k)}{k!} \quad (1)$$

1. Find the formula for computing

$$S_n = 1^2 + 2^2 + 3^2 + \cdots + n^2 \quad (2)$$

$$S_n = \frac{n(n+1)}{2} \quad (3)$$

2. The formula is derived from the equality  $(n+1)^3 - n^3 = 3n^2 + 3n + 1$

$$S_n = 1^2 + 2^2 + 3^2 + \cdots + n^2 \quad (4)$$

$$S_n = \frac{n(n+1)(2n+1)}{6} \quad (5)$$

3. To solve quadratic equation  $ax^2 + bx + c = 0$  where  $a \neq 0$  we calculate the discriminant

$$\Delta = b^2 - 4ac$$

$$\text{or } \Delta = b^2 - 4ac$$

- Roots of the equation is given by the formula

$$x_1 = \frac{-b - \sqrt{\Delta}}{2a} \quad (6)$$

$$x_2 = \frac{-b + \sqrt{\Delta}}{2a} \quad (7)$$

or precisely,

$$x = \frac{-b \pm \sqrt{\Delta}}{2a} \quad (8)$$

Solve  $\sqrt{3}x^2 + \sqrt[3]{5}x + \sqrt[4]{7} + \sqrt[5]{5}x = 0$ .