Chapter 1

First

EXERCISES

1. In problem i.-iii., determine whether the given differential equation is sepa-

i.
$$\frac{dy}{dx} - \sin(x+y) = 0$$
 ii. $\frac{dy}{dx} = 4y^2 - 3y + 1$

ii.
$$\frac{dy}{dx} = 4y^2 - 3y + 1$$

iii.
$$\frac{ds}{dt} = t \ln{(s^{2t})} + 8t^2$$

2. In problem iv.-vii., solve the equation

iv.
$$\frac{dx}{dt} = 3xt^2$$

$$\mathbf{v.} \quad y^{-1}dy + ye^{\cos x}\sin xdx = 0$$

$$\mathbf{vi.} \quad (x+xy^2)dx + ye^{\cos x}\sin xdx = 0$$

vi.
$$(x+xy^2)dx + ye^{\cos x}\sin x dx = 0$$
 vii. $\frac{dy}{dt} = \frac{y}{t+1} + 4t^2 + 4t$, $y(1) = 10$

1.2 EXERCISES

Another exercise.

1. If you don't need a horizontal list, you can simply use \Question

Chapter 2

Second

EXERCISES

1. Eight systems of differential equations and five direction fields are given below. Determine the system that corresponds to each direction field and sketch the solution curves that correspond to the initial conditions $(x_0, y_0) =$ (0,1) and $(x_0,y_0)=(1,-1)$.

$$\mathbf{i.} \quad \frac{dx}{dt} = -x \\ dy$$

$$\frac{dt}{dy} = y - 1$$

ii.
$$\frac{dx}{dt} = x^2 - 1$$

i.
$$\frac{dx}{dt} = -x$$

$$\frac{dy}{dt} = y - 1$$
ii.
$$\frac{dx}{dt} = x^2 - 1$$

$$\frac{dy}{dt} = y$$
iii.
$$\frac{dx}{dt} = x + 2y$$

$$\frac{dy}{dt} = -y$$
iv.
$$\frac{dx}{dt} = 2x$$

$$\frac{dx}{dt} = x$$
v.
$$\frac{dx}{dt} = x$$
vi.
$$\frac{dx}{dt} = x - 1$$

$$\frac{dy}{dt} = -y$$

$$\frac{dx}{dt} = 2x$$

$$\frac{dt}{dy} = y$$

$$\frac{dx}{dt} = x$$

$$\frac{dt}{dy} = 2y$$

$$\frac{dx}{dt} = x - 1$$

vii.
$$\frac{dx}{dt} = x^2 - 1$$

$$\frac{dy}{dt} = -y$$
viii.
$$\frac{dx}{dt} = x - 2y$$

$$\frac{dy}{dt} = -y$$

$$\frac{dt}{dy} = -y$$

$$\mathbf{viii.} \frac{dx}{dt} = x - 2y$$

$$\frac{dy}{dt} = -y$$

EXERCISES

Since these are systems, maybe it's better to put the aligned environment within \left\{ and \right.:

1. Eight systems of differential equations and five direction fields are given below. Determine the system that corresponds to each direction field and sketch the solution curves that correspond to the initial conditions $(x_0, y_0) =$ (0,1) and $(x_0,y_0)=(1,-1)$.

i.
$$\begin{cases} \frac{dx}{dt} = -x \\ \frac{dy}{dt} = y - 1 \end{cases}$$
 ii.
$$\begin{cases} \frac{dx}{dt} = x^2 - 1 \\ \frac{dy}{dt} = y \end{cases}$$
 iii.
$$\begin{cases} \frac{dx}{dt} = x + 2y \\ \frac{dy}{dt} = -y \end{cases}$$
 iv.
$$\begin{cases} \frac{dx}{dt} = 2x \\ \frac{dy}{dt} = y \end{cases}$$
 v.
$$\begin{cases} \frac{dx}{dt} = x \\ \frac{dy}{dt} = 2y \end{cases}$$
 vi.
$$\begin{cases} \frac{dx}{dt} = x - 1 \\ \frac{dy}{dt} = -y \end{cases}$$

ii.
$$\begin{cases} \frac{dx}{dt} = x^2 - \\ \frac{dy}{dt} = y \end{cases}$$

iii.
$$\begin{cases} \frac{dx}{dt} = x + 2\\ \frac{dy}{dt} = -y \end{cases}$$

$$\mathbf{iv.} \quad \left\{ \begin{array}{l} \frac{dx}{dt} = 2x \\ \frac{dy}{dt} = y \end{array} \right.$$

$$\mathbf{v.} \quad \left\{ \begin{array}{l} \frac{dx}{dt} = x \\ \frac{dy}{dt} = 2y \end{array} \right.$$

vi.
$$\begin{cases} \frac{dx}{dt} = x - 1 \\ \frac{dy}{dt} = -y \end{cases}$$

vii.
$$\begin{cases} \frac{dx}{dt} = x^2 - \\ \frac{dy}{dt} = -y \end{cases}$$

vii.
$$\begin{cases} \frac{dx}{dt} = x^2 - 1 \\ \frac{dy}{dt} = -y \end{cases}$$
 viii.
$$\begin{cases} \frac{dx}{dt} = x - 2y \\ \frac{dy}{dt} = -y \end{cases}$$

Chapter 3

Answer to all problems

CHAPTER 1

Exercises 1.1, page 1

- **i.1.** This is a solution of Ex 1
- ii. This is a solution of Ex 2
- iii. This is a solution of Ex 3
- **i2.** This is a solution of Ex 4
- v. This is a solution of Ex 5
- vi. This is a solution of Ex 6
- vii. This is a solution of Ex 7

Exercises 1.2, page 1

1. This is a solution of Ex 1

CHAPTER 2

Exercises 2.1, page 3

- **i.1.** This is a solution of Ex 1
- ii. This is a solution of Ex 2

- iii. This is a solution of Ex 3
- iv. This is a solution of Ex 4
- v. This is a solution of Ex 5
- vi. This is a solution of Ex 6
- vii. This is a solution of Ex 7
- viii. This is a solution of Ex 8

Exercises 2.2, page 4

- **i.1.** This is a solution of Ex 1
- **ii.** This is a solution of Ex 2
- iii. This is a solution of Ex 3
- iv. This is a solution of Ex 4
- v. This is a solution of Ex 5
- vi. This is a solution of Ex 6
- vii. This is a solution of Ex 7
- viii. This is a solution of Ex 8