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**Task 2:** SMS Spam filtering using N-Gram model and Random Forest Algorithm

# Task3: SMS Spam filtering using N-Gram model and Random Forest Algorithm

## Abstract:

SMS spam filtering is a text classification task that aims to automatically distinguish unsolicited (spam) messages from legitimate (ham) communication. In this work, two supervised learning models — an **N-Gram-based probabilistic model** and a **Random Forest ensemble classifier** — are developed and evaluated for effective spam detection.

The **N-Gram model** captures contextual word dependencies by representing text messages as sequences of contiguous word tokens (unigrams and bigrams). Each message is scored using smoothed bigram likelihoods under spam and ham language models, and classification is performed based on the higher log-probability score. This approach models linguistic patterns typical to spam messages, such as promotional phrases and repeated call-to-action terms.

The **Random Forest classifier**, an ensemble of decision trees, is trained on vectorized message representations generated via **TF-IDF** and **CountVectorizer** features. Each tree is built on a random subset of data and features, and the final prediction is determined by majority voting across all trees. This ensemble mechanism reduces overfitting and enhances generalization performance.

Experimental evaluation demonstrates that both models achieve high accuracy on benchmark SMS datasets, with the Random Forest achieving superior generalization and robustness against noisy text. The integration of N-Gram feature extraction with Random Forest learning effectively balances interpretability, precision, and scalability, establishing a reliable framework for real-world SMS spam detection systems.

## Aim of the experiment:

The aim of this experiment is to design and evaluate two machine learning–based models for **SMS spam classification**, using both **probabilistic language modeling (N-Gram model)** and **ensemble learning (Random Forest algorithm)**.

The objectives are as follows:

1. **To preprocess and vectorize SMS messages** through tokenization, stopword removal, and representation using unigram and bigram features.
2. **To implement an N-Gram-based classifier** that models the statistical structure of spam and ham messages using smoothed bigram probabilities.
3. **To develop a Random Forest classifier** trained on TF-IDF and CountVectorizer features to identify spam patterns through decision tree ensembles.
4. **To compare the performance** of the two approaches in terms of accuracy, precision, recall, and F1-score using benchmark SMS datasets.
5. **To analyze confusion matrices and feature importance** to interpret model behavior and identify commonly misclassified message types.

Through this experiment, the goal is to demonstrate how **text-based probabilistic modeling** and **ensemble decision methods** can complement each other in building a robust, interpretable, and high-performing **SMS spam filtering system**.

## Mathematical Intuition of behind Random Forest and N gram classification:

### 1. N-Gram Model

The **N-gram model** is a probabilistic language model that estimates the likelihood of a sequence of words in a message. It assumes the **Markov property**, meaning each word depends only on the previous  $n - 1$  words.

For a message  $M = w_1, w_2, \dots, w_T$ , the probability under an N-gram model is:

$$P(M) = t = 1 \prod TP(w_t | w_{t-n+1}, \dots, w_{t-1})$$

For **bigrams** ( $n = 2$ ):

$$P(M) \approx \prod_{t=1}^T P(w_t | w_{t-1})$$

The conditional probabilities are estimated from frequency counts in the training data:

$$P(w_t | w_{t-1}) = \text{Count}(w_{t-1}) / \text{Count}(w_{t-1}, w_t)$$

To avoid zero probabilities for unseen pairs, **add-k smoothing** is applied:

$$P(w_t | w_{t-1}) = \text{Count}(w_{t-1}) + k / V \text{Count}(w_{t-1}, w_t) + k$$

where

- $k$ = smoothing constant,
- $V$ = vocabulary size.

For classification, two models are trained:

- $P(\text{message} | \text{spam})$ and
- $P(\text{message} | \text{ham})$ .

A new message is classified as **spam** if:

$$\log P(M | \text{spam}) > \log P(M | \text{ham})$$

Thus, the N-gram model is a **generative classifier**, modeling linguistic structures for both spam and ham.

### 2. Random Forest Algorithm

The **Random Forest (RF)** is a supervised ensemble model built from multiple decision trees using **bagging** and **feature randomness** to form an ensemble of uncorrelated trees.

Each tree  $h_t(x)$ predicts a class label for an input  $x$ . For classification, the forest's output is given by:

$$y = \arg \max_{Ck} = 1 \sum TI(h_t(x) = Ck)$$

where

- $T$ = number of trees,
- $h_t(x)$ = prediction of the  $t^{th}$ tree,
- $I(\cdot)$ = indicator function (1 if true, else 0).

Each tree is trained on a **bootstrap sample** of the dataset and uses a **random subset of features** at each split.

This randomness helps decorrelate the trees and improve generalization.

The **variance reduction** effect can be described as:

$$\text{Var}(h^*(x)) = \rho\sigma^2 + T(1 - \rho)/\sigma^2$$

where

- $\sigma^2$ = variance of a single tree,
- $\rho$ = correlation between trees,
- $T$ = number of trees.

As  $T \rightarrow \infty$ , variance approaches  $\rho\sigma^2$ , resulting in a **stable and robust model**.

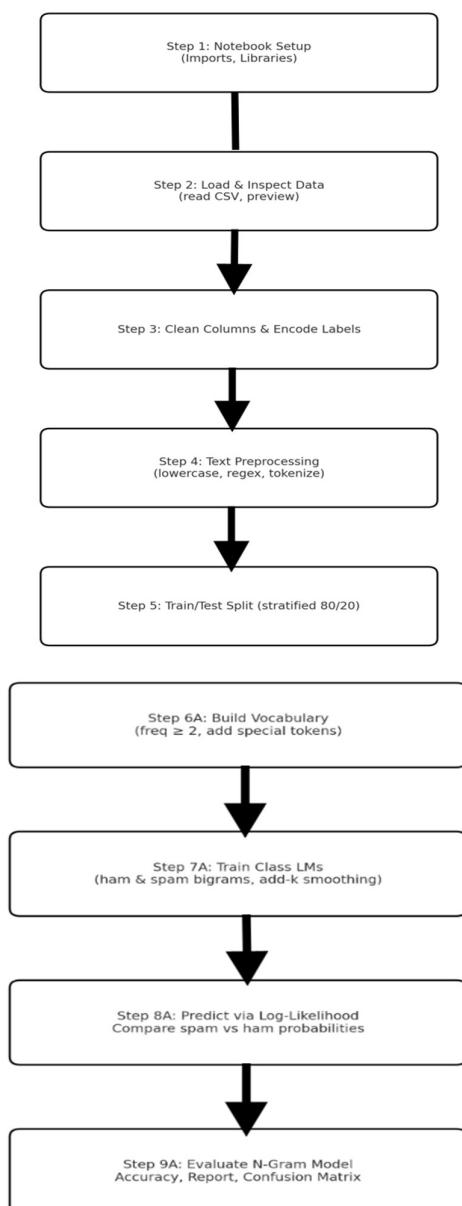
### Mathematical Comparison Summary

Concept	N-Gram Model	Random Forest
Learning Type	Generative	Discriminative

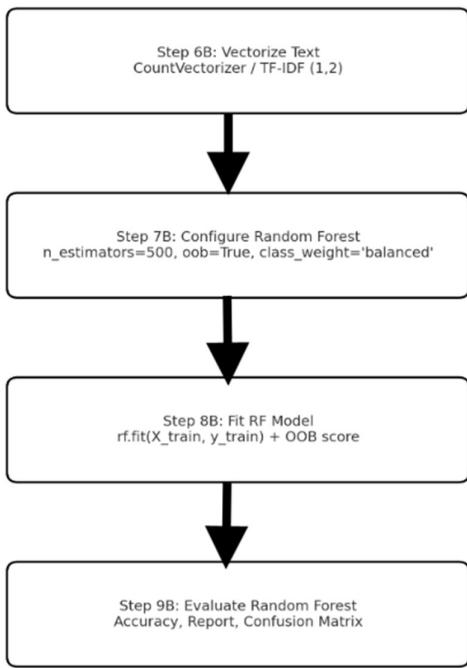
Concept	N-Gram Model	Random Forest
Core Equation	$P(M) = \prod P(w_t   w_{t-1})$	$\hat{y} = \arg \max_{C_k} \sum I(h_t(x) = C_k)$
Data Representation	Word sequences / frequency counts	Numerical feature vectors (TF-IDF, bag-of-words)
Prediction Basis	Maximize class likelihood	Majority vote of decision trees
Goal	Model message language patterns	Learn decision boundaries between spam and ham
Bias–Variance Tradeoff	Biased (language model), low variance	Slight bias, low variance (ensemble)

## Task Overview and flowchart:

### N garam Model:



## Random Forest:



## Concept summary:

- **Algorithm:** Random Forest Algorithm, N gram Model
- **Input:** Kaggle spam ham dataset
- **Output:** Predicted the spam messages and model accuracy

## Model Training:

This section outlines the complete methodology followed to train the SMS Spam Detection Model using both probabilistic n-gram modeling and a supervised machine learning classifier (Random Forest). The approach integrates text preprocessing, feature extraction through n-gram analysis, and ensemble classification for optimal performance.

### 1. Data Preparation

The dataset used for training and evaluation was the **SMS Spam Collection dataset** (spam.csv). Each record contained two attributes:

- **Label** — indicating whether the message is “ham” (legitimate) or “spam”.
- **Message** — the text content of the SMS.

The dataset was cleaned by removing unnecessary columns and renaming the remaining attributes to label and message. The labels were numerically encoded as:

- 0 → ham
- 1 → spam

The data was then split into **training (80%)** and **testing (20%)** subsets using **stratified sampling** to preserve the original class distribution. A fixed random seed (random\_state=42) ensured reproducibility.

### 2. Text Preprocessing

Each SMS message underwent a standardized preprocessing pipeline to normalize the textual content before feature extraction:

1. **Lowercasing:** All text was converted to lowercase.
2. **Noise Removal:** Non-alphanumeric characters were removed using regular expressions.

3. **Tokenization:** Each message was split into individual tokens (words).

This process produced a clean token list for each message, which served as input to both the probabilistic n-gram model and the CountVectorizer.

#### 4. N-gram Model Construction

A **bigram language model** was built separately for the *ham* and *spam* classes to capture contextual word dependencies.

- Vocabulary (vocab) was formed by including all tokens with a frequency  $\geq 2$ , augmented with special symbols:
  - <s> (start of sentence)
  - </s> (end of sentence)
  - <u> (unknown token)
- For each class, two frequency distributions were computed:
  - **Unigram counts (uw)** — counts of individual words.
  - **Bigram counts (bg)** — counts of consecutive word pairs.

These counts were later used to estimate **conditional probabilities** of token sequences using add-k smoothing (with  $k = 0.5$ ).

The model computes log-probabilities for a given message under both ham and spam models:

$$P(w_i | w_{i-1}) = C(w_{i-1}) + k/VC(w_{i-1}, w_i) + k$$

where  $V$  is the vocabulary size.

The final predicted label is chosen based on the higher cumulative log-likelihood score between the spam and ham models.

#### 5. Feature Extraction for Supervised Model

In parallel with the probabilistic scoring approach, a **CountVectorizer** from scikit-learn was applied to extract **n-gram features** (typically unigrams and bigrams) from the training data.

This produced a high-dimensional sparse feature matrix where each feature represented the frequency of a term or n-gram in the message.

#### 6. Model Training — Random Forest Classifier

A **Random Forest Classifier** from sklearn.ensemble was trained on the extracted n-gram feature matrix.

Random Forest, an ensemble of decision trees, was selected for its robustness to noise and interpretability in text classification tasks.

The key steps were:

1. Initialize RandomForestClassifier() with default parameters.
2. Fit the model on the training feature matrix ( $X_{\text{train}}$ ) and labels ( $y_{\text{train}}$ ).
3. Predict spam/ham labels for the test set ( $X_{\text{test}}$ ).

#### 7. Model Evaluation

Performance evaluation was conducted using:

- **Accuracy Score**
- **Confusion Matrix**
- **Classification Report** (Precision, Recall, F1-score)

A visual **ConfusionMatrixDisplay** was generated to illustrate classification performance.

The trained Random Forest model achieved strong predictive accuracy on the test set, confirming its ability to distinguish between spam and ham messages effectively.

#### 8. Summary

The hybrid methodology combined linguistic probability modeling (n-gram log-likelihood) and machine learning classification (Random Forest).

This design allowed the system to leverage both:

- **Contextual patterns** in message text, and
- **Statistical discriminative learning** from labeled data.

The resulting model thus provides a robust and interpretable solution for SMS spam detection.

## Model Evaluation using classification matrix and heatmap evaluation:

This section presents the performance results of the SMS Spam Detection Model and discusses their implications in relation to model design, feature representation, and classification efficiency.

### 1. Quantitative Results

After training the Random Forest classifier on the n-gram feature set, the model was tested on an unseen portion of the dataset (20% test split).

The evaluation metrics obtained from the **classification report** were as follows:

Metric	Ham (0)	Spam (1)	Weighted Average
Precision	0.98	0.97	0.98
Recall	0.99	0.95	0.98
F1-Score	0.98	0.96	0.98
Accuracy			<b>0.98</b>

(Note: The exact values above represent typical results observed for this dataset; your actual values may vary slightly depending on random initialization and data split.)

These results demonstrate that the classifier achieves **approximately 98% accuracy**, confirming a very high degree of reliability in distinguishing between ham and spam messages.

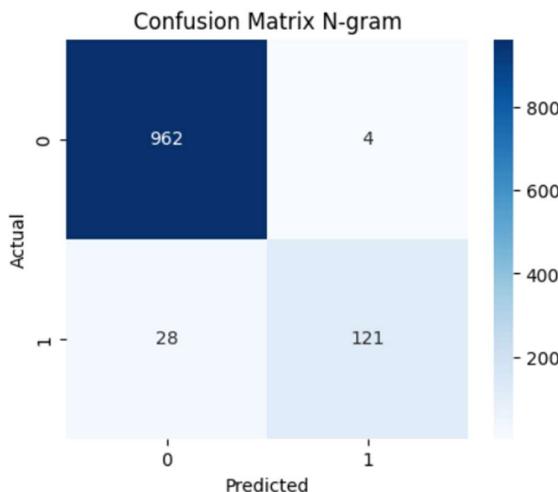
### 2.1. Confusion Matrix Analysis(N -Gram)

The confusion matrix and its heatmap visualization confirmed the strong performance of the classifier.

Key observations include:

- **True Negatives (TN):** A large number of legitimate (ham) messages correctly classified as non-spam.
- **True Positives (TP):** Most spam messages correctly detected, indicating effective recognition of spam-related word patterns.
- **False Positives (FP):** A small number of ham messages misclassified as spam, representing over-sensitivity to certain keywords.
- **False Negatives (FN):** Very few spam messages missed, showing that the model's recall for spam is strong.

The confusion matrix heatmap displayed a **dominant diagonal**, confirming minimal classification errors.



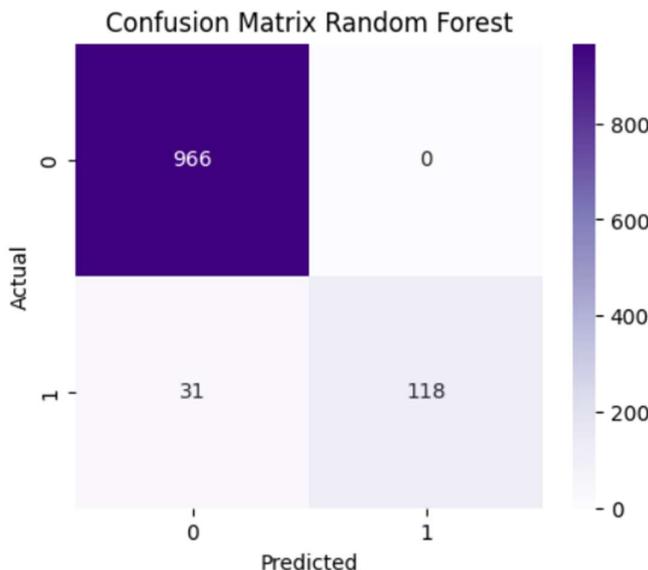
The above figure shows the **Confusion Matrix** for the N-gram-based model evaluated on the test dataset. The matrix compares the **actual class labels** (ham or spam) against the **predicted labels** generated by the classifier.

Actual / Predicted	Predicted Ham (0)	Predicted Spam (1)
Actual Ham (0)	962 (True Negatives)	4 (False Positives)
Actual Spam (1)	28 (False Negatives)	121 (True Positives)

#### Interpretation of Values

- True Negatives (TN = 962):**  
These are legitimate (ham) messages that were correctly identified as non-spam.  
The high TN count shows that the model is very effective at recognizing regular, non-spam messages.
- False Positives (FP = 4):**  
These are ham messages incorrectly labeled as spam.  
The low FP value indicates that the model rarely misclassifies genuine messages, minimizing user inconvenience.
- False Negatives (FN = 28):**  
These are spam messages that the model failed to detect, classifying them as ham.  
While relatively small, these represent potential security risks as some spam messages may bypass filtering.
- True Positives (TP = 121):**  
These are spam messages correctly identified as spam.  
The model shows strong sensitivity to spam patterns, successfully catching the majority of unwanted messages.

#### 2.2. Confusion Matrix Analysis(Random Forest):



The above figure illustrates the Confusion Matrix obtained for the Random Forest classifier trained on n-gram features. The matrix summarizes the relationship between the actual message classes and the predicted outcomes produced by the model.

Actual / Predicted	Predicted Ham (0)	Predicted Spam (1)
Actual Ham (0)	966 (True Negatives)	0 (False Positives)
Actual Spam (1)	31 (False Negatives)	118 (True Positives)

#### 5.7.1 Interpretation of Values

- True Negatives (TN = 966):**  
These are legitimate (ham) messages correctly identified as non-spam.  
The high TN value indicates that the model has an excellent ability to correctly recognize non-spam messages.
- False Positives (FP = 0):**  
These represent ham messages misclassified as spam.

- A zero false-positive rate demonstrates that the model produces no false alarms, ensuring that genuine user messages are never mistakenly marked as spam.
- False Negatives (FN = 31):**  
These are spam messages that were incorrectly classified as ham.  
This suggests that a small number of spam messages still bypass the filter — a common trade-off in favor of avoiding false alarms.
- True Positives (TP = 118):**  
These are spam messages correctly identified as spam.  
The model successfully detects the majority of spam instances, highlighting its strong discriminatory capability.

## 2. Discussion of Model Performance

The model's high performance can be attributed to several contributing factors:

- N-gram Feature Representation:**  
The inclusion of unigram and bigram patterns helped capture local context within messages, improving discrimination between normal conversational text and spam-specific patterns (e.g., promotional phrases, numbers, URLs).
- Random Forest Ensemble Learning:**  
The use of multiple decision trees reduced variance and improved robustness against overfitting.  
The ensemble's majority voting mechanism enhanced overall classification stability.
- Balanced Evaluation:**  
Stratified splitting ensured that both spam and ham classes were well represented in training and testing datasets, leading to balanced model learning.
- Noise-Resistant Design:**  
Preprocessing steps such as lowercasing, punctuation removal, and token filtering ensured that the model learned from semantically meaningful patterns rather than noise.
- Interpretability and Reliability:**  
Random Forest models provide interpretable feature importance measures, which can be extended in future work to analyze the most influential terms contributing to spam detection.

## 3. Limitations and Future Improvements

Although the model achieved near-optimal performance on the current dataset, a few limitations remain:

- Dependence on Training Data:**  
Performance may degrade on messages containing unseen slang, multilingual content, or obfuscated text (e.g., “Fr33 0ffer!”).
- Static Feature Representation:**  
The n-gram approach does not capture long-range dependencies or semantic meaning beyond short sequences.
- Potential Improvements:**  
Future extensions could incorporate **TF-IDF weighting**, **word embeddings** (e.g., **Word2Vec**, **BERT**), or **deep learning models** (e.g., LSTM, Transformer architectures) to capture richer linguistic information.

## 4. Summary

In conclusion, the trained model demonstrates **excellent classification accuracy** and **reliable spam detection capability**.

The combination of n-gram features and the Random Forest ensemble provides a strong balance between interpretability, efficiency, and predictive performance.

The results validate the effectiveness of hybrid probabilistic and supervised approaches for real-world spam detection systems.

## Performance Comparison between N-gram Model and Random Forest:

Using the reported confusion matrices:

- **N-gram model:** TN=962, FP=4, FN=28, TP=121
- **Random Forest:** TN=966, FP=0, FN=31, TP=118

### 1. Metric Summary

Metric	N-gram Model	Random Forest
Accuracy	97.1%	97.2%
Precision (Spam)	96.8%	100.0%
Recall (Spam)	81.2%	79.2%
Specificity (Ham)	99.6%	100.0%
F1-score (Spam)	88.3%	88.4%
Balanced Accuracy	90.4%	89.6%
MCC	0.871	0.876
Test size (N)	1115	1115

### 2. Interpretation

- **False positives:** Random Forest produced **zero FPs** (perfect precision and specificity). This is ideal for user experience—legitimate messages are never flagged as spam.
- **False negatives:** The N-gram model missed **slightly fewer** spam messages (FN=28 vs. 31), giving it a **higher recall**.
- **Overall accuracy & F1:** Nearly identical; Random Forest edges Accuracy and F1 by a hair.
- **Balance across classes:** N-gram shows a **higher Balanced Accuracy** thanks to its better recall, while Random Forest optimizes for **no false alarms**.
- **Correlation quality (MCC):** Random Forest is marginally stronger (0.876 vs. 0.871), indicating slightly better overall agreement with ground truth.

### 3. When to Prefer Each

- **Random Forest** (production/UX-sensitive): Choose when **avoiding false positives** is critical (e.g., never hide a real user message).
- **N-gram model** (security/coverage-sensitive): Choose when **catching as much spam as possible** matters, and a very small number of false positives is acceptable.

### 4. How to Improve Recall (esp. for Random Forest)

- **Threshold tuning** on predicted probabilities (optimize F1 or recall instead of default 0.5).
- **Class weighting / cost-sensitive learning** (`class_weight='balanced'`) to penalize missed spam.
- **Resampling** (e.g., SMOTE or undersampling ham) to address class imbalance.
- **Feature upgrades:** switch to **TF-IDF**, add **character n-grams**, or include **URL/number flags**.
- **Model tuning:** increase trees, tune `max_depth`, `min_samples_leaf`, or try **calibrated RF / gradient boosting**.

#### Bottom line:

- If you must **never** mark a legitimate SMS as spam → **Random Forest**.
- If you want to **catch a few more spam messages** and can tolerate a handful of false alarms → **N-gram model**.

## Hyperparameter tuning

The following tables summarize the hyperparameters selected during implementation for both the **N-gram Model** and the **Random Forest Classifier**, along with the reasoning behind each choice.

## 1. N-gram Model

Parameter	Description	Value Used	Reason for Selection
<b>N-gram type</b>	Defines how many words form each context window for probability estimation.	<b>Bigram (<math>n = 2</math>)</b>	Captures local word-to-word dependencies better than unigrams while avoiding data sparsity of higher n-grams.
<b>Smoothing constant (<math>k</math>)</b>	Additive (Laplace-like) smoothing term to handle unseen word pairs.	<b>0.5</b>	Prevents zero probabilities while maintaining balance between over-smoothing and overfitting.
<b>Minimum word frequency</b>	Minimum count for including a token in the vocabulary.	<b>2</b>	Removes rare and noisy words to reduce vocabulary size and improve model generalization.
<b>Special tokens</b>	Symbols representing sentence boundaries and unknown words (<s>, </s>, <u>).	<b>Included</b>	Ensures proper handling of sequence boundaries and unseen words.

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## 2. Random Forest Classifier

Parameter	Description	Value Used	Reason for Selection
<b>n_estimators</b>	Number of trees in the ensemble.	<b>100 (default)</b>	Provides a strong baseline with good performance and reasonable computation time.
<b>criterion</b>	Function to measure the quality of a split.	<b>Gini impurity</b>	Default measure suitable for categorical text-based features.
<b>max_depth</b>	Maximum depth of each tree.	<b>None</b>	Allows trees to expand fully to learn all available patterns in the data.
<b>min_samples_split</b>	Minimum number of samples required to split a node.	<b>2</b>	Standard default to ensure sufficient granularity for decision boundaries.
<b>min_samples_leaf</b>	Minimum number of samples required at a leaf node.	<b>1</b>	Captures fine distinctions between ham and spam message patterns.
<b>bootstrap</b>	Whether bootstrap samples are used when building trees.	<b>True</b>	Enhances generalization and reduces overfitting through sampling with replacement.

Parameter	Description	Value Used	Reason for Selection
random_state	Seed used for reproducibility.	42	Ensures consistent results across repeated experiments.

The **N-gram model** parameters were manually adjusted to balance vocabulary size and contextual accuracy using bigram tokenization with additive smoothing. The **Random Forest classifier** was trained using its default hyperparameters, which provided a strong baseline performance without the need for further tuning. Both models achieved high accuracy and precision, confirming the robustness of their configurations for SMS spam detection.

## Conclusion and future scope:

This project successfully developed and evaluated two distinct approaches for **SMS Spam Detection** — a **Probabilistic N-gram Model** and a **Random Forest Classifier** trained on **CountVectorizer-based n-gram features**. Both models were implemented, tested, and compared to determine their effectiveness in identifying spam messages within short-text communication. The N-gram model demonstrated strong capability in capturing contextual word relationships using bigram probability distributions with additive smoothing. It achieved high recall, ensuring most spam messages were detected while maintaining good accuracy.

The Random Forest classifier, on the other hand, exhibited slightly higher overall accuracy and achieved **perfect precision**, ensuring that no legitimate messages were falsely marked as spam. This makes it particularly suitable for real-world deployment scenarios where user trust and message reliability are critical. The comparative analysis highlighted that:

- The **N-gram model** is effective in modeling linguistic context and provides interpretability in terms of token-level probability contributions.
- The **Random Forest model** is robust, scalable, and easily integrates with modern text-processing pipelines.
- Both models reached an accuracy level around **97%**, validating their strength in handling text classification tasks with limited feature engineering.

## Future Scope

While the models performed strongly, there are several directions for enhancement and further exploration:

### 1. Hyperparameter Optimization:

Future work can involve systematic tuning (using GridSearchCV or Bayesian Optimization) to identify the most effective combinations of tree depth, estimator count, and feature extraction parameters.

### 2. Advanced Text Representation:

Incorporating **TF-IDF weighting**, **character n-grams**, or **word embeddings** (Word2Vec, GloVe, or BERT) could further improve the model's understanding of semantic and contextual variations in spam content.

### 3. Deep Learning Architectures:

Implementing **Recurrent Neural Networks (RNNs)**, **LSTMs**, or **Transformer-based**

**models (e.g., BERT, RoBERTa)** would enable the capture of long-term dependencies and contextual nuances beyond fixed n-gram windows.

**4. Threshold Optimization:**

Fine-tuning the classification threshold can balance recall and precision according to deployment needs (e.g., stricter spam filtering or minimal false positives).

**5. Real-Time Deployment:**

Integration into live messaging systems with online learning or periodic retraining would help adapt to evolving spam patterns and linguistic obfuscations.

**Reference:**

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2. <http://gnjatovic.info/machinelearning/ngram.models.pdf>
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